

Precision Measurement of The Pion Form Factor

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Users Group Workshop and Annual Meeting

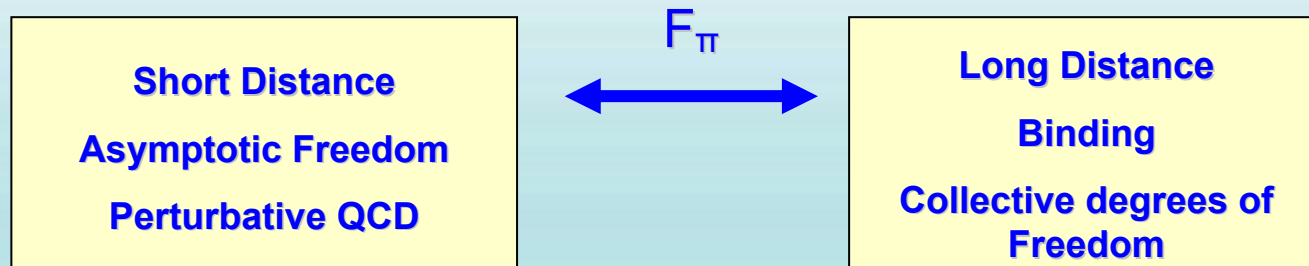
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- Pion Form Factor via Pion Electroproduction
- Precision Measurements in Hall C JLab
- Results ($F_{\pi-2}$)

Hadronic Form Factors in QCD

- Fundamental issue: quantitative description of hadrons in terms of underlying constituents
 - **Theory: Quantum Chromo-Dynamics (QCD) describes strong interactions**
 - **Degrees of freedom: quarks and gluons**



- Studies of short/long distance scales:
 - Theory – QCD framework, GPD's, lattice, models
 - Experiments – **form factors**, neutral weak nucleon structure

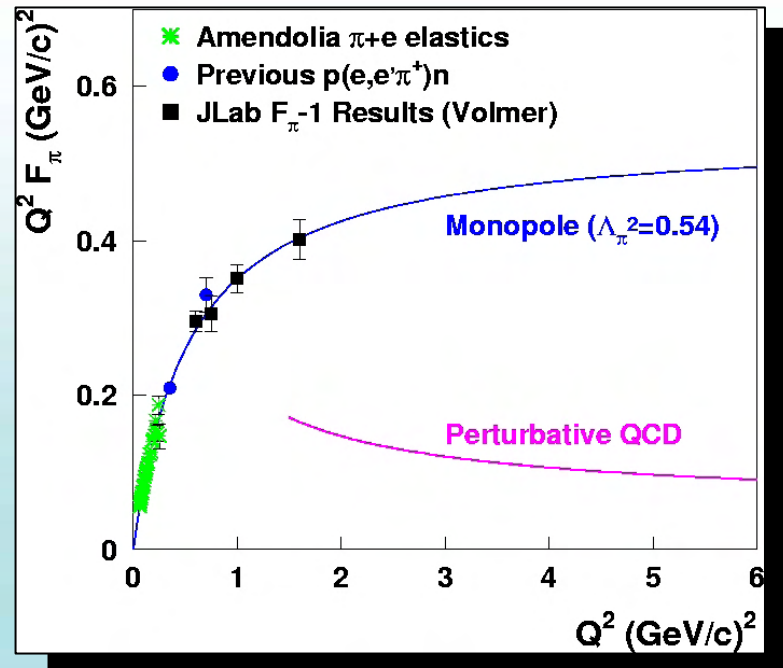
Pion Electromagnetic Form Factor

$F_{\pi}(Q^2)$ and pQCD

- Good observable for studies of hadronic structure
 - Simple valence structure, $q\bar{q}$
 - “Hydrogen atom” of QCD
- **High Q^2** scaling predicted by Farrar-Jackson (*PRL* **43** (1979) 246)

$$F_{\pi} \rightarrow 8\pi \frac{\alpha_s f_{\pi}^2}{Q^2}$$

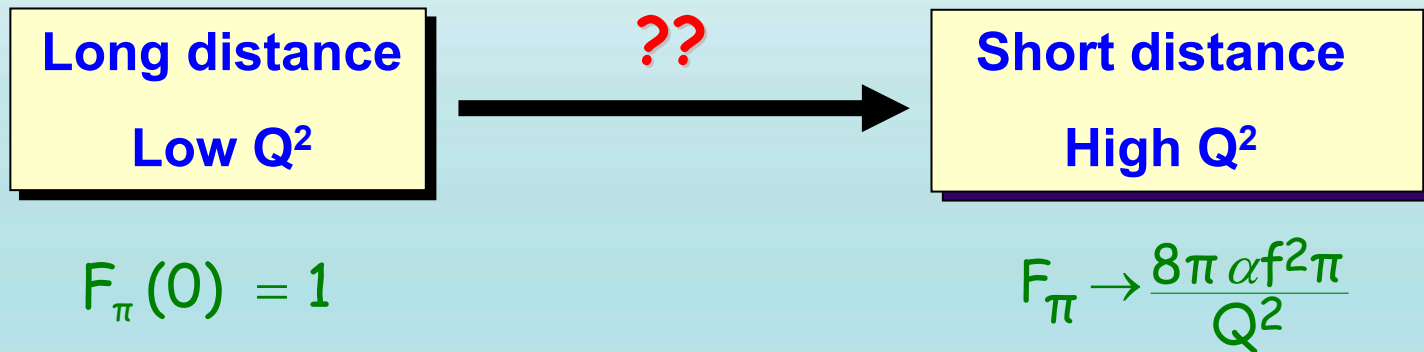
$f_{\pi}^2 = 133 \text{ MeV}$ is the $\pi^+ \rightarrow \mu^+ \nu$ decay constant



- **Small Q^2** : vector meson dominance gives reasonable description with normalization $F_{\pi}(0)=1$ by charge conservation

Summary F_π Calculations

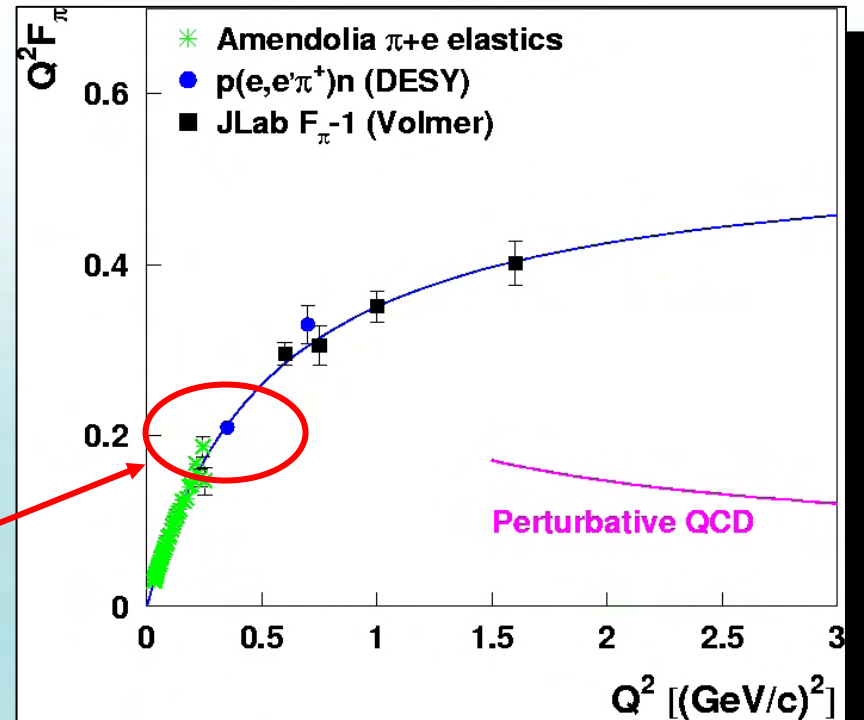
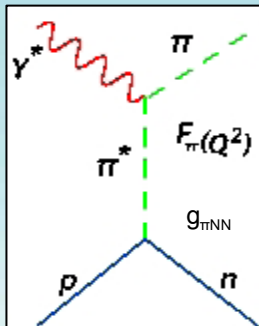
- Limits on F_π well defined and many model calculations available for transition region
- Key Point: Know there is asymptotic limit, but how to get there and what governs transition?



- **Need experimental data to study behavior of QCD in transition from long distance to short distance scales**

F_π via Pion Electroproduction

- F_π can be measured directly from π^+e scattering (S.R. Amendolia et al., NP **B277** (1986)) up to $Q^2 \sim 0.3$ GeV^2
- No “free pion” target – to extend measurement of F_π to larger Q^2 values use “virtual pion cloud” of the proton
- Method check - Extracted results are in good agreement with π^+e data

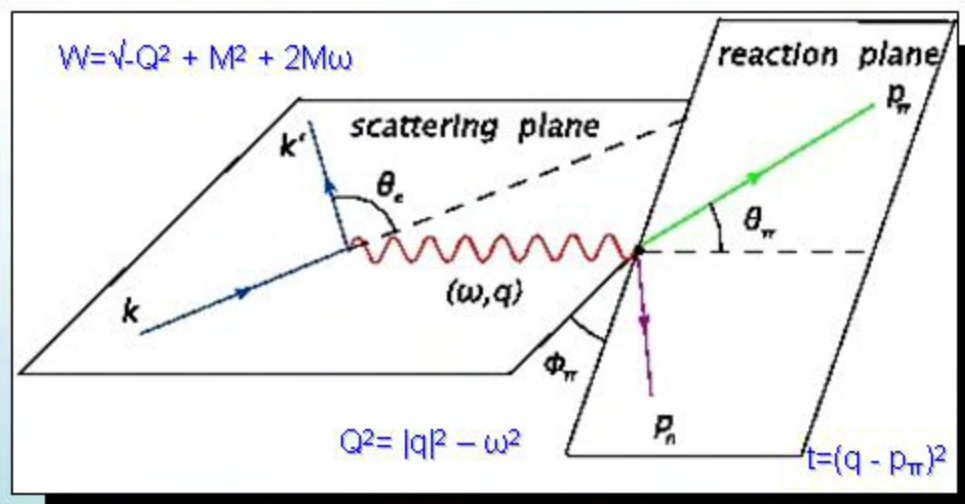


S.R. Amendolia et al., Nucl. Phys. **B277** (1986)

P. Brauel, et al., Z. Phys. **C3** (1979) 101.

J. Volmer et al PRL **86** (2001)

Extracting F_π from Pion Electroproduction Data



- The lab cross section can be expressed in terms of virtual photon flux (Γ_v), Jacobian (\mathcal{J}) and virtual photon cross section.

$$\frac{d\sigma}{dE d\Omega_\gamma d\Omega_\pi} = \Gamma_v \mathcal{J}(t, \varphi \rightarrow \Omega_\pi) \frac{d^2\sigma}{d\Omega_\pi}$$

$$\frac{d^2\sigma}{dt d\varphi} = \frac{d\sigma_T}{dt d\varphi} + \epsilon \frac{d\sigma_L}{dt d\varphi} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt d\varphi} \cos \varphi_\pi + \epsilon \frac{d\sigma_{TT}}{dt d\varphi} \cos 2 \varphi_\pi$$

- In t-pole approximation:

$$\sigma_L \propto \frac{-t g_{\pi NN}^2(t)}{(t - m_\pi^2)^2} Q^2 F_\pi^2(Q^2, t)$$

- In the analysis F_π is **extracted** from σ_L data using a model incorporating pion electroproduction (VGL/Regge)

Precision F_{π} data up to $Q^2=2.45$ GeV^2 ($F_{\pi-2}$)

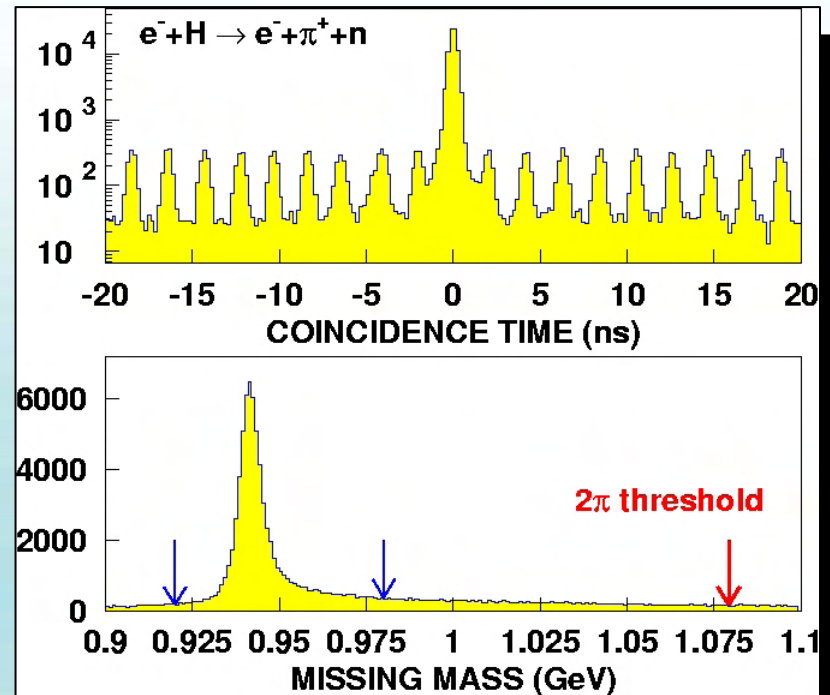
- Extension of $F_{\pi-1}$ at highest possible value of Q^2 with 6 GeV beam at JLab
 - New data at higher W
 - Repeat $Q^2=1.60 \text{ GeV}^2$ closer to $t=m_{\pi}$
- Successfully completed in Hall C at JLab 2003
 - Coincidence measurement: HMS detects pions, SOS detects electrons
 - Pion electroproduction from H and ^2H
 - Extracted σ_L , σ_T , σ_{TT} , and σ_{LT} at $W=2.22 \text{ GeV}$



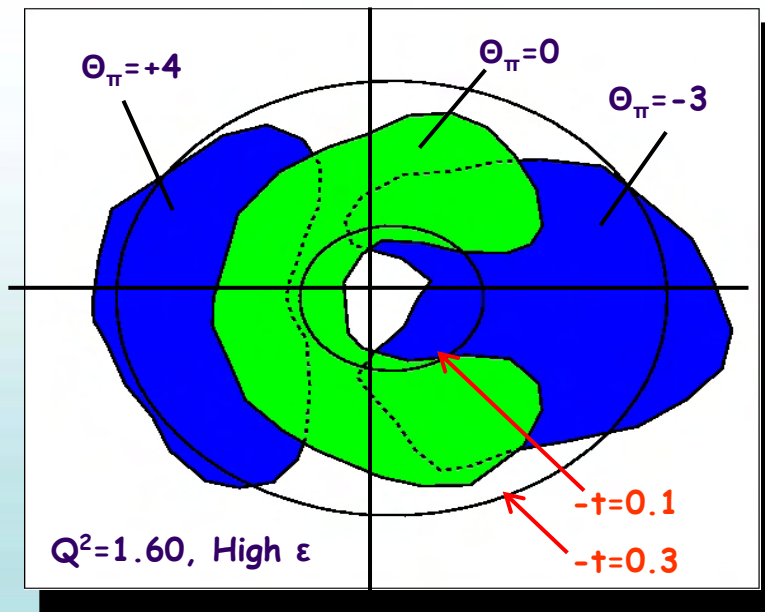
Exp	Q^2 (GeV^2)	W (GeV)	$ t $ (GeV^2)	E_e (GeV)
$F_{\pi-1}$	0.6-1.6	1.95	0.03-0.150	2.445-4.045
$F_{\pi-2}$	1.6,2.45	2.22	0.093,0.189	3.779-5.246

Good Event Selection

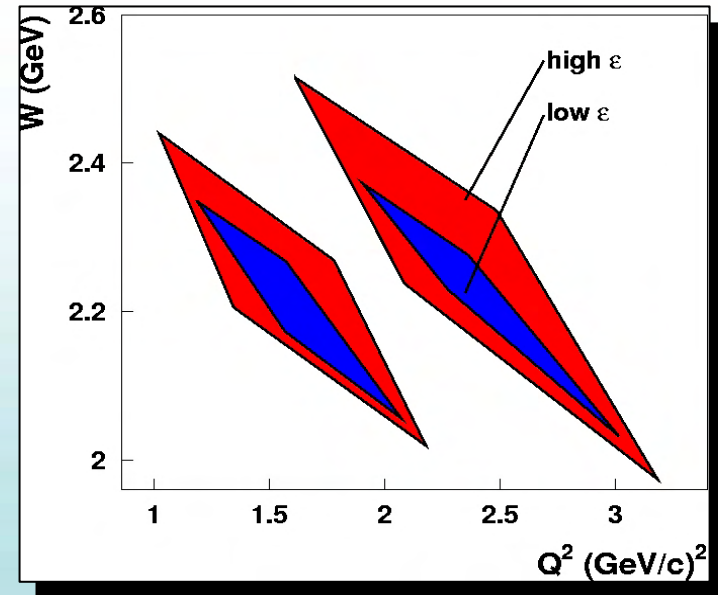
- Coincidence measurement between charged pions in HMS and electrons in SOS
 - Coincidence time resolution ~200-230 ps
 - Cut: ± 1 ns
- Protons in HMS rejected using coincidence time and Aerogel Cerenkov
- Electrons in SOS identified by gas Cerenkov /Calorimeter
- Exclusive neutron final state selected with missing mass cut: $0.92 < MM < 0.98$ GeV



$F_{\pi-2}$ Kinematic Coverage



- Have full coverage in ϕ BUT acceptance not uniform
- Measure σ_{TT} and σ_{LT} by taking data at three angles: $\theta_{\pi q}=0^\circ$, $+4^\circ$, -3°



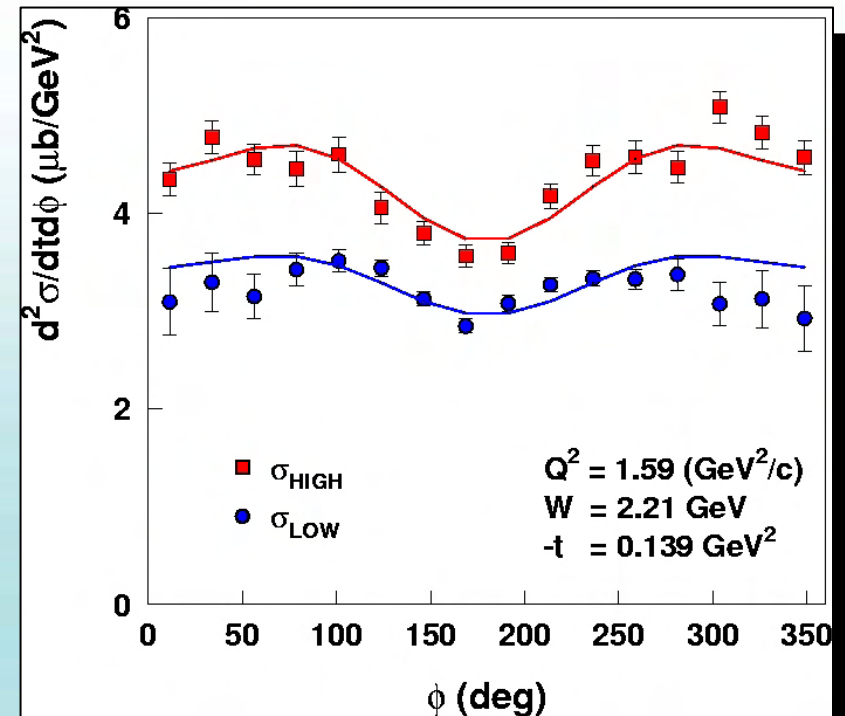
- W/Q^2 phase space covered at low and high ϵ is different
- For L-T separation use cuts to define common W/Q^2 phase space

F_π-2 Data Analysis

- Compare experimental yields to Monte Carlo of the experiment
 - Model for H(e,e'π⁺) based on pion electroproduction data
 - Radiative effects, pion decay, energy loss, multiple scattering
 - COSY model for spectrometer optics

$$\sigma_{\text{exp}} = \frac{Y_{\text{exp}}}{Y_{\text{SIMC}}} \sigma_{\text{model}}$$

- Extract σ_L by simultaneous fit using measured azimuthal angle (ϕ_{π}) and knowledge of photon polarization (ϵ).



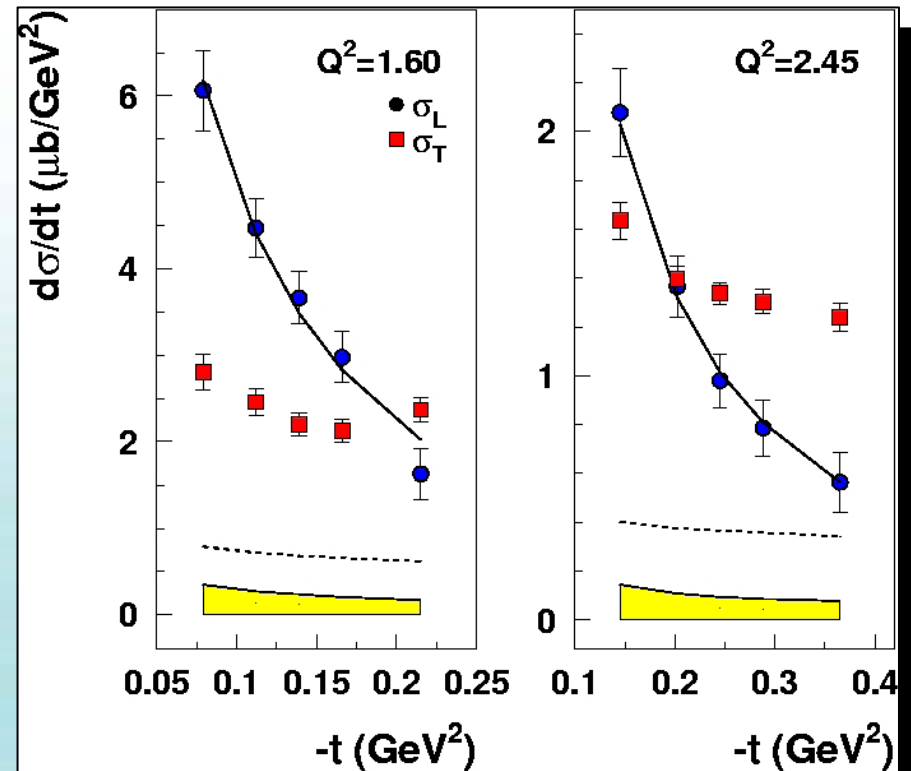
$$\frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt d\phi} + \frac{d\sigma_T}{dt d\phi} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt d\phi} \cos\phi_{\pi} + \epsilon \frac{d\sigma_{TT}}{dt d\phi} \cos 2\phi_{\pi}$$

Comparison to VGL/Regge Model

- Pion electroproduction in terms of exchange of π and ρ like particles (*Vanderhaeghen, Guidal, Laget, PRC 57 (1998) 1454*)
 - Model parameters fixed from pion photoproduction
 - Free parameters: F_π , F_ρ
 - ρ exchange does not significantly influence σ_L at small $-t$

$$F_\pi = \frac{1}{1 + Q^2/\Lambda_\pi^2}$$

Fit to σ_L to model gives F_π at each Q^2

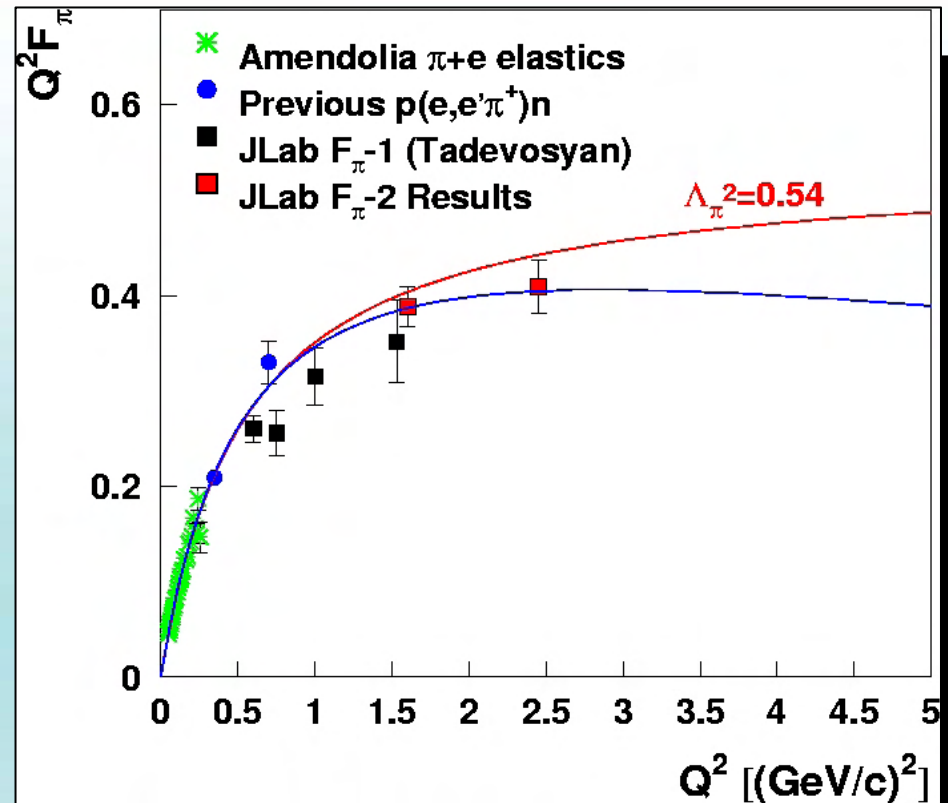


$$\Lambda_\pi^2 = 0.513, 0.491 \text{ GeV}^2, \Lambda_\rho^2 = 1.7 \text{ GeV}^2$$

- Points include 1.0(0.6)% point-to-point systematic uncertainty (dominated by acceptance)
- 3.5 % normalization (correlated) uncertainty (radiative corrections, pion absorption, pion decay, kinematic uncertainties)
- 1.8(1.9)% “t-correlated” uncertainties, influence t-dependence at fixed ε

F_{π^-2} Results

- Data point at $Q^2=1.60 \text{ GeV}^2$ to check model dependence of F_{π^-} extraction
 - Agreement between F_{π^-1} ($W=1.95 \text{ GeV}$) / F_{π^-2} ($W=2.22 \text{ GeV}$) to $\sim 5\%$
 - Note: new point is closer to the pion pole by $\sim 40\%$
- JLab F_{π^-} data below monopole form, $\Lambda_{\pi}^2=0.54 \text{ GeV}^2$
 - Indicates relative contribution of hard/soft physics at moderate Q^2



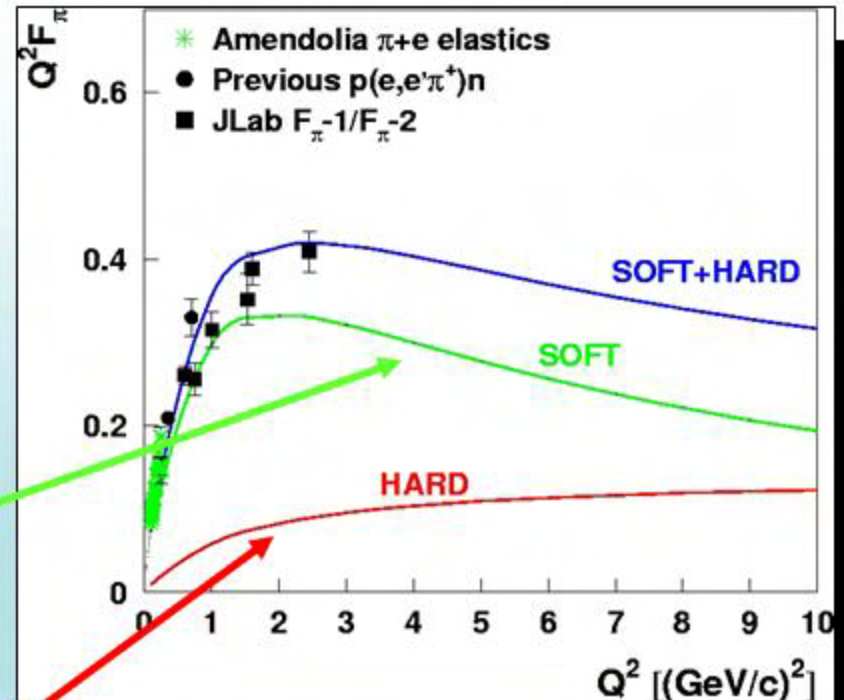
Hard and Soft Contributions

- QCD Sum Rules
 - Interpolate between perturbative and non-perturbative regions using dispersion relations and Operator Product Expansion
- SOFT: QCD SR \rightarrow Local Quark-Hadron duality relation

$$F_{\pi}^{\text{soft}} = 1 - \frac{1 + 6s_0/Q^2}{(1 + 4s_0/Q^2)^{3/2}}$$

- HARD: Based on interpolation between value at $Q^2=0$ and asymptotic behaviour

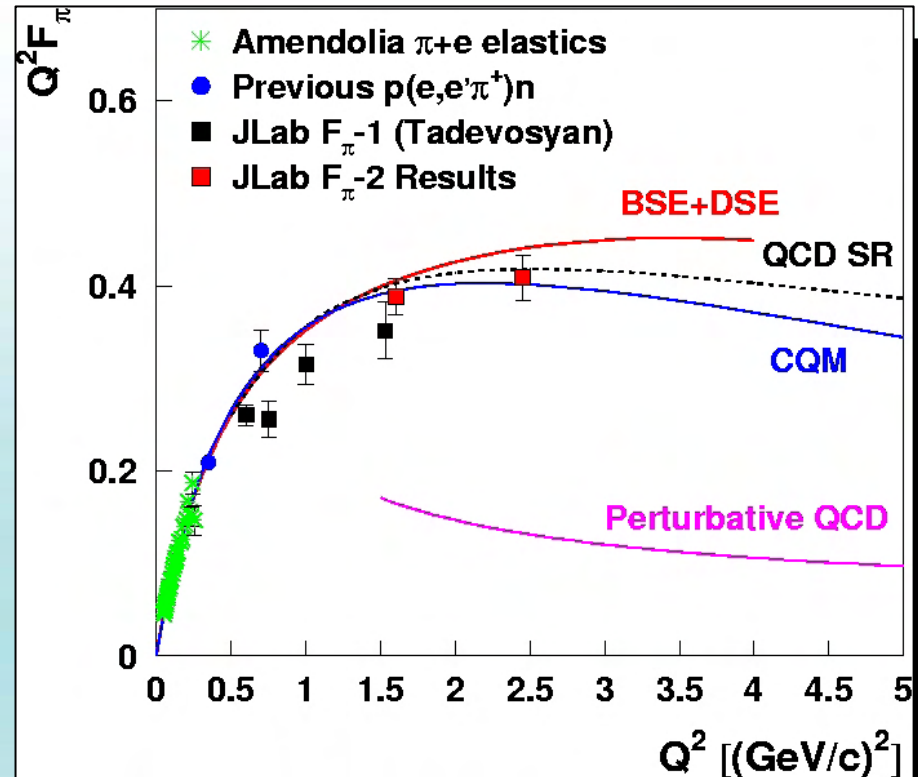
$$F_{\pi}^{\text{hard}} = \frac{\alpha_s}{\pi} \frac{1}{(1 + Q^2/2s_0)}$$



V.A. Nesterenko and A.V. Radyushkin, Phys. Lett. B115 (1982) 410

Compare F_{π} Models

- Variety of models on the market – how do we know which one is “right”?
- $F_{\pi-2}$ result in a region of Q^2 where calculations start to diverge
 - BUT cannot rule out any calculations yet
- Still far from pQCD prediction



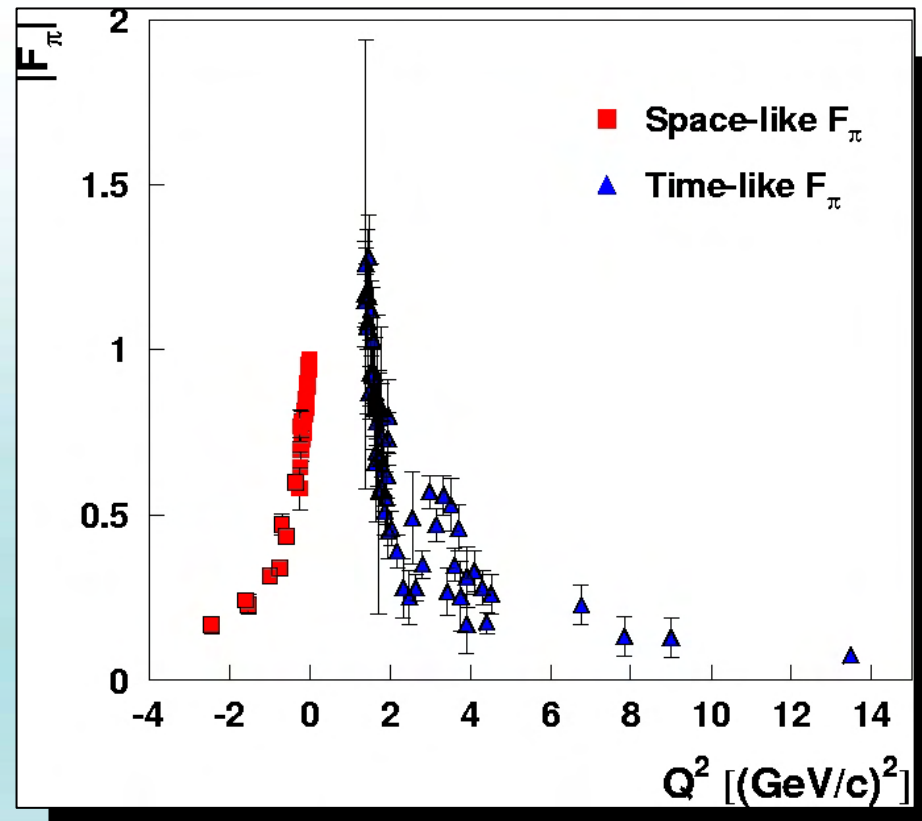
V.A. Nesterenko and A.V. Radyushkin, Phys. Lett. **B115** (1982) 410

P. Maris and P. Tandy Phys Rev **C61** (2000)

C.-W. Hwang, Phys Rev **D64** (2001)

F_π Time-like and Space-like

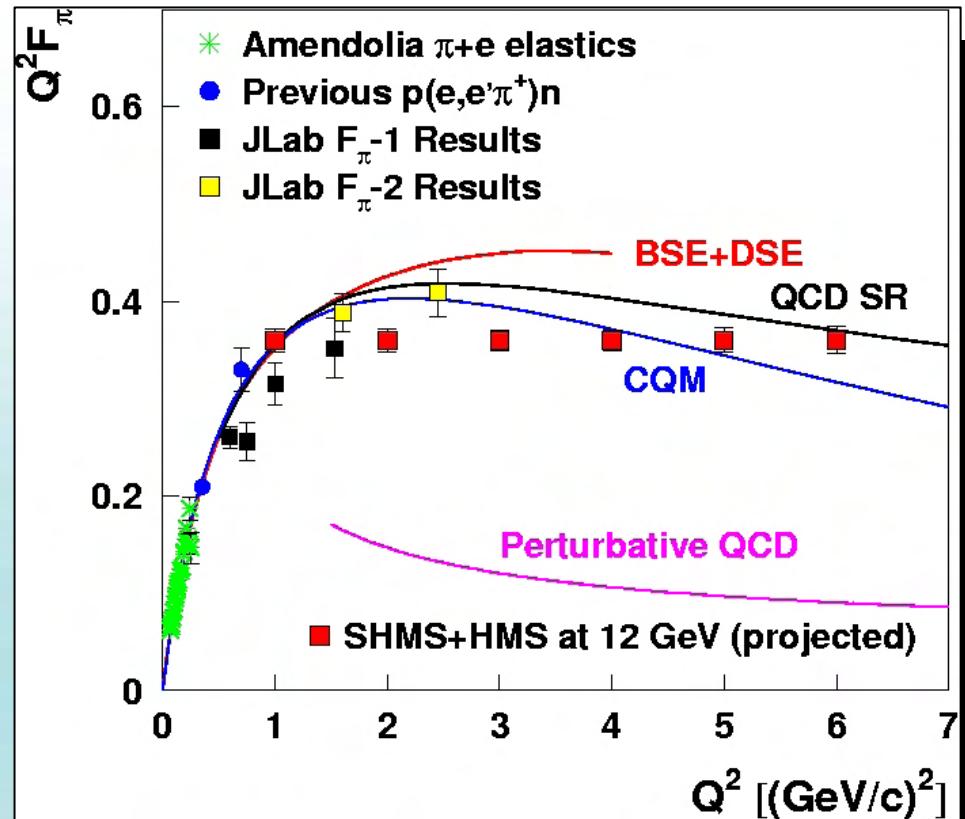
- Expect same asymptotic prediction for both space-like and time-like data
 - The way one gets there may be different
- Calculations in time-like region complicated by explicit resonances



Timelike data from P.K. Zweber Ph.D. thesis (2006)

F_{π} at 12 GeV

- Significant progress on theoretical front expected in next 5 years – Lattice, GPD etc.
- Experiments need higher energy electron beam to reach the kinematic region where pQCD expectation may be approached
- SHMS+HMS in Hall C will allow F_{π} to be measured up to $Q^2 \sim 6 \text{ GeV}^2$ – 12 GeV proposal
- Small forward angle crucial for F_{π} experiment since need to reach low $-t$ values.



Summary

- F_{π} good observable to study transition region to perturbative QCD
 - Contribution of soft and hard physics
- $F_{\pi-2}$ results up to $Q^2 = 2.45 \text{ GeV}^2$
 - Data will constrain models describing the treatment of non-perturbative physics at higher Q^2
 - Still far from pQCD prediction
 - Good agreement with data point at $Q^2=1.60 \text{ GeV}^2$ gives confidence in reliability of extraction method
- Studies of F_{π} at higher electron beam energy will allow us to reach the kinematic range where pQCD expectation may be approached
 - Measurement at JLab with 11 GeV beam up to $Q^2 \sim 6 \text{ GeV}^2$

JLab F_π-2 Collaboration

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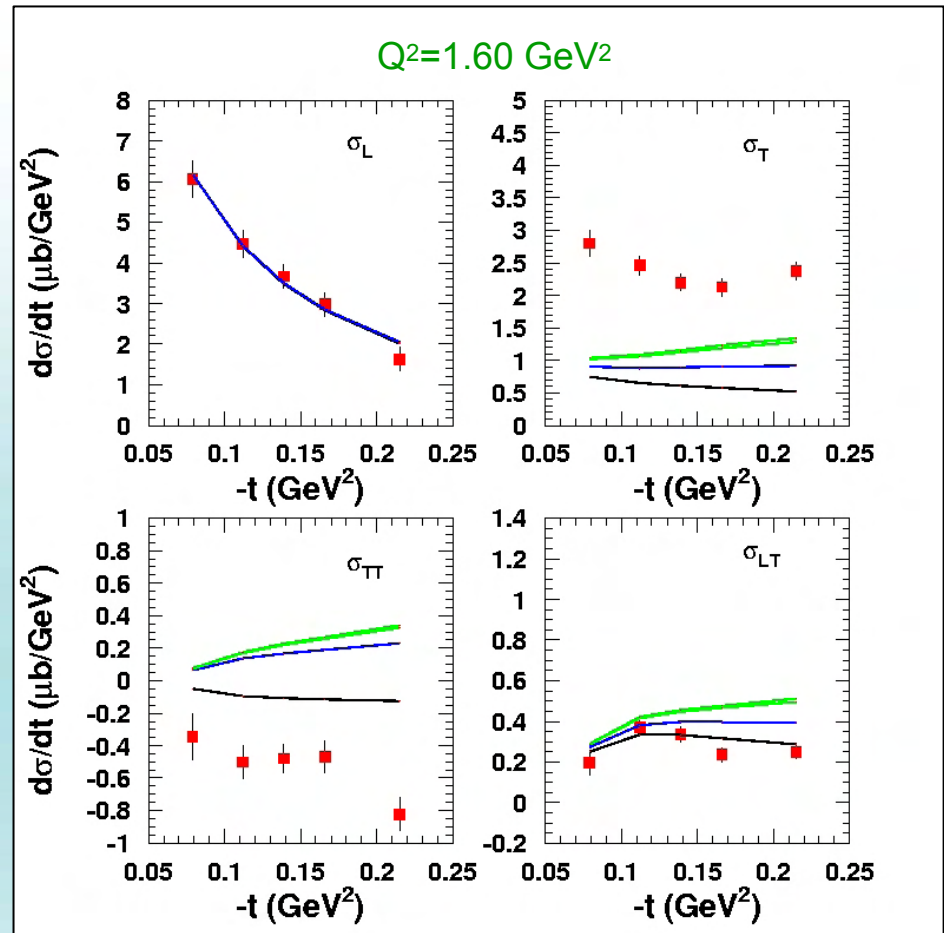
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Comparison to VGL – ρ trajectory

- Influence of ρ cutoff on cross sections – vary Λ_ρ between 1.1 and 5 GeV^2
 - σ_T, σ_{TT} systematically underpredicted
 - Little influence on σ_L

Q^2 (GeV/c) ²	$ t $ (GeV/c) ²	ρ exchange effect
1.60	0.06-0.21	0.5-1.0%
2.45	0.11-0.37	0.5-3.0%



$$\Lambda_{\pi}^2 = 0.513, 0.491 \text{ GeV}^2$$

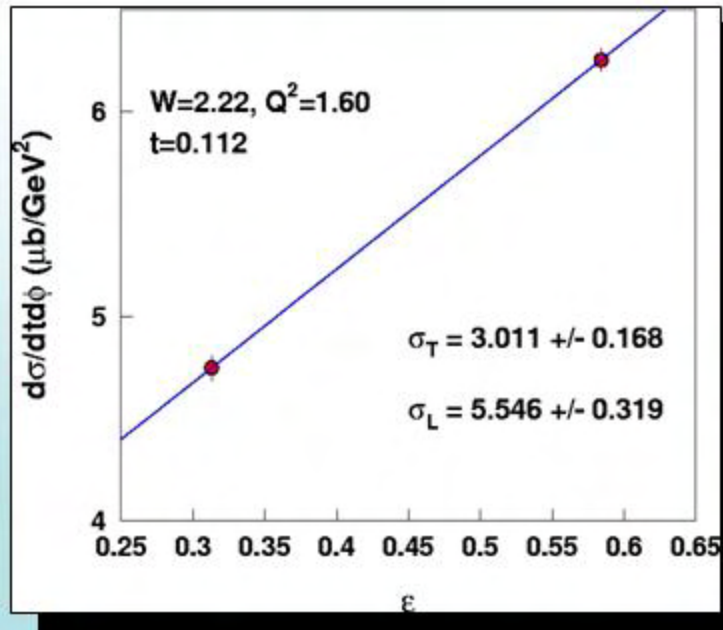
F_{π^-2} Uncertainties

- Uncertainty in separated cross sections has both statistical and systematic sources
- Statistical uncertainty in ranges between 1 and 2%

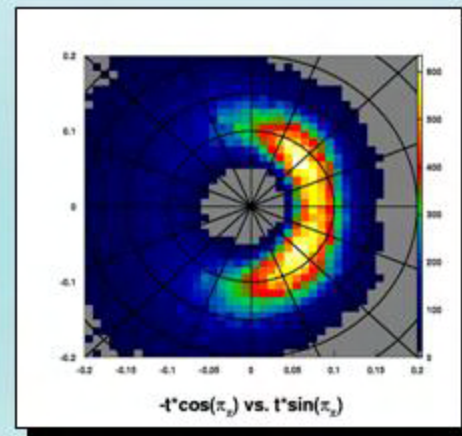
Source	Pt-Pt	Scale	t-correlated
Acceptance	1.0(0.6)%	1.0%	0.6%
Radiative Corrections	0.1%	2.0%	0.4%
Pion Absorption	-	2.0%	0.1%
Pion Decay	0.03%	1.0%	-
Model Dependence	0.2%	-	1.1(1.3)%
Kinematics	0.2%	-	1.0%
HMS Tracking	0.1%	1.0%	0.4%
Charge	-	0.5%	0.3%
Target Thickness	-	0.8%	0.2%
Detection Efficiency	-	0.5%	0.3%

- Point-to-point errors amplified by $1/\Delta\varepsilon$ in L-T separation
- Scale errors propagate directly into separated cross section
- Uncertainties in spectrometer quantities parameterized using over-constrained ${}^1\text{H}(e,e'p)$ reaction
 - Beam energy and momenta to $<0.1\%$
 - Spectrometer angles to $\sim 0.5\text{mrad}$
- Spectrometer acceptance verified by comparing e-p elastic scattering data to global parameterization
 - Agreement better than 2%

“Simple” Longitudinal-Transverse Separation



- For **uniform** ϕ -acceptance, $\sigma_{TT}, \sigma_{LT} \rightarrow 0$ when integrated over ϕ
- Determine $\sigma_T + \varepsilon \sigma_L$ for high and low ε in each t -bin for each Q^2
- Isolate σ_L , by varying photon polarization, ε

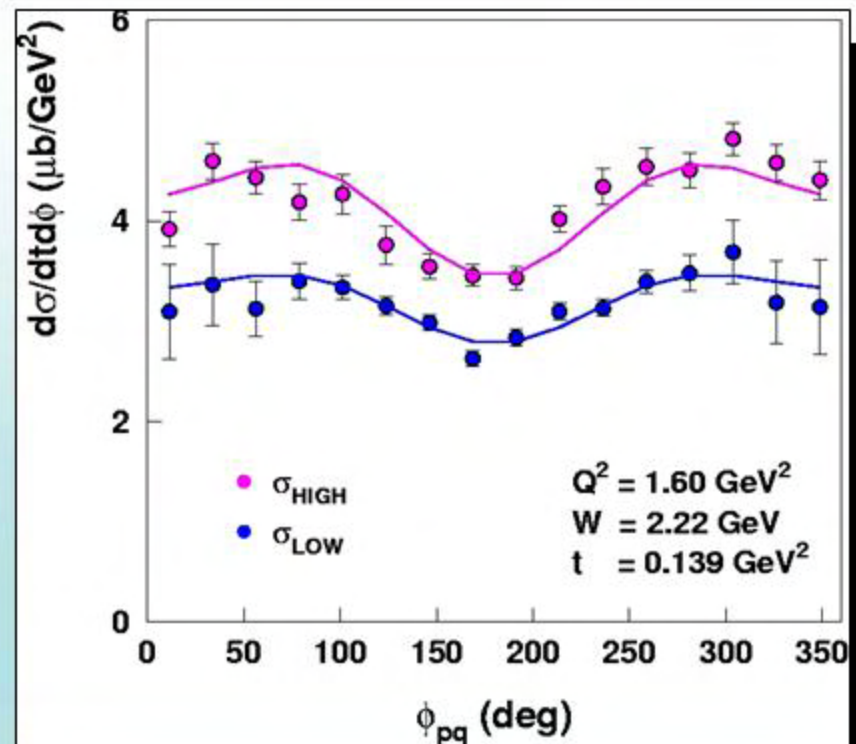


$$\varepsilon = \left(1 + 2 \left(1 + \frac{W^2}{Q^2} \right) \tan^2 \left(\frac{\theta_e}{2} \right) \right)^{-1}$$

$$\frac{d^2\sigma}{dt d\phi} = \frac{d\sigma_T}{dt d\phi} + \varepsilon \frac{d\sigma_L}{dt d\phi} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt d\phi} \cos \phi_\pi + \varepsilon \frac{d\sigma_{TT}}{dt d\phi} \cos 2\phi_\pi$$

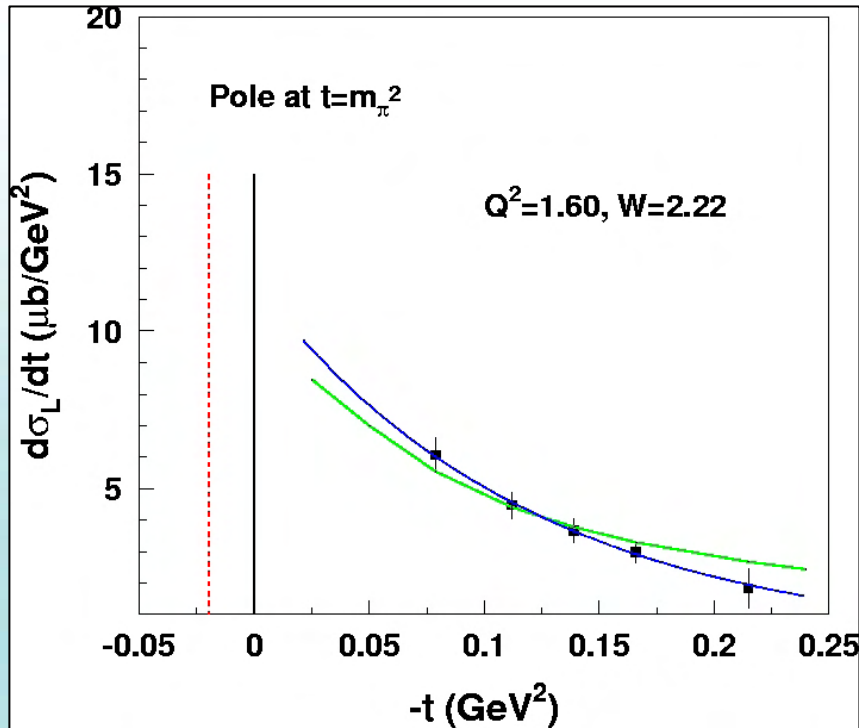
“Real” Cross Section Separation

- Cross Section Extraction
 - ϕ acceptance not uniform
 - In reality, must measure σ_{LT} and σ_{TT}
- Extract σ_L by simultaneous fit using measured azimuthal angle (ϕ_{π}) and knowledge of photon polarization (ϵ)



$$\frac{d^2\sigma}{dt d\phi} = \frac{d\sigma_T}{dt d\phi} + \epsilon \frac{d\sigma_L}{dt d\phi} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt d\phi} \cos\phi_{\pi} + \epsilon \frac{d\sigma_{TT}}{dt d\phi} \cos 2\phi_{\pi}$$

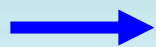
Extracting F_π from σ_L Data



- In t-pole approximation:

$$\sigma_L \propto \frac{-t g_{\pi NN}^2(t)}{(t-m_\pi^2)^2} Q^2 F_\pi^2(Q^2, t)$$

- Want smallest possible $-t$ to maximize contribution from π -pole to σ_L
- Need to know t-dependence of σ_L to extract F_π



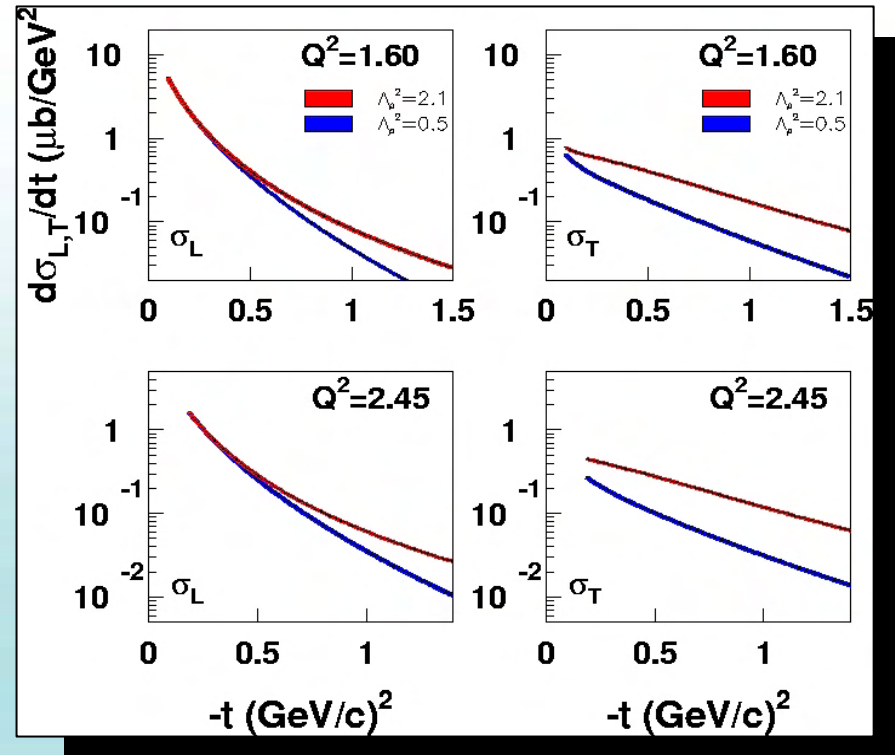
- In the analysis F_π is extracted using a model incorporating pion electroproduction (VGL/Regge)

VGL Regge Model

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 - Free parameters: F_π
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$$F_\pi = \frac{1}{1 + Q^2/\Lambda_\pi^2}$$

Fit to σ_L to model gives F_π at each Q^2



Q^2 (GeV/c) 2	$ t $ (GeV/c) 2	ρ exchange effect
1.60	0.06-0.21	0.5-1.0%
2.45	0.11-0.37	0.5-3.0%

Precision F_π Data From JLab

($F_\pi - 1$)

- Ran in Hall C at JLab in 1998, thesis students: **J. Volmer and K. Vansyoc**
 - Measured pion electroproduction from H and ^2H
 - Extracted σ_L , σ_T , σ_{TT} , and σ_{LT} at $W=1.95$ GeV, $Q^2 = 0.6, 0.75, 1.0, 1.6$ GeV 2
- F_π was determined by comparing σ_L to a Regge calculation by Vanderhaeghen, Guidal, Laget (VGL, PRC **57**(1998)1454)
 - Model parameters fixed from pion photo-production, free parameters: F_π and F_ρ .

$$F_\pi = \frac{1}{1 + Q^2 / \Lambda_\pi^2}$$

Fit to σ_L to model gives F_π at each Q^2

