



11th Workshop on Hadron physics in China  
and Opportunities Worldwide

August 23 - 28, 2019

Nankai University

# 3D nucleon structure programm in Hall B at JLab

JUSTUS-LIEBIG-



UNIVERSITÄT  
GIESSEN



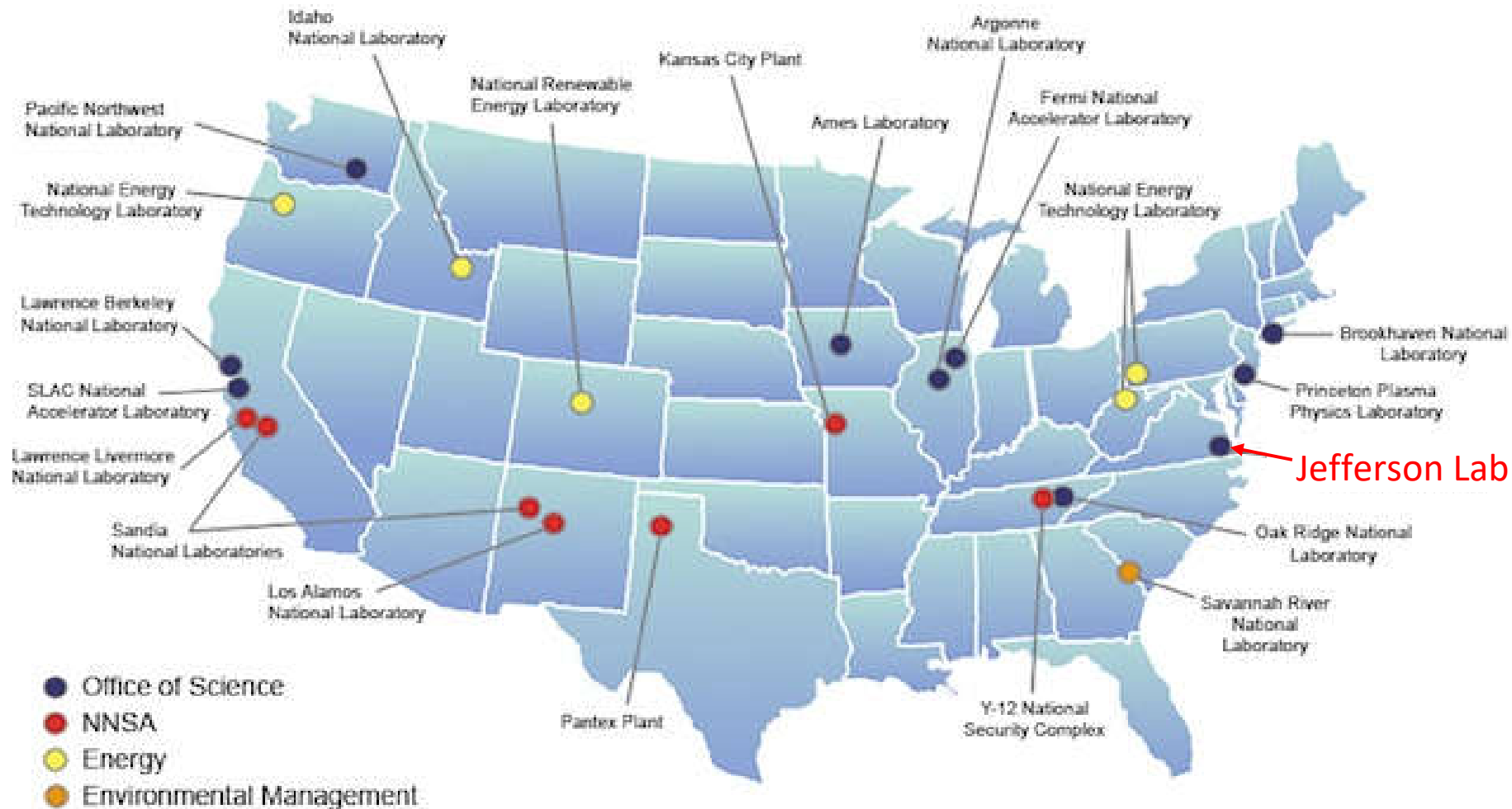
Stefan Diehl

*Justus Liebig University Giessen*

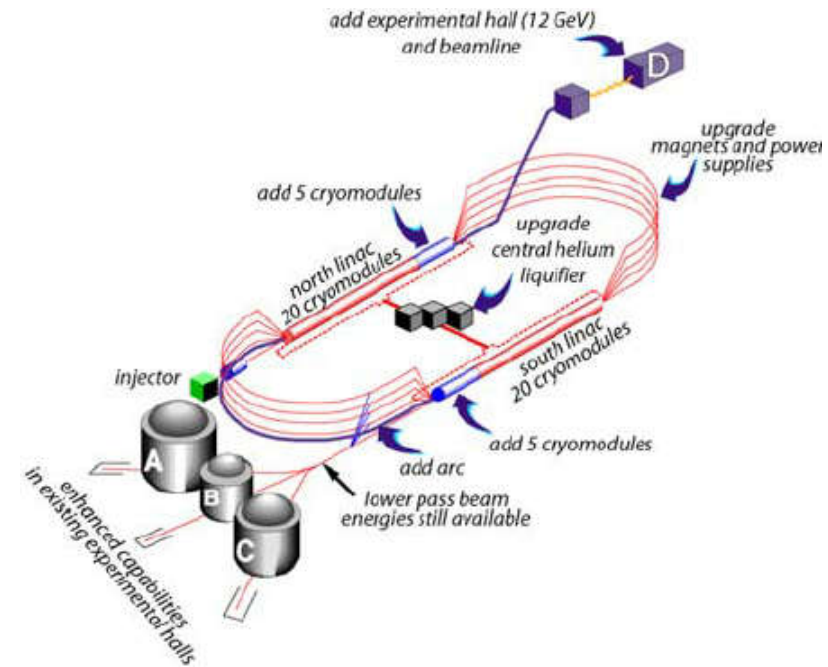
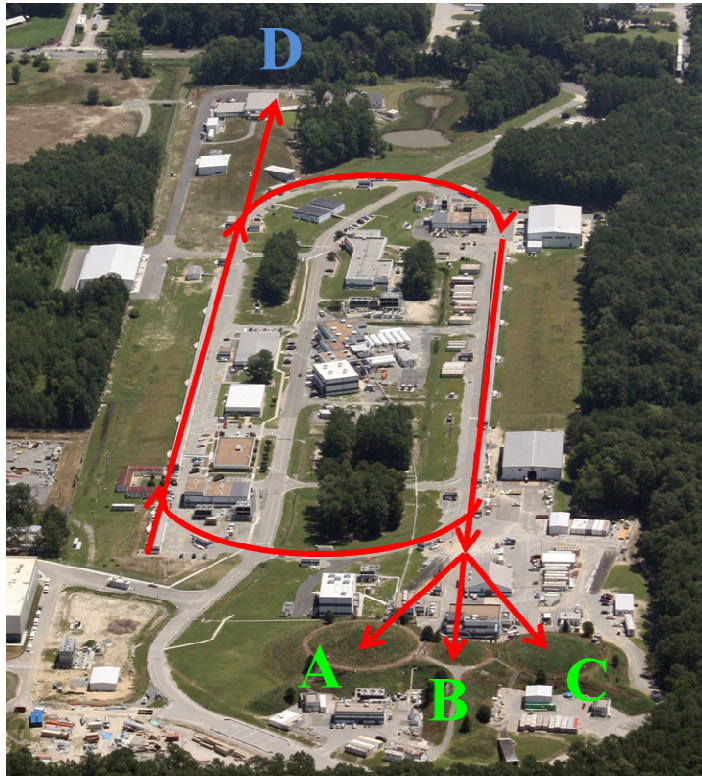
*University of Connecticut*

August 23, 2019

# Thomas Jefferson National Accelerator Facility (Jefferson Lab)



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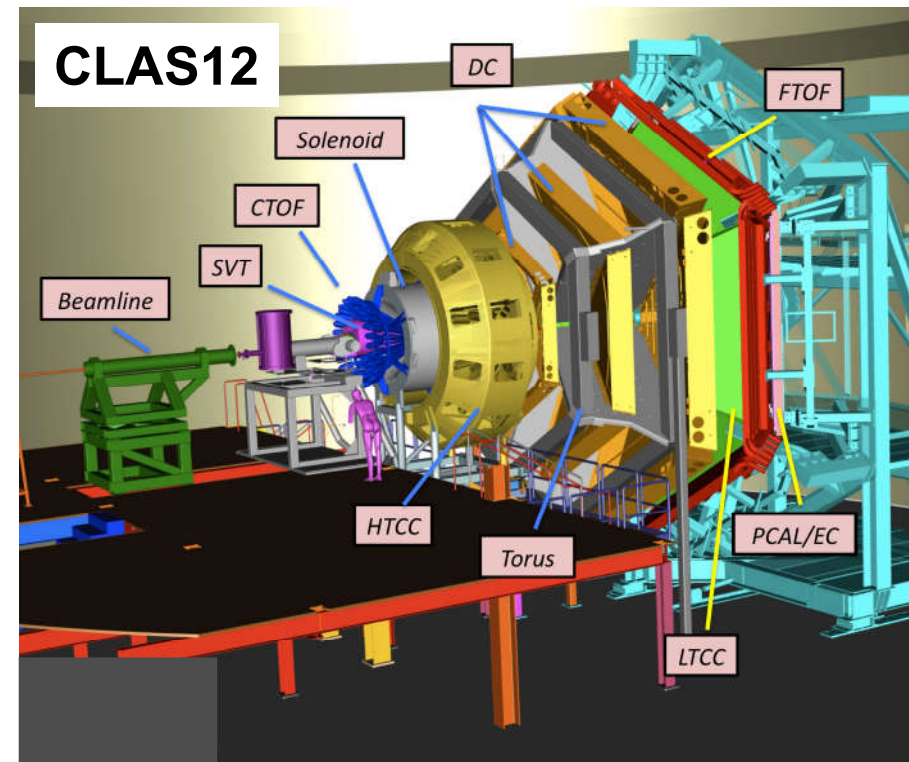
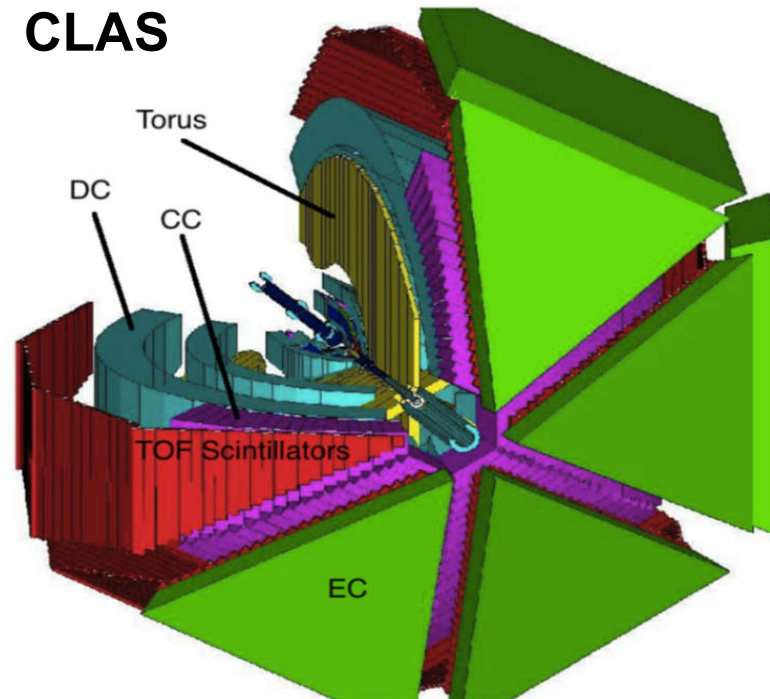
## Physics Operation

- ➡ CEBAF Upgrade completed in September 2017
  - electron beam
  - $E_{\text{max}} = 12 \text{ GeV}$
  - $I_{\text{max}} = 90 \mu\text{A}$
  - $\text{Pol}_{\text{max}} \sim 90\%$

- 4 halls running simultaneously since January 2018
- Highest intensity tagged photon beam at 9 GeV
- World-record polarized electron beams
- Nuclear experiments at ultra-high luminosities, up to  $10^{39}$  electrons-nucleons /cm<sup>2</sup>/s

## CLAS / CLAS12 in Hall B at Jefferson Lab

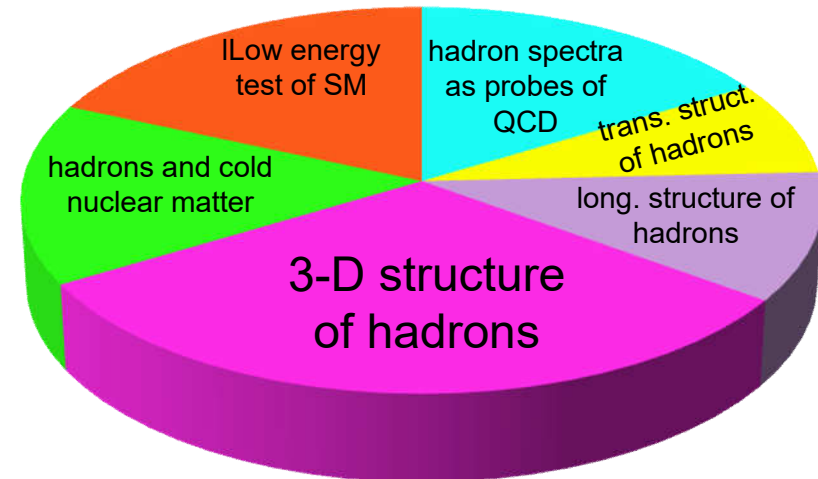
### CLAS



- ▶  $\mathcal{L} = 1 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- ▶ Inclusive electron trigger (all calibration reactions will be analyzed in parallel)
- ▶ Electrons in the forward detector
- ▶ Protons in the central detector and forward detector
- ▶ Photons in the forward detector and forward tagger

## Jefferson Lab Experiments for the next decade

- JLab's primary mission is to explore the fundamental nature of **confined states of quarks and gluons**, including the nucleons that comprise the mass of the visible universe.
  - How are quarks confined in nuclear matter?
  - What is the internal landscape of protons and neutrons?
  - How do the properties of protons and neutrons emerge from their constituent quarks and gluons?
  - How do the nuclear forces that lead to nuclei, arise from the basic interactions?
  - Can we discover evidence for Physics beyond the standard model?



**12 GeV Physics Program:  
A Decade of Approved  
Experiments**

## QCD Science Questions

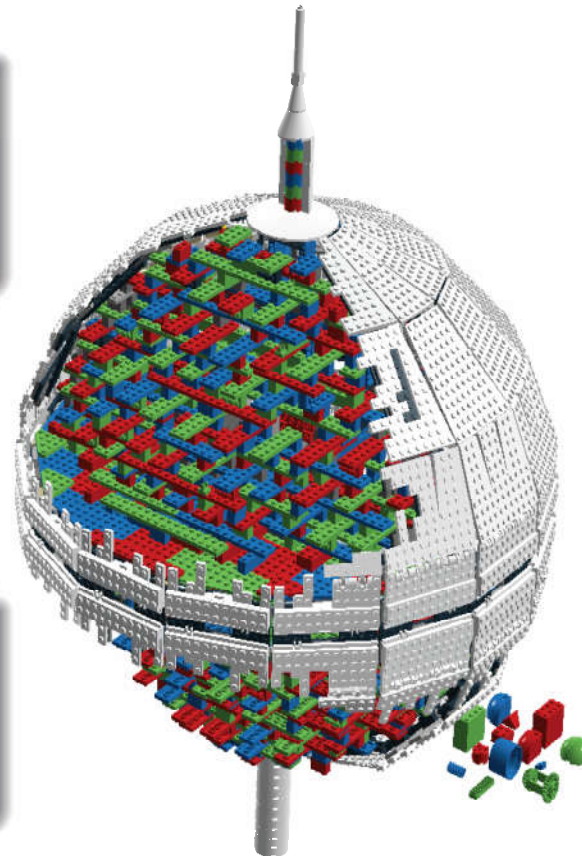
How are the quarks and gluons, and their intrinsic spins distributed in space & momentum inside the nucleon?

How can we recover the well-known characteristics of the nucleon from the properties of its **colored building blocks**?

Mass?  
Spin?  
Charge?

...

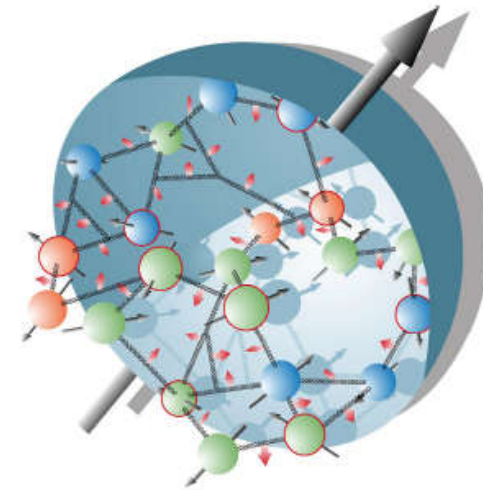
What are the relevant **effective degrees of freedom** and **effective interaction** at large distance?



What is the role of orbital angular motion?

## The Incomplete Nucleon: Spin Puzzle

- Proton has spin-1/2
- Proton is a composite system consisting of spin-1/2 quarks and spin-1 gluons



This implies that the sum of angular momentum of quarks and gluons together must amount to 1/2. Can be due to:

Quark spin

Quark orbital momentum

Gluon spin

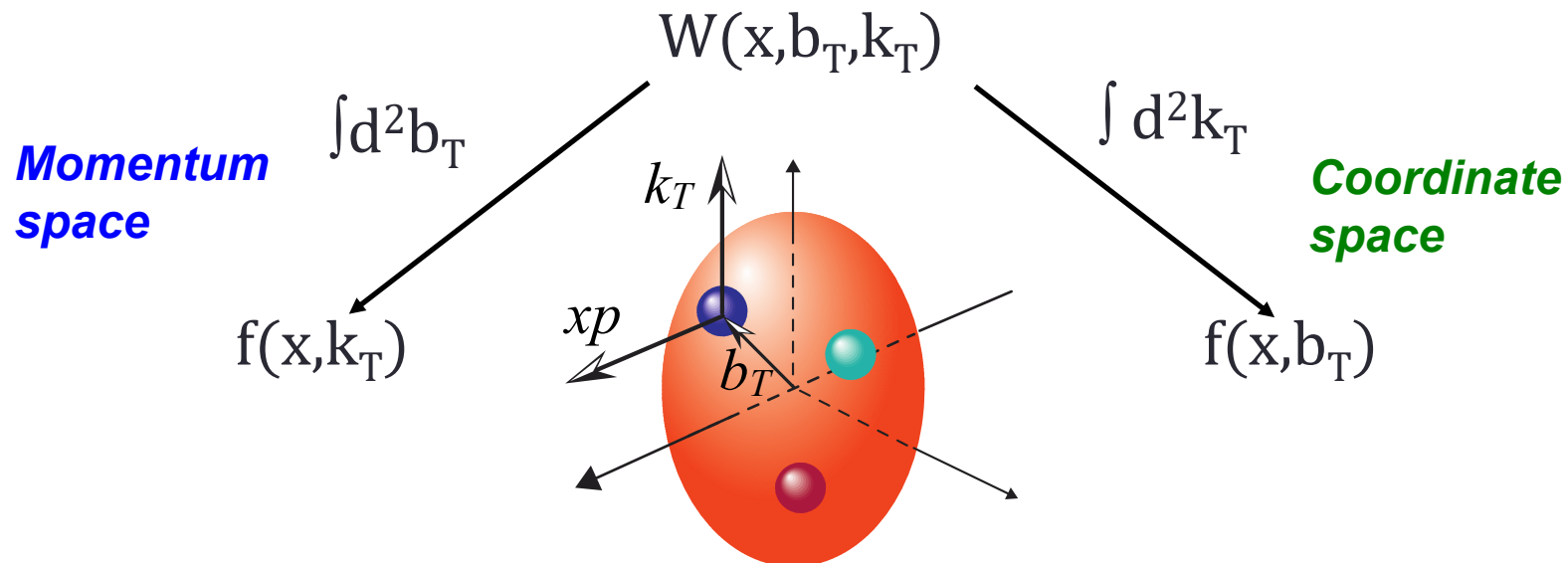
Gluon orbital momentum

**Classical:  $\sim \mathbf{r} \times \mathbf{p}$**

**Needs a cross-product or something three-dimensional!**

## 3-Dimensional Imaging Quarks and Gluons

### Wigner functions $W(x, b_T, k_T)$



Spin-dependent 3D **momentum space** images from semi-inclusive scattering  
 → **TMDs**

Spin-dependent 2D **coordinate space** (transverse) + 1D (longitudinal momentum) images from exclusive scattering  
 → **GPDs**

Position and momentum → Orbital motion of quarks and gluons



## Generalized Parton Distributions (GPDs)

$$W_{\Gamma}(\mathbf{r}, k) = \frac{1}{2M_N} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{-i\mathbf{q}\cdot\mathbf{r}} \left\langle \mathbf{q}/2 \left| \hat{W}_{\Gamma}(0, k) \right| -\mathbf{q}/2 \right\rangle ,$$

$$W_{\Gamma}(\mathbf{r}, \mathbf{k}) = \int \frac{dk^-}{(2\pi)^2} W_{\Gamma}(\mathbf{r}, k)$$

		quark pol.		
		N/q	$U$	$L$
nucleon pol.	$U$	$H$		$\bar{E}_T$
	$L$		$\tilde{H}$	$\tilde{E}_T$
	$T$	$E$	$\tilde{E}$	$H_T, \tilde{H}_T$

$\bar{E}_T = 2\tilde{H}_T + E_T$

Integrate over transverse  
**momentum** space

Generalized Parton  
Distributions (GPD)  $H, \tilde{H}, E, \tilde{E}$

3-D nucleon imaging in  
transverse coordinate and  
longitudinal momentum space

## Interpretation of GPDs in the kinematic limits

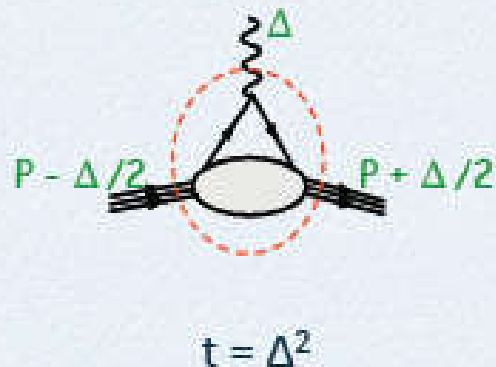
→ in forward kinematics ( $\xi=0, t=0$ ) : **PDF limit**

$$H^q(x, \xi = 0, t = 0) = q(x)$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

$E, \tilde{E}^q$  do not appear in forward kinematics (DIS) → **new information**

→ first moments of GPDs : **elastic form factor limit**



$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t)$$

→ Dirac FF

$$\int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t)$$

→ Pauli FF

$$\int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = G_A^q(t)$$

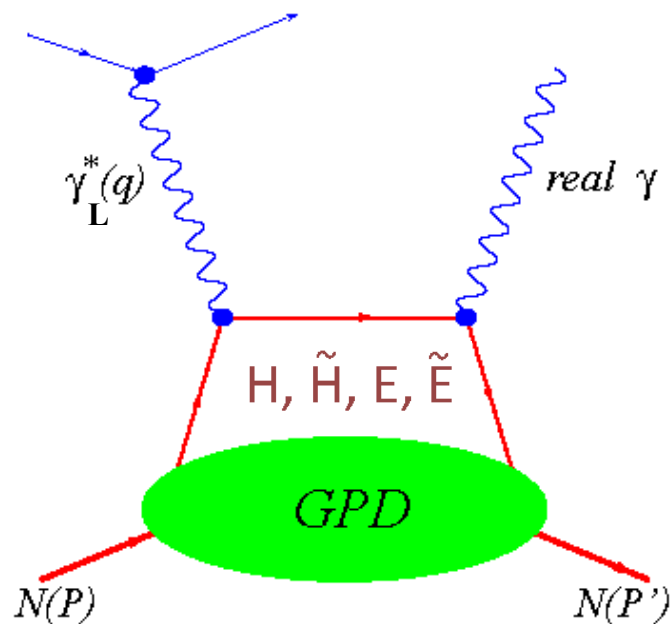
→ axial FF

$$\int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = G_P^q(t)$$

→ pseudoscalar FF

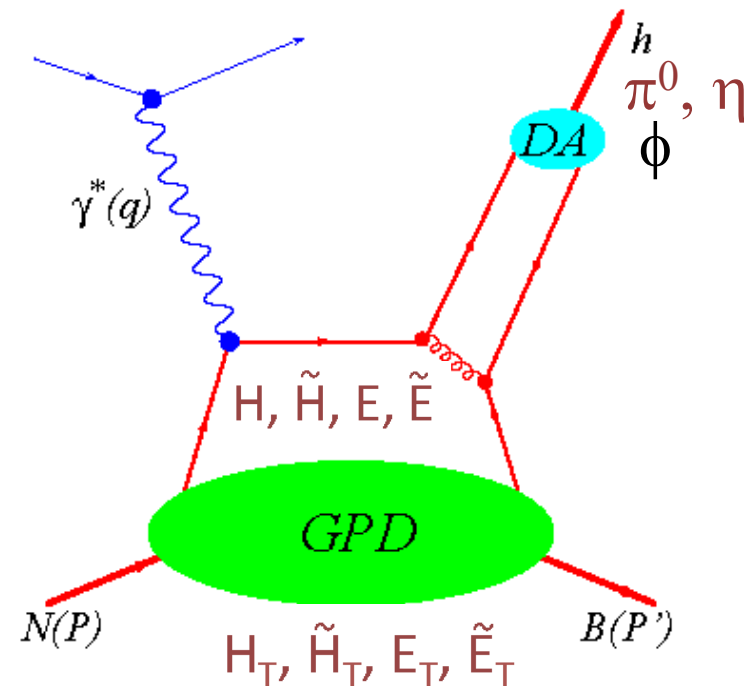
## Study GPDs: Deeply Virtual Exclusive Processes

### Deeply Virtual Compton Scattering (DVCS)



- + Clean process
- Only sensitive to chiral even GPDs

### Deeply Virtual Meson Production (DVMP)



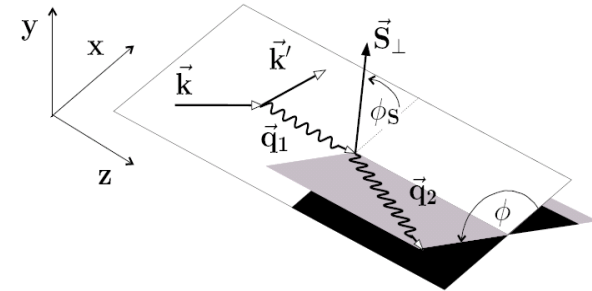
- + Enables Flavour decomposition of GPDs
- + Access to transversity degrees of freedom described by chiral-odd GPDs
- Distribution Amplitude (DA) is involved as additional soft non pert. Quantity

## A path towards extracting GPDs

$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

$$\xi \sim x_B/(2-x_B)$$

$$k = t/4M^2$$



Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \{F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E\} d\phi$$



$$H(\xi, t)$$

Unpolarized beam, longitudinal target:

$$\Delta\sigma_{UL} \sim \sin\phi \{F_1 \tilde{H} + \xi(F_1 + F_2)(H + \xi/(1+\xi)E)\} d\phi$$



$$\tilde{H}(\xi, t)$$

Unpolarized beam, transverse target:

$$\Delta\sigma_{UT} \sim \cos\phi \sin(\phi_s - \phi) \{k(F_2 H - F_1 E)\} d\phi$$



$$E(\xi, t)$$

Unpolarized total cross section:

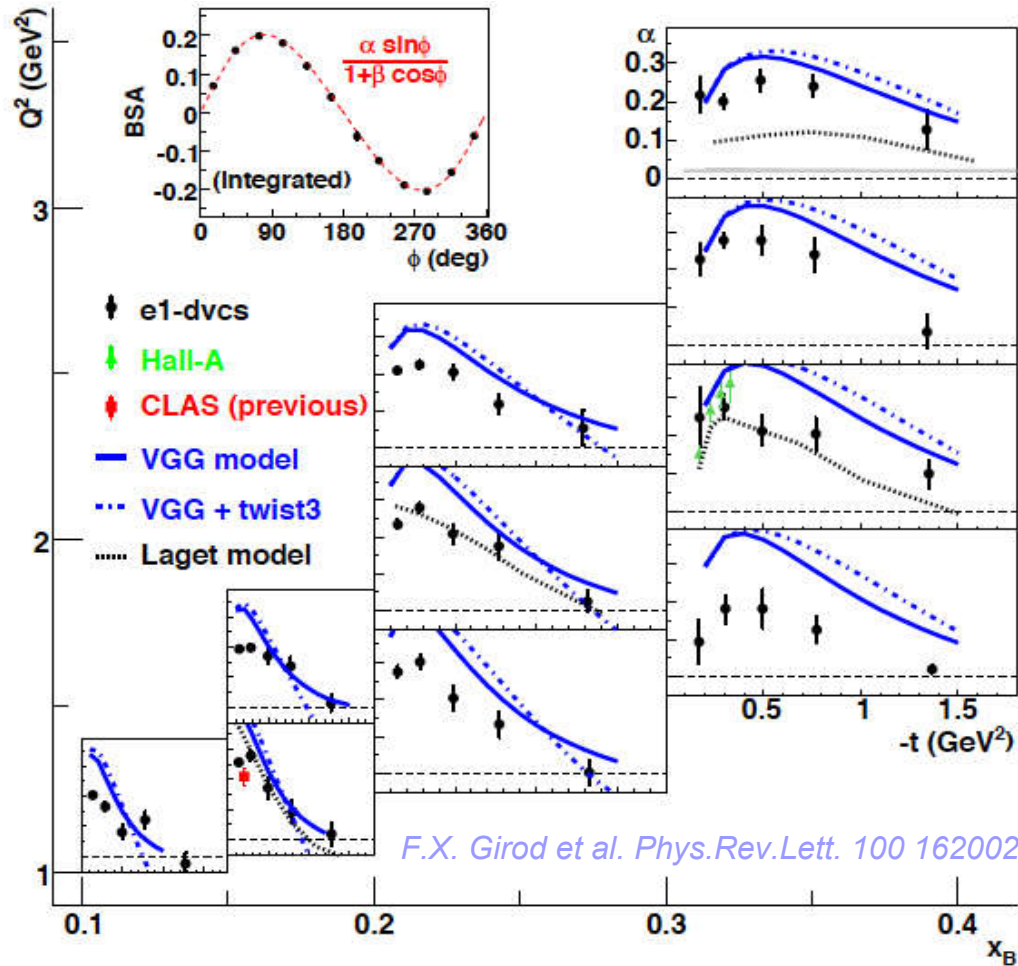
Separates h.t. contributions to DVCS



$$\text{Re}(T^{\text{DVCS}})$$

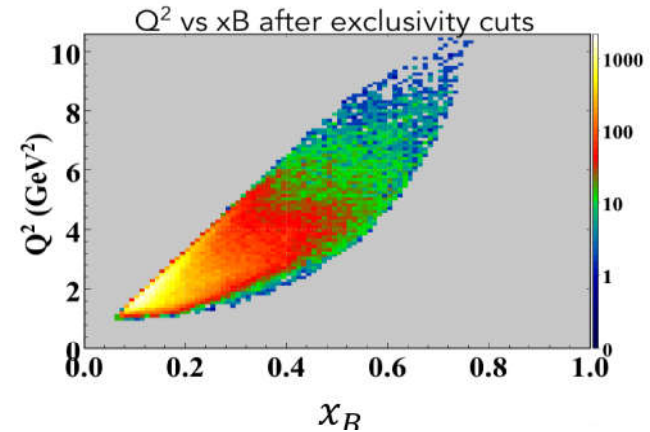
# DVCS Beam Spin Asymmetry

## CLAS at 6 GeV

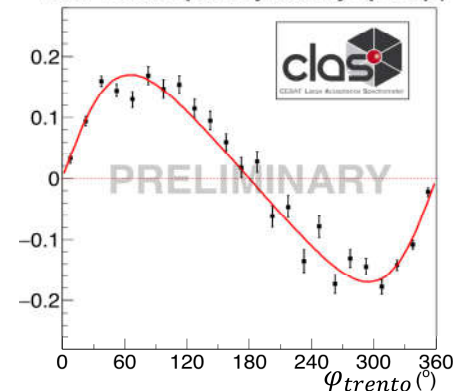


## CLAS12 at 10.6 GeV

- extended kinematic coverage
- increased statistics
- neutron target



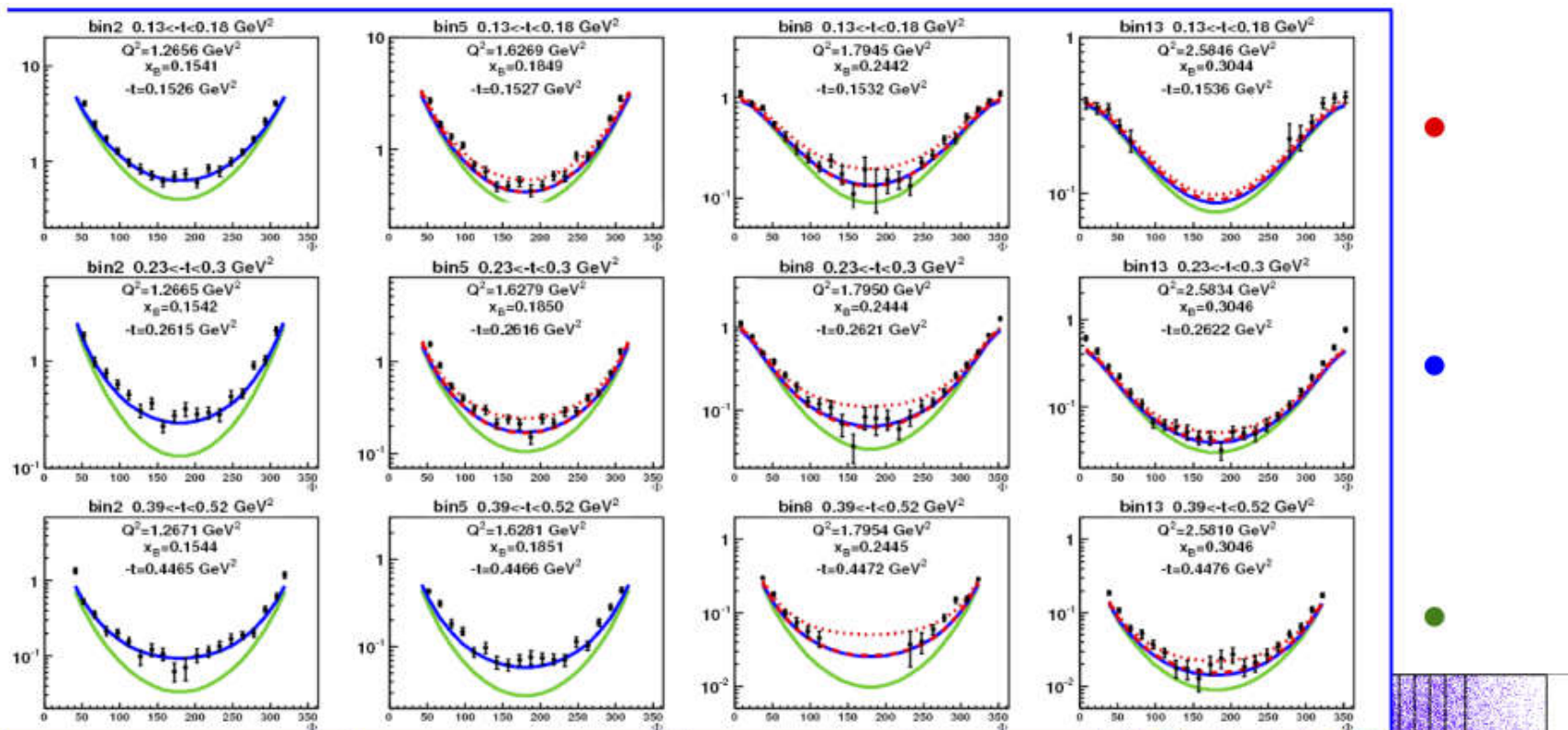
Raw Beam-Spin Asymmetry  $ep \rightarrow e\gamma$



G. Christiaens

Precision in a large phase space  $Q^2, x_B, t$

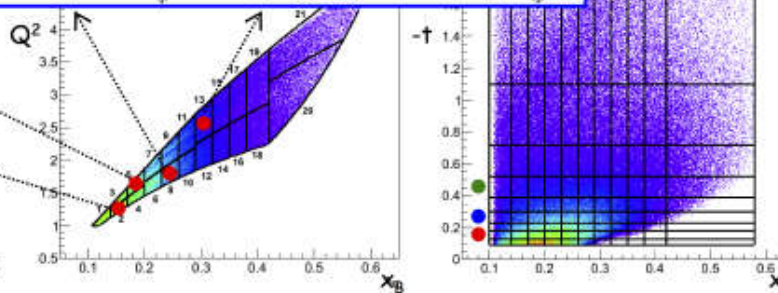
# DVCS Unpolarized Cross-Sections with 6 GeV CLAS



$$\bullet \frac{d^4\sigma_{ep \rightarrow ep\gamma}}{dQ^2 dx_B dt d\Phi} \text{ (nb/GeV}^4\text{)}$$

— BH      — VGG (H only)  
⋯ KM10    --- KM10a

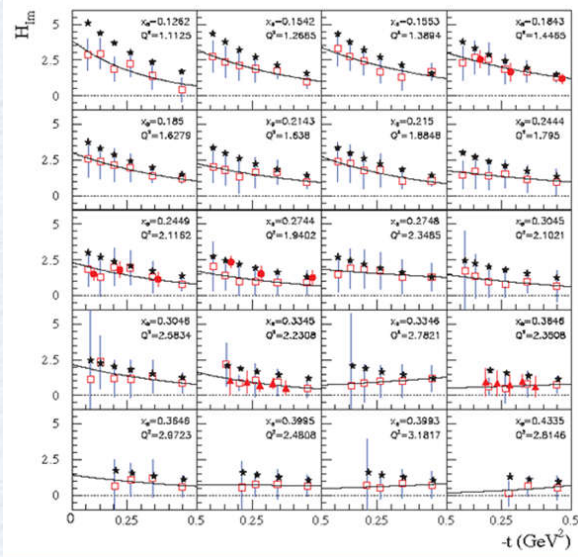
VGG : Vanderhaeghen, Guichon, Guidal      KM : Kumericki, Mueller



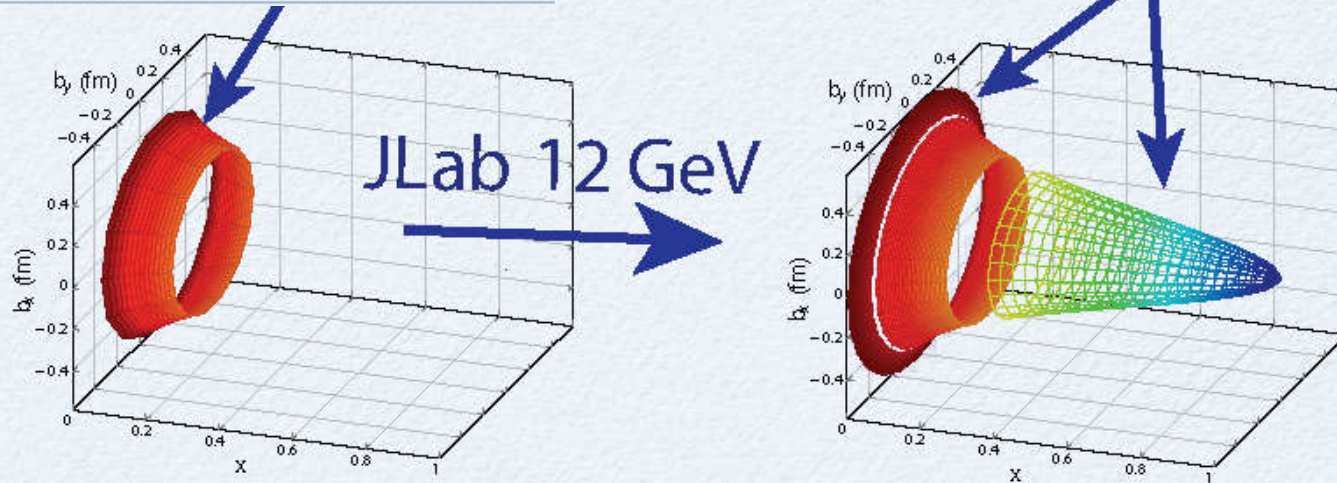
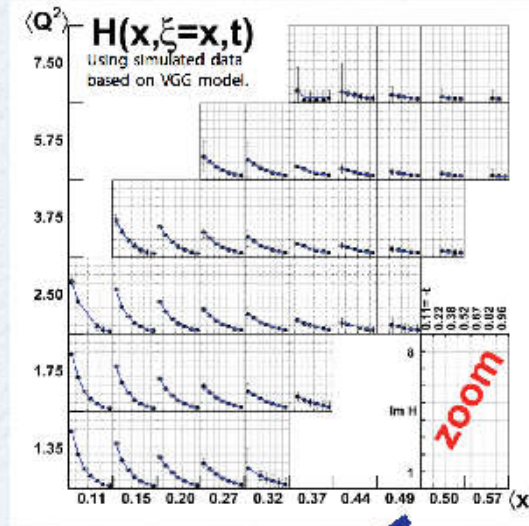
H.-S. Jo et al., PRL 115 212003 (2015)

# Projections for Compton Form Factors at JLab 12 GeV

Düpré-Guidal-Vanderhaeghen-PRD **95** 011501 (R) (2017)

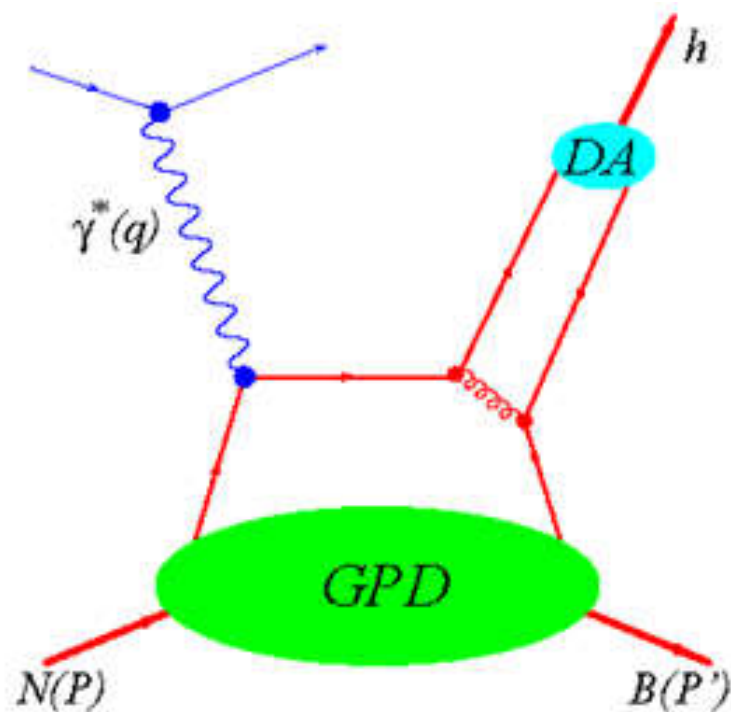


CLAS12 projections E12-06-119 with DVCS  $A_{UL}$  and  $A_{LU}$



courtesy of Z.E. Meziani

## Deeply Virtual Meson Production (DVMP)



	Meson	Flavor
$\mathcal{H}_T, \mathcal{E}_T$	$\pi^+$	$\Delta u - \Delta d$
	$\pi^0$	$2\Delta u + \Delta d$
	$\eta$	$2\Delta u - \Delta d + 2\Delta s$
$\mathcal{H}, \mathcal{E}$	$\rho^+$	$u - d$
	$\rho^0$	$2u + d$
	$\omega$	$2u - d$
	$\phi$	$g$

$H^q$	$\tilde{H}^q$	$E^q$	$\tilde{E}^q$	parton helicity conserving (chiral-even) GPDs
$H_T^q$	$\tilde{H}_T^q$	$E_T^q$	$\tilde{E}_T^q$	parton helicity-flip (chiral-odd) GPDs



## Chiral-odd / transversity GPDs

- Jaffe and Ji have shown that the first Mellin moment of transversity PDF  $h_1^q(x)$  gives us the tensor charge  $\delta q$

$$\delta q = \int_{-1}^1 h_1^q(x) dx = \int_0^1 (h_1^q(x) - \bar{h}_1^q(x)) dx$$

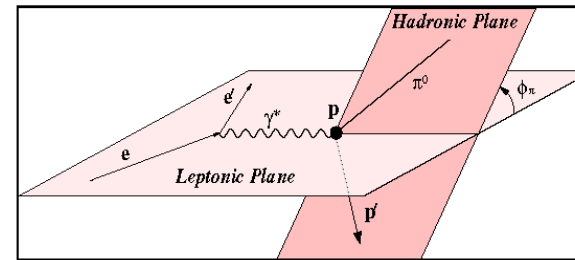
- We can interpret tensor charge as the absolute magnitude of transversely polarized valence quarks inside a transversely polarized nucleon.
- Given the relations between transversity PDF  $h_1^q(x)$  and chiral-odd GPD  $H_T(x, \xi, t)$  one can obtain the tensor charge  $\delta q$  through GPD in the forward limit:

$$h_1^q(x) = H_T(x, \xi = 0, t = 0)$$

# Differential Cross Sections for hard exclusive meson production

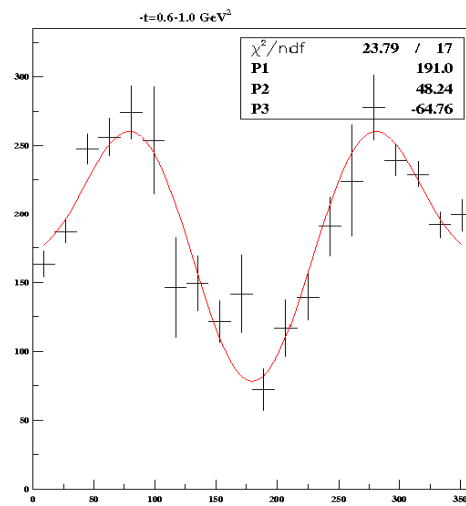
Structure Functions

$$\sigma_U = \sigma_T + \epsilon \sigma_L \quad \sigma_{TT} \quad \sigma_{LT}$$

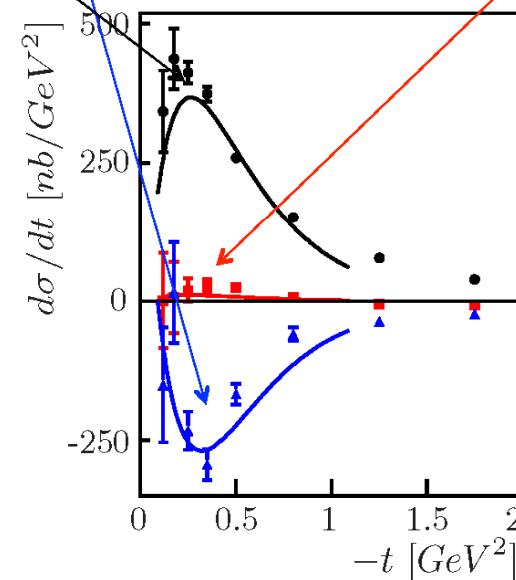


$$ep \rightarrow ep\pi^0$$

$$\frac{d\sigma}{dt d\phi}(Q^2, x, t, \phi) = \frac{1}{2\pi} \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi$$



$\phi$  distribution



# CLAS data and GPD theory predictions

## 2 theoretical models:

**Golosokov, Kroll**  
Eur. Phys. J. A. 47: 112 (2011)

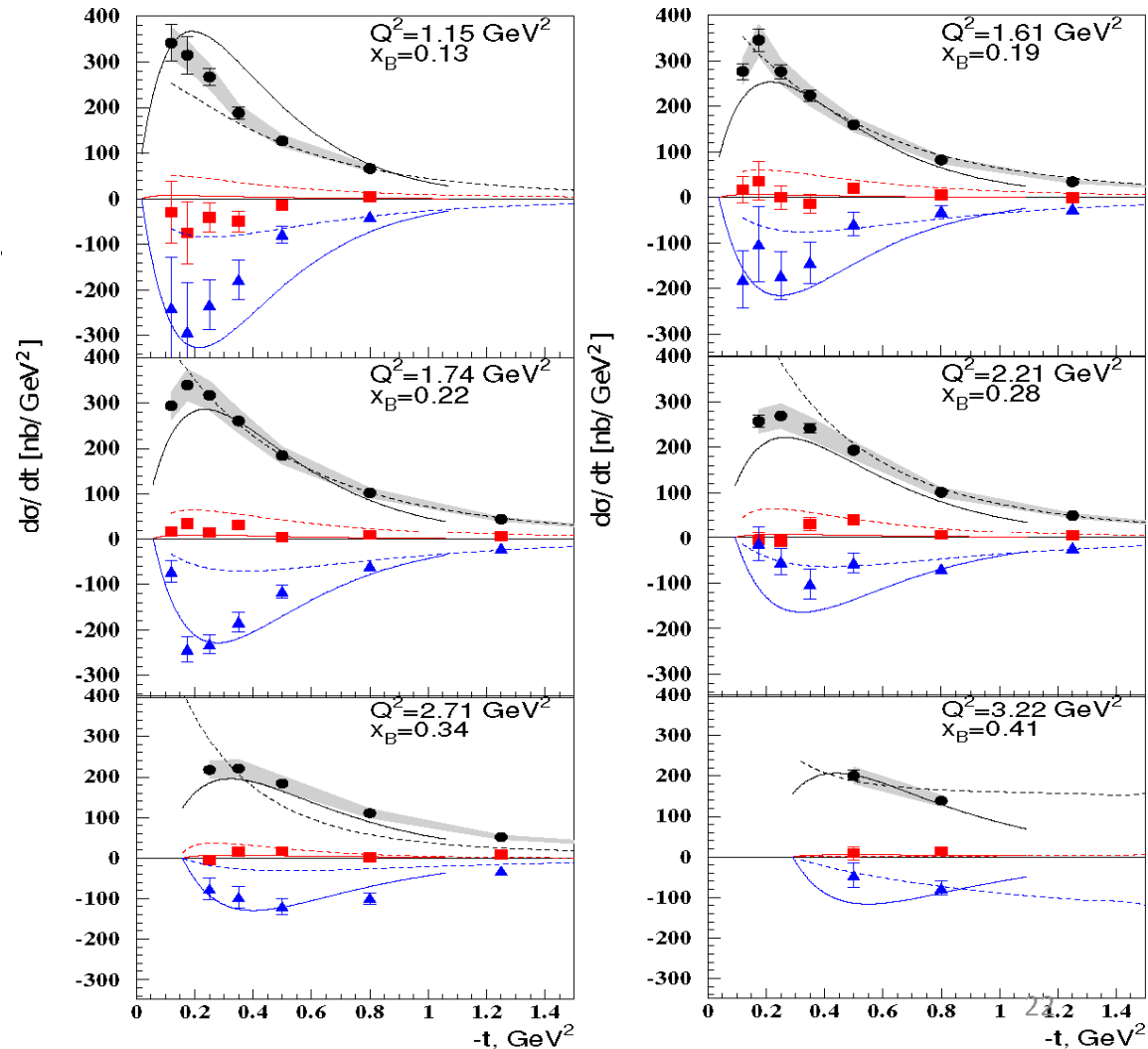
→ Only  $H_T$  and  $\bar{E}_T$  have a significant contribution to pseudoscalar meson electroproduction

→ GPD parametrized based on data

**Goldstein, Hernandez, Liuti**  
Phys. Rev. D 84, 034007 (2011)

→ Model allows flexible parametrization of GPDs

→ chiral-even and chiral-odd sector related with parity relations of the helicity amplitudes



Solid: S. Golosokov and P. Kroll  
Dots: S. Liuti and G. Goldstein

CLAS collaboration. I Bedlinskiy et al.  
Phys.Rev.Lett. 109 (2012) 112001

# Extraction of form factors and flavour decomposition

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha\mu_p^2}{2k'Q^8} \left[ (1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

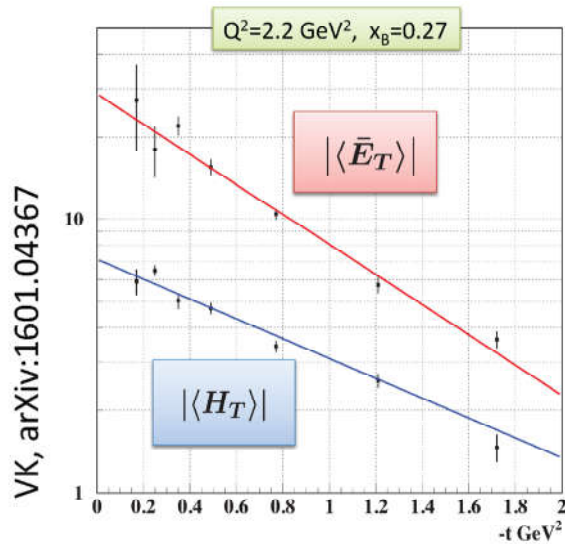
$$\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha\mu_p^2}{k'Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$

Goloskokov, Kröll  
Transversity GPD model

$$|\langle \bar{E}_T \rangle^{\pi,\eta}|^2 = \frac{k'Q^8 16m^2}{4\pi\alpha\mu_p^2 t'} \frac{d\sigma_{TT}^{\pi,\eta}}{dt}$$

$$|\langle H_T \rangle^{\pi,\eta}|^2 = \frac{2k'Q^8}{4\pi\alpha\mu_p^2} \frac{1}{1-\xi^2} \left[ \frac{d\sigma_T^{\pi,\eta}}{dt} + \frac{d\sigma_{TT}^{\pi,\eta}}{dt} \right]$$

## $\pi^0$ Generalized Form Factors



- $E_T > H_T$
- $t$ -dependence is **steeper** for  $\bar{E}_T$  than for  $H_T$

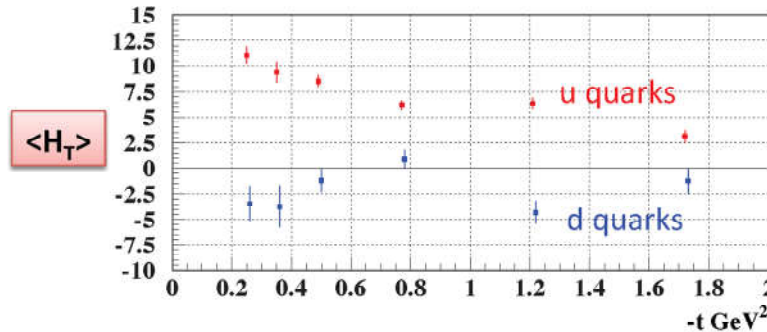
- GPDs appear in different flavor combinations for  $\pi^0$  and  $\eta$

$$H_T^\pi = \frac{1}{3\sqrt{2}} [2H_T^u + H_T^d]$$

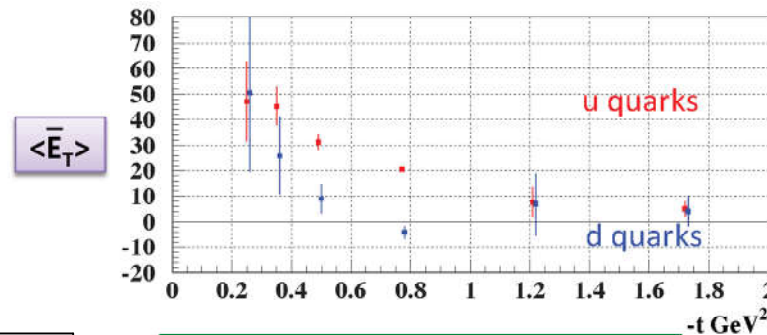
$$H_T^\eta = \frac{1}{\sqrt{6}} [2H_T^u - H_T^d]$$

$$H_T^u = \frac{3}{2\sqrt{2}} [H_T^\pi + \sqrt{3}H_T^\eta]$$

$$H_T^d = \frac{3}{\sqrt{2}} [H_T^\pi - \sqrt{3}H_T^\eta]$$



- $\langle H_T \rangle^u$  and  $\langle H_T \rangle^d$  have different signs for u and d-quarks



- $|\langle \bar{E}_T \rangle|^d$  and  $|\langle \bar{E}_T \rangle|^u$  have the same signs

VK arXiv: 1601.04367 [hep-ex] 2016

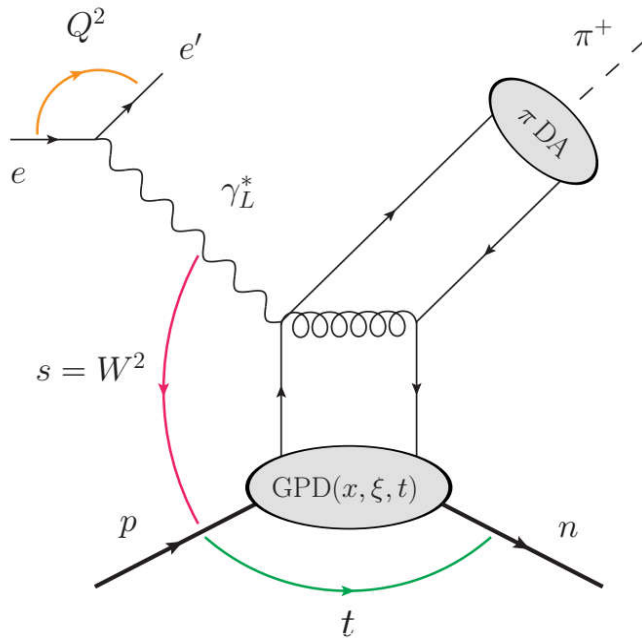
# GPD and TDA based descriptions

colinear factorization theorem

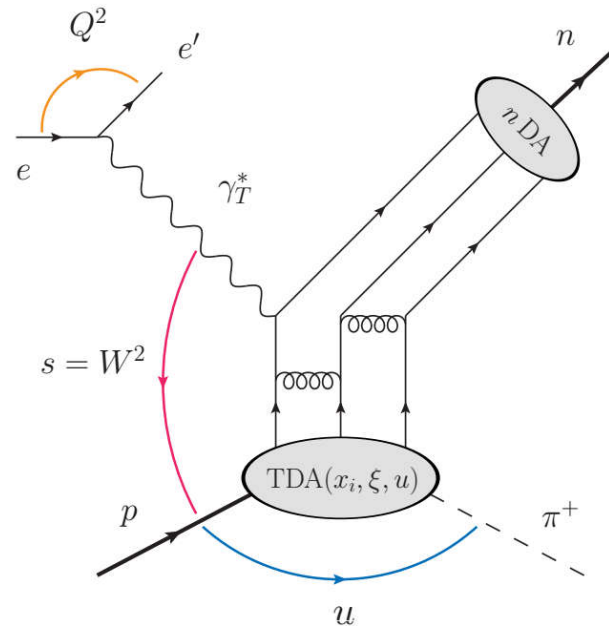
**GPD based description**  
large  $Q^2$  and  $s$   
small  $t$  channel contribution

**TDA based description**  
large  $Q^2$  and  $s$   
small  $u$  channel contribution

- probe partonic correlations between states of different baryonic charge
- access to non-minimal Fock components of baryon light-cone wave functions
- Femto-photography of hadrons from a new perspective
- Spatial imaging of the structure of the pion cloud inside the nucleon



$\pi$  in forward region

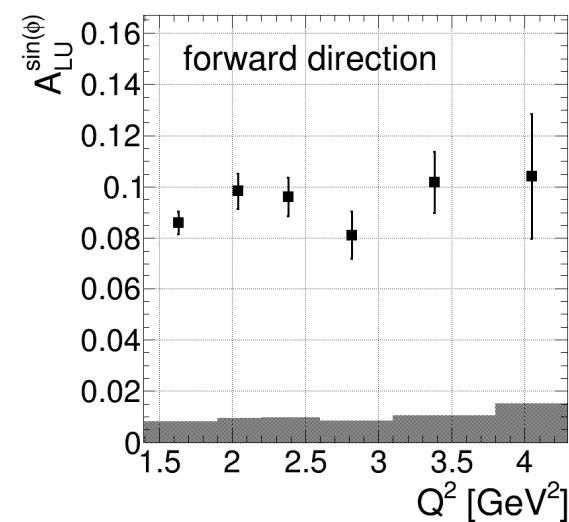
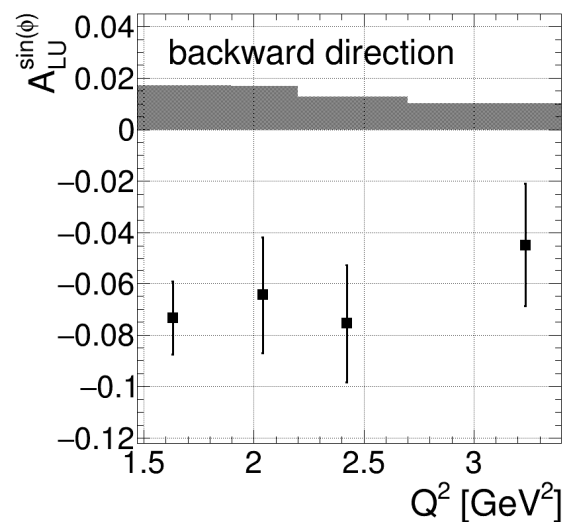
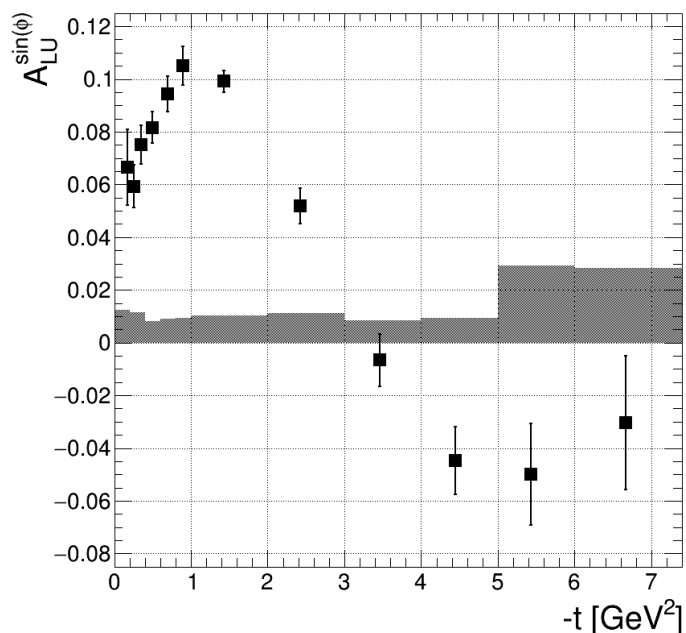
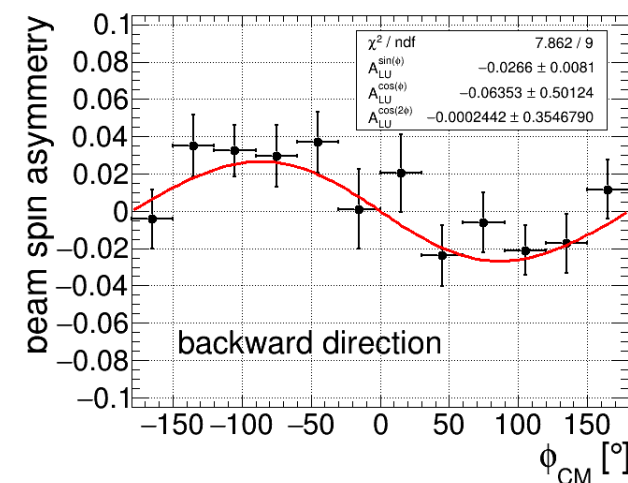
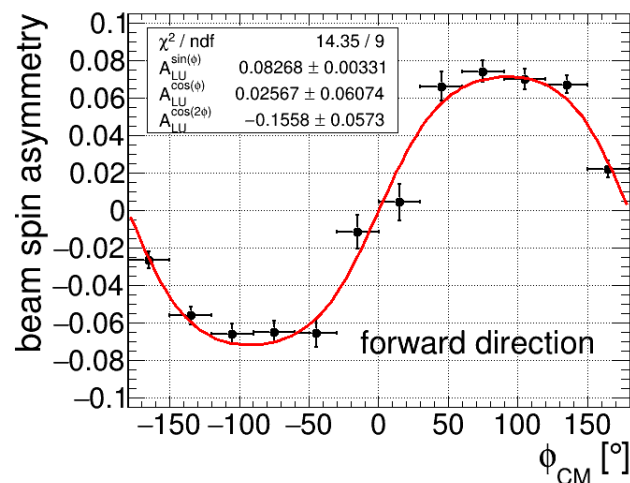


$\pi$  in backward region

# Extraction of $A_{LU}^{\sin(\phi)}$ for the hard exclusive $\pi^+$ channel

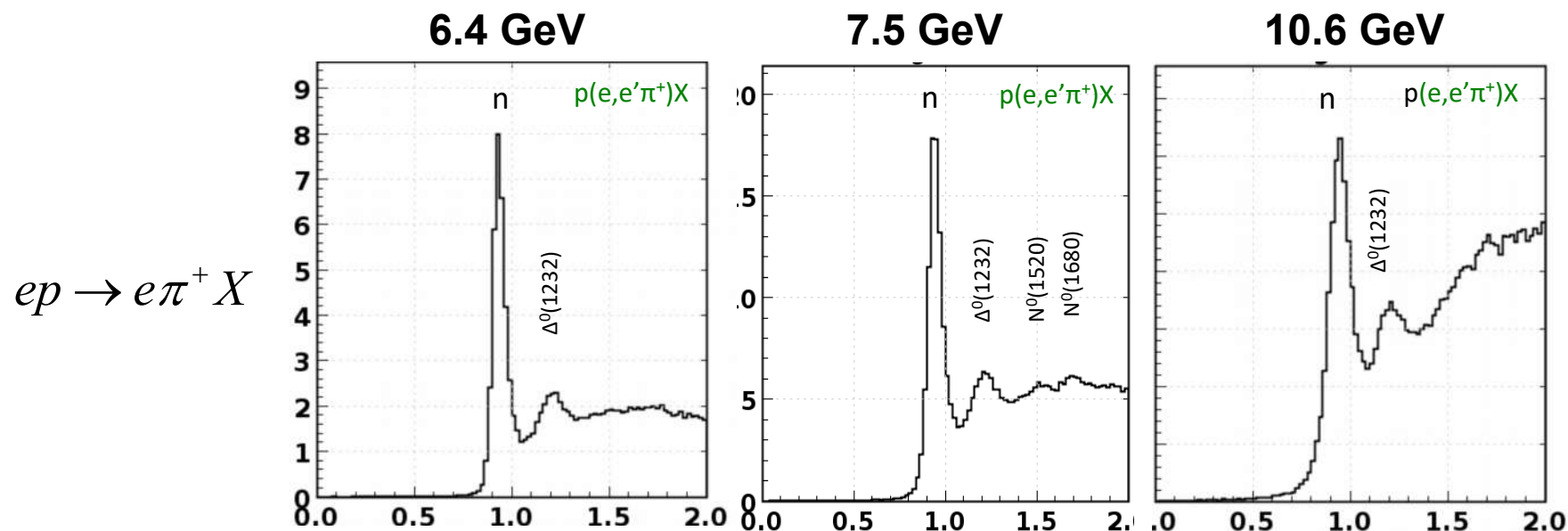
$$BSA_i = \frac{1}{P_e} \cdot \frac{N_i^+ - N_i^-}{N_i^+ + N_i^-}$$

$$BSA = \frac{A_{LU}^{\sin \phi} \sin \phi}{1 + A_{UU}^{\cos \phi} \cos \phi + A_{UU}^{\cos(2\phi)} \cos(2\phi)}$$

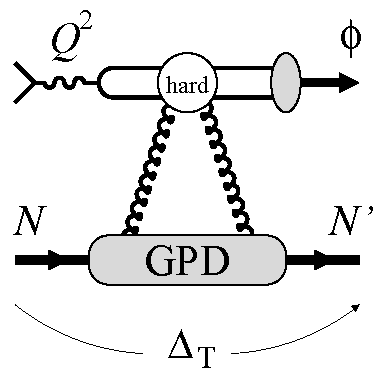


S. Diehl (JLU + UConn)

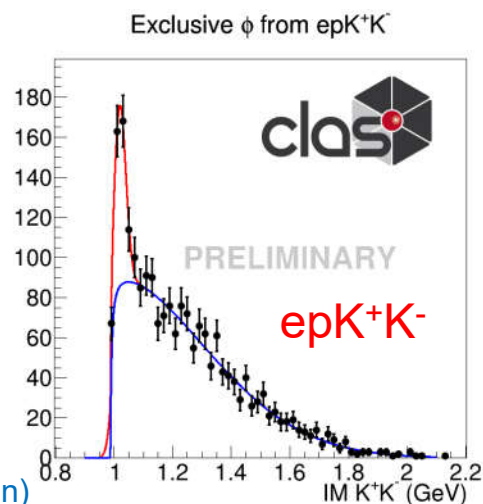
## CLAS12 DVMP program just started ....



### Exclusive $\Phi$ Production



B. Clary (Uconn)



- Exclusive  $\Phi$  production probes gluon GPDs
- Transverse spatial distribution of gluons

$x < 0.01$  measured at HERA, FNAL  
 $x > 0.1$  practically unknown

## Transverse Momentum Distributions (TMDs)

- Spin-dependent 3D **momentum space** images from semi-inclusive scattering  
quark pol.

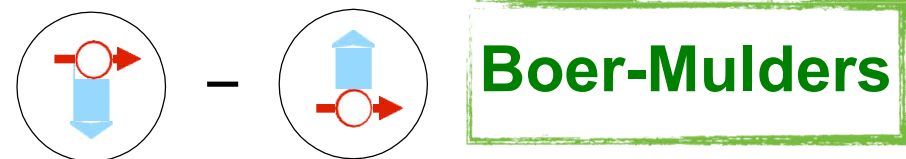
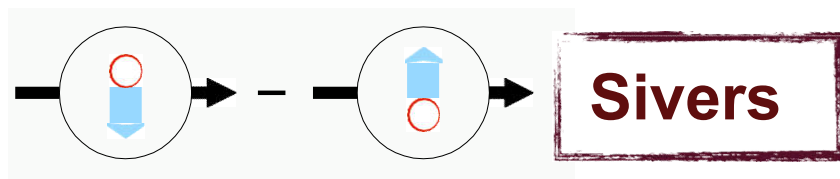
	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

- TMDs in black survive transverse - momentum integration
- TMDs in red are T - odd
- All colored TMDs vanish if there is no quark orbital angular momentum
- Any quantitative statement about the total orbital angular momentum is model dependent

Azimuthal asymmetries generated by correlations  
between quark transverse momentum and

the nucleon transverse spin

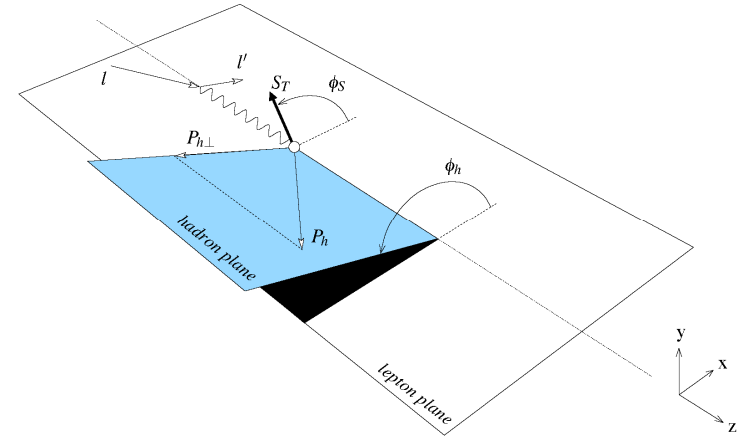
the parton transverse spin





# Semi-Inclusive Deep Inelastic Scattering (SIDIS)

$$\begin{aligned}
 & \frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} F_{UU,T}(x, z, P_{h\perp}^2, Q^2) \\
 &= \frac{\alpha^2}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right. \\
 &+ \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\
 &+ S_L \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 &+ S_T \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\
 &+ \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} \\
 &+ \left. \left. \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] + S_T \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \right. \\
 &+ \left. \left. \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}
 \end{aligned}$$



## → 18 Structure Functions

**EXPERIMENT:** Setting the proper beam and target polarization conditions (U, L, T)

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} C \left[ -\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} \left( xh H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) - \frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M} \left( x f^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right],$$

$$F_{UU}^{\cos 2\phi_h} = C \left[ -\frac{2(\hat{\mathbf{h}} \cdot \mathbf{k}_T)(\hat{\mathbf{h}} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{MM_h} h_1^\perp H_1^\perp \right],$$

← Collins FF  
← Boer-Mulders

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} = C \left[ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M} f_{1T}^\perp D_1 \right]$$

← Sivers

## Longitudinally polarized beam and unpolarized target

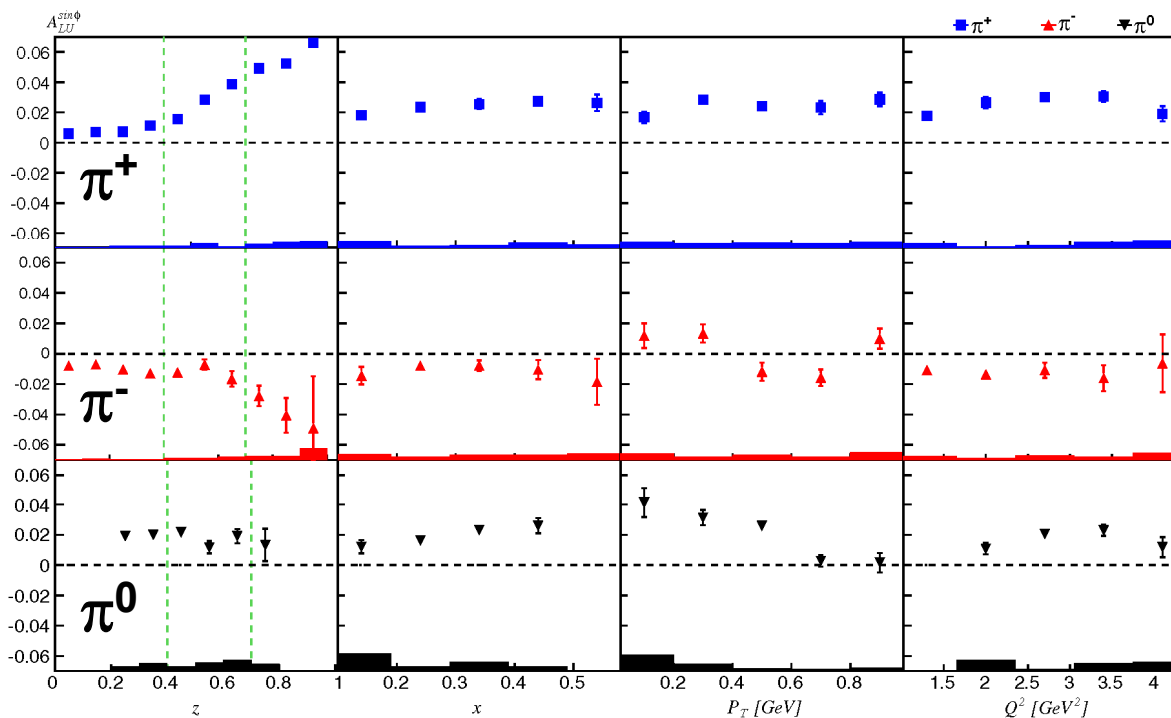
$$\frac{d\sigma}{dx_B dQ^2 dz d\phi_h dp_{h\perp}^2} = K(x, y, Q^2) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\}$$

$$F_{LU}^{\sin\phi} = \frac{2M}{Q} \mathcal{C} \left( -\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} \left( x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M} \left( x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right)$$

twist-3 pdf      Collins FF      unpolarized dist. function      twist-3 FF      twist-3 t-odd dist. function      Boer-Mulders      twist-3 FF

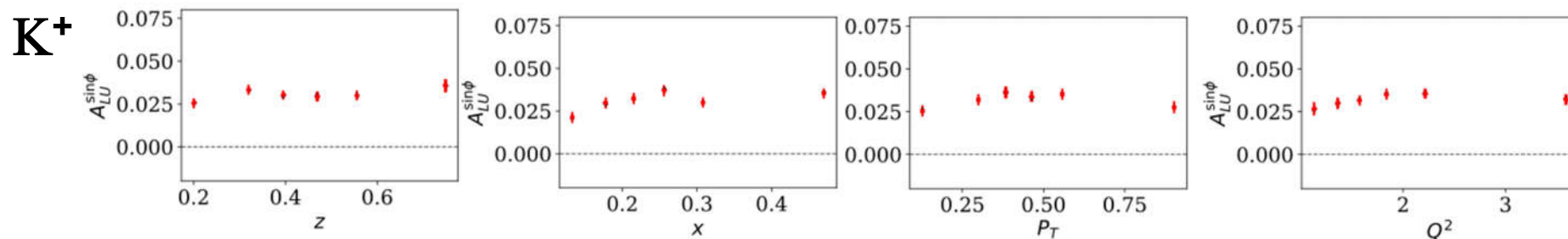
➔ TMD and Fragmentation Functions

# $A_{LU}^{\sin(\phi)}$ measurement for $\pi^+$ , $\pi^-$ , $\pi^0$ and $K^+$ with CLAS



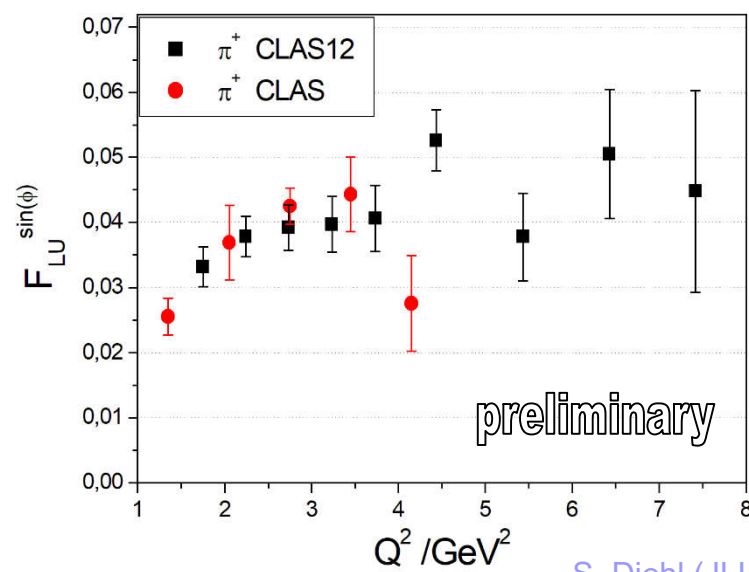
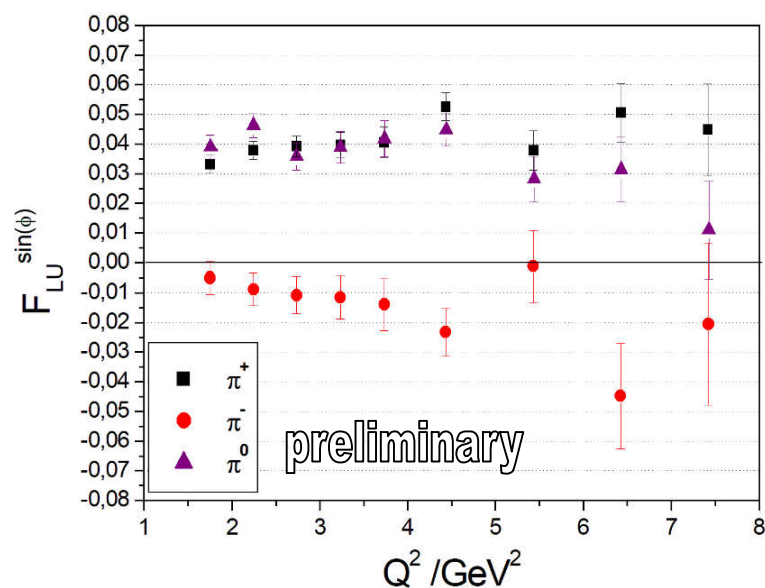
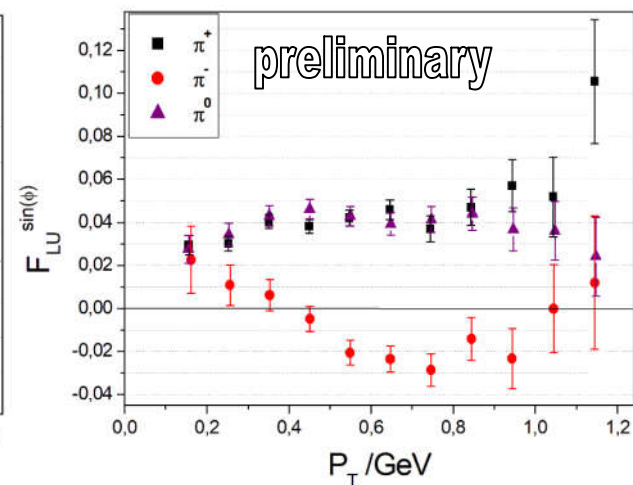
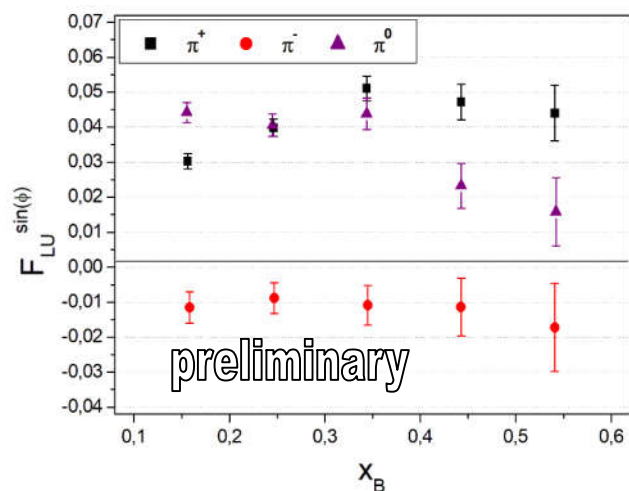
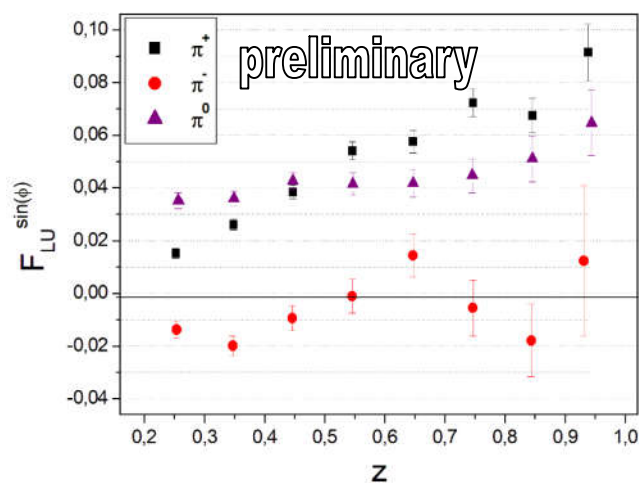
W. Gohn, Ph.D thesis (UConn)  
Phys. Rev. D 89, 072011

Flavor dependences, and their understanding is important for interpretation of spin-azimuthal asymmetries



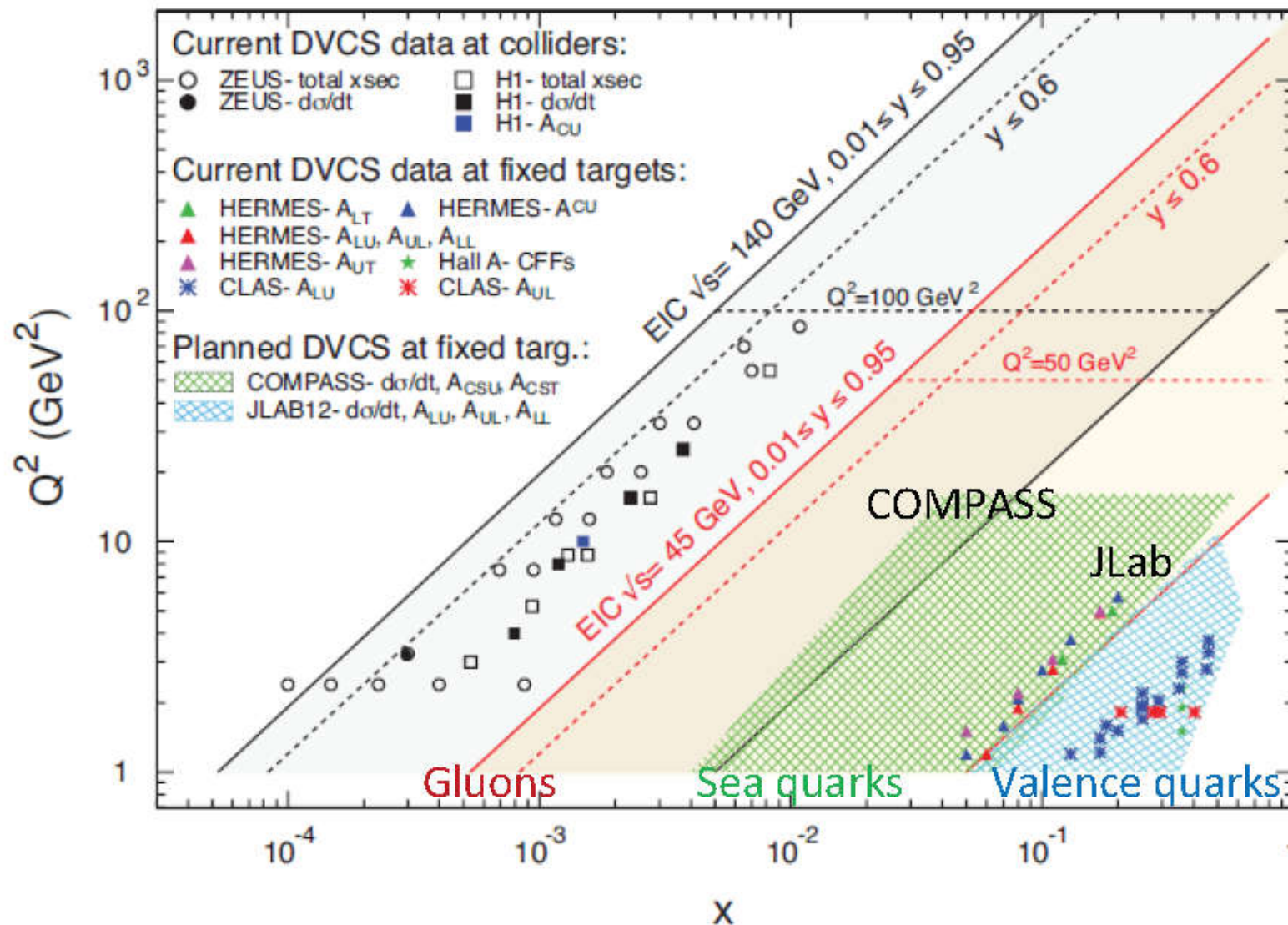
D. Riser, Ph.D thesis (UConn)

# $F_{LU}^{\sin(\phi)}$ measurement for $\pi^+$ , $\pi^-$ and $\pi^0$ with CLAS12 ( $E_{\text{beam}} = 10.6 \text{ GeV}$ )



S. Diehl (JLU + UConn)

## Past, Present and Future 3-D Experiments



## Summary

- ➡ TMDs and GPDs provide a unifying framework to study the 3-D quark and gluon structure of the nucleon
- ➡ 3-D imaging of nucleon will uncover rich dynamics of QCD
- ➡ Exciting time has just started with CLAS12 high precision and high statistics measurements with large kinematic coverages!

