

FRAGMENTATION FUNCTIONS



Anselm Vossen



FRAGMENTATION FUNCTIONS (FOCUS ON RECENT e^+e^- RESULTS FROM BELLE RESULTS)

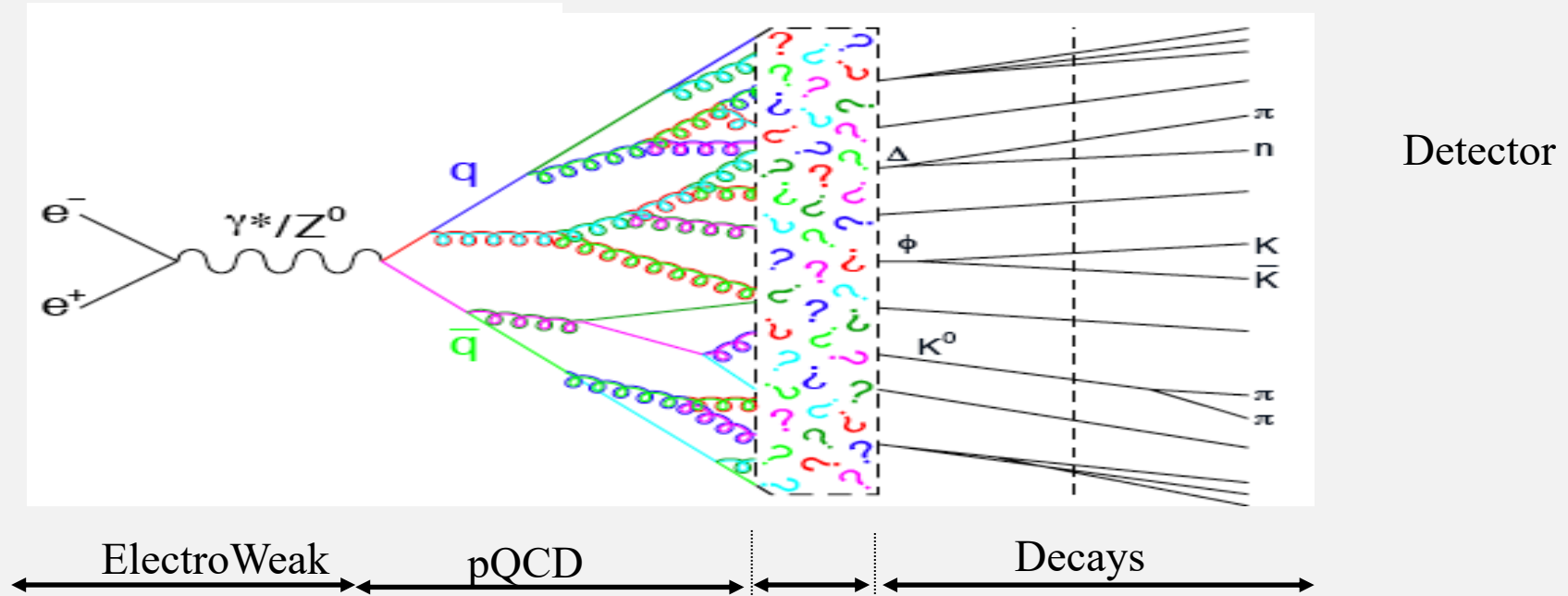


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FACTORIZED QCD: HADRONIZATION DESCRIBED BY FRAGMENTATION FUNCTIONS

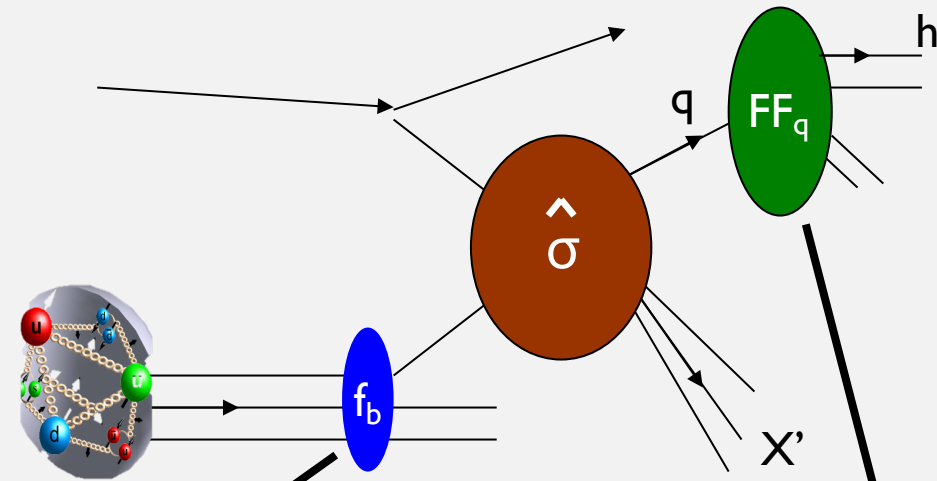
Field, Feynman (1977): Fragmentation functions encode the information on how partons produced in hard-scattering processes are turned into an observed colorless hadronic bound final-state [PRD 15 (1977) 2590]



- Complementary to the study of nucleon structure (PDFs)
- Cannot be computed on the lattice
- Questions to be asked
 - **Macroscopic effect (distribution, polarization) of microscopic properties (quantum numbers)?**
 - Effect of QCD vacuum the quark is traversing
 - Study of the formation of hadrons \rightarrow e.g. Phys.Rev. D97 (2018) no.7, 072005

ACCESS NUCLEON STRUCTURE THROUGH **FRAGMENTATION FUNCTIONS**

- **Proton Structure extracted using QCD factorization theorem**
- **FFs contribute to virtually all processes**
- **Essential for model indep. Etraction of e.g.**
 - Transverse spin structure
 - TMDs
 - ...



$$\frac{d^2\sigma(ep \rightarrow \pi X)}{dx dz} \propto \underbrace{q(x, k_T)}_{\text{Proton Structure}} \times \underbrace{\frac{d\sigma^2(e q \rightarrow e' q')}{dx}}_{\text{pQCD}} \times \underbrace{FF(z, p_T)}_{\text{fragmentation function}}$$

SINGLE HADRON PRODUCTION IN SIDIS IS A WELL TRAVELLED PATH



Observables:

z : fractional energy of the quark carried by the hadron

$p_{h,T}$: transverse momentum of the hadron wrt the quark direction: **TMD FFs**

Parton polarization → Hadron Polarization ↓	Spin averaged	longitudinal	transverse
spin averaged	$D_1^{h/q}(z, p_T) = \left[\bullet \rightarrow \bigcirc \right]$		$H_1^{\perp h/q}(z, p_T) = \left[\uparrow \rightarrow \bigcirc \right] - \left[\downarrow \rightarrow \bigcirc \right]$
longitudinal			
Transverse (here Λ)			

“YOU THINK YOU UNDERSTAND
SOMETHING?---NOW ADD SPIN...**IN
HADRONIZATION!**”

- → **polarized final states**
- → **di-hadron correlations**
- Explore spin-orbit correlation in hadronization
- **Additional degrees of freedom in final state make targeted extraction of nucleon structure possible → see $h_1(x)$, $e(x)$**

ENTER POLARIZATION IN THE FINAL STATES



Observables:

z : fractional energy of the quark carried by the hadron

$p_{h,T}$: transverse momentum of the hadron wrt the quark direction: **TMD FFs**

Parton polarization \rightarrow Hadron Polarization \downarrow	Spin averaged	longitudinal	transverse
spin averaged	$D_1^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \right]$		$H_1^{\perp h/q}(z, p_T) = \left[\uparrow \rightarrow \text{blue circle} \right] - \left[\downarrow \rightarrow \text{blue circle} \right]$
longitudinal		$G_1^{\Lambda/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \rightarrow \text{green arrow} \right] - \left[\bullet \leftarrow \text{red circle} \rightarrow \text{green arrow} \right]$	$H_{1L}^{h/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{green circle} \rightarrow \text{green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{green circle} \rightarrow \text{green arrow} \right]$
Transverse (here Λ)	$D_{1T}^{\perp \Lambda/q}(z, p_T) = \left[\bullet \rightarrow \text{blue circle with green arrow} \right]$	$G_{1T}^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{green circle with green arrow} \right] - \left[\bullet \leftarrow \text{green circle with green arrow} \right]$	$H_1^{\Lambda/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{red circle with green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{red circle with green arrow} \right]$ $H_{1T}^{\perp \Lambda/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{green circle with green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{green circle with green arrow} \right]$

- Analogue \rightarrow similar to PDFs encoding spin/orbit correlations
- Determining final state polarization needs self analyzing decay (Λ)
- Gluon FFs similar but with circular/linear polarization (not as relevant for e^+e^-)

DI-HADRON FRAGMENTATION FUNCTIONS






Additional Observable:

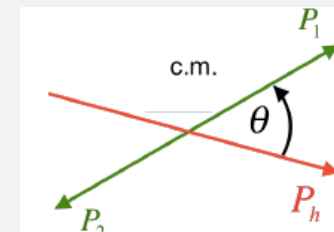
$$\vec{R} = \vec{P}_1 - \vec{P}_2 :$$

The relative momentum of the hadron pair is an additional degree of freedom:

the orientation of the two hadrons w.r.t. each other and the jet direction can be an indicator of the quark transverse spin

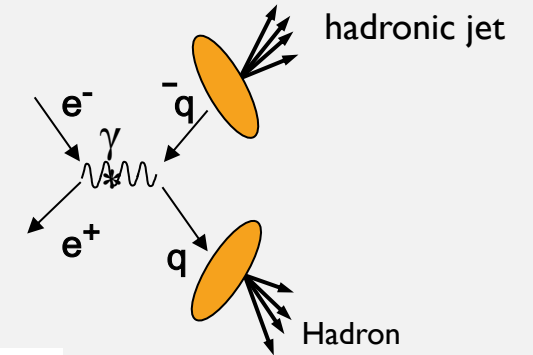
Parton polarization → Hadron Polarization ↓	Spin averaged	longitudinal	transverse
spin averaged	$D_1^{h/q}(z, M)$ 		
longitudinal			
Transverse		$G_1^\perp(z, M, P_h, \theta) =$ T-odd, chiral-even → jet handedness QCD vacuum structure 	$H_1^\perp(z, M) =$ T-odd, chiral-odd Colinear 

- Relative momentum of hadrons can carry away angular momentum
 - Partial wave decomposition in θ
 - Relative and total angular momentum → In principle endless tower of FFs



ACCESS OF FFS FOR LIGHT MESONS IN E^+E^- (SPIN AVERAGED CASE)

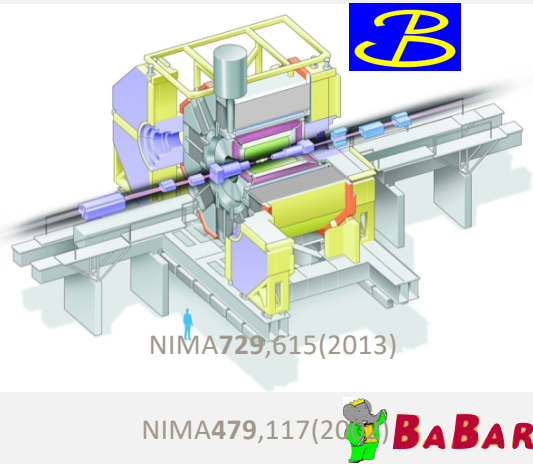
$$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^{e^+e^- \rightarrow hX}}{dz} := \frac{1}{\sum_q e_q^2} (2F_1^h(z, Q^2) + F_L^h(z, Q^2)),$$



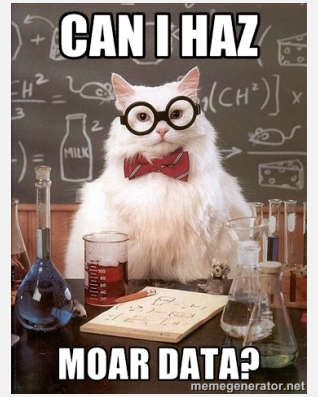
$$2F_1^h(z, Q^2) = \sum_q e_q^2 \left(D_1^{h/q}(z, Q^2) + \frac{\alpha_s(Q^2)}{2\pi} \left(C_1^q \otimes D_1^{h/q} + C_1^g \otimes D_1^{h/g} \right) (z, Q^2) \right)$$

- Cleanest process \rightarrow testbed for QCD calculations
- Limited access to flavor
 - (Use different couplings to γ^* and Z^0)
 - (Use polarization (SLD) and parity violating coupling)
 - **Use back-to-back correlations for different flavor combinations**
- Limited access to gluon FF
 - From evolution
 - From three jet events (but theory treatment not clear)

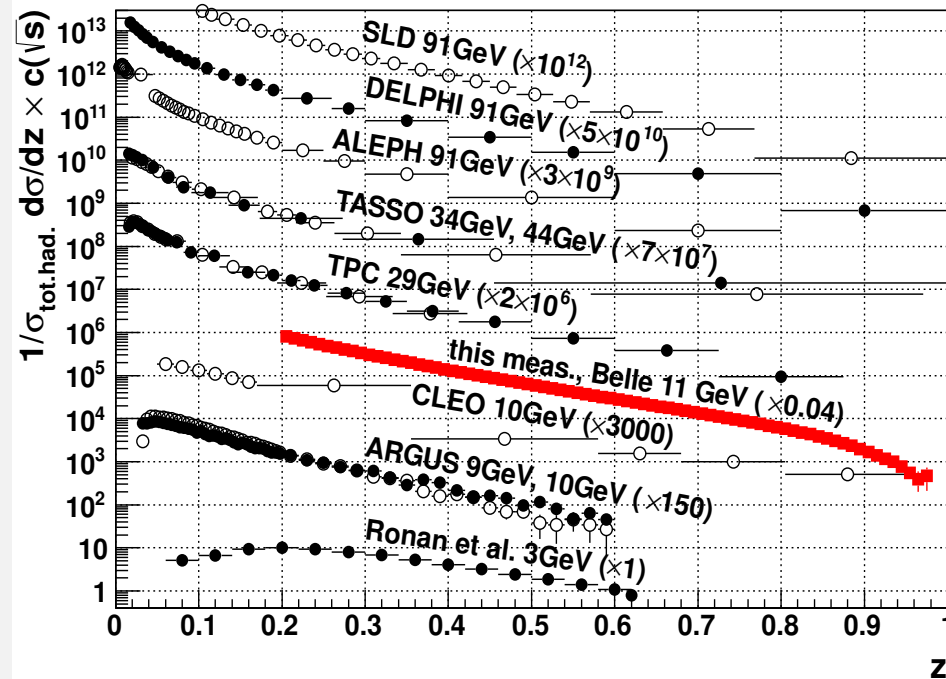
- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.425$
- $L \sim 1$ ab $^{-1}$



ROLE OF B-FACTORIES



World Data (Sel.) for $e^+e^- \rightarrow \pi^+X$ Production

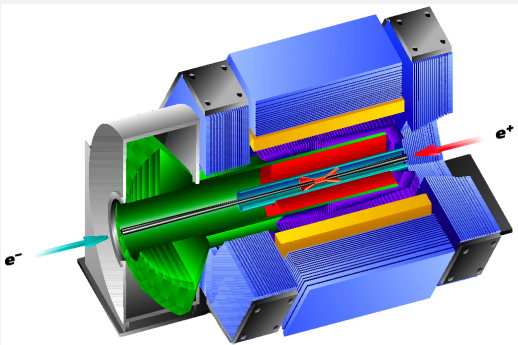


Dominated by B factories

Limited lever arm in \sqrt{s} in particular at high z

Precision data includes charged single hadrons π, K, ρ, D, Λ , charmed baryons...

Well described at NNLO (e.g. DSS, NNFF)



- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.65$
- $L \sim 500$ fb $^{-1}$

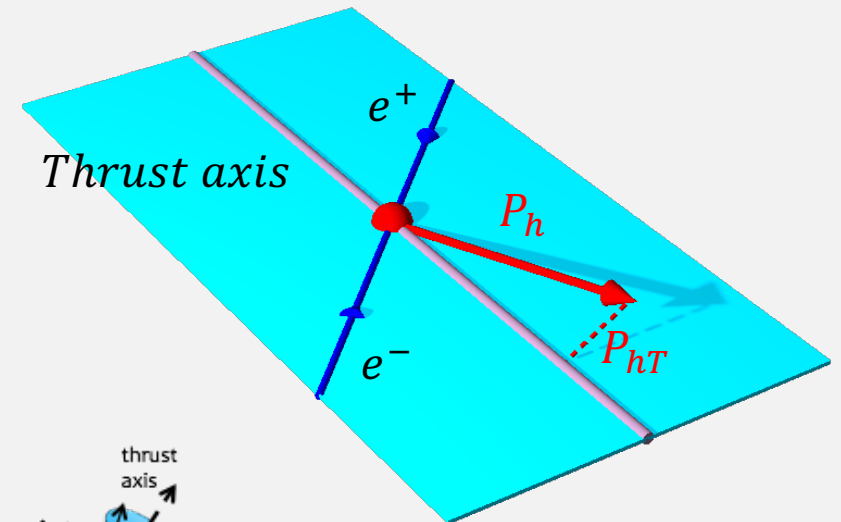
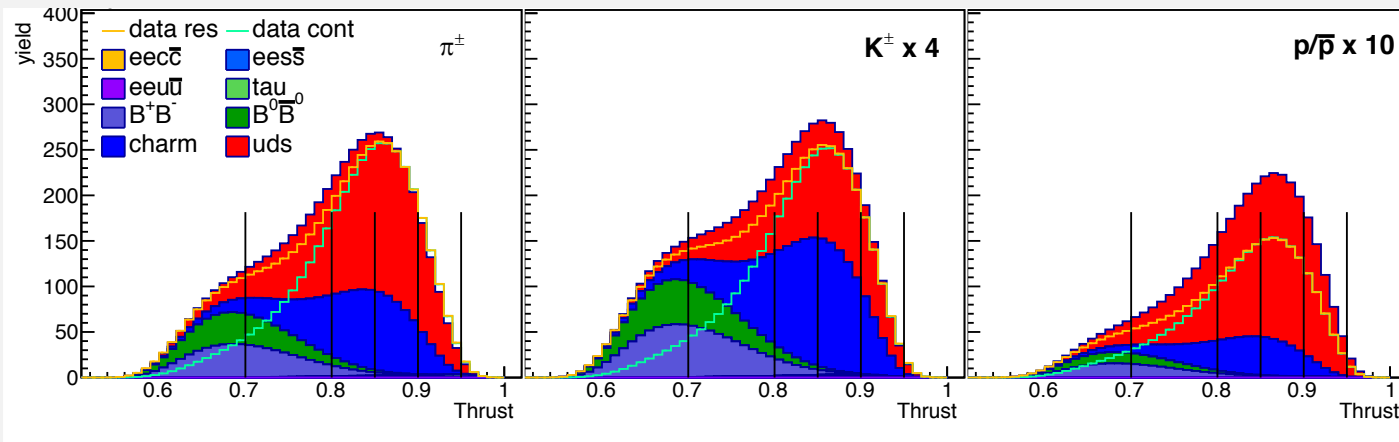
Phys.Rev.Lett. 111 (2013) 062002 (Belle)

Phys.Rev. D88 (2013) 032011 (BaBar)

NEW: P_T DEPENDENCE

PHYS.REV. D99 (2019) NO.11, 112006

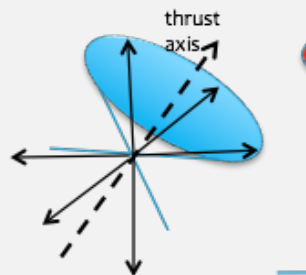
- Quasi inclusive hadron production gives access to transverse momentum in fragmentation
- **Transverse momentum measured with respect to thrust axis**
- Analysis performed differentially in bins of $z, P_{hT}, Thrust$ ($18 \times 20 \times 6$)



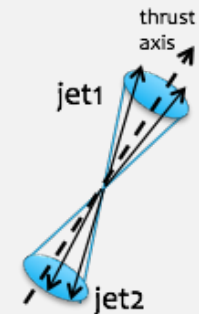
$$T = \sum_i \frac{|\mathbf{P} \cdot \hat{\mathbf{n}}|}{|P|}$$

thrust axis $\equiv \hat{\mathbf{n}}$

$$0.5 \leq T \leq 1$$

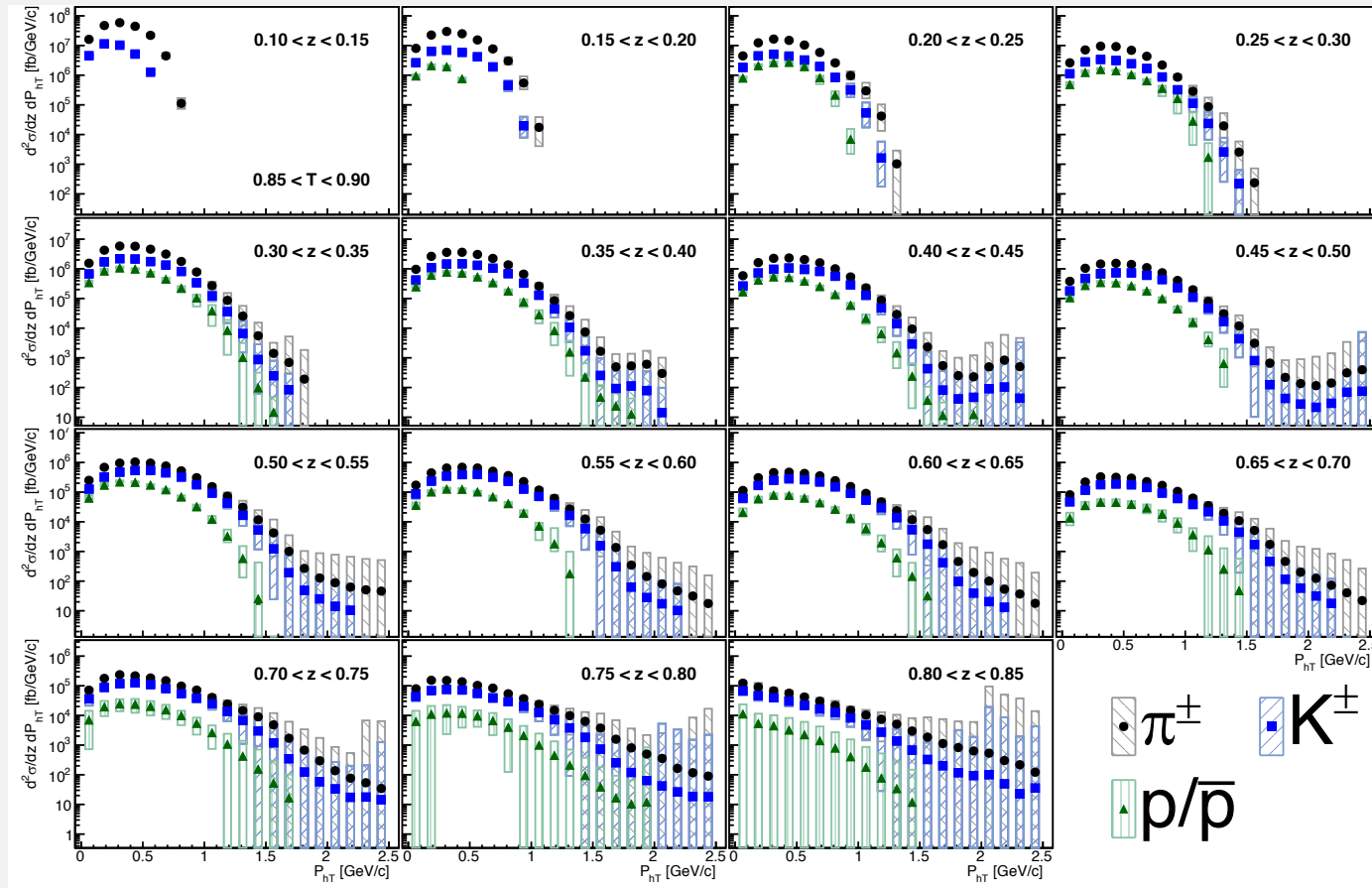


$T \sim 0.5$



$T \sim 1$

TRANSVERSE MOMENTUM DISTRIBUTIONS



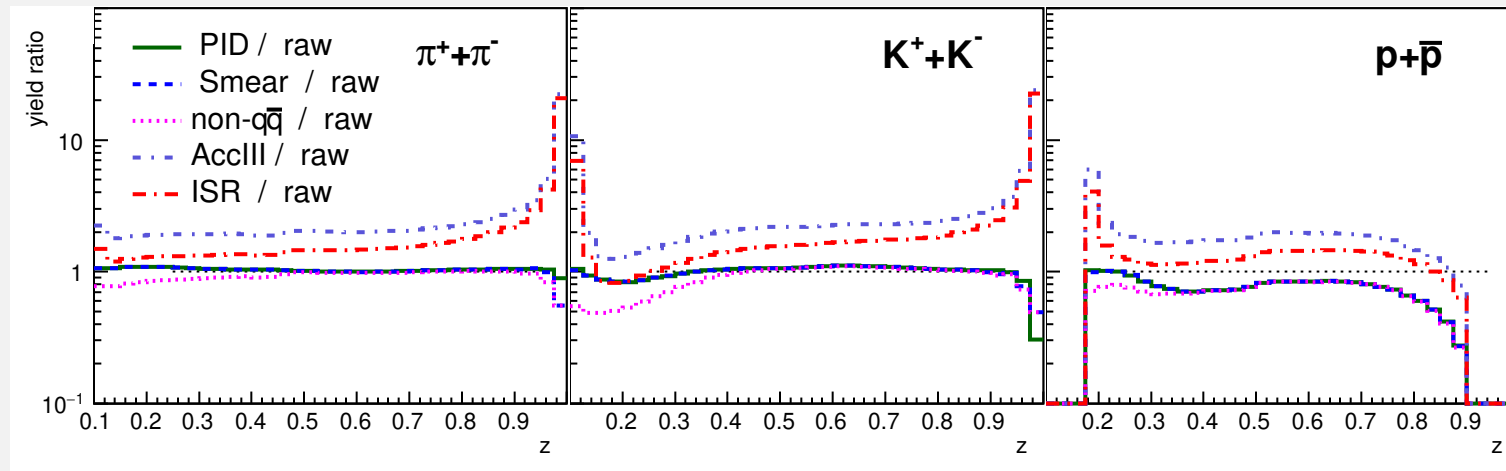
- $0.85 < \text{Thrust } T < 0.9$
 - Transverse momenta mostly Gaussian
 - Possible deviations for large P_{hT} tails, but also large uncertainties

FROM HADRON YIELDS TO CROSS-SECTIONS

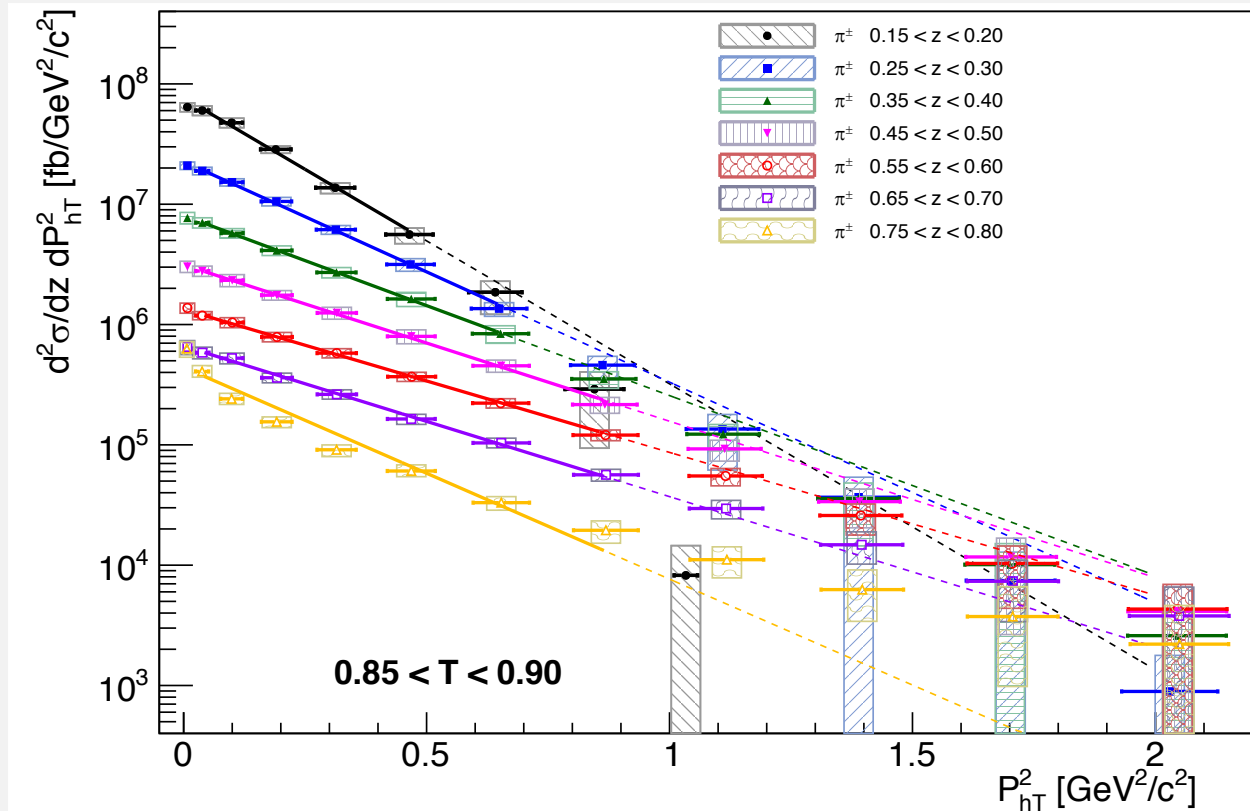
- **Hadron yields undergo a series of corrections**
 - Particle (mis) identification [e.g. not every identified pion was a pion]
 - Smearing unfolding [e.g. measured and true momentum might differ]
 - Non $\bar{q}q$ -processes [e.g. two photon processes, $\Upsilon \rightarrow B\bar{B}\dots$]
 - “ 4π ”-correction [selection criteria and limited acceptance]
 - QED radiation [initial-state radiation (ISR)]
- **Collins asymmetries also corrected for false asymmetries and axis (mis)reconstruction**

FROM HADRON YIELDS TO CROSS-SECTIONS

- **Example: single hadron inclusive cross-sections**
 - Largest effect for mesons **from acceptance** and **ISR corrections**
 - Larger PID correction for protons than for mesons

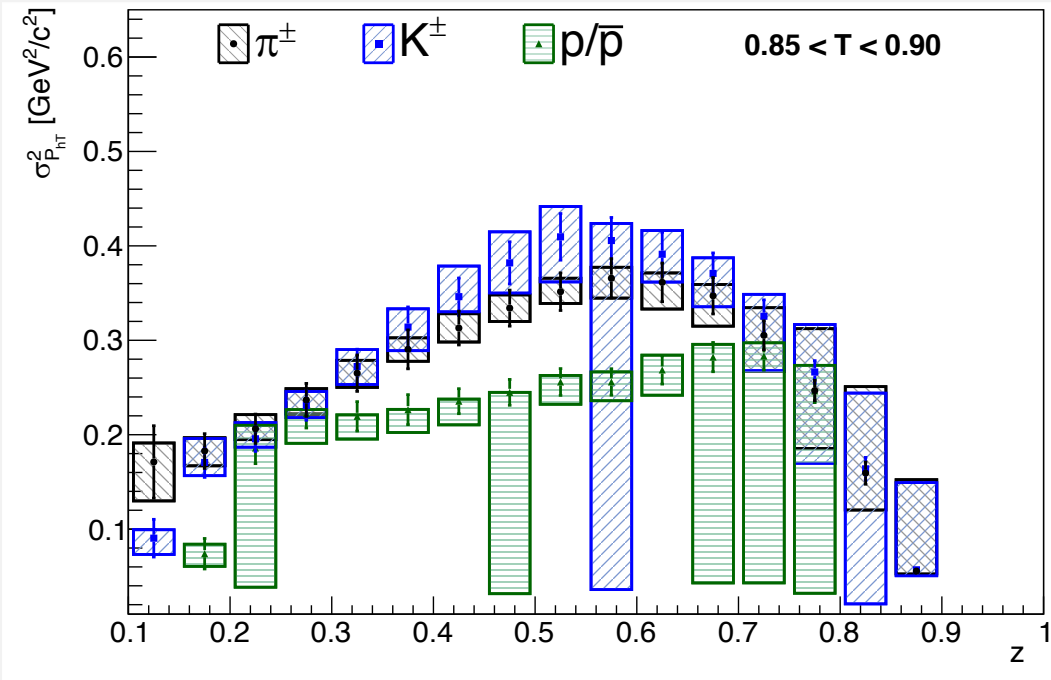


TRANSVERSE MOMENTUM: GAUSSIAN WIDTHS

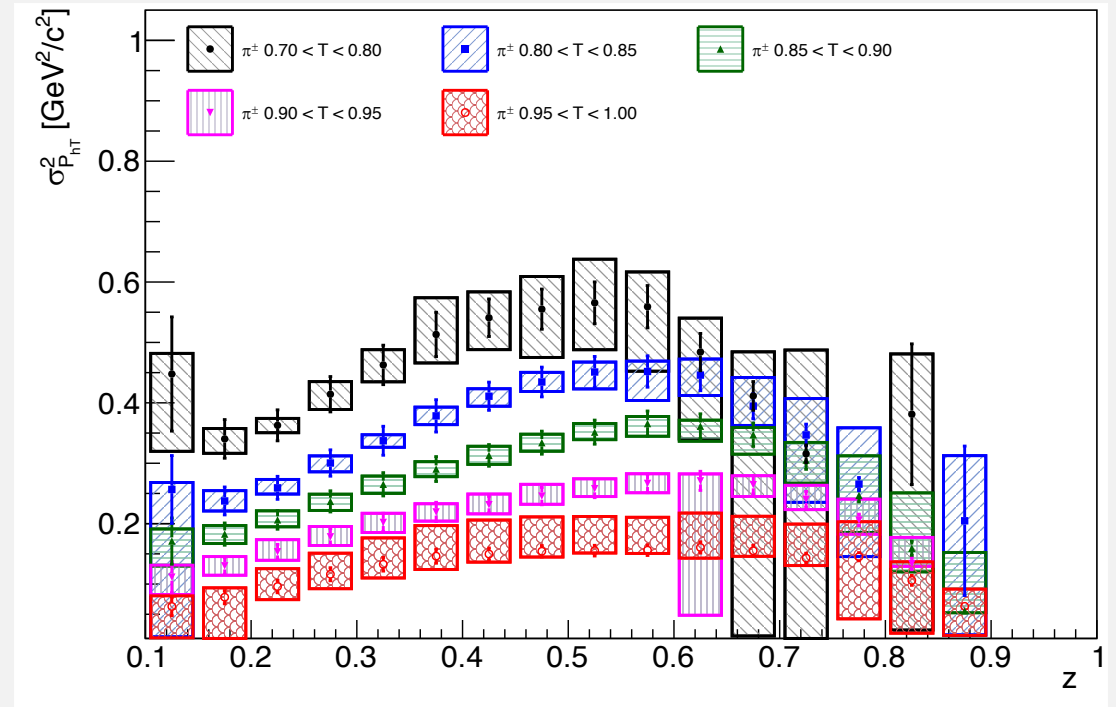


- $0.85 < T < 0.9$
 - Fit Gauss to low P_{hT} data
 - Mostly well described with possible exception at high z
 - Deviation from Gauss at large P_{hT}
 - Clear increase in width with z for low values of z

GAUSSIAN WIDTH AS A FUNCTION OF Z AND T

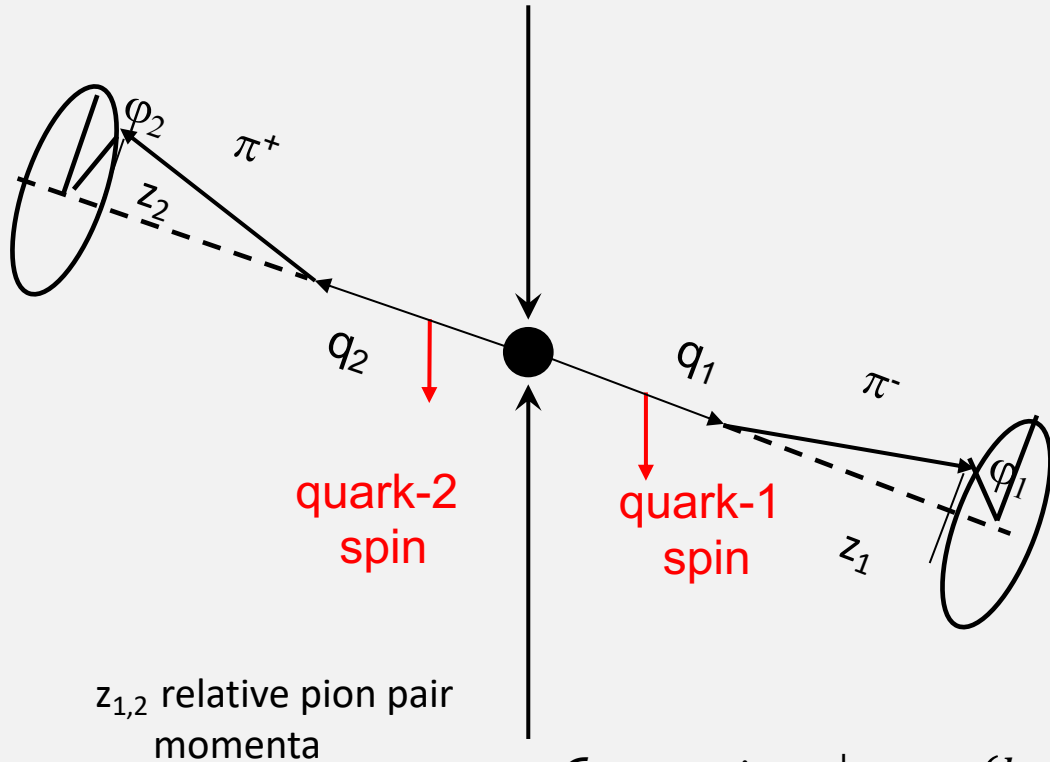


- General increase with z with turnover at larger values of z for mesons
- Protons with smaller width and more linear rise with z



- General increase with z with turnover at larger values of z for mesons
- Clear decrease of widths with increase of T
 - Particles more and more collimated

COLLINS FFs IN e^+e^-

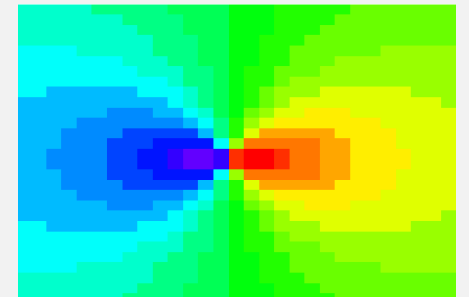


$$\text{Cross-section } e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X$$

$$\propto D_1^\perp \overline{D_1^\perp} + H_1^\perp \overline{H_1^\perp} \cos(\phi_1 + \phi_2)$$

• First non-zero independent measurement of the Collins effect for pion pairs in e^+e^- annihilation by Belle Collaboration @ $\sqrt{s} \sim 10.6$ GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032) from SIDIS and e^+e^-

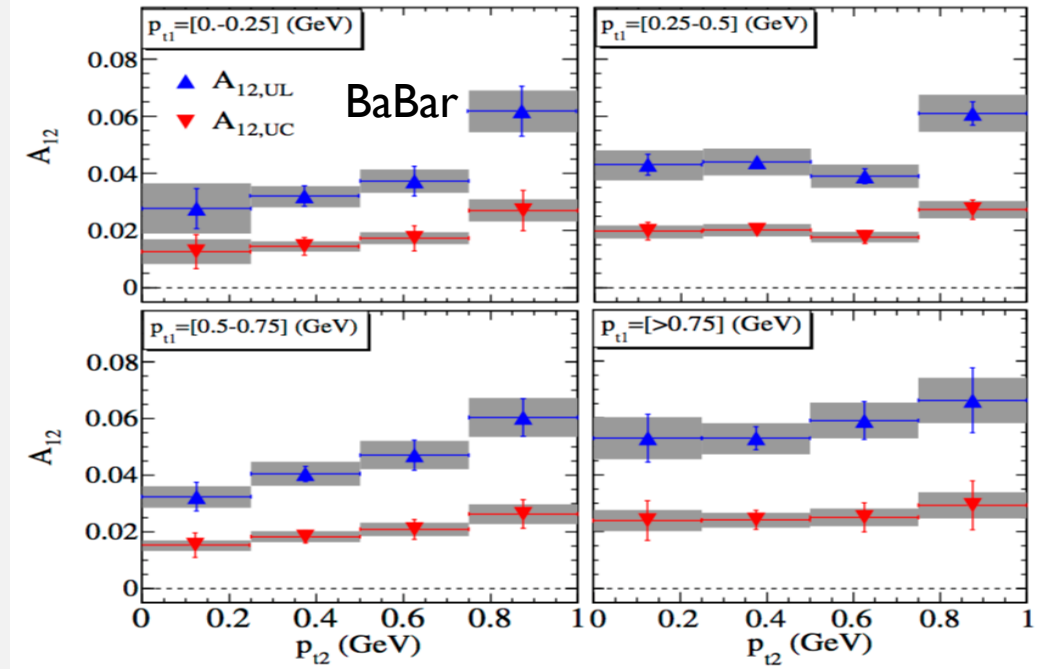
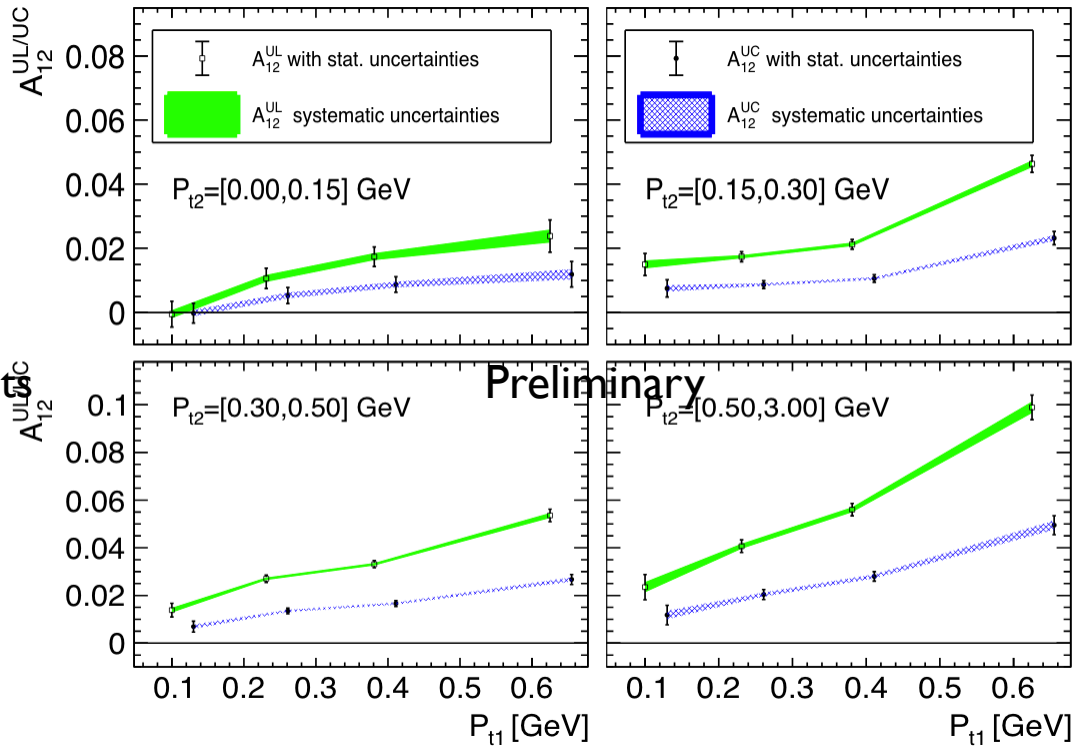
- Confirmed by BaBar @ $\sqrt{s} \sim 10.6$ GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and $K\pi$)
- Measured at BESIII @ $\sqrt{s} = 3.65$ GeV (PRL 116,42001(2016))



- Access spin dependence and p_T dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities

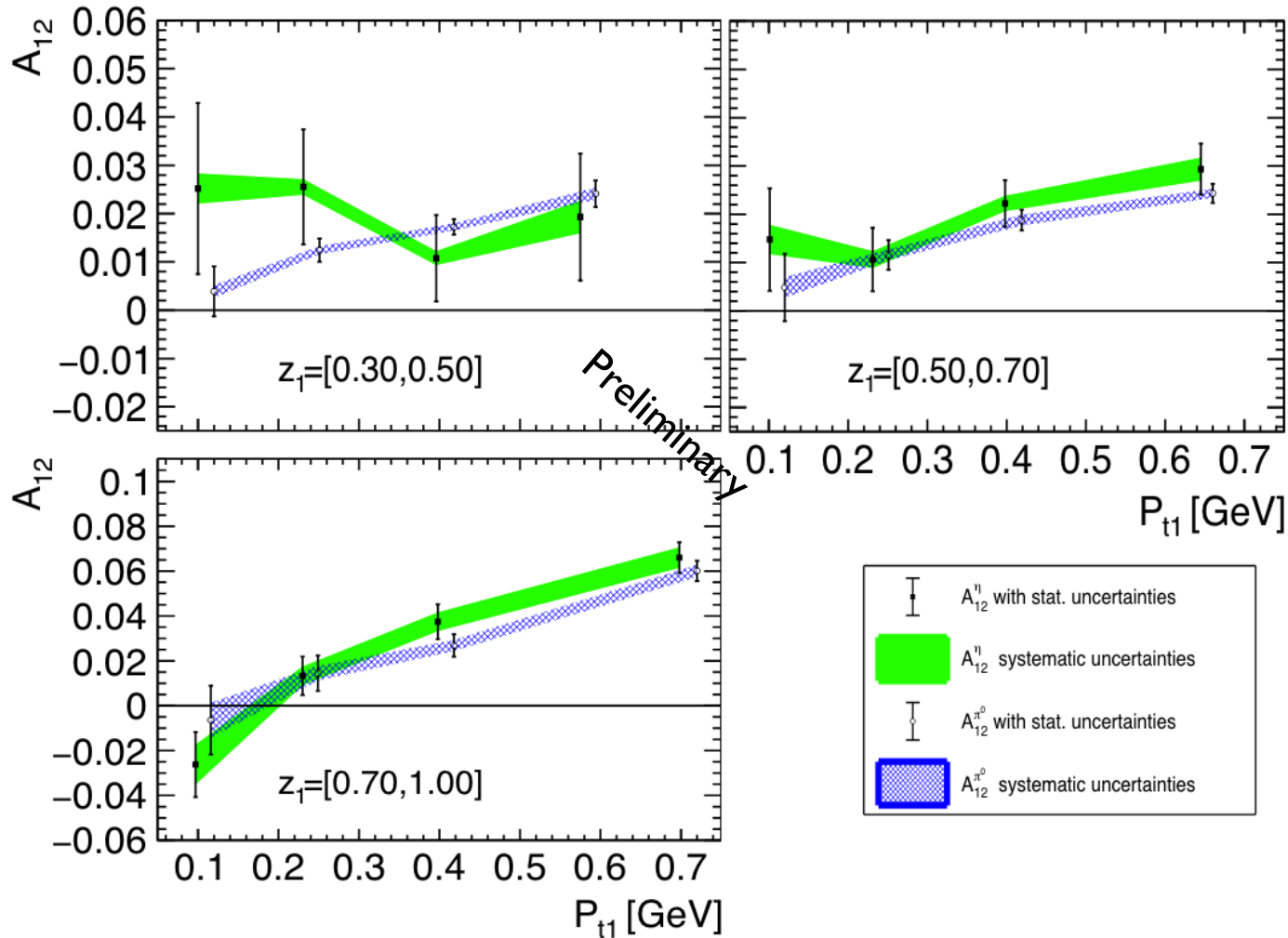
NEW PT DEPENDENCE FROM BELLE

Unlike/Likesign
 Ratios to cancel
 acceptance effects
Unlike:
 $\frac{fav*fav+dis*dis}{fav*dis}$
Like:
 $\frac{fav*dis}{fav*dis}$



- Trend consistent with BaBar
- Direct comparison difficult due to different correction schemes (thrust vs $q\bar{q}$ -axis)

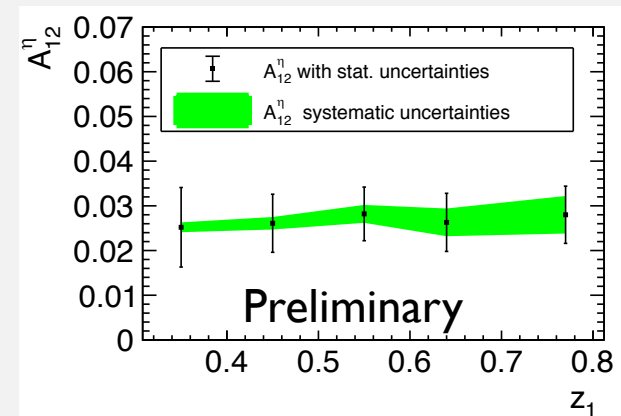
NEW π^0/η FROM BELLE



$$\mathcal{R}_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} = \frac{\pi^0\pi^+ + \pi^0\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

$$\mathcal{R}_{12}^{\eta} = \frac{R_{12}^{\eta\pm}}{R_{12}^L} = \frac{\eta\pi^+ + \eta\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

- **Rise with $z_{1,2}$, similar to charged pions**



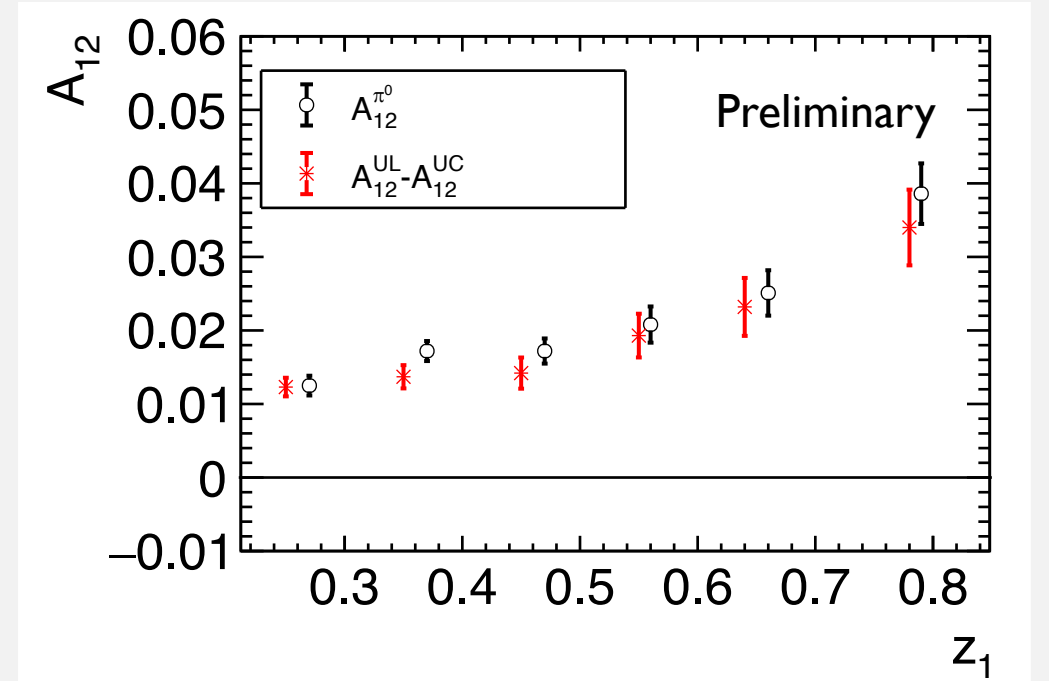
- η almost flat except large z

CONSISTENCY BETWEEN NEUTRAL AND CHARGED PIONS

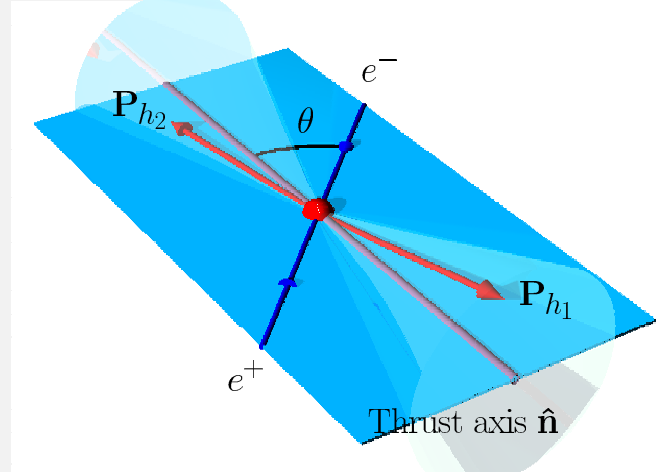
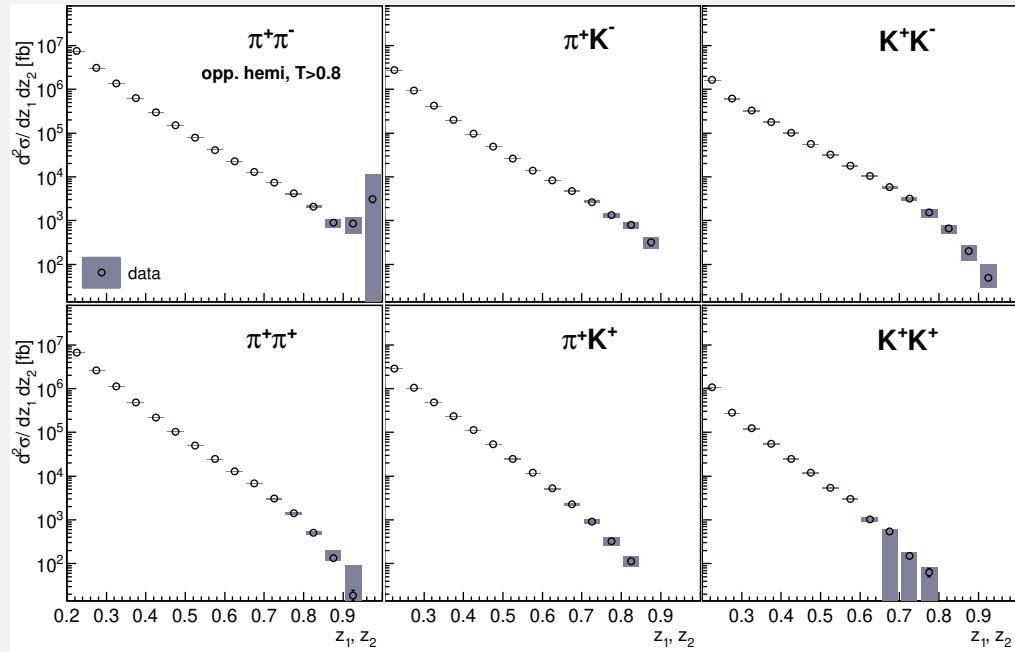
$$\mathcal{R}_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} \approx 1 + \cos(\phi_{12}) \frac{\sin^2(\theta)}{1 + \cos^2(\theta)}$$

$$\times \left\{ \frac{5(H_1^{\perp, fav} + H_1^{\perp, dis}) \otimes (H_1^{\perp, fav} + H_1^{\perp, dis}) + 4H_{1,s \rightarrow \pi}^{\perp, dis} \otimes H_{1,s \rightarrow \pi}^{\perp, dis}}{5(D_1^{fav} + D_1^{dis}) \otimes (D_1^{fav} + D_1^{dis}) + 4D_{1,s \rightarrow \pi}^{dis} \otimes D_{1,s \rightarrow \pi}^{dis}} - \frac{10H_1^{\perp, fav} \otimes H_1^{\perp, dis} + 2H_{1,s \rightarrow \pi}^{\perp, dis} H_{1,s \rightarrow \pi}^{\perp, dis}}{10D_1^{fav} \otimes D_1^{dis} + 2D_{1,s \rightarrow \pi}^{dis} \otimes D_{1,s \rightarrow \pi}^{dis}} \right\}.$$

$$= A_{12}^{UL} - A_{12}^{UC} \text{ (Isospin)}$$



PRD92 (2015) 092007 BACK-TO-BACK

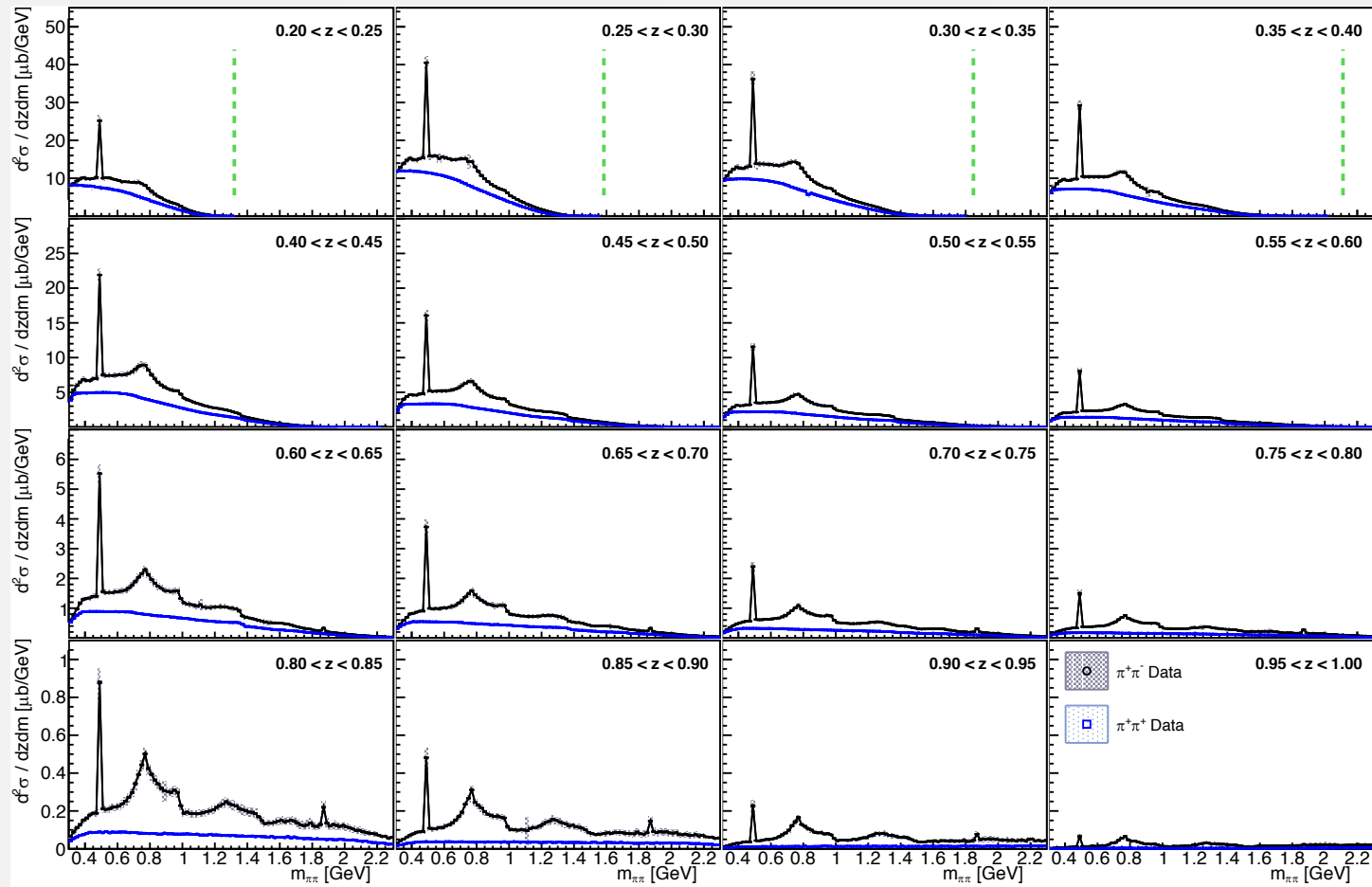


$$T = \max \frac{\sum_h |P_h^{CMS} \cdot \hat{n}|}{\sum_h |P_h^{CMS}|}$$

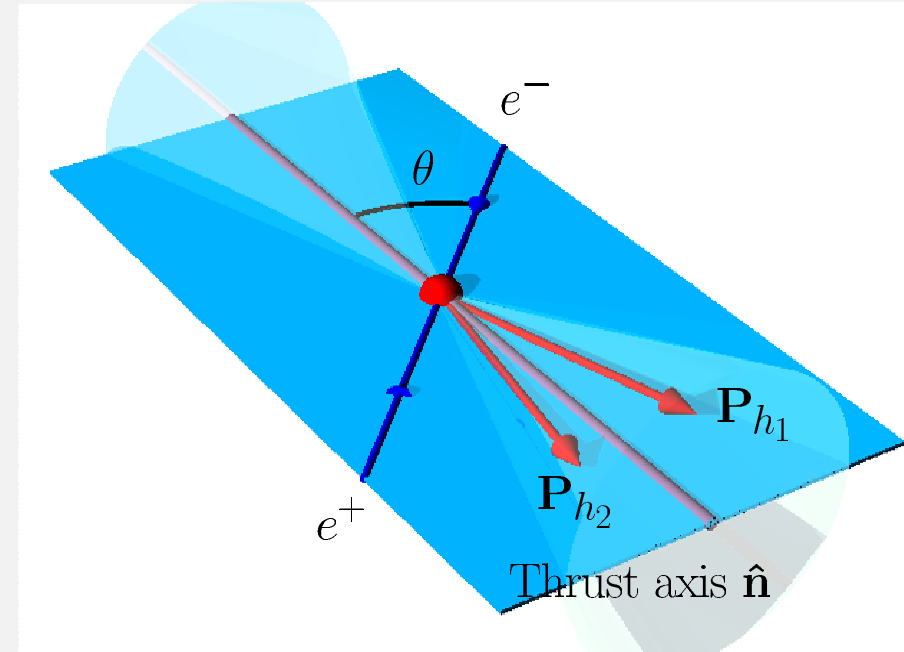
- Also
 - 'any-hemisphere' (a la de Florian & Vanni (Phys Lett B 578 (2004) 139))
 - Same-hemisphere \rightarrow di-hadrons

MASS DEPENDENCE OF DI-HADRONS IN SAME HEMISPHERE \rightarrow DI-HADRON FF

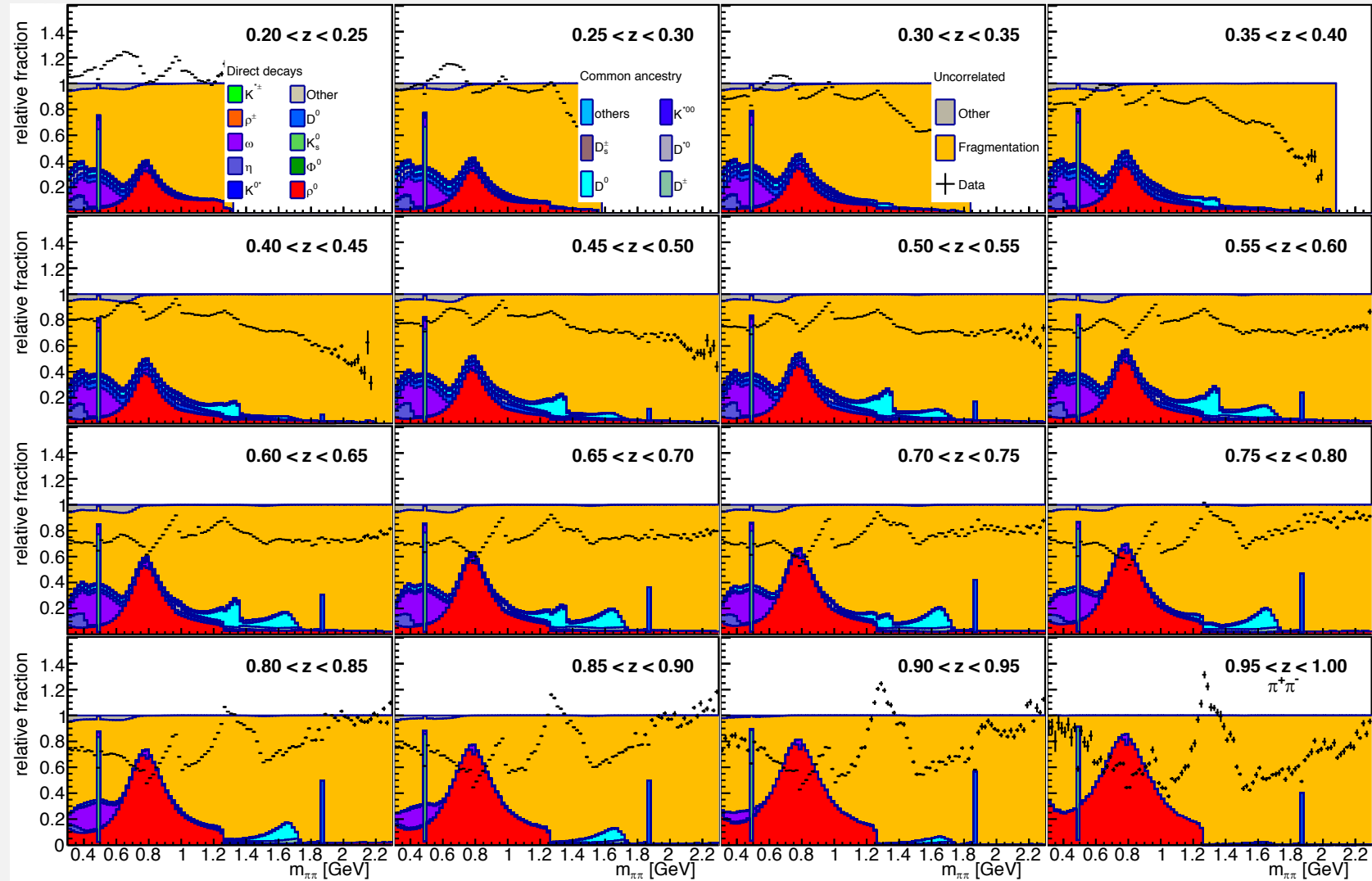
(Phys.Rev. D96 (2017) no.3, 032005)



m [GeV]

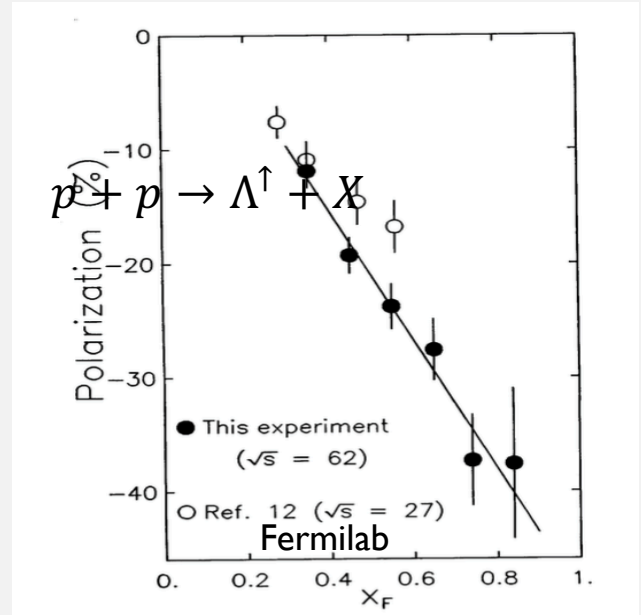


IMPORTANCE OF CORRELATED PRODUCTION



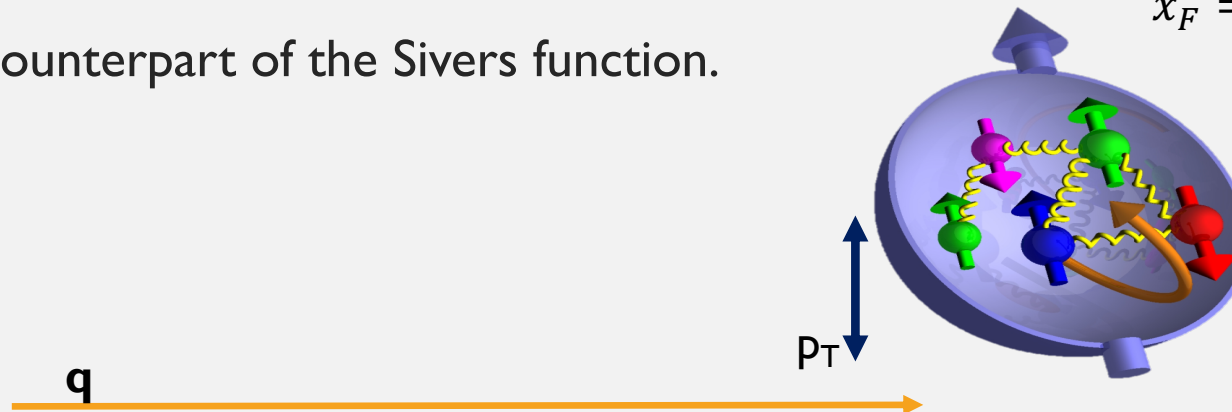
POLARIZED HYPERON PRODUCTION

- Large Λ transverse polarization in unpolarized pp collision **PRL36, 1113 (1976); PRL41, 607 (1978)**
- Caused by polarizing FF $D_{1T}^\perp(z, p_\perp^2)$?
- Polarizing FF is chiral-even, has been proposed as a test of universality. **PRL105,202001 (2010)**
- OPAL experiment at LEP has studied transverse Λ polarization, no significant signal was observed. **Eur. Phys. J. C2, 49 (1998)**
- FF counterpart of the Sivers function.



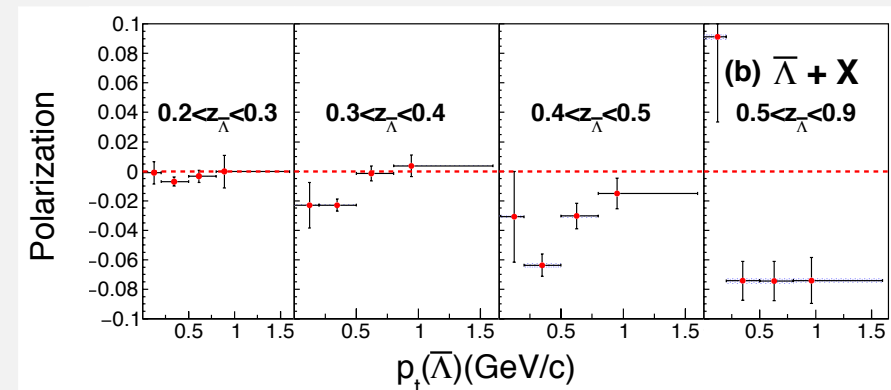
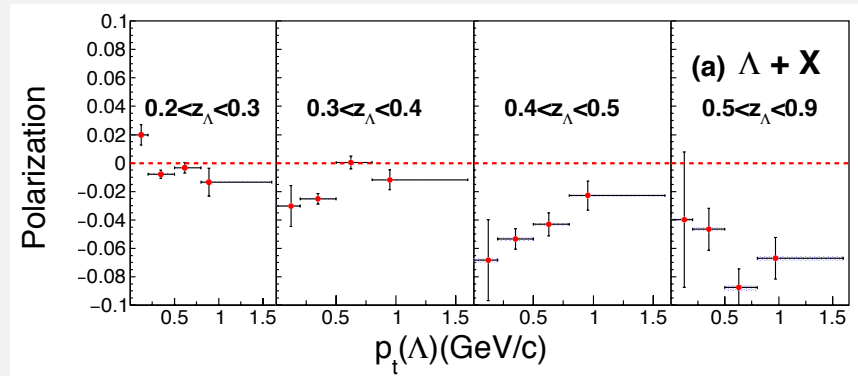
ISR data
(Phys.Lett. B185 (1987) 209)

$$x_F = p_L / \max p_L \sim LO x_1 - x_2 \sim \text{forward } x_1$$

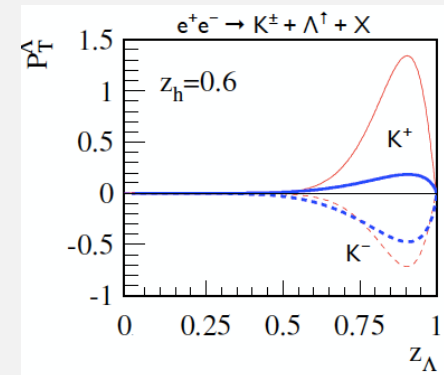
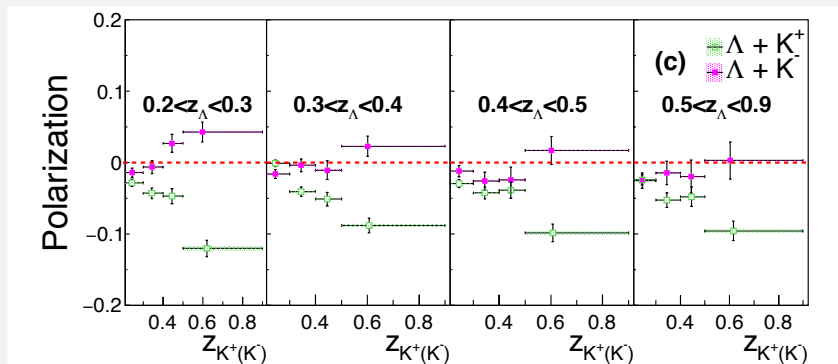
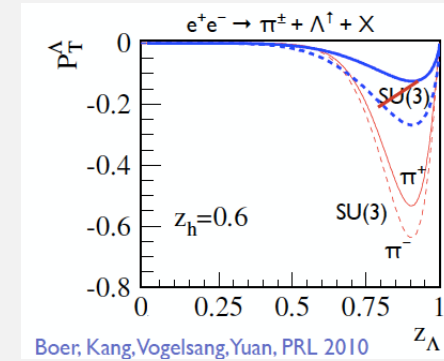
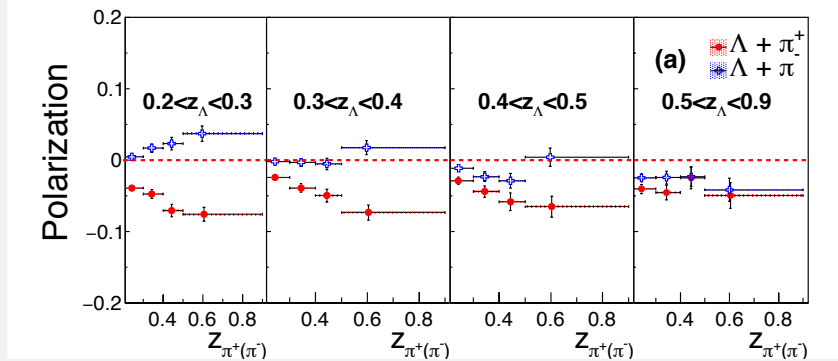


Z_Λ , P_T DEPENDENCE OF OBSERVED Λ POLARIZATION

- Polarization rises with p_t in the lowest z_Λ and highest z_Λ bin. But the dependence reverses around 1 GeV in the intermediate z_Λ bins \rightarrow **Unexpected!**
- Results are consistent between Λ and ($\bar{\Lambda}$)

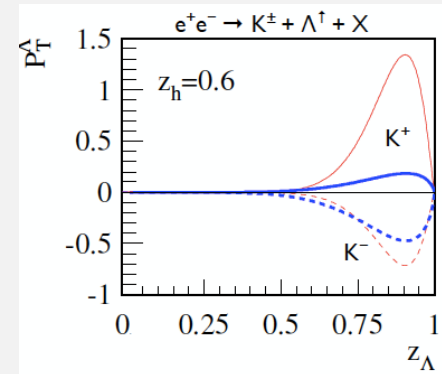
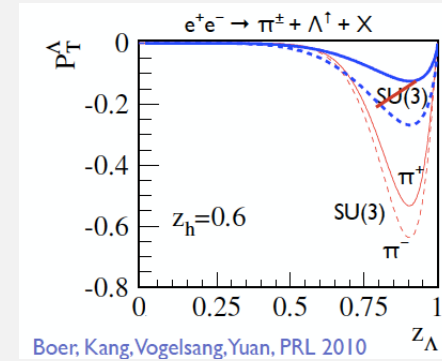
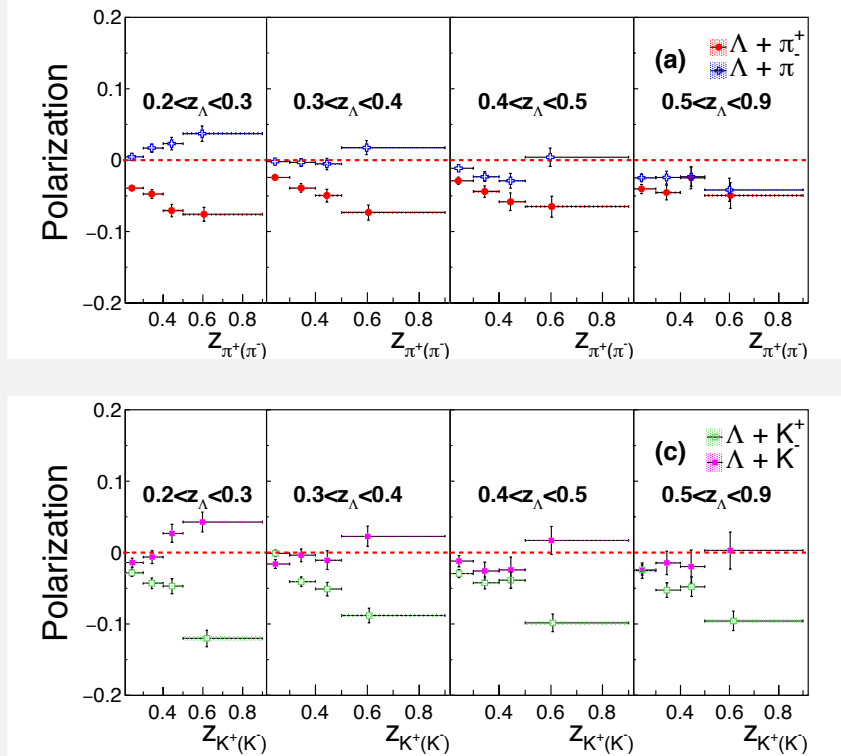


TENSION WITH THEORY: ASSOCIATED PRODUCTION

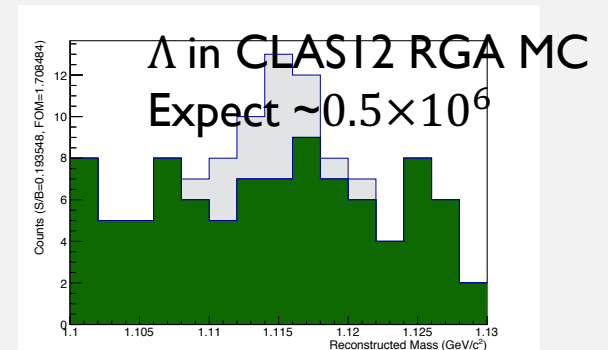


- Correlation with opposite hemisphere light meson \rightarrow quark flav/charge dependence
 - Sign of asymmetry dependent on quark charge of Sivers
- Only experimental results on T-odd, chiral even FF \rightarrow **Important to understand!**

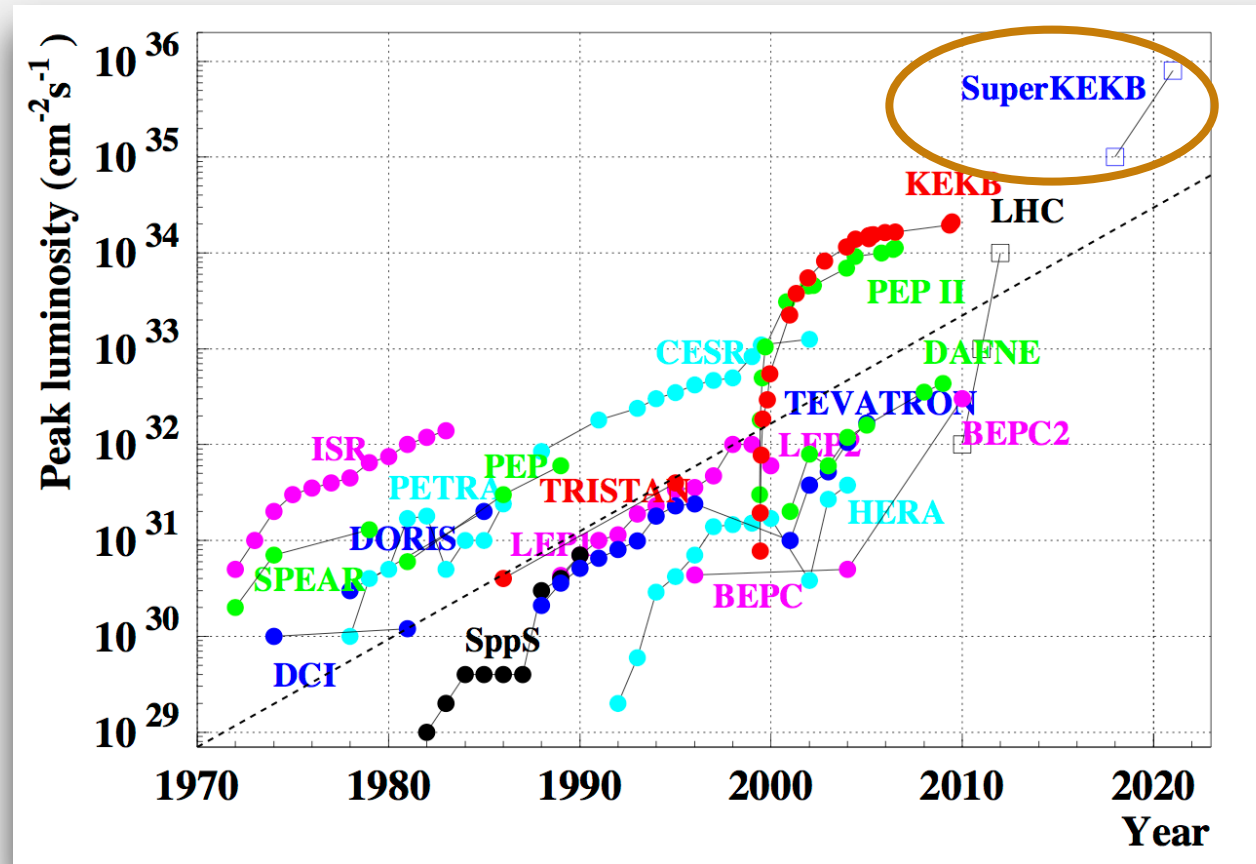
TENSION WITH THEORY: ASSOCIATED PRODUCTION



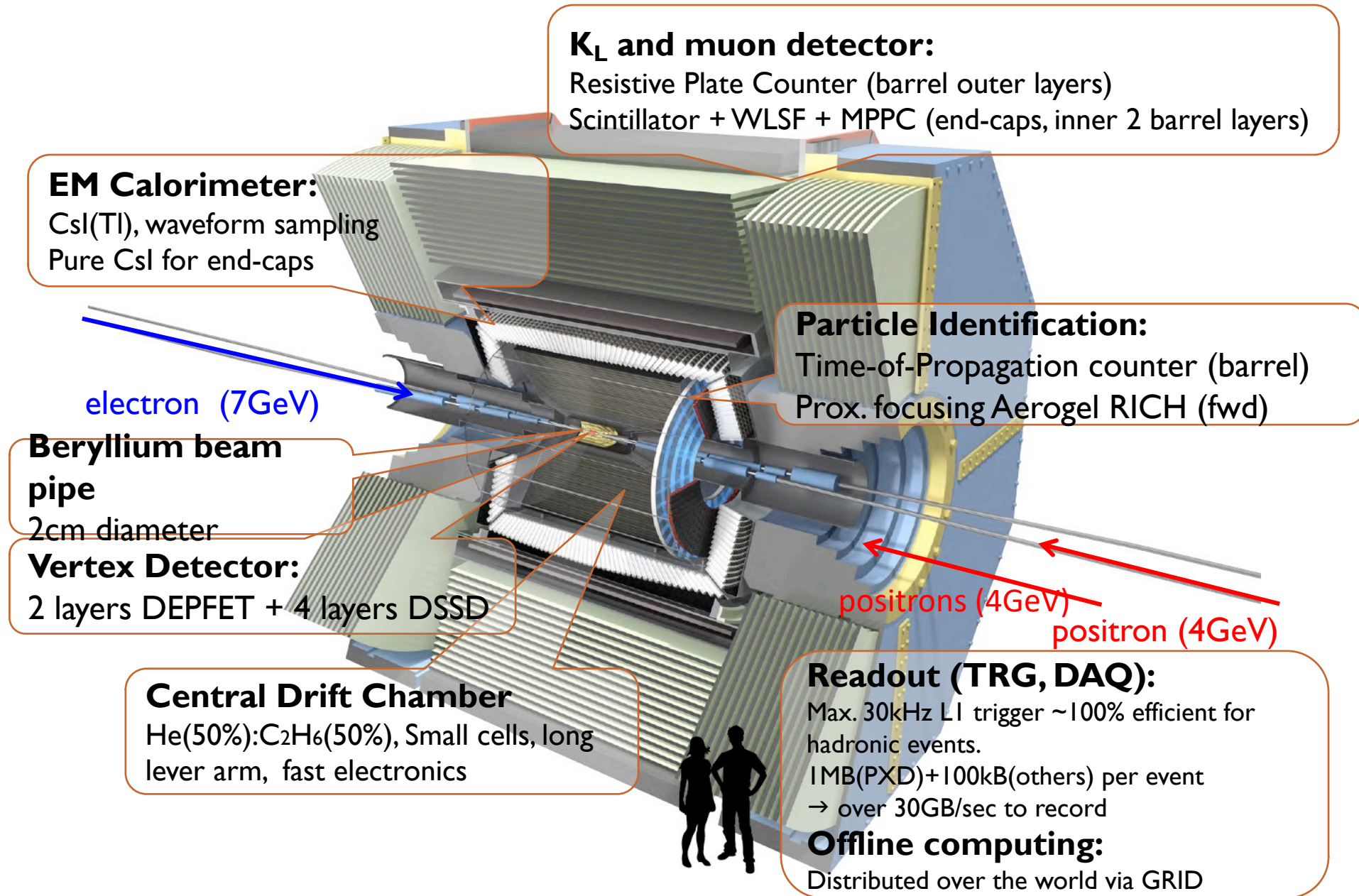
- Correlation with opposite hemisphere light meson \rightarrow quark flav/charge dependence
 - Sign of asymmetry dependent on quark charge of Sivers
- Only experimental results on T-odd, chiral even FF \rightarrow **Important to understand!**
- **E.g. Lambda polarization at CLAS12 or EIC**



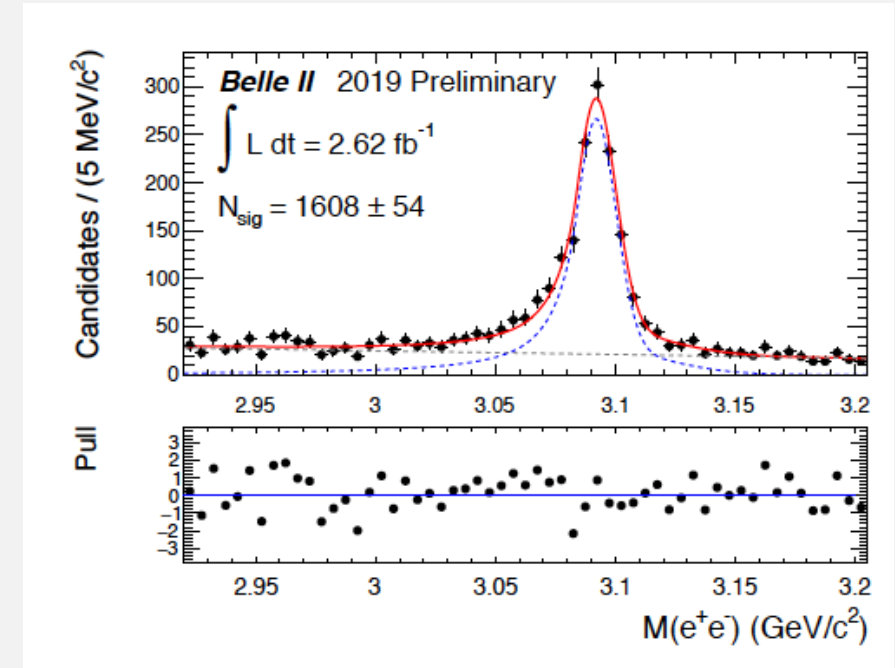
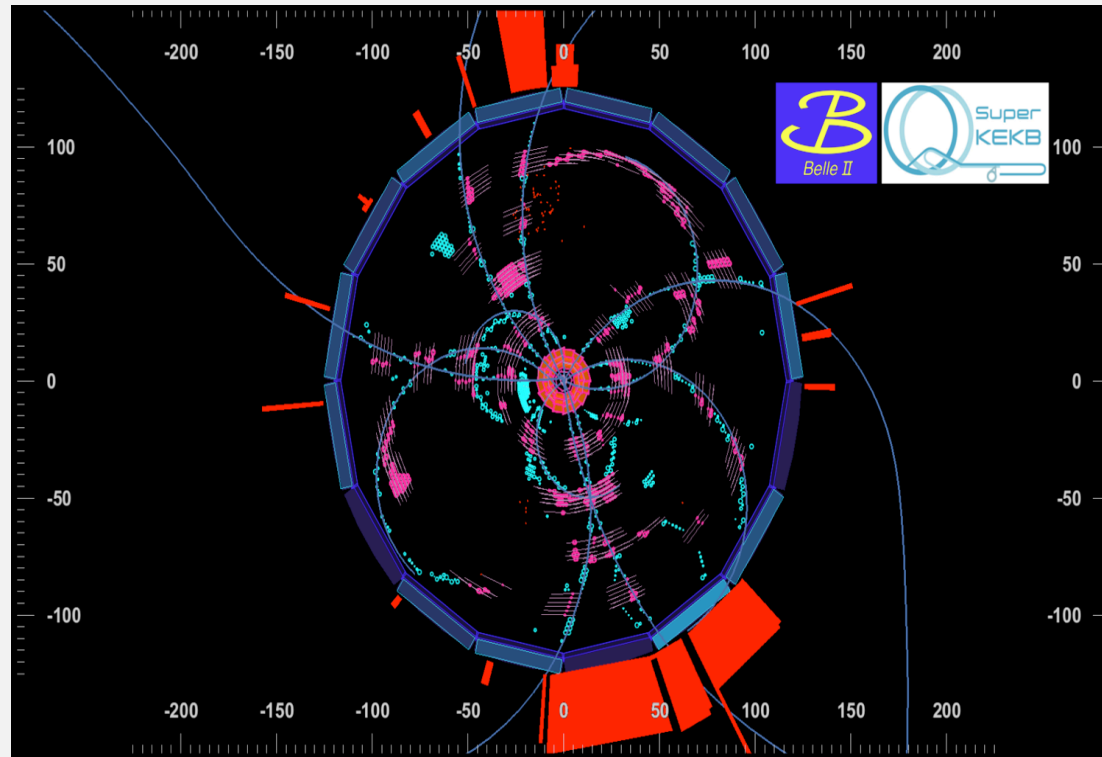
THE FUTURE IS NOW: NEXT GENERATION B FACTORY SUPERKEKB



CUT VIEW OF BELLE II DETECTOR



2019: First Collisions in Phase 3, the Physics Run



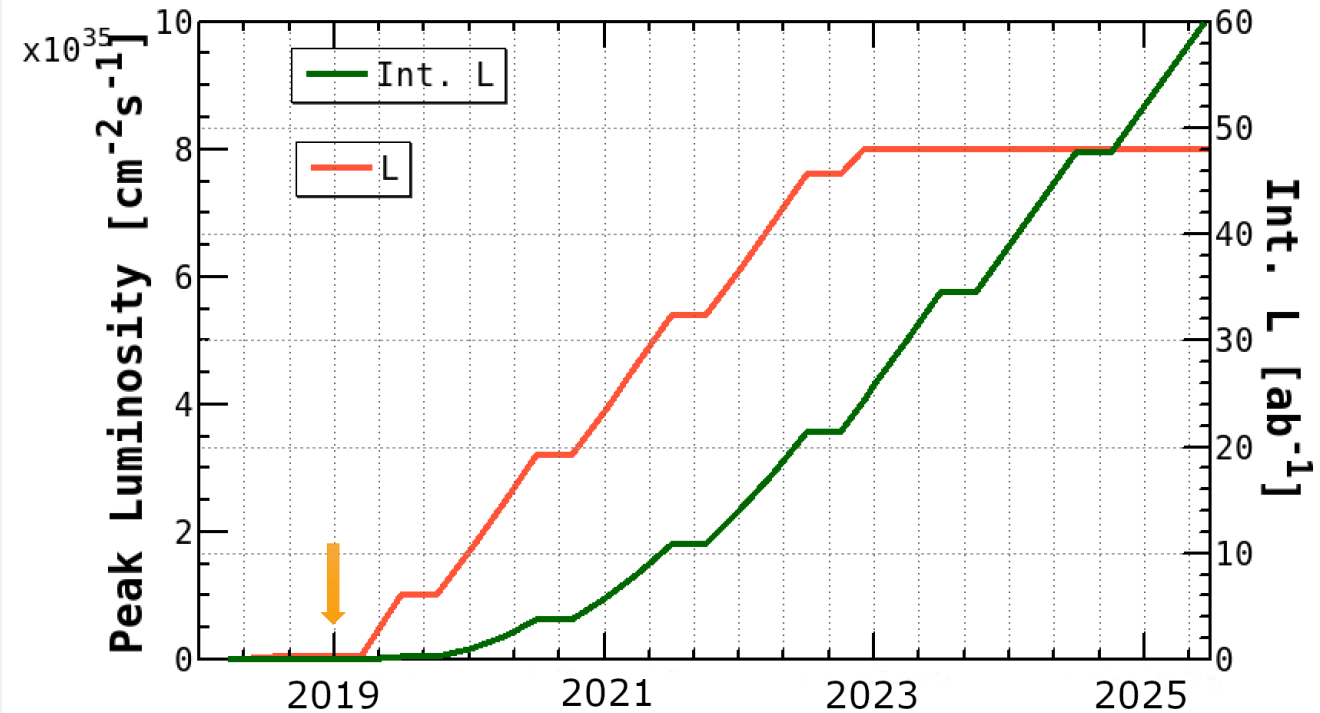
Clear signals for $B \rightarrow J/\psi X$ in $\sim 1/2$ of Phase 3 data.

SUPERKEKB/BELLE II LUMINOSITY PROFILE

Belle/KEKB recorded $\sim 1000 \text{ fb}^{-1}$. Now have to change units on the y-axis to ab^{-1}

Beam currents *only* a factor of two higher than KEKB ($\sim \text{PEP-II}$)

“nano-beams” are the key; vertical beam size is **50nm** at the IP



SUMMARY AND OUTLOOK

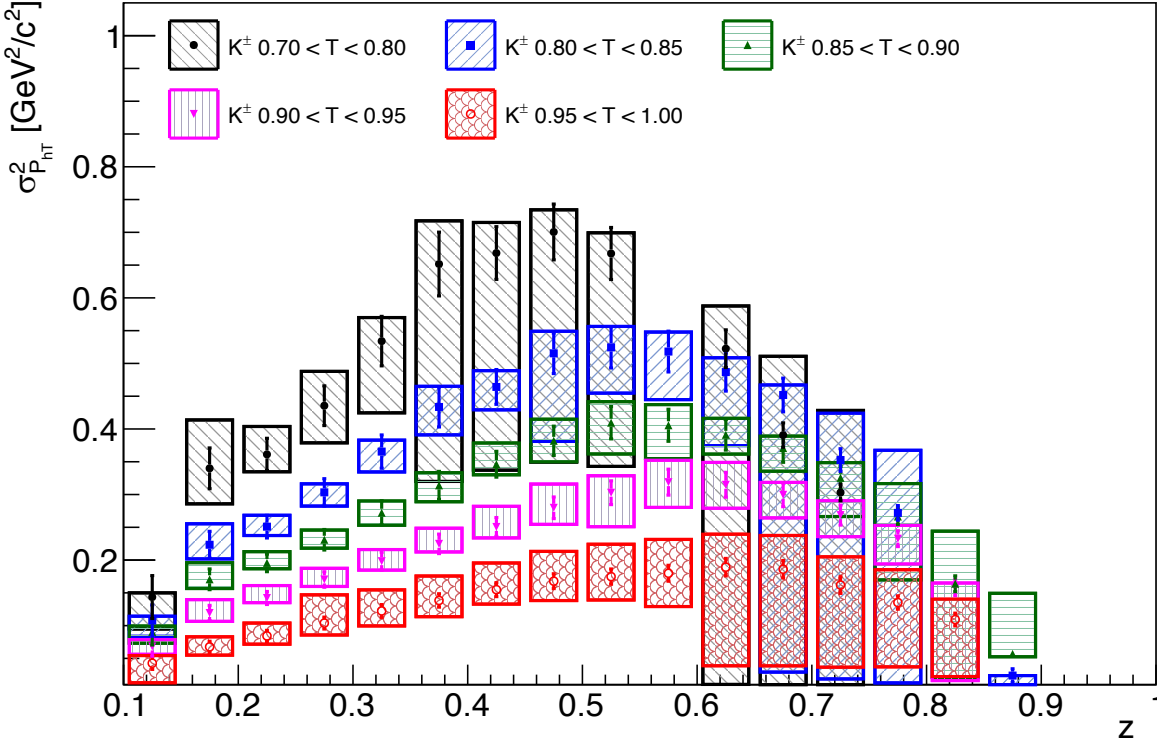
- **Precision measurements of FFs was essential in recent progress in the field of TMDs**
- **A continued program is needed**
 - for the model independent extraction of TMDs and transverse spin structure (and more) from JLab I2 and EIC
 - Studying hadronization
 - Exploring complex QCD mechanisms in a clean configuration
- **Pioneering measurements at Belle and precision measurements at Belle II in the future**



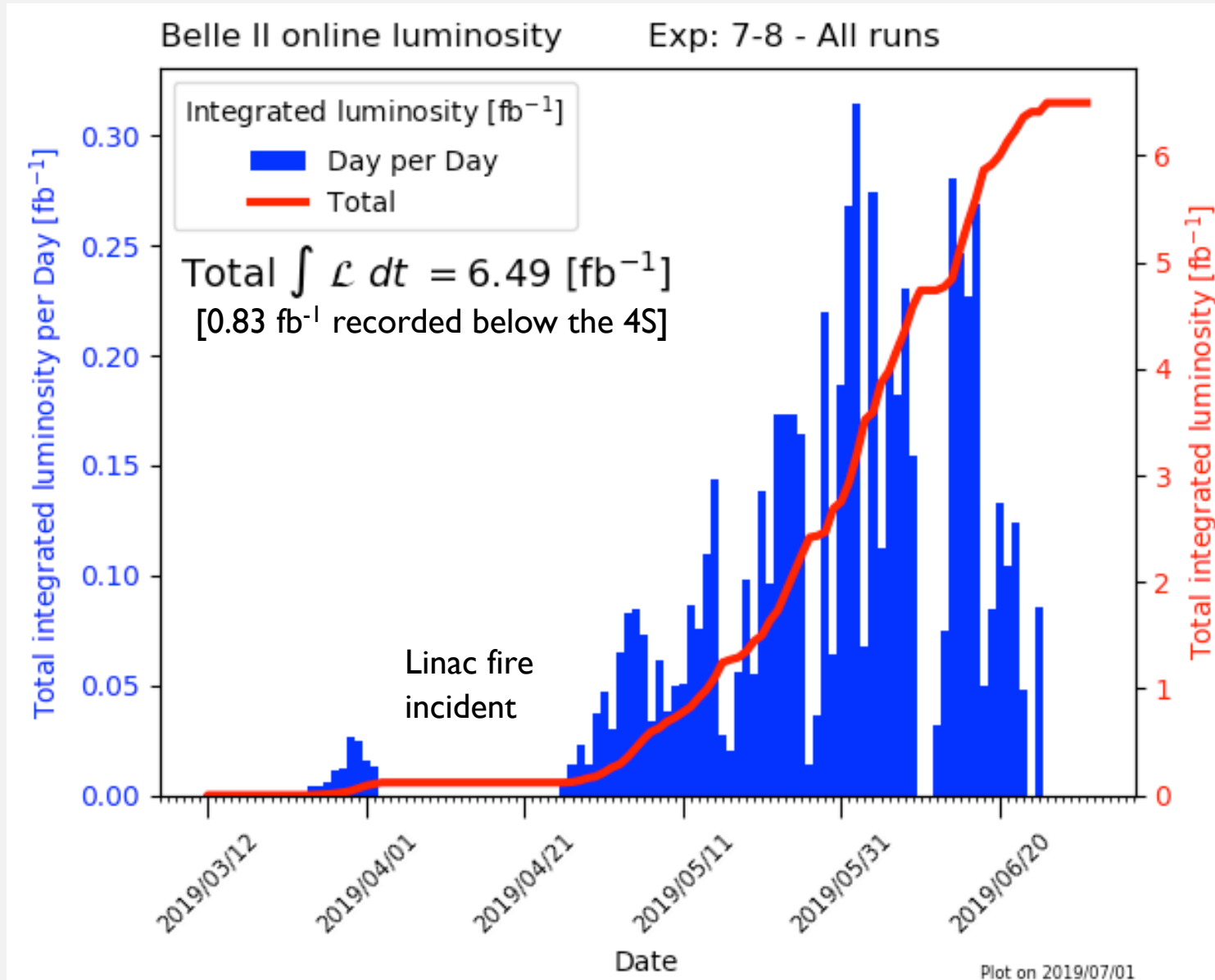
NEED FOR **PRECISION FF PROGRAM** IN THE 12GEV/EIC ERA

- **Fundamental questions in QCD**
 - Study spin-orbit correlations in Hadronization
 - Universality of TMD FFs → Analogue to questions in the PDF sector (Sivers)
 - e^+e^- : Testbed for QCD calculations
 - Generally: Test our models/theory for hadron formation
- **Essential to JLAB 12GeV+EIC**
 - Model independent extraction of transverse spin structure
 - Model independent extraction of TMDs
 - Access to twist3 PDFs

THRUST DEPENDENCE



Spring 2019, First Phase 3 Physics Run: “It was a wild ride”



Only 2 months of collisions.

$L(\text{peak}) \sim 5.5 \times 10^{33} / \text{cm}^2 / \text{sec}$
($\beta_y^* = 3 \text{mm}$)

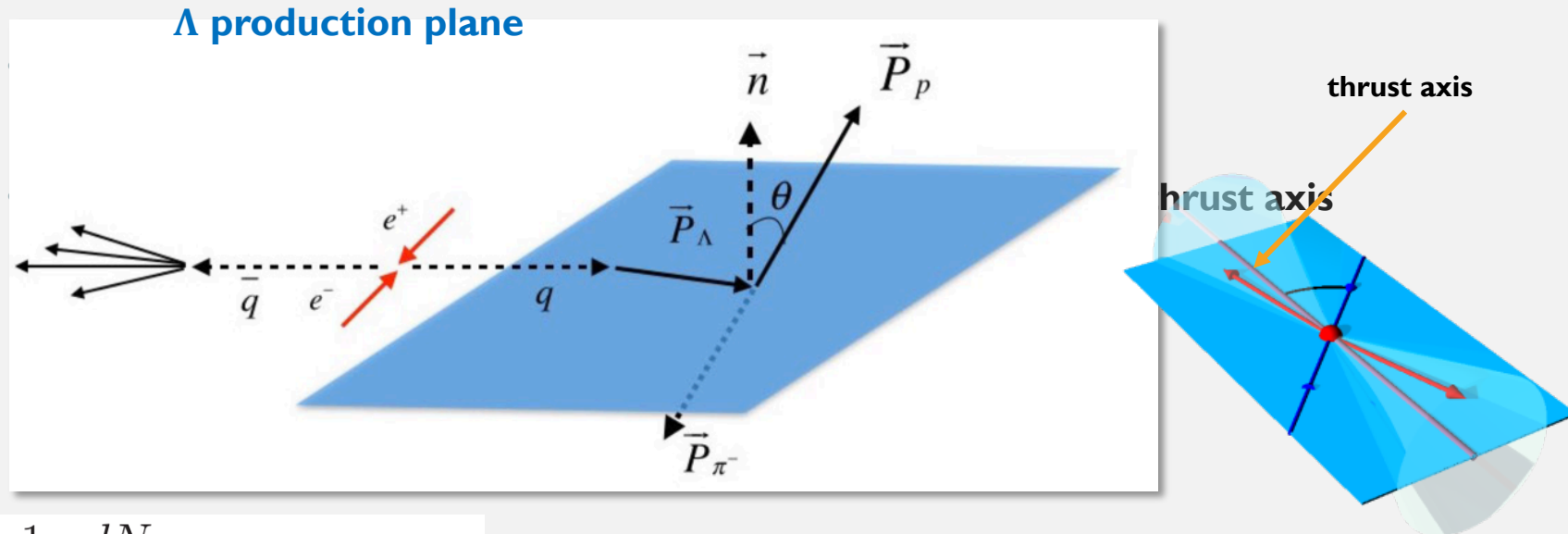
$L(\text{SuperKEKB peak, last week}) \sim 1.2 \times 10^{34} / \text{cm}^2 / \text{sec}$
($\rightarrow \beta_y^* = 2 \text{mm}$)

Comparable to PEP-II best but bkg's X 3 too large to turn on Belle II

OBSERVABLES IN Λ RESTFRAME

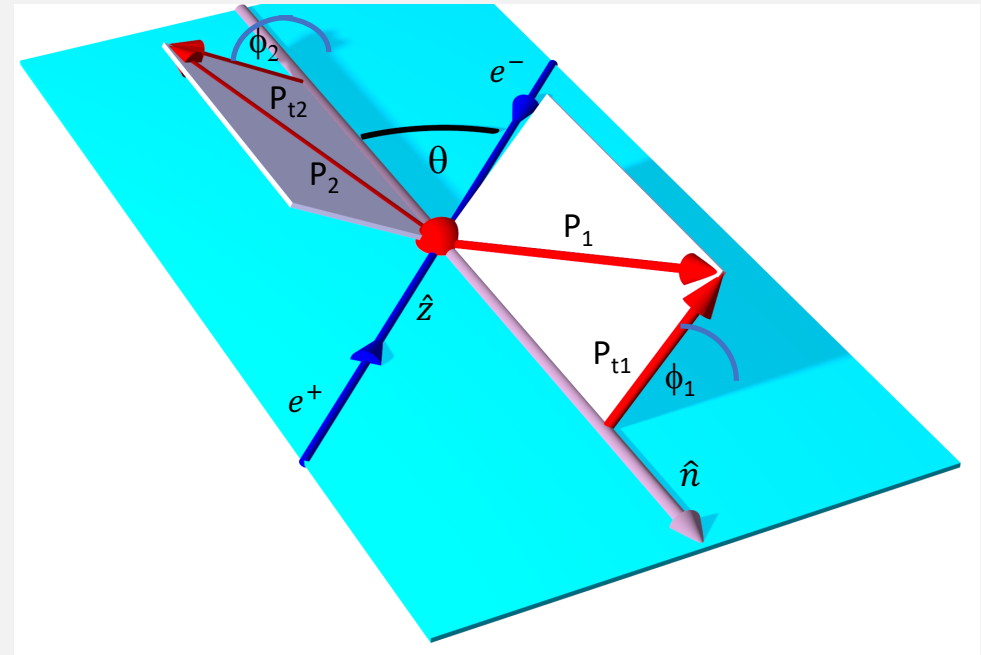
\hat{n} is perpendicular to the Λ production plane.

- Self-analyzing decay leads to polarization dependent distribution

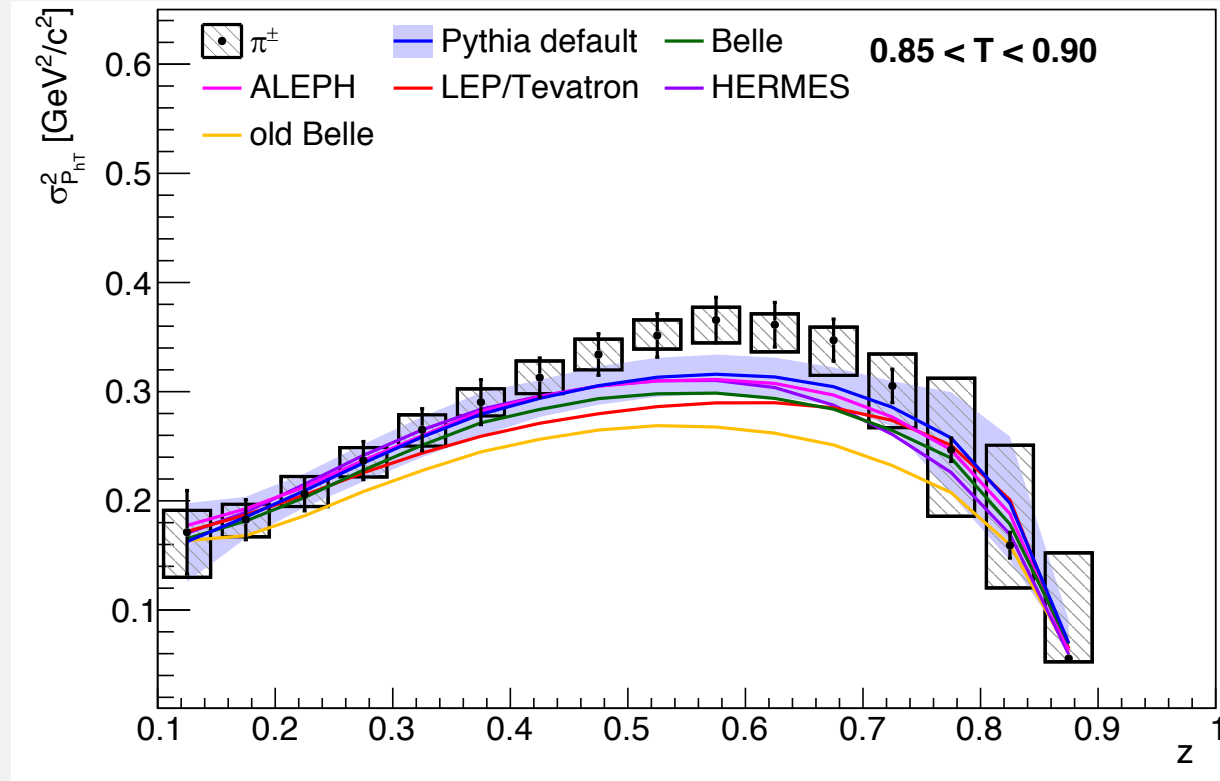


$$\frac{1}{N} \frac{dN}{d\cos\theta} = 1 + \alpha P \cos\theta$$

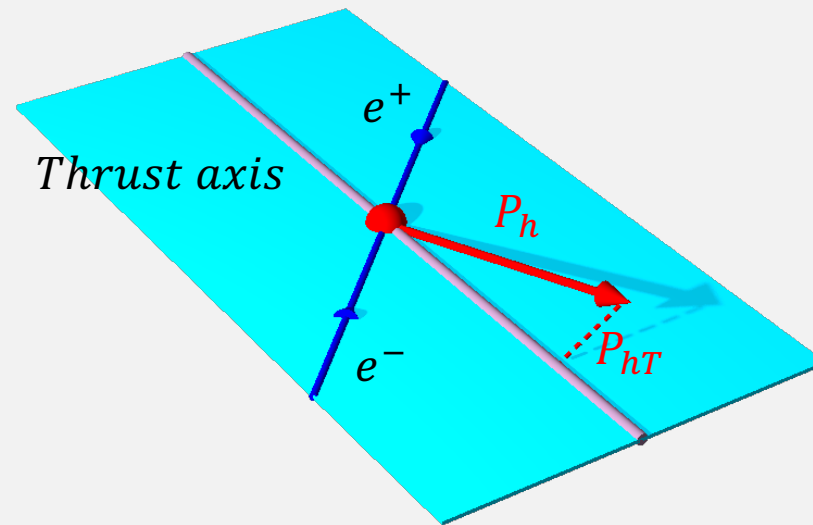
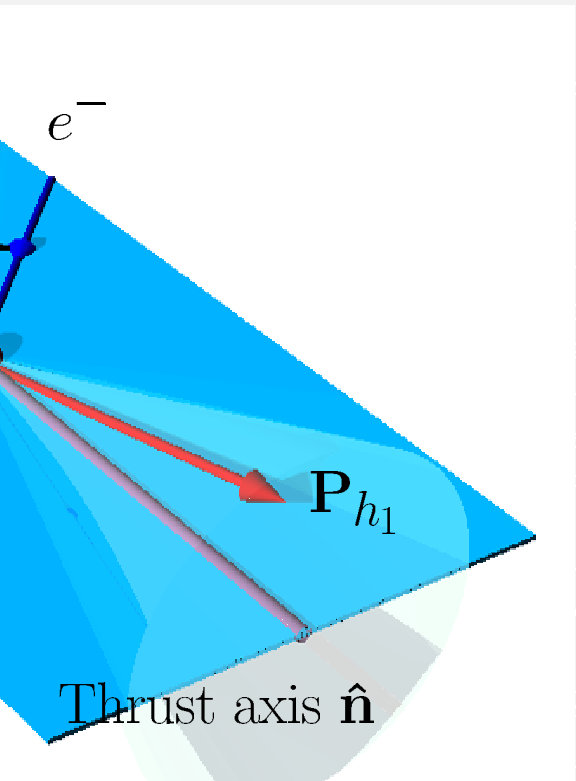
COLLINS



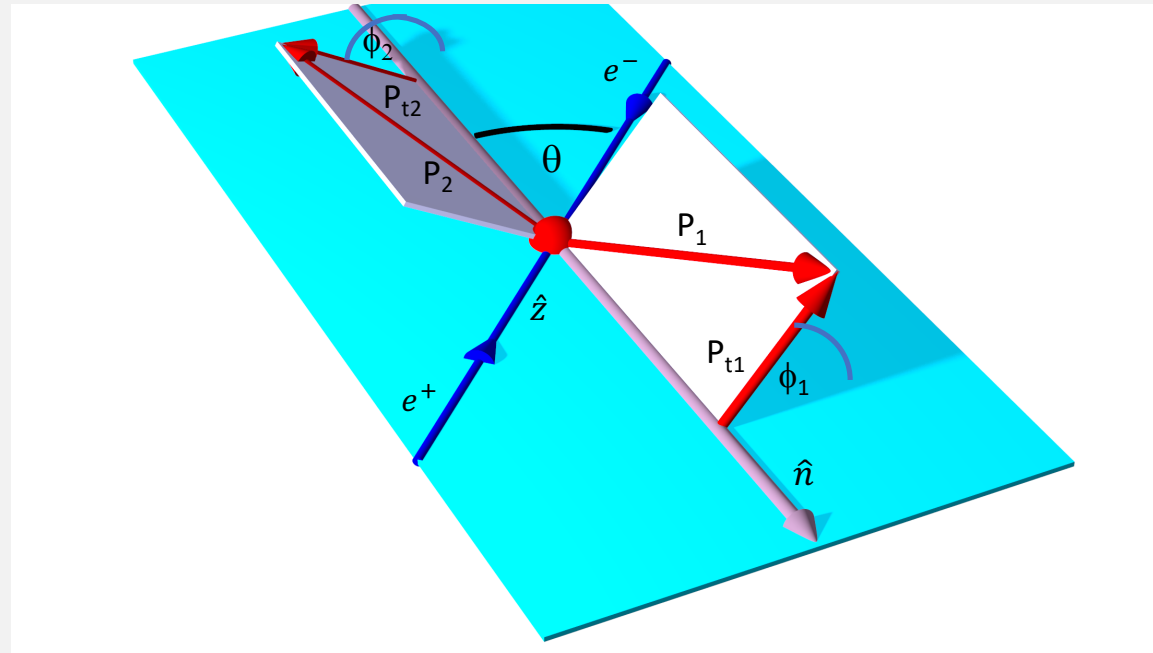
COMPARISON OF GAUSSIAN WIDTHS WITH MC MODELS



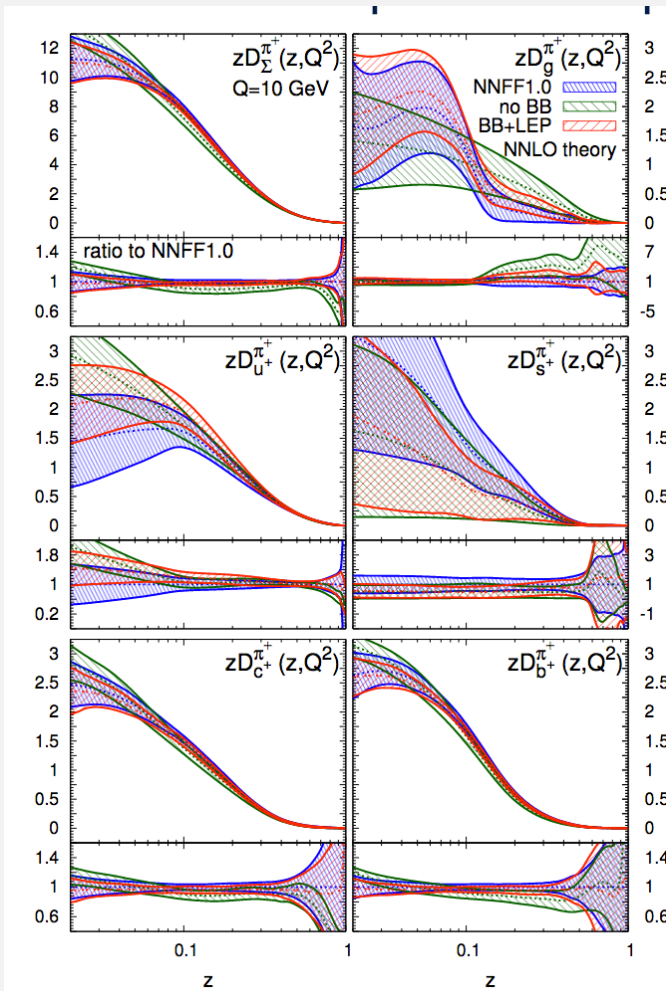
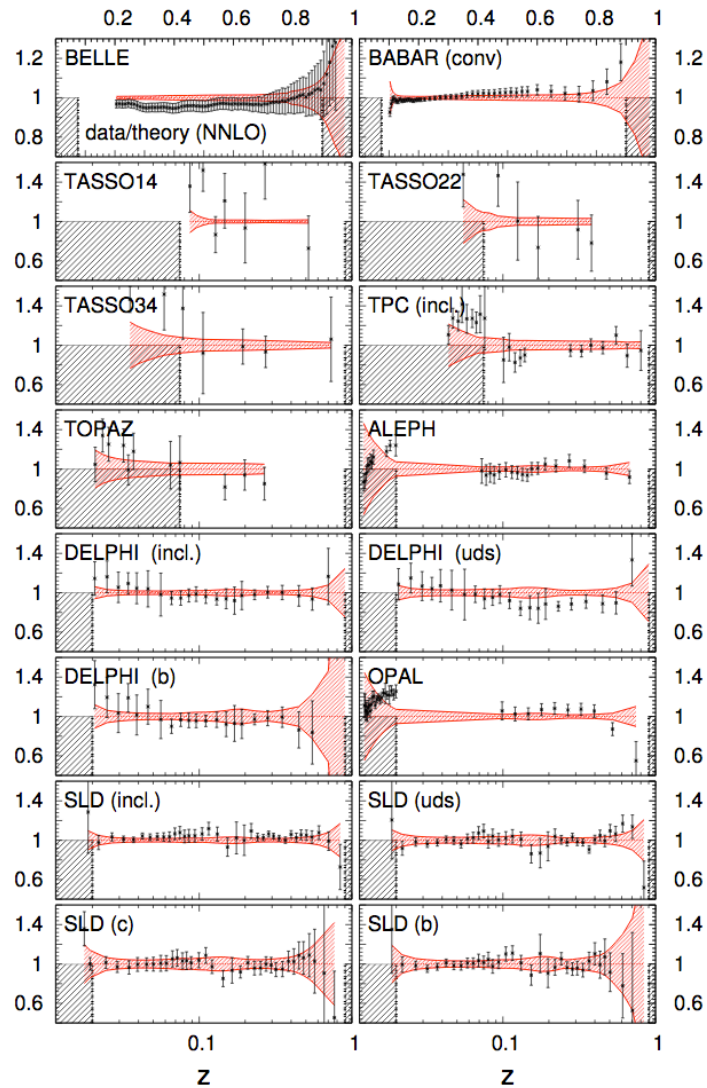
- Discrepancy at intermediate z



POLARIZED (E.G. COLLINS)



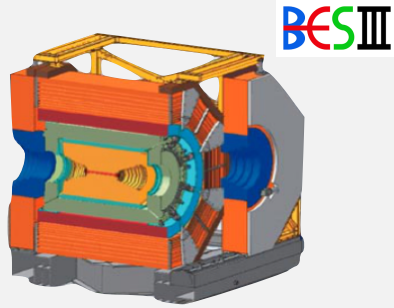
INCLUSIVE π/K WELL DESCRIBED BY THEORY AT NNLO



- Here
 - NNFF, [EPJ C77 (2017) 516
 - but DSS similar

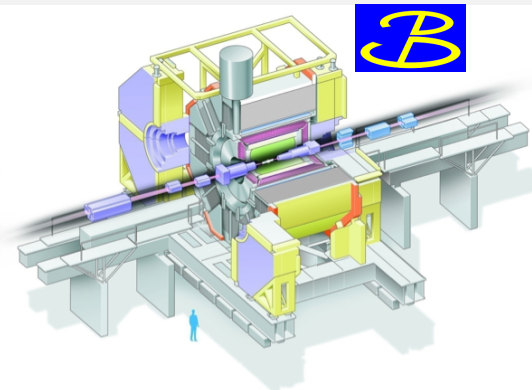
THE BESII, BELLE AND BABAR EXPERIMENTS

NIMA614,345(2010)



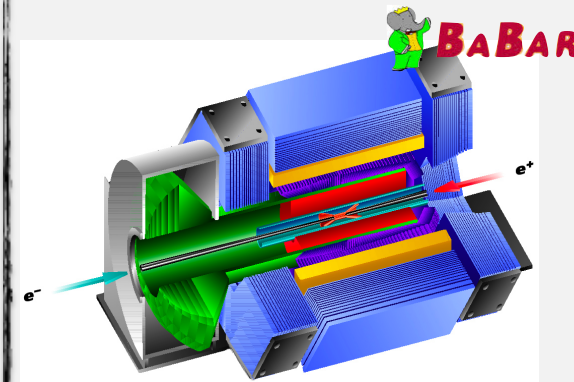
- Symmetric e^+e^- collider
- $\sqrt{s} = [2 - 4.6]$ GeV
- 62 pb^{-1} @ 3.65 GeV used for Collins studies
- Below open-charm threshold

- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.425$
- $L \sim 1 \text{ ab}^{-1}$



NIMA479,117(2002)

NIMA729,615(2013)

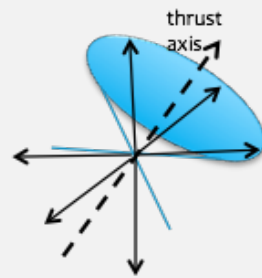


- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.65$
- $L \sim 500 \text{ fb}^{-1}$

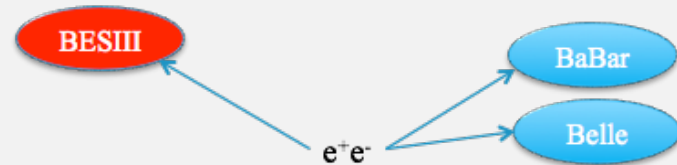
$$T = \sum_i \frac{|\mathbf{P} \cdot \hat{\mathbf{n}}|}{|P|}$$

thrust axis $\equiv \hat{\mathbf{n}}$

$$0.5 \leq T \leq 1$$



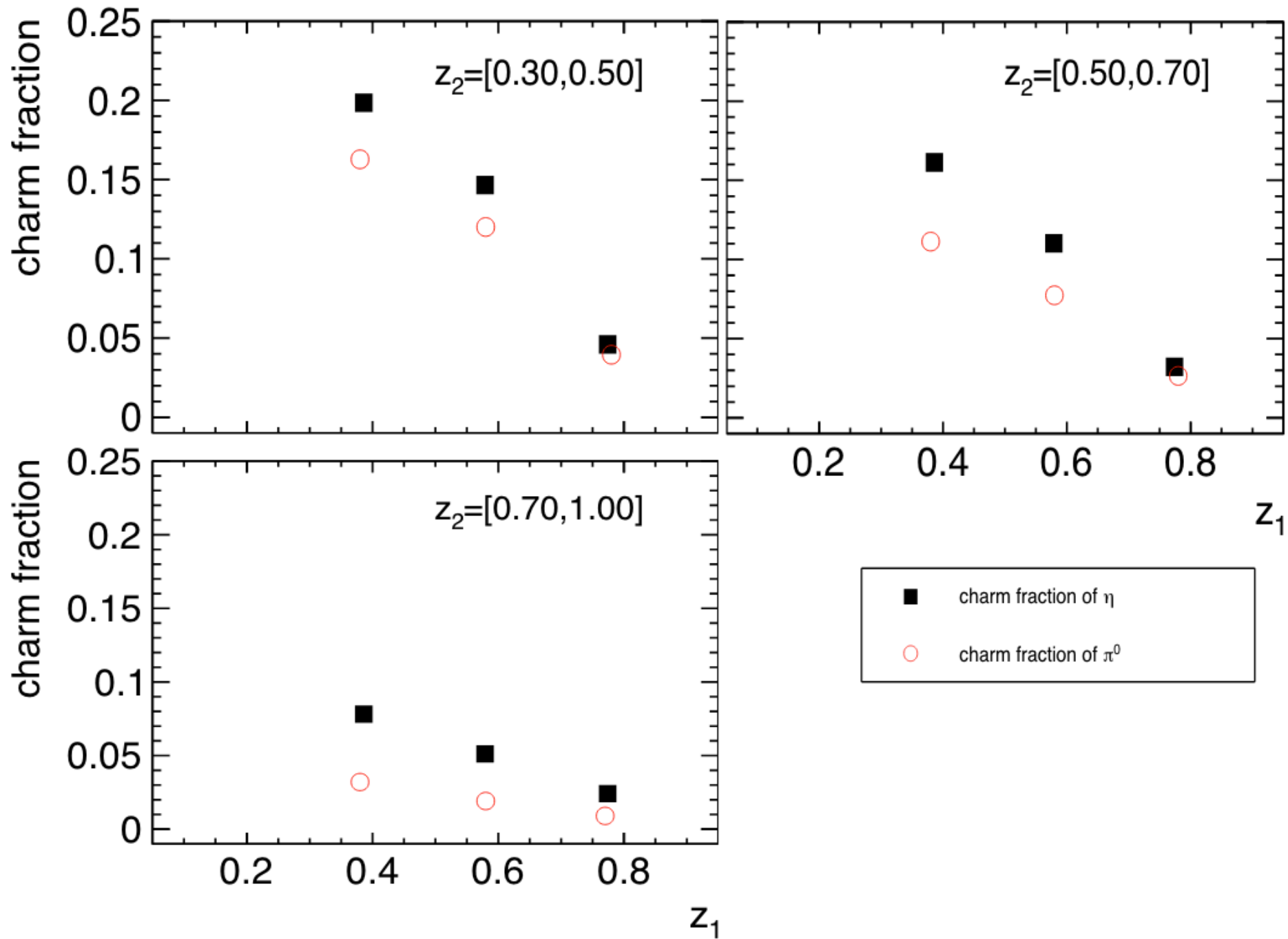
$T \sim 0.5$



1-10 GeV^2 25 GeV^2 100 GeV^2 Q^2



$T \sim 1$



“YOU THINK YOU UNDERSTAND
SOMETHING?---NOW ADD SPIN...**IN
HADRONIZATION!**”

- → **polarized final states**
- → **di-hadron correlations**
- Explore spin-orbit correlation in hadronization
- **Additional degrees of freedom in final state make targeted extraction of nucleon structure possible → see $h_1(x)$, $e(x)$**
- New Fragmentation Functions
- **Obvious relevance for the EIC**
 - Here: Results from RHIC, Belle and plans at Jlab/Belle

KEKB → SUPERKEKB: DELIVER INSTANTANEOUS LUMINOSITY X 40

e^+ 4 GeV 3.6 A

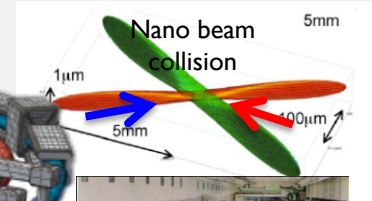
e^- 7 GeV 2.6 A

(~2x KECB)

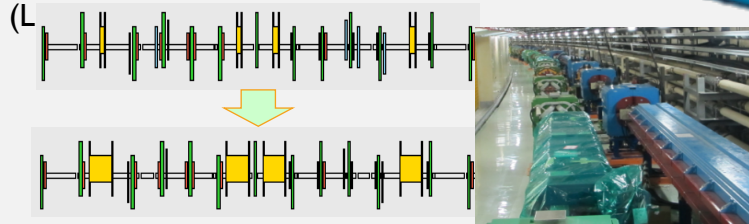
Belle II

New superconducting final focusing quads (QCS) near the IP

SuperKEKB
Target: $L = 8 \times 10^{35} / \text{cm}^2 / \text{s}$



Replace short dipoles with longer ones



Redesign the lattices of HER & LER to squeeze the emittance

TiN-coated beam pipe with antechambers
Cu for wigglers and Al alloy for the rest



Damping ring (new)

@1.1 GeV
To inject low emittance positrons

Low emittance gun
To inject low emittance electrons

$$L = \frac{\gamma_{\pm}}{2e r_e} \left(1 - \frac{\sigma_y^*}{\sigma_x^*} \frac{I_{\pm} \xi_{\pm y}}{\beta^*} \frac{R_L}{R_y} \right)$$

Reinforce RF systems for higher beam current

Positron source
New positron target / capture section

ENTER POLARIZATION IN THE FINAL STATES



Observables:

z : fractional energy of the quark carried by the hadron

$p_{h,T}$: transverse momentum of the hadron wrt the quark direction: **TMD FFs**

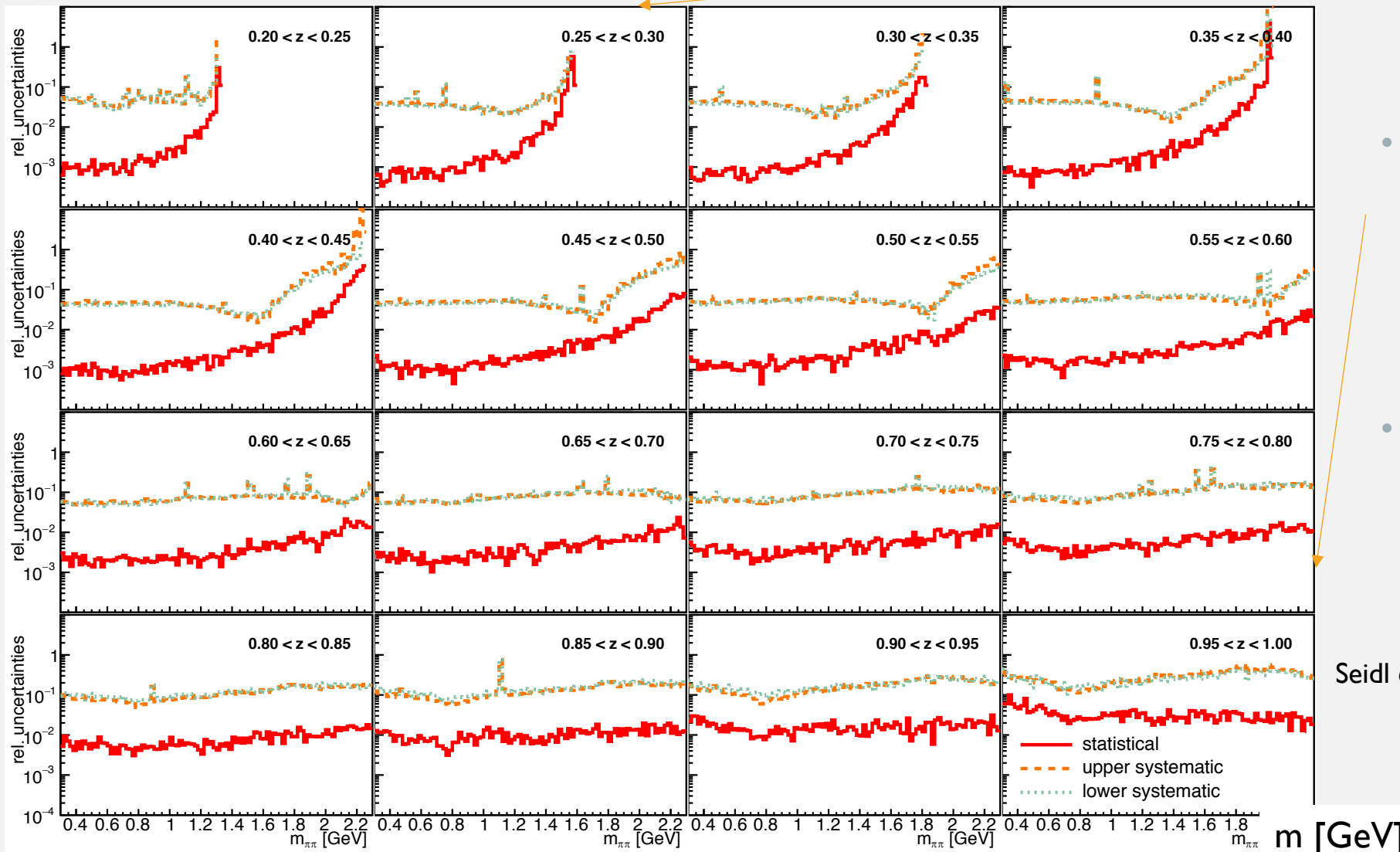
Parton polarization \rightarrow Hadron Polarization \downarrow	Spin averaged	longitudinal	transverse
spin averaged	$D_1^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \right]$		$H_1^{\perp h/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{blue circle} \right] - \left[\downarrow \bullet \rightarrow \text{blue circle} \right]$
longitudinal		$G_1^{\Lambda/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \rightarrow \text{green arrow} \right] - \left[\bullet \leftarrow \text{red circle} \rightarrow \text{green arrow} \right]$	$H_{1L}^{h/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{green circle} \rightarrow \text{green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{green circle} \rightarrow \text{green arrow} \right]$
Transverse (here Λ)	$D_{1T}^{\perp \Lambda/q}(z, p_T) = \left[\bullet \rightarrow \text{blue circle with green arrow} \right]$	$G_{1T}^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{green circle with green arrow} \right] - \left[\bullet \leftarrow \text{green circle with green arrow} \right]$	$H_1^{\Lambda/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{red circle with green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{red circle with green arrow} \right]$ $H_{1T}^{\perp \Lambda/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{green circle with green arrow} \right] - \left[\downarrow \bullet \rightarrow \text{green circle with green arrow} \right]$

- Analogue \rightarrow similar to PDFs encoding spin/orbit correlations
- Determining final state polarization needs self analyzing decay (Λ)
- Gluon FFs similar but with circular/linear polarization (not as relevant for e^+e^-)

DI-HADRONS

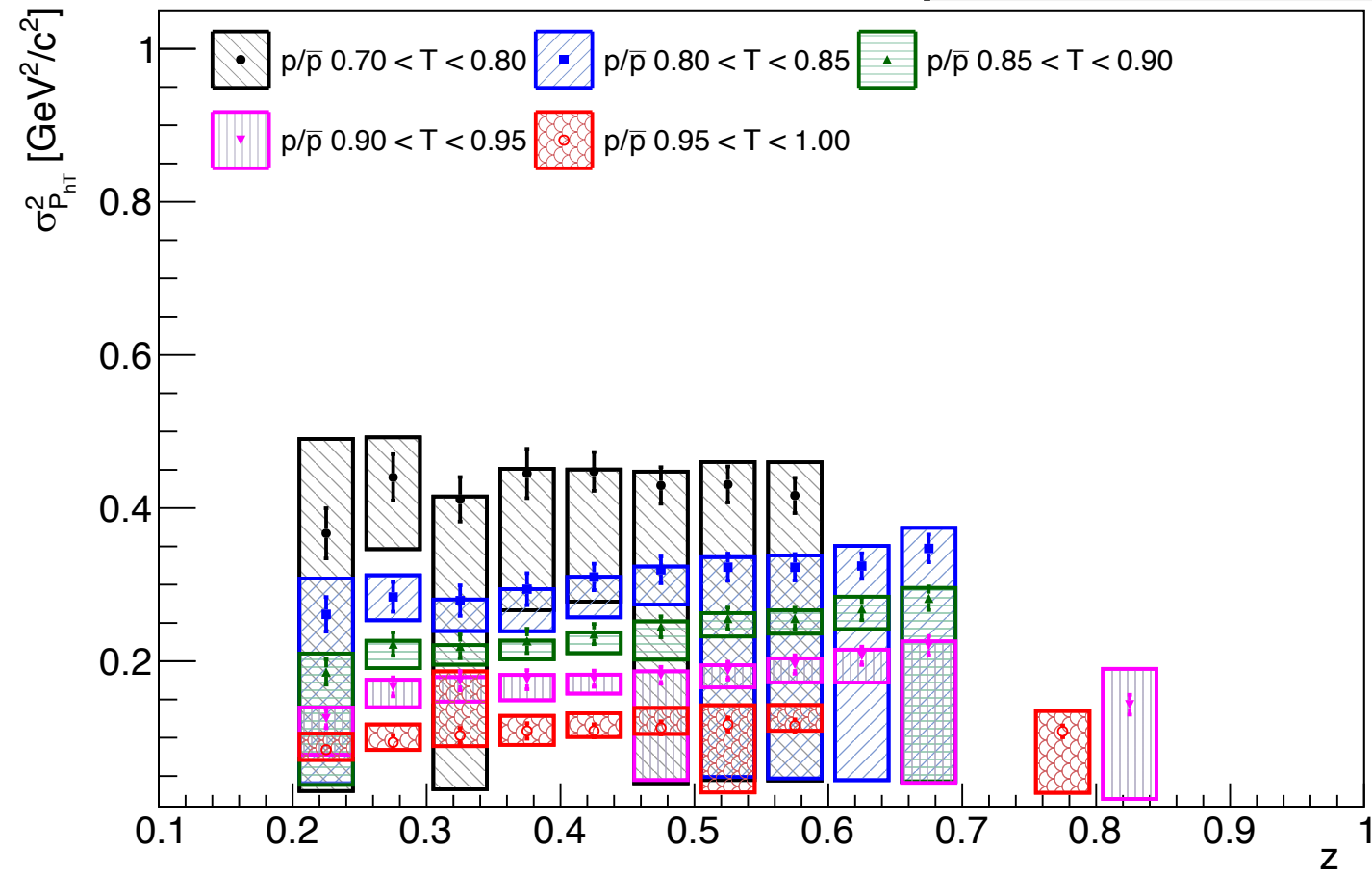
RESULTS SYSTEMATICS DOMINATED

- Low z : Dominated by PID uncertainties
Belle II prospects: Improved PID, higher statistics to improve uncertainties on PID



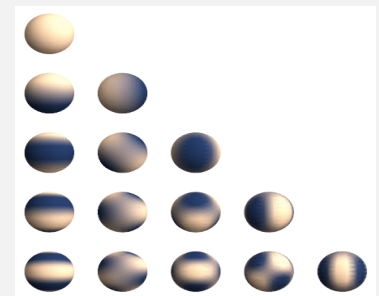
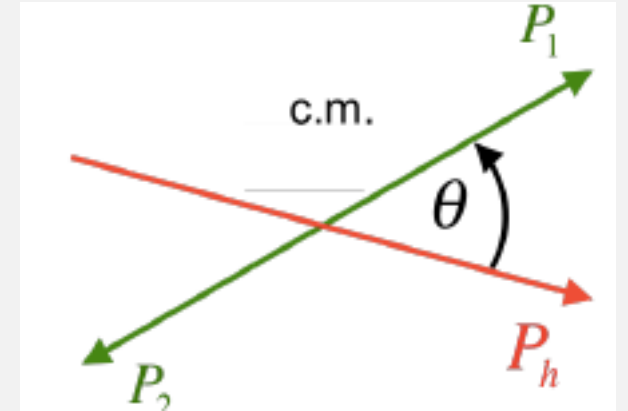
- High z : Dominated by ISR uncertainties
Belle II prospects: better understanding of ISR radiation with better statistics

Seidl et. al. Phys.Rev. D96 (2017) no.3, 032005



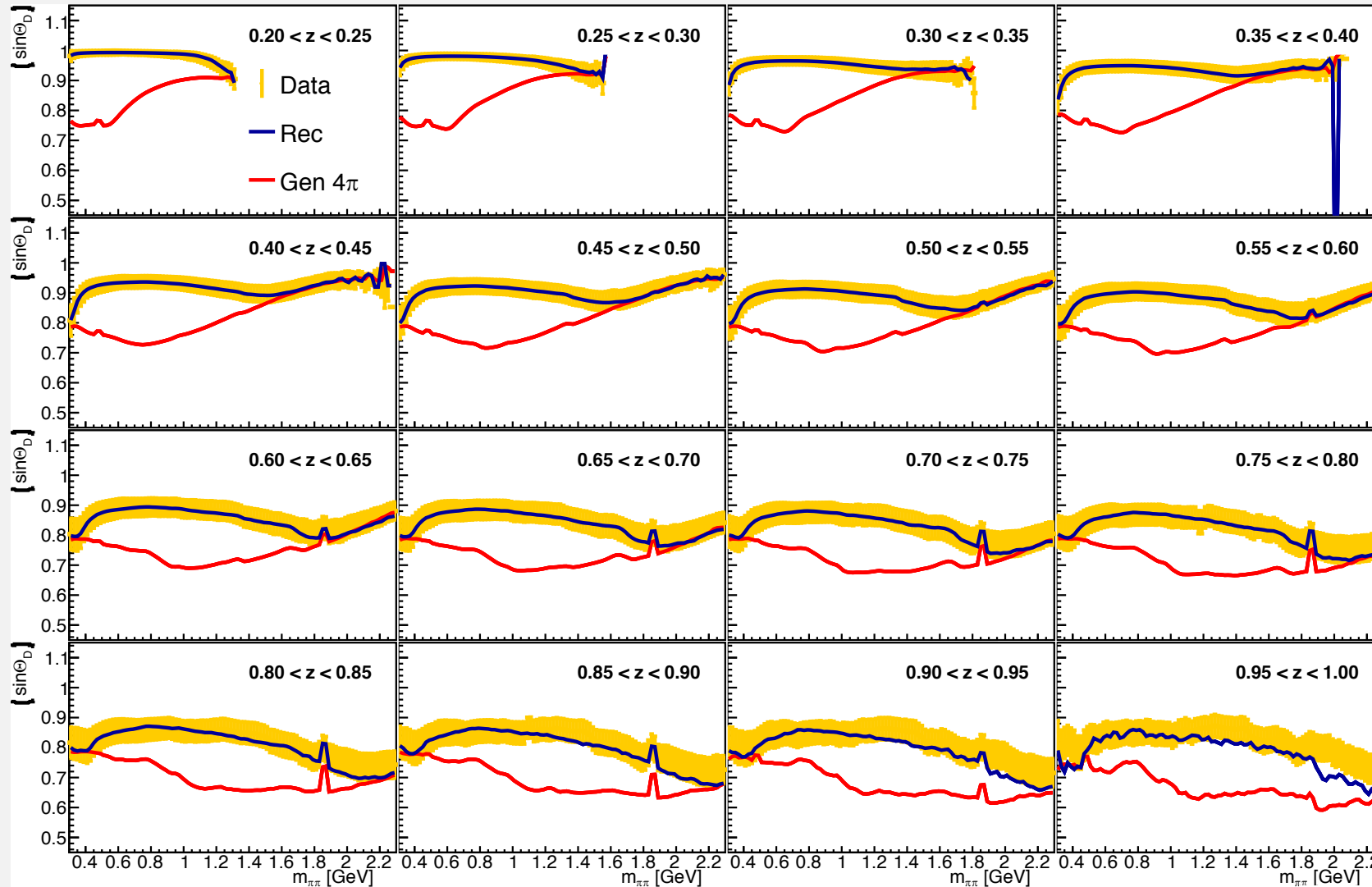
BELLE II PROSPECTS

- Partial Wave decomposition (more general: θ dependence)
- Higher order PWs lead to different moments in θ and ϕ
- In models, evolution of the different PWs different
- Important to have a full picture to understand mixing effects in ratios/partial integrals/acceptance
- Missing info from partial wave estimated to have effects up to 10% e.g. on extraction of transversity



ACCEPTANCE IMPACT ON PARTIAL WAVE COMPOSITION

Belle II prospects:
Sufficient statistics
for full partial wave
decomposition



m [GeV]

ACCELERATOR DESIGN: NANO BEAM SCHEME

Invented by Pantaleo Raimondi for SuperB

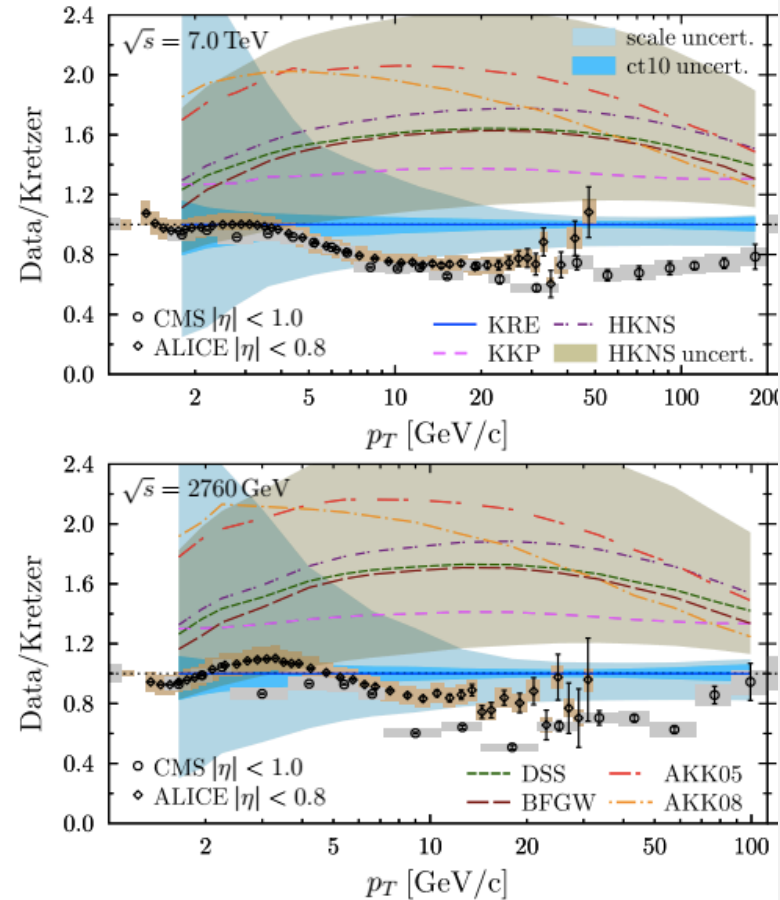
$$L = \frac{\gamma_{\pm}}{2er_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi}{\beta_{y\pm}^*} \frac{R_L}{R_{\xi_y}}$$

Lorentz factor γ_{\pm}
 Beam current I_{\pm}
 Beam-Beam parameter $\xi \propto \sqrt{(\beta_y^*/\epsilon_y)}$
 Geometrical reduction factors (crossing angle, hourglass effect) $\frac{R_L}{R_{\xi_y}}$
 Vertical beta function at IP $\beta_{y\pm}^*$
 Beam aspect ratio at IP $\frac{\sigma_y^*}{\sigma_x^*}$

	E (GeV) LER/HER	β_y^* (mm) LER/HER	β_x^* (cm) LER/HER	ϕ (mrad)	I (A) LER/HER	L (cm ⁻² s ⁻¹)
KEKB	3.5/8.0	5.9/5.9	120/120	11	1.6/1.2	2.1 x 10 ³⁴
SuperKEKB	4.0/7.0	0.27/0.30	3.2/2.5	41.5	3.6/2.6	80 x 10 ³⁴

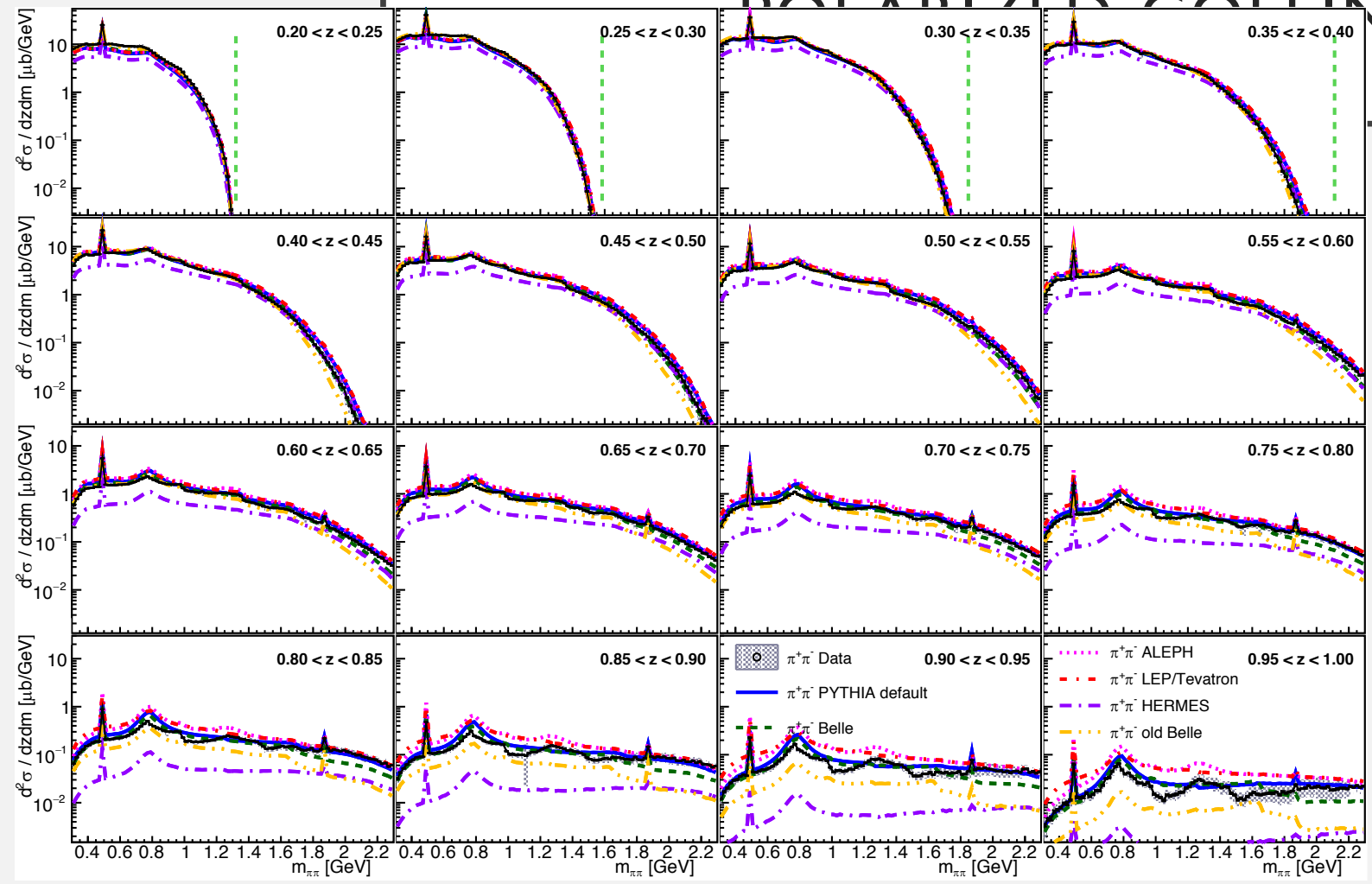
SURPRISES POSSIBLE WHEN NEW DATA BECOMES AVAILABLE

- **Example:**
 - Hadron Spectra at the LHC confronted with current FF sets
 - **Large disagreement!**



D. d'Enterria, K. J. Eskola, I. Helenius, H. Paukkunen,
Nucl. Phys. B883 (2014) 615.

POLARIZED COLLINS

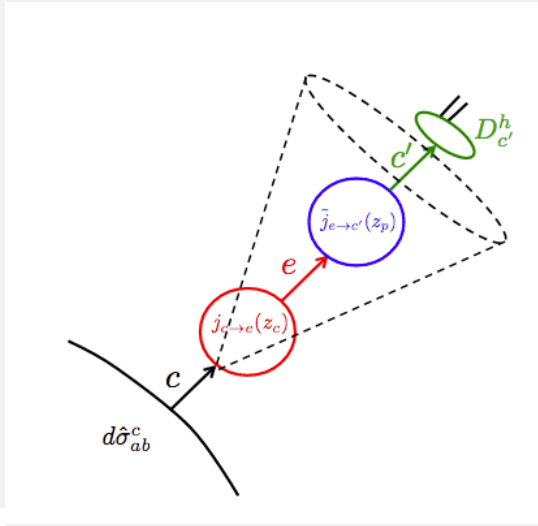


$$= \frac{1}{\sum_q e_q^2} (2F_1^h(z, Q^2) + F_L^h(z, Q^2)),$$

$$\frac{d^3\sigma^{pp \rightarrow (h, \text{jet})X}}{dP_T^{\text{jet}} d\eta^{\text{jet}} dz} \propto \sum_{i,j,k} f_1^{i/p_a}(x_a) \otimes f_1^{j/p_b}(x_b) \otimes \hat{\sigma}^{ij \rightarrow k \text{jet}} \otimes D_1^{h/p_k}\left(\frac{z}{z_k}\right)$$

- h-h, Jet-hadron (back-to-back)
- γ -hadron (back-to-back)
- Hadron in jet

$$\frac{E_h d^3\sigma^{pp \rightarrow hX}}{d^3P_h} = \sum_{i,j,k,l} \int \frac{dx_a}{x_a} \int \frac{dx_b}{x_b} \int \frac{dz}{z^2} f_1^{i/p_a}(x_a) f_1^{j/p_b}(x_b) D_1^{h/k}(z) \hat{\sigma}^{ij \rightarrow kl} \delta(\hat{s} + \hat{t} + \hat{u}),$$

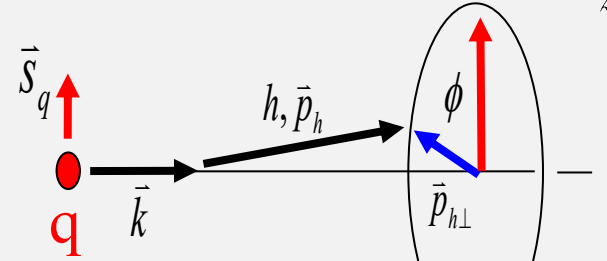
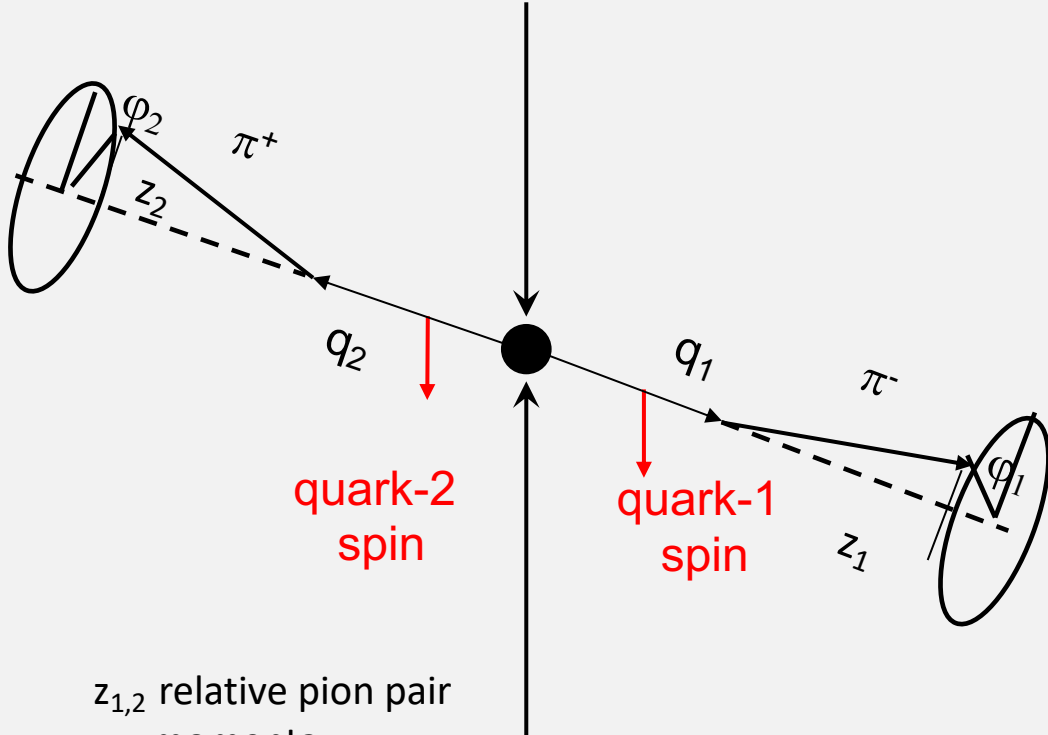


Kaufmann, Mukherjee, Vogelsang, **Phys.Rev. D92 (2015) no.5, 054015**

CORRELATION MEASUREMENTS IN e^+e^-

J. Collins, Nucl. Phys. B396, (1993) 161

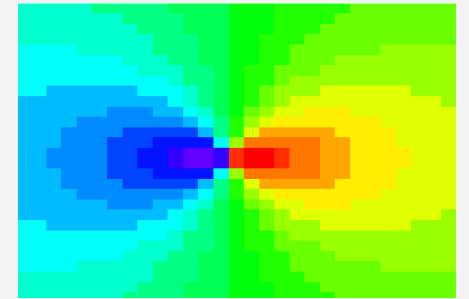
$$D_{q\uparrow}^h(z, P_{h\perp}) = D_{1,q}^h(z, P_{h\perp}^2) + H_{1,q}^{\perp h}(z, P_{h\perp}^2) \frac{(\hat{\mathbf{k}} \times \mathbf{P}_{h\perp}) \cdot \mathbf{S}_q}{zM_h}$$



• First non-zero independent measurement of the Collins effect for pion pairs in e^+e^- annihilation by Belle Collaboration @ $\sqrt{s} \sim 10.6$ GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032) from SIDIS and e^+e^-

- Confirmed by BaBar @ $\sqrt{s} \sim 10.6$ GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and $K\pi$)
- Measured at BESIII @ $\sqrt{s} = 3.65$ GeV (PRL 116,42001(2016))

$$\text{Cross-section } e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X \\ \propto D_1^\perp \overline{D_1^\perp} + H_1^\perp \overline{H_1^\perp} \cos(\phi_1 + \phi_2)$$



- Access spin dependence and p_T dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities