

# Physics with an Electron-Ion Collider

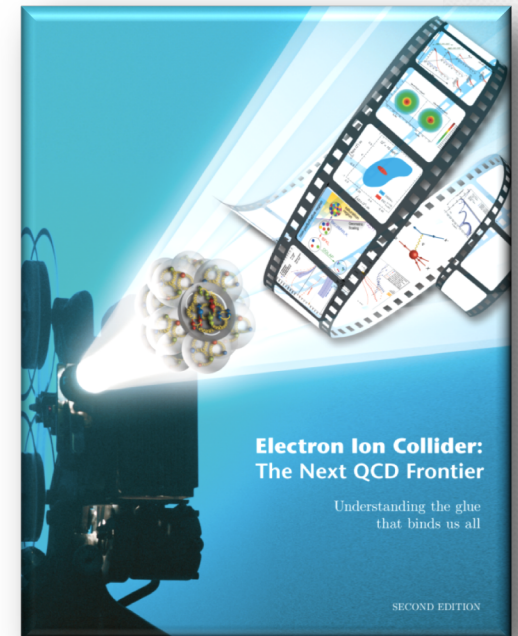
Jian-ping Chen (陈剑平), Jefferson Lab, Virginia, USA

Pre-Workshop Lectures, Hadron-China2018, July 25, 2018

- *I: Introduction, Overview,*
- *II: Form Factors*
- *III: 1-d Structure : Parton Distribution Functions*
- *IV: 3-d Structure: TMDs and GPDs*

*Not covered:*

- *Spin Structure (Xiaochao Zheng's lecture)*
- *Parity Violation (Xiaochao Zheng's lecture)*
- *Hadron Spectroscopy*
- *Quark Gluon Structure of Nuclei*



# Physics with an Electron-Ion Collider

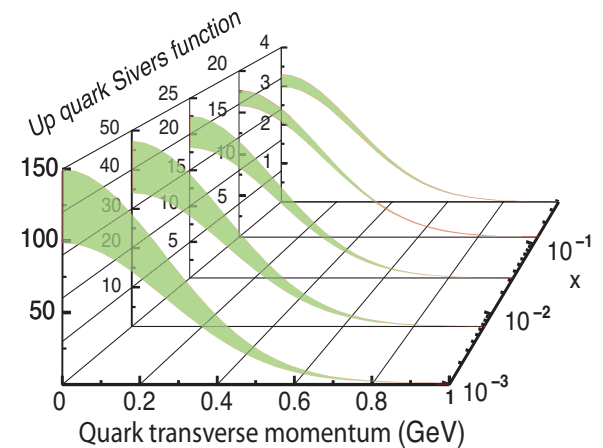
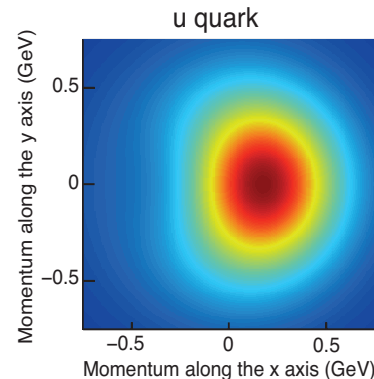
## *I: Introduction and Overview*

- Introduction and History
- Electron (Lepton) As A Clean Probe
- Facilities:

Fixed Target: SLAC, HERMES, COMPASS, Jefferson Lab, ...

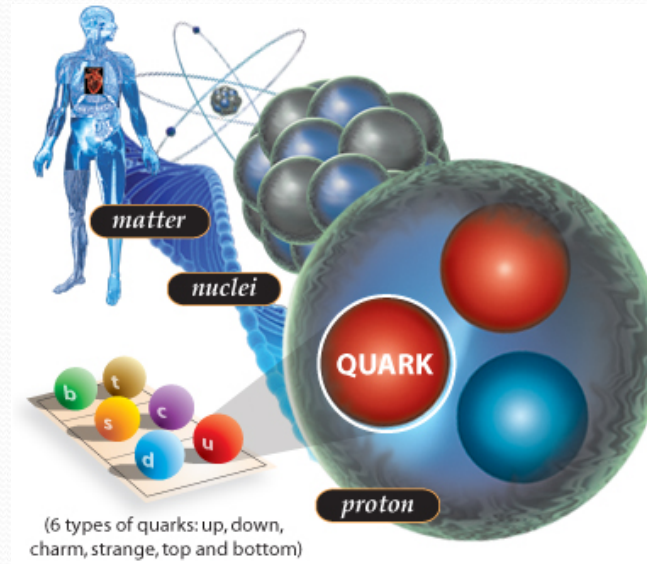
Electron-Ion Collider : HERA, Future EIC: JLEIC, e-RHIC, EicC, LHeC

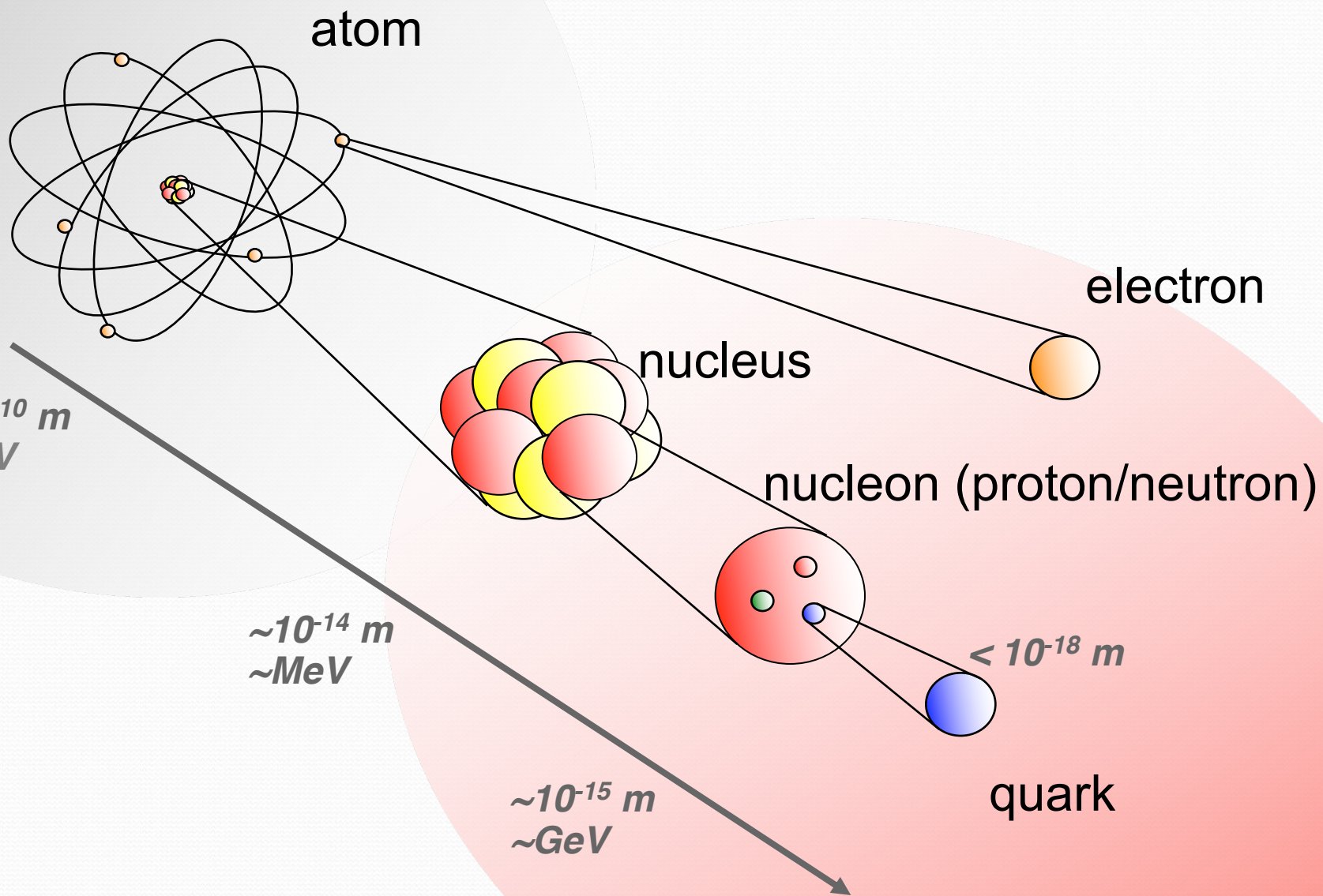
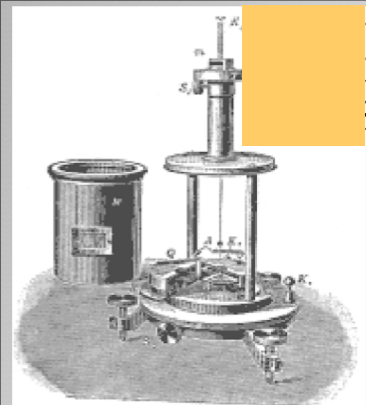
- EIC Experiments:
  - Focus on e-N



# Introduction: What and Why

## Nucleon Structure and Strong Interaction (QCD)

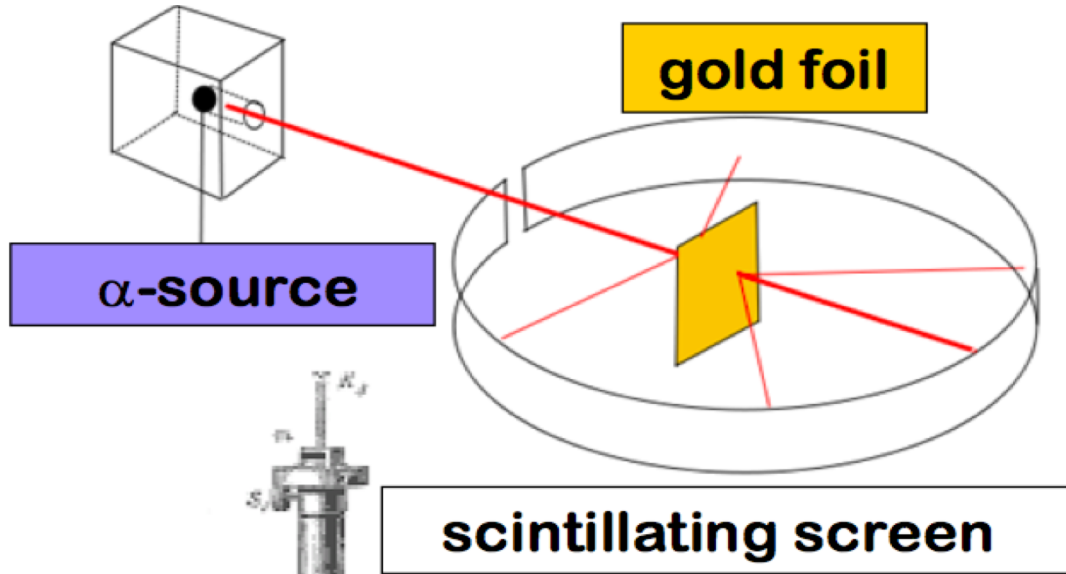




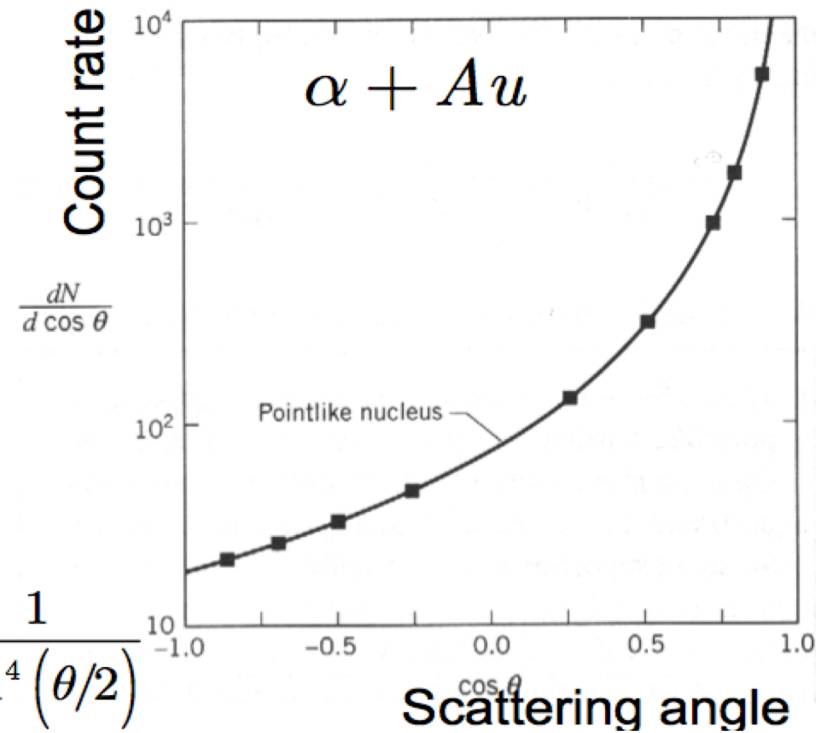
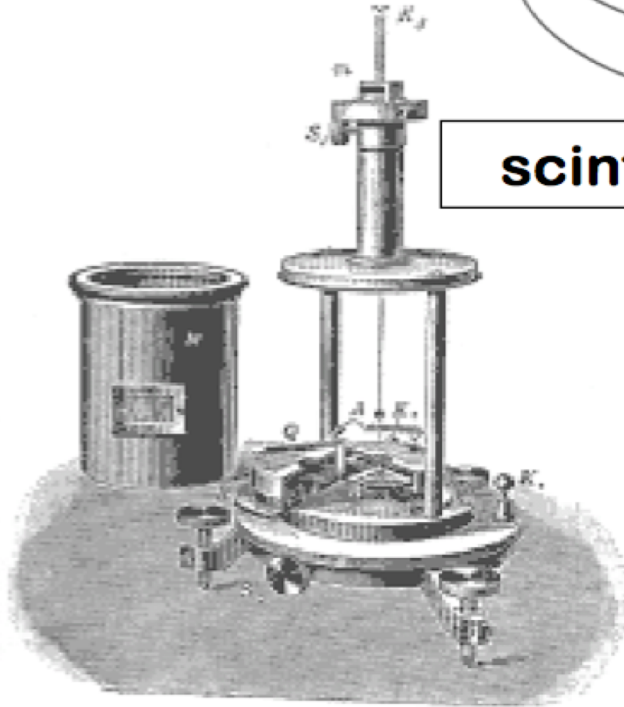
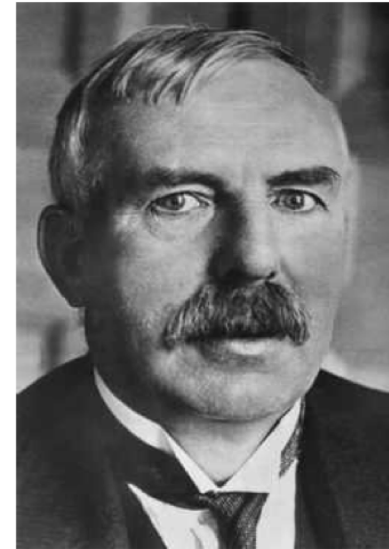
# Rutherford Scattering

Discovery of Nucleus

~5 MeV



Ernest Rutherford,  
Nobel Prize 1908



$$\frac{d\sigma}{d\Omega} = (zZ\alpha)^2 \left( \frac{\hbar c}{4E_{\text{kin}}} \right)^2 \frac{1}{\sin^4(\theta/2)}$$

Scattering off a hard sphere;  $r_{\text{nucleus}} \sim 10^{-4} r_{\text{atom}} \sim 10^{-14} \text{ m}$

# Discovery of (Electron) Spin

- 1896 Zeeman Effect : effect of a magnetic field on light  
-> atomic level splitting due to electron spin

- 1922 Stern-Gerlach experiment  
silver beam split

in inhomogeneous field

Bohr magneton:  $\mu_e = e\hbar/2m_e c$

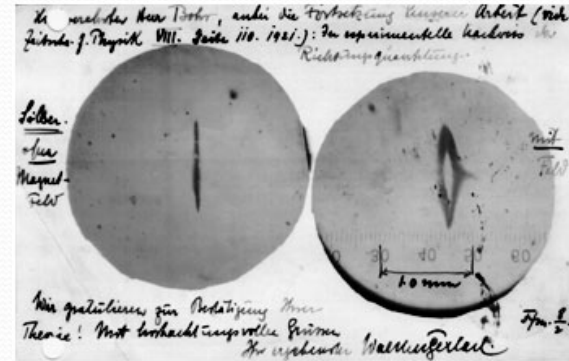
- 1925 spinning electron

Uhlenbeck and Goudsmit, Pauli

spin: internal property,  $S_e = 1/2$

- 1928 Dirac equation

relativistic effect: spin  $\leftrightarrow$  magnetic moment



Postcard from Gerlach to Bohr



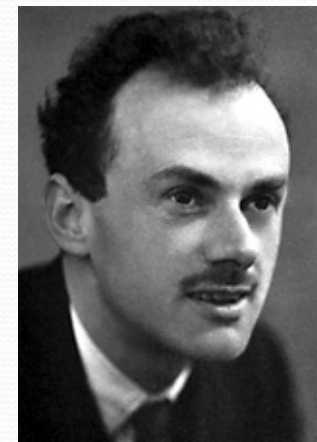
Pieter Zeeman

**Nobel Prize 1902**



Wolfgang Pauli  
for "Pauli Principle"

**Nobel Prize 1945**



Paul Dirac

**Nobel Prize 1933**

# Anomalous Magnetic Moment (of Proton)

## ■ 1933 Otto Stern

Magnetic moment of the proton

-- expected:  $\mu_p = e\hbar/2m_p c$  (since  $S_p = 1/2$ )

-- measured:  $\mu_p = e\hbar/2m_p c(1 + \kappa_p)$  !

anomalous magnetic moment (a.m.m)  $\kappa_p = 1.5 \pm 10\%$

➤ first (indirect) evidence proton has structure



Otto Stern  
Nobel Prize 1943

## ■ 1943 Nobel Prize awarded to Stern

for 'development of the molecular ray method and his discovery of the magnetic moment of protons'

now:  $\kappa_p = 1.792847386 \pm 0.000000063$

and  $\kappa_n = -1.91304275 \pm 0.000000045$

# Neutron, Mesons and Quark Model



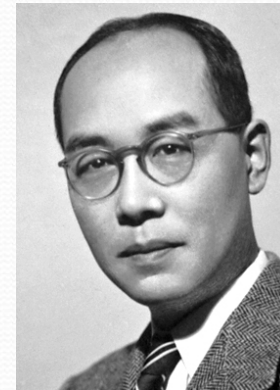
James Chadwick  
**Nobel Prize 1935**



Cecil Frank Powell  
**Nobel Prize 1950**



Murray Gell-Mann  
**Nobel Prize 1969**



Hideki Yukawa  
**Nobel Prize 1949**

- 1932: Discovery of the neutron by Chadwick  
proton, neutron: basic building blocks for nuclei
- 1935: Yukawa “strong” force  $\rightarrow \pi$  meson
- 1937: Discovery of “meson”
- 1946: Powell, “ $\pi$  and  $\mu$  mesons”  
 $\mu$  mesons  $\rightarrow$  muon

Zoo of hadrons

- 1964 Gell-Mann  
Classify strong interacting particles (hadrons)  
with a simple quark model

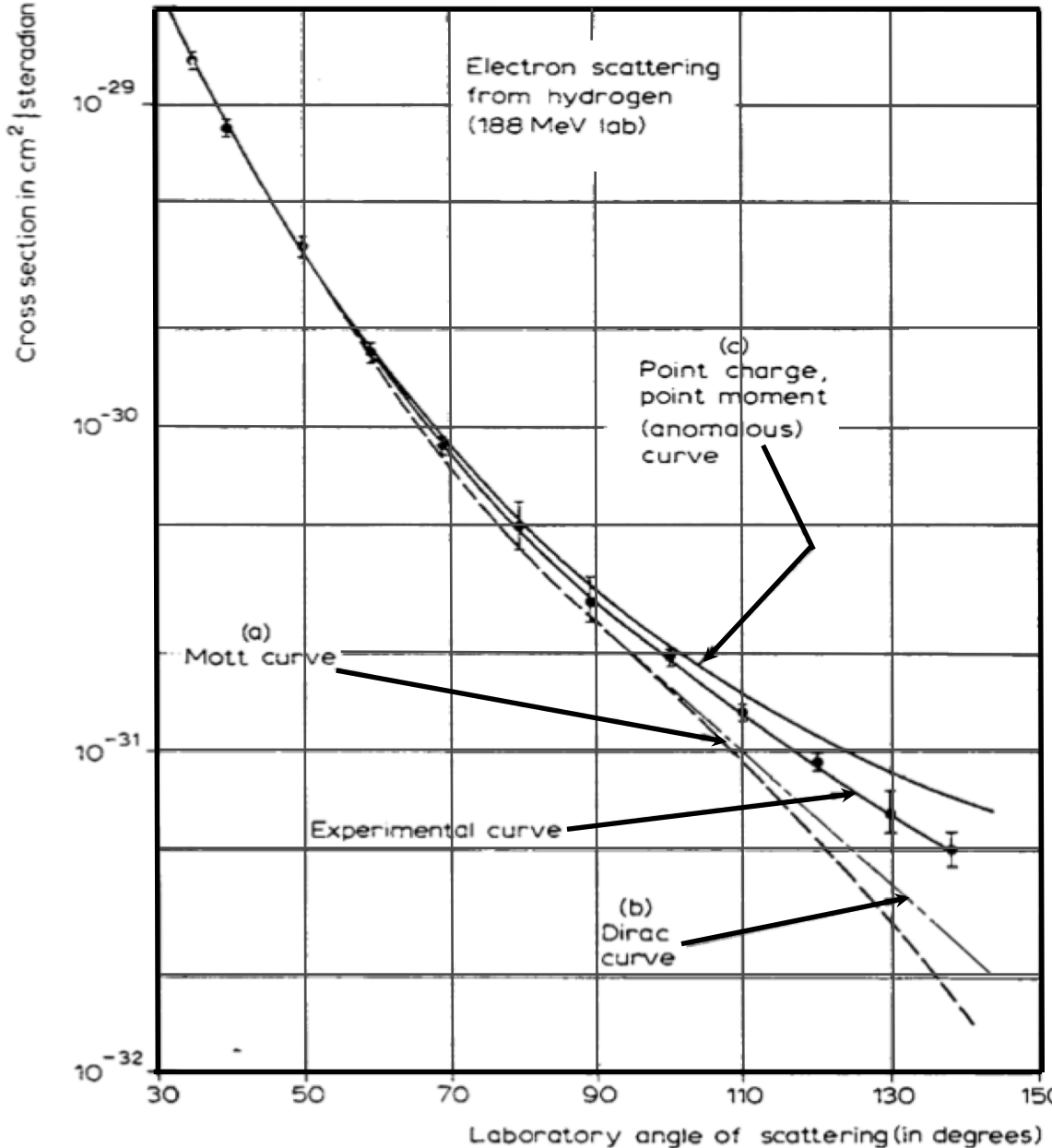
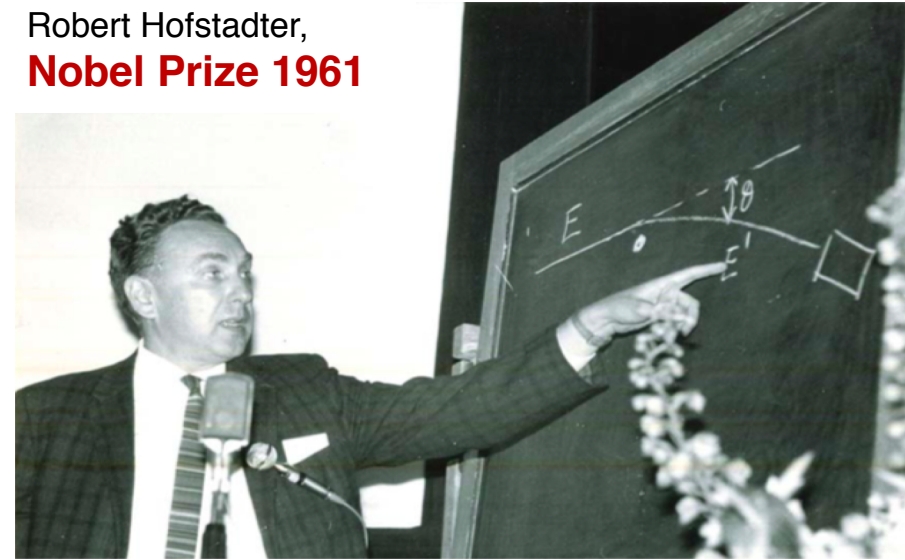


# Elastic Electron Scattering

~200 MeV

Discovery: Proton Has Structure

Robert Hofstadter,  
Nobel Prize 1961



Scattering off a spin-1/2 Dirac particle:

$$\frac{d\sigma}{d\Omega} = \left( \frac{\alpha}{4ME \sin^2(\theta/2)} \right)^2 \frac{E'}{E} \left[ \frac{q^2}{2M} \sin^2(\theta/2) + \cos^2(\theta/2) \right]$$

The proton has an anomalous magnetic moment,

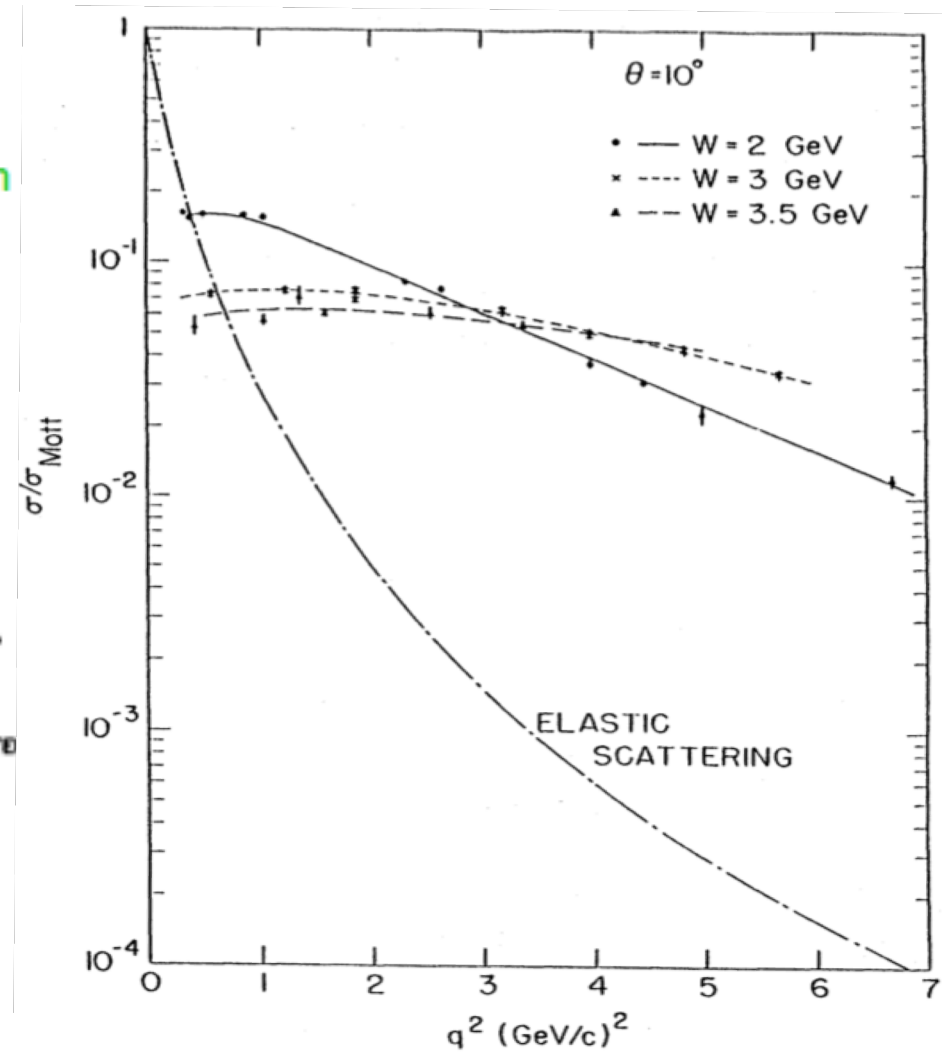
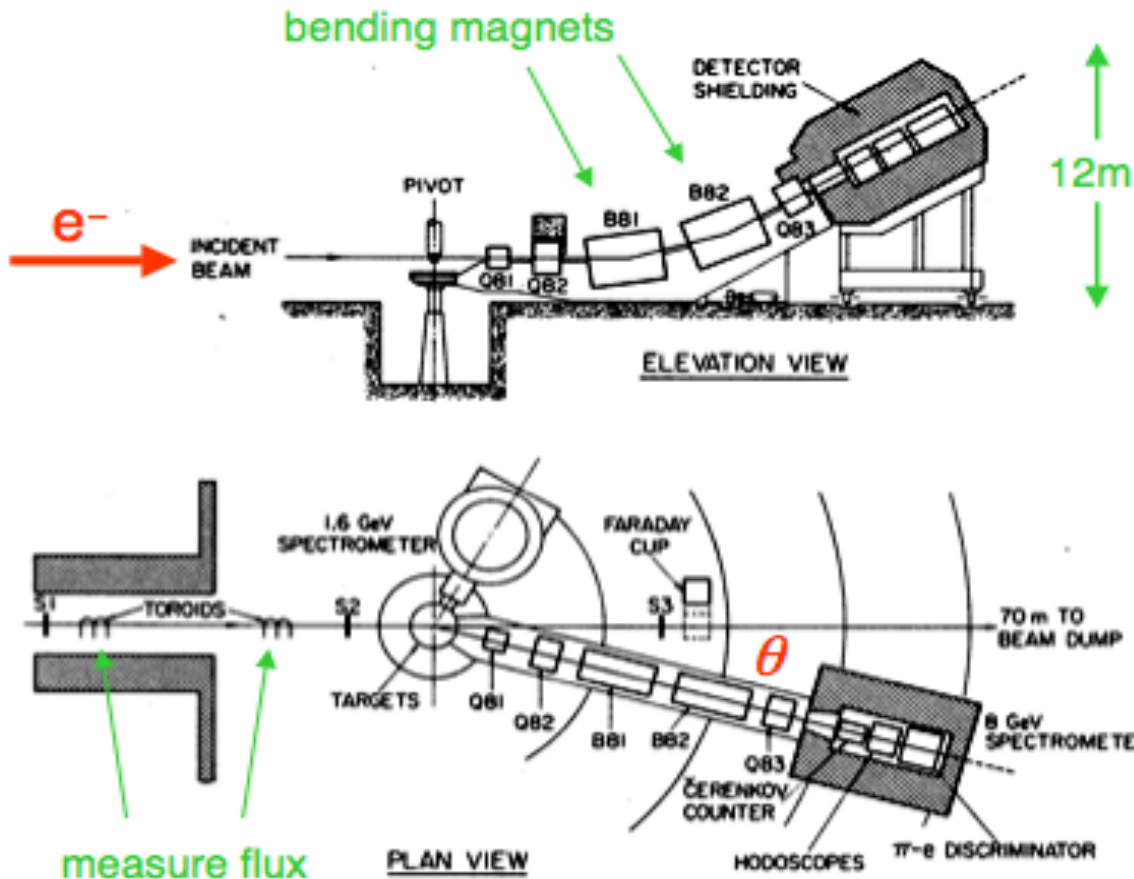
$$g_p \neq 2, \quad g_p \simeq 5.6$$

and, hence, internal (spin) structure.

# Deep-Inelastic Electron Scattering

$\sim 10$  GeV

Discovery of Quarks (Partons)

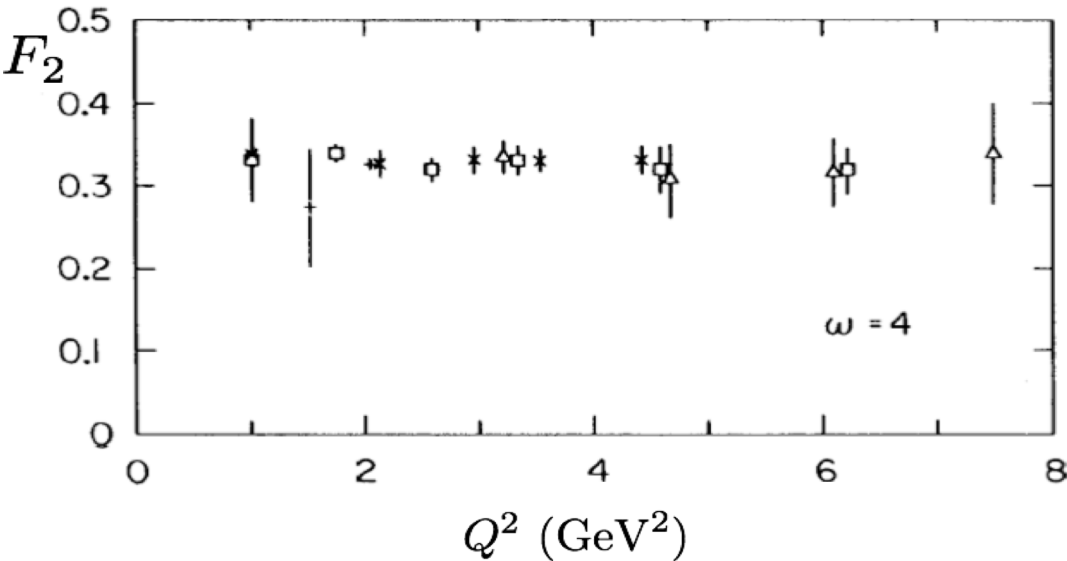


# Deep-Inelastic Electron Scattering

## Discovery of Quarks (Partons)

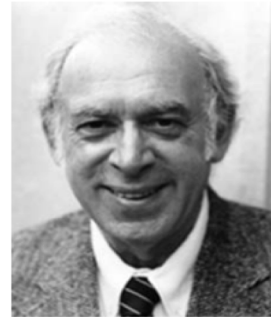
**Bjorken scaling:**

+ 6°    □ 18°  
 × 10°    △ 26°



*Point particles cannot be further resolved; their measurement does not depend on wavelength, hence  $Q^2$ ,*

*Spin-1/2 quarks cannot absorb longitudinally polarized vector bosons and, conversely, spin-0 (scalar) quarks cannot absorb transversely polarized photons.*



J.T. Friedman



R. Taylor

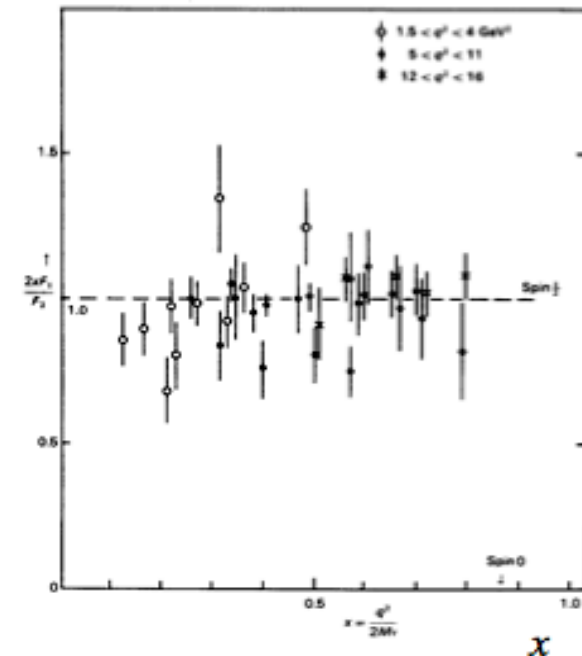


H.W. Kendall

**Nobel Prize 1990**

**Callan-Gross relation:**

$$\frac{2xF_1}{F_2}$$



spin 1/2

spin 0

# *Birth of QCD*

- Problems with simple quark model:
  1. pion mass is light ( $\sim 140$  MeV) compared with nucleon (1 GeV) and  $\rho$  meson (770 MeV)  
→ spontaneous breaking of chiral symmetries  
quark mass  $\sim 300$  MeV ?
  2. Pauli principle → new degree of freedom: color  
no free quarks observed !
- 1972-73 Gell-Mann, Fritzsche, Leutwyler,  
Gross, Politzer, Wilczek  
SU(3) color gauge field → QCD

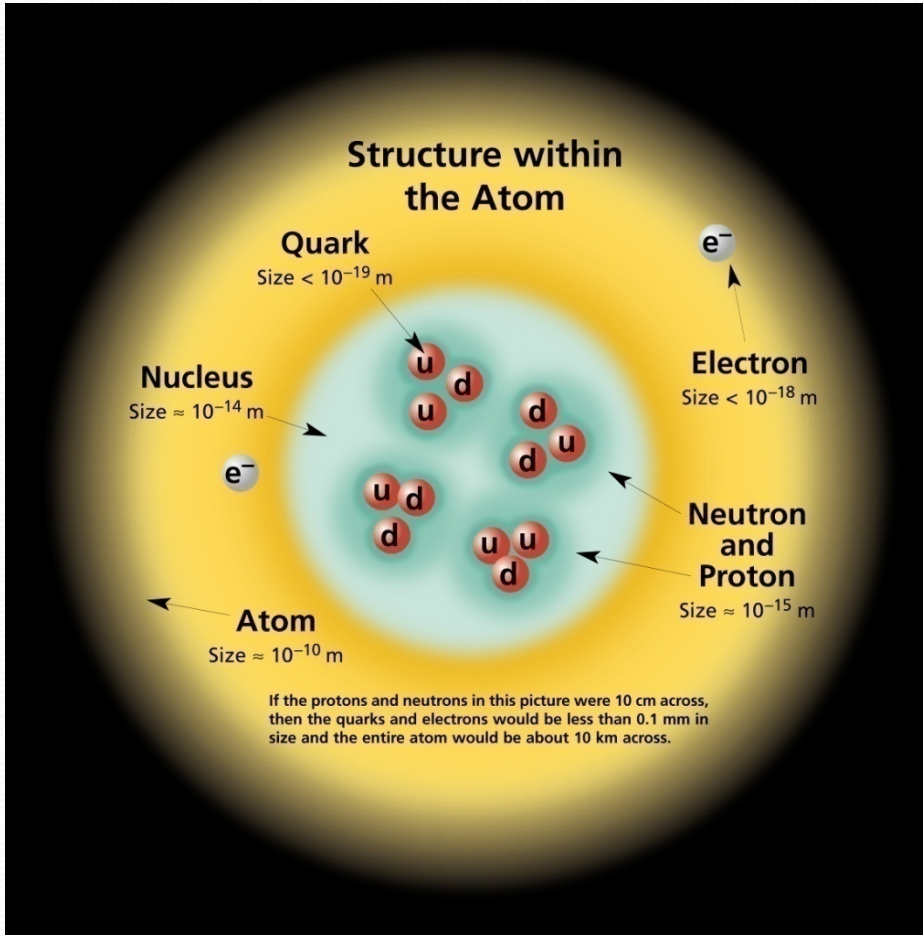


David Gross, H. David Politzer, Frank Wilczek  
**Nobel Prize 2004**

# What Is the World Made of?

Visible Matter → Atom → Electrons + Nucleus

Nucleus → Nucleons(proton,neutron) → Quarks: proton=uud, neutron=udd



FERMIONS			matter constituents spin = 1/2, 3/2, 5/2, ...		
Leptons spin = 1/2			Quarks spin = 1/2		
Flavor	Mass GeV/c <sup>2</sup>	Electric charge	Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
$\nu_e$ electron neutrino	$< 1 \times 10^{-8}$	0	<b>u</b> up	0.003	2/3
<b>e</b> electron	0.000511	-1	<b>d</b> down	0.006	-1/3
$\nu_\mu$ muon neutrino	$< 0.0002$	0	<b>c</b> charm	1.3	2/3
<b><math>\mu</math></b> muon	0.106	-1	<b>s</b> strange	0.1	-1/3
$\nu_\tau$ tau neutrino	$< 0.02$	0	<b>t</b> top	175	2/3
<b><math>\tau</math></b> tau	1.7771	-1	<b>b</b> bottom	4.3	-1/3

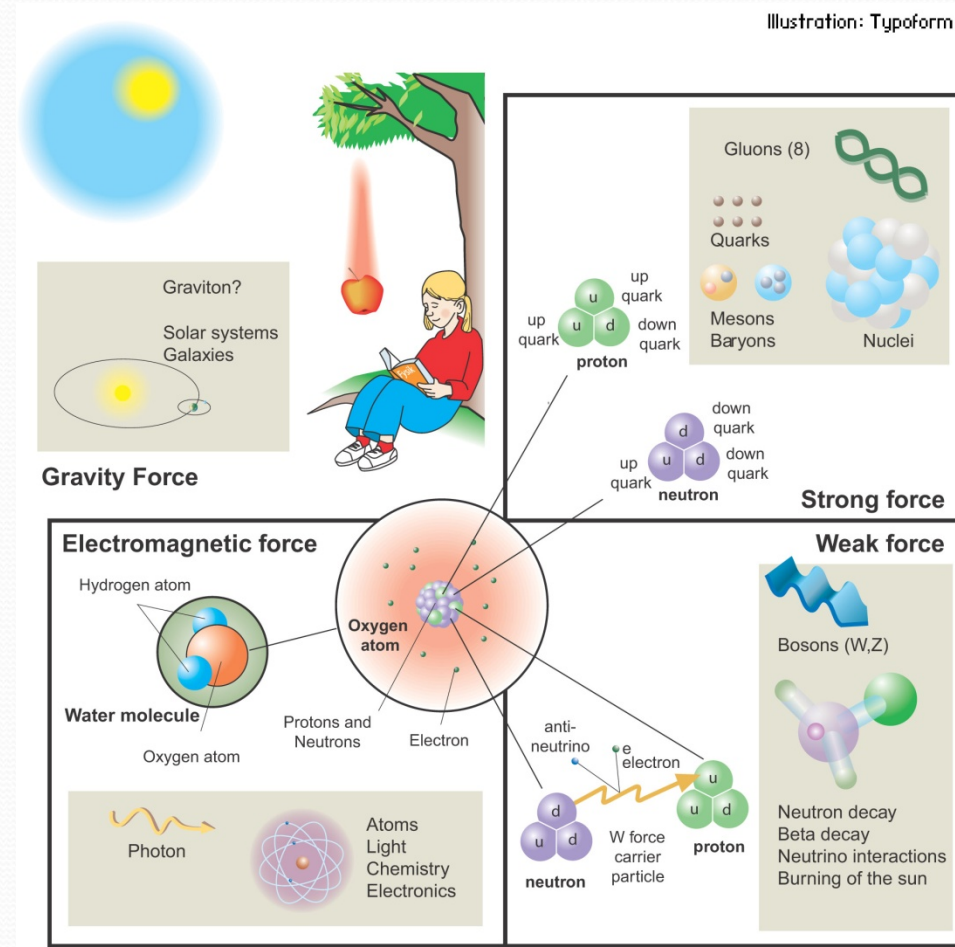


So everything is made of quarks and leptons, eh? Who would have *thought* it was so simple?

# What Holds the World Together?

## Four Known Interactions

- Gravitational Interaction (graviton?)  
long range, always attractive  
strength, extremely weak,  $\sim 10^{-40}$
- Electromagnetic Interaction ( $\gamma$ )  
long range, electric charge (e)  
strength (coupling constant),  $\alpha = 1/137$
- Weak Interaction (W, Z)  
short range, weak charge  
strength,  $10^{-4} \sim 10^{-7}$
- Strong Interaction (gluons)  
short range, color charge,  
strength, running coupling,  $\alpha_s = 0.1 \sim 1$   
*confinement*



# Standard Model

## Electro-weak and Quantum Chromodynamics (QCD)

FERMIONS			matter constituents spin = 1/2, 3/2, 5/2, ...		
Leptons spin = 1/2			Quarks spin = 1/2		
Flavor	Mass GeV/c <sup>2</sup>	Electric charge	Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
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<b><math>\tau</math></b> tau	1.7771	-1	<b>b</b> bottom	4.3	-1/3

BOSONS			force carriers spin = 0, 1, 2, ...		
Unified Electroweak spin = 1			Strong (color) spin = 1		
Name	Mass GeV/c <sup>2</sup>	Electric charge	Name	Mass GeV/c <sup>2</sup>	Electric charge
$\gamma$ photon	0	0	<b>g</b> gluon	0	0
<b>W<sup>-</sup></b>	80.4	-1			
<b>W<sup>+</sup></b>	80.4	+1			
<b>Z<sup>0</sup></b>	91.187	0			

## PROPERTIES OF THE INTERACTIONS

Property \ Interaction	Gravitational	Weak	Electromagnetic	Strong	
		(Electroweak)		Fundamental	Residual
Acts on:	Mass – Energy	Flavor	Electric Charge	Color Charge	See Residual Strong Interaction Note
Particles experiencing:	All	Quarks, Leptons	Electrically charged	Quarks, Gluons	Hadrons
Particles mediating:	Graviton (not yet observed)	<b>W<sup>+</sup> W<sup>-</sup> Z<sup>0</sup></b>	$\gamma$	Gluons	Mesons
Strength relative to electromag for two u quarks at:	10 <sup>-41</sup>	0.8	1	25	Not applicable to quarks
for two protons in nucleus	10 <sup>-41</sup>	10 <sup>-4</sup>	1	60	
	10 <sup>-36</sup>	10 <sup>-7</sup>	1	Not applicable to hadrons	20

# What Are the Challenges?

- Success of the Standard Model

Electro-Weak theory tested to very good level of precision

Discovery of Higgs particle

Strong interaction theory (QCD) tested in the high energy (short distance) region

- Major challenges:

Understand QCD in the strong region (distance of the nucleon size)

Understand quark-gluon structure of the nucleon

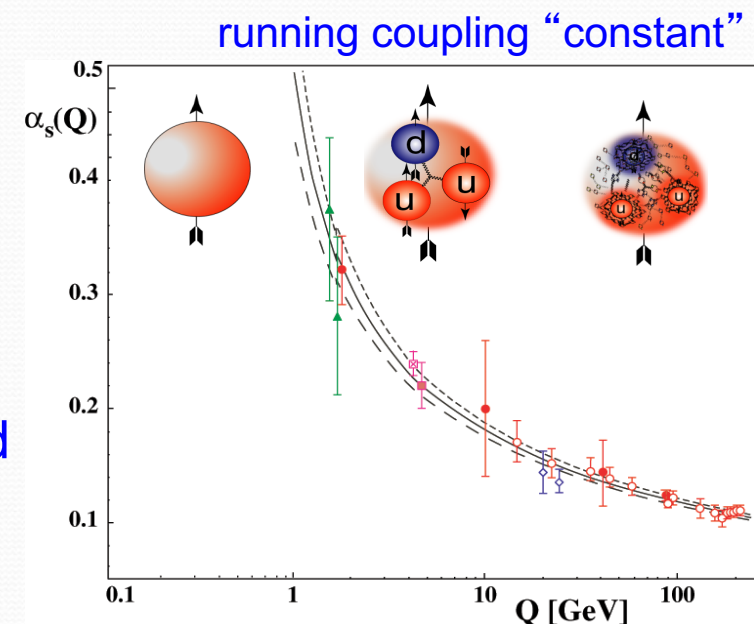
Confinement

- Beyond Standard Model

Energy frontier: LHC search Beyond SM

Precision tests of Standard Model at low energy

Precision information of nucleon structure needed





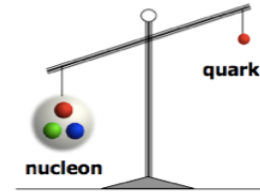
# Nucleon Structure: A Universe Inside

- Nucleon: proton = (uud), neutron = (udd) + sea quarks + gluons
- Nucleon: **99% of the visible mass in universe**

## ➤ Proton mass “puzzle”:

Quarks carry  $\sim 1\%$  of proton's mass

*How does glue dynamics generate the energy for nucleon mass?*



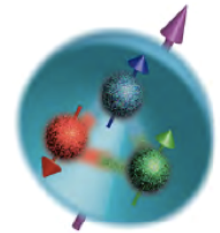
$$m_q \sim 10 \text{ MeV}$$

$$m_N \sim 1000 \text{ MeV}$$

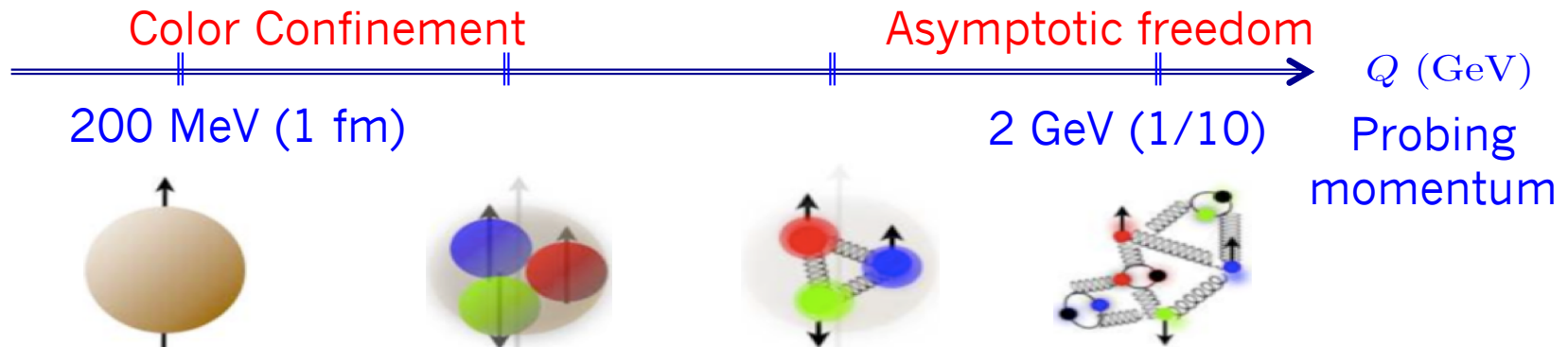
## ➤ Proton spin “puzzle”:

Quarks carry  $\sim 30\%$  of proton's spin

*How does quark and gluon dynamics generate the rest of the proton spin?*



## ➤ 3D structure of nucleon: 3D in momentum or (2D space +1 in momentum)



*How does the glue bind quarks and itself into a proton and nuclei?  
Can we scan the nucleon to reveal its 3D structure?*

# Recent Theoretical Developments

- **Dynamical Chiral Symmetry Breaking  $\leftrightarrow$  Confinement**

- Responsible for  $\sim 99\%$  of the nucleon mass
- Higgs mechanism is (almost) irrelevant to light quarks

- **Recent development in theory**

- Lattice QCD
- Bound State QCD: Dyson-Schwinger
- Ads/CFT: Holographic QCD
- QCD Dynamics
- .....

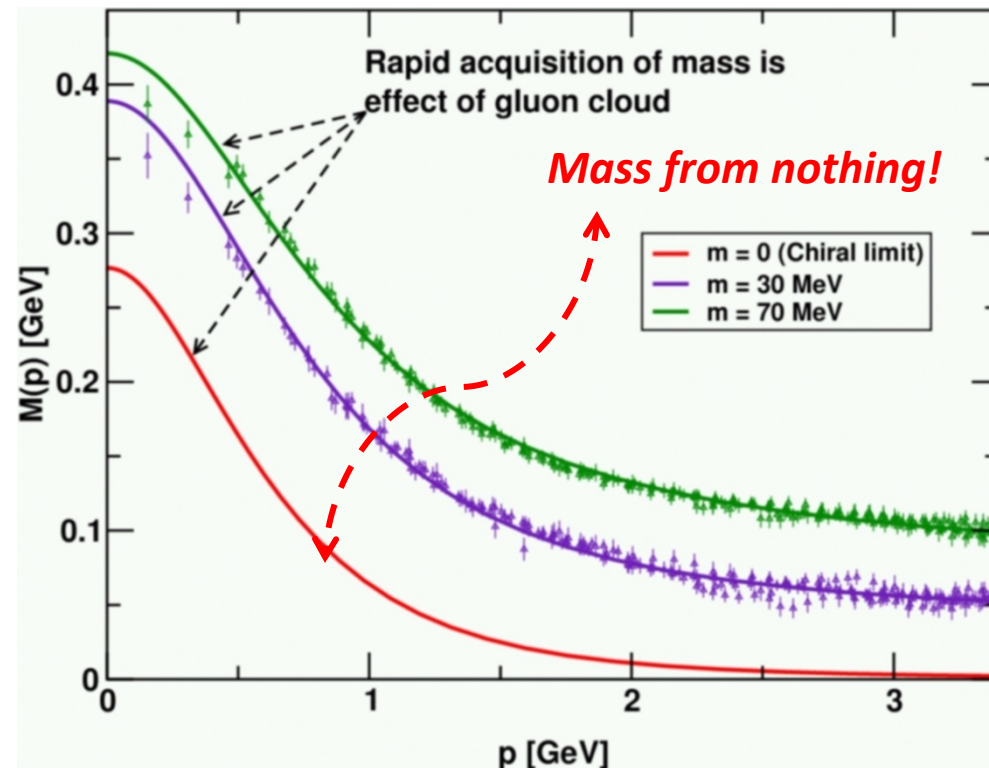
- **Direct comparison becomes possible**

- **LQCD: Moments of PDFs**
- **x-dependence of PDFs, TMDs, GPDs**

X. Ji, PRL 111, 039103 (2013)

H. W. Lin, et al., Phys. Rev. D 91, 054510 (2015)

Quasi-PDF, .....

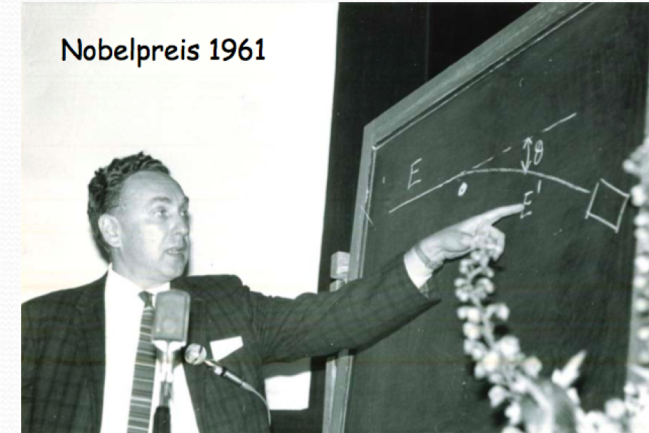


How: Electron Scattering and e-p/e-A colliding

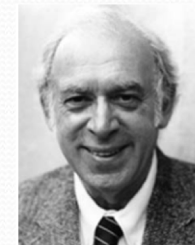
**A Clean Probe To Study Nucleon Structure and QCD**

# Electron Scattering and Nucleon Structure

- Clean probe to study nucleon structure  
only electro-weak interaction, well understood
- Elastic Electron Scattering: Form Factors  
→ 60s: established nucleon has structure (Nobel Prize)  
electrical and magnetic distributions
- Resonance Excitations  
→ internal structure, rich spectroscopy (new particle search)  
constituent quark models
- Deep Inelastic Scattering  
→ 70s: established quark-parton picture (Nobel Prize)  
parton distribution functions (PDFs)  
polarized PDFs : Spin Structure



Robert Hofstadter,  
**Nobel Prize 1961**



J.T. Friedman



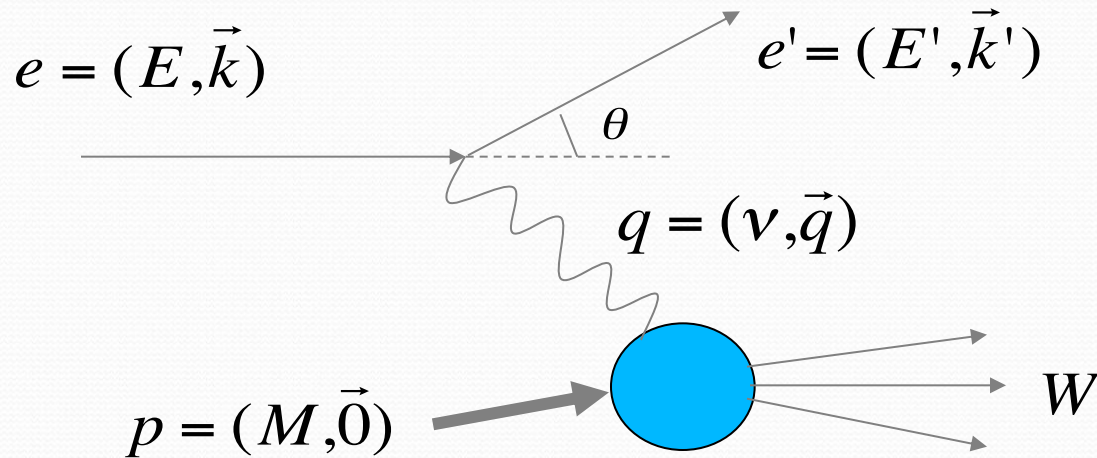
R. Taylor



H.W. Kendall

**Nobel Prize 1990**

# Inclusive Electron Scattering



4-momentum transfer squared

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

Invariant mass squared

$$W^2 = M^2 + 2M\nu - Q^2$$

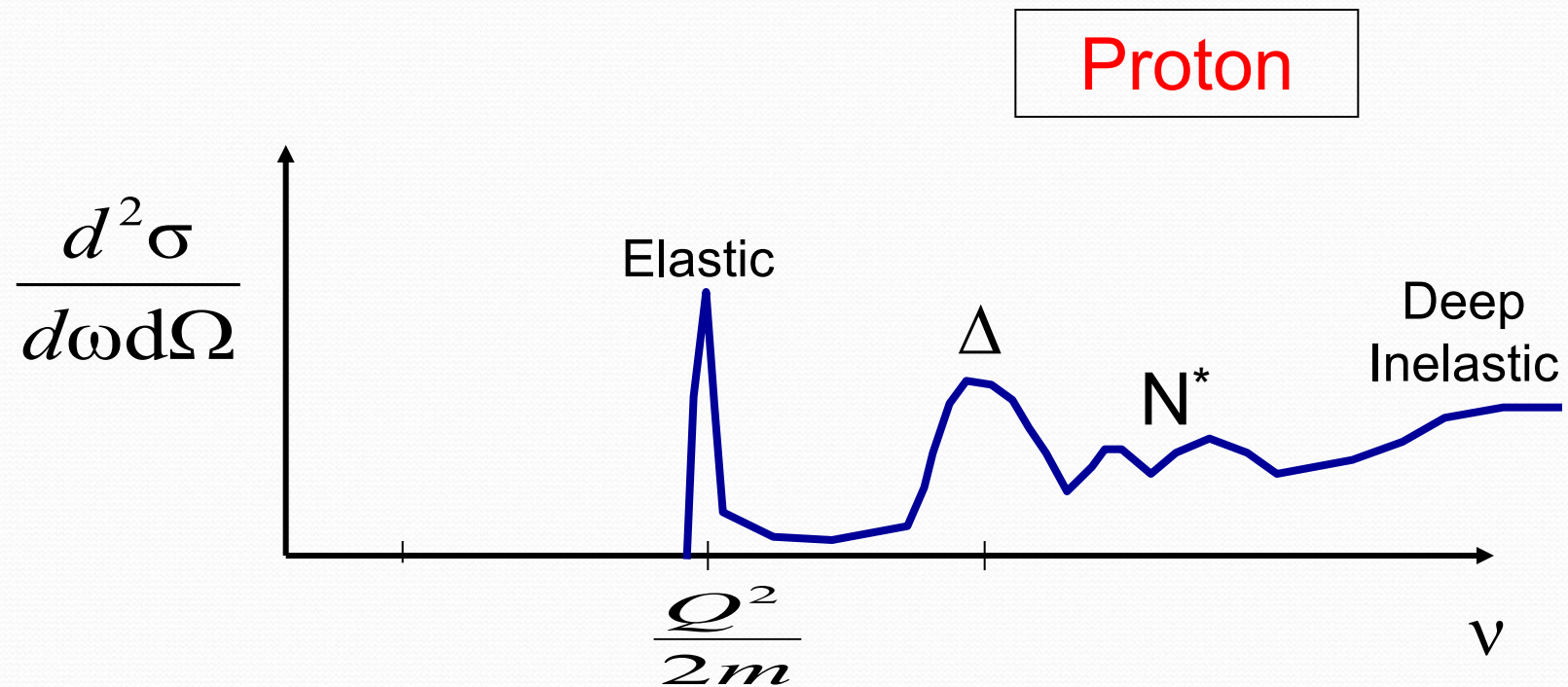
Unpolarized:

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_M \left[ \frac{1}{\nu} F_2(\nu, Q^2) + \frac{2}{M} F_1(\nu, Q^2) \tan^2 \frac{\theta}{2} \right]$$

$$\sigma_M = \frac{\alpha^2 E' \cos^2(\theta/2)}{4E^3 \sin^4(\theta/2)}$$

$F_1$  and  $F_2$ : information on the nucleon/nuclear structure

# Typical Electron Scattering Spectra at Fixed $Q^2$



# Facilities for e-N and e-A

**JLab 12 Program and Future EIC**

# *Experimental Facilities for e-N (e-A)*

- SLAC: Fix target, 20/50 GeV (polarized) electron beam,, polarized p, d and  $^3\text{He}$
- CERN: EMC/NMC/SMC/COMPASS  
Fixed target,  $\sim 200$  GeV polarized  $\mu$  beam on polarized p, d
- DESY: HERA, unpolarized e-p collider. 27.5 GeV x 920 GeV  
HERMES, fixed target, polarized e-/e+ 27 GeV beam,  
polarized internal p, d,  $^3\text{He}$
- JLab: fixed target, 6/12 GeV polarized e beam, polarized p,d, $^3\text{He}$   
highest luminosity  $10^{39}$ .
- Low energy facilities: Mainz, MIT-Bates, Saclay, NIKHEF, ...
- Future EIC: e-RHIC, JLEIC, EIC@HIAF, LHeC, ...

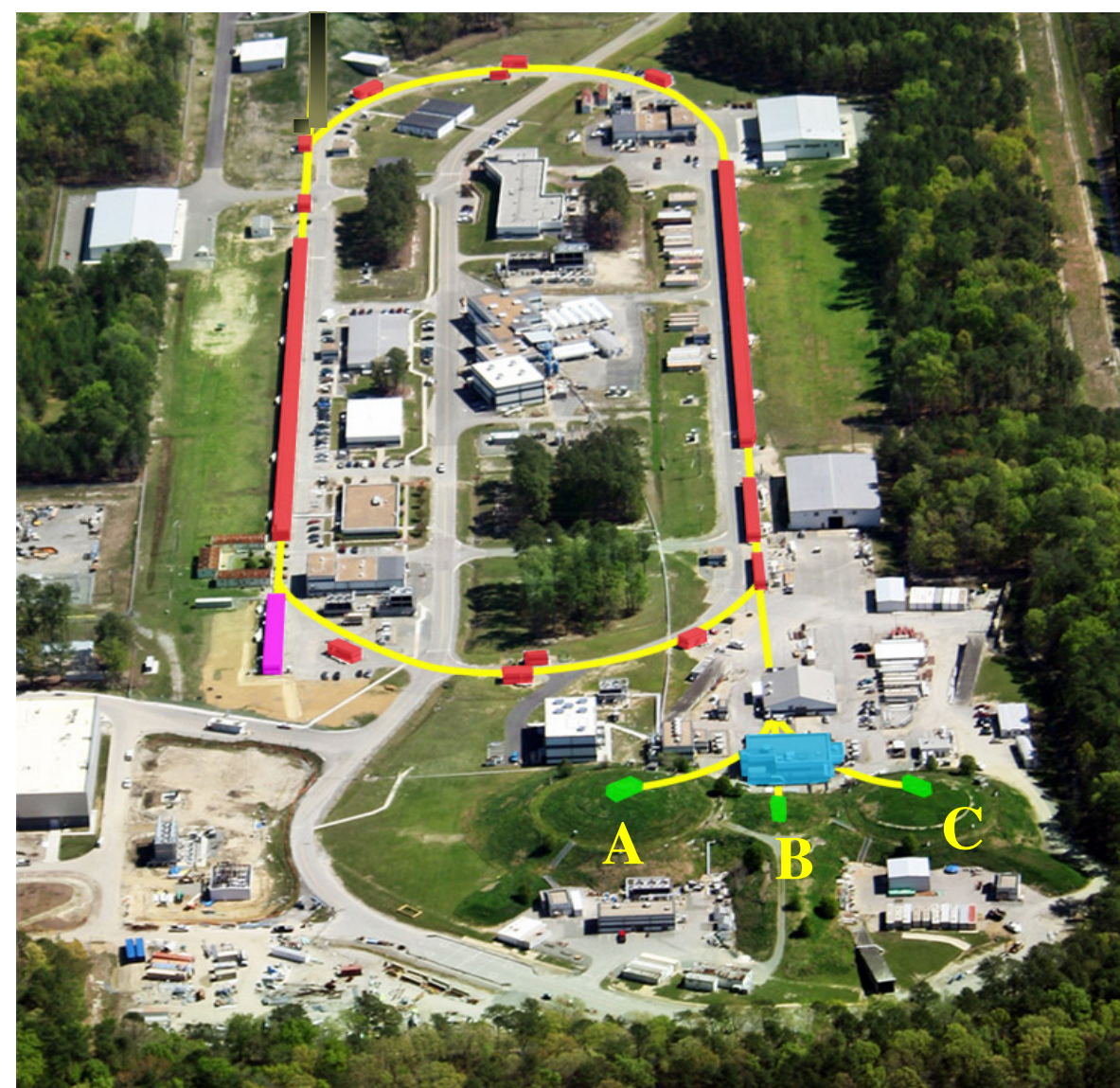


# Jefferson Lab at a Glance

## CEBAF

- **High-intensity** electron accelerator based on **CW SRF** technology
- $I_{\max} = 200 \mu\text{A}$
- $\text{Pol}_{\max} = 90\%$
- $E_{\max} = 6 \text{ GeV}$ : 1995-2012
- **Energy Upgrading to 12 GeV (2012-2017)**
- **12 GeV data taking started**

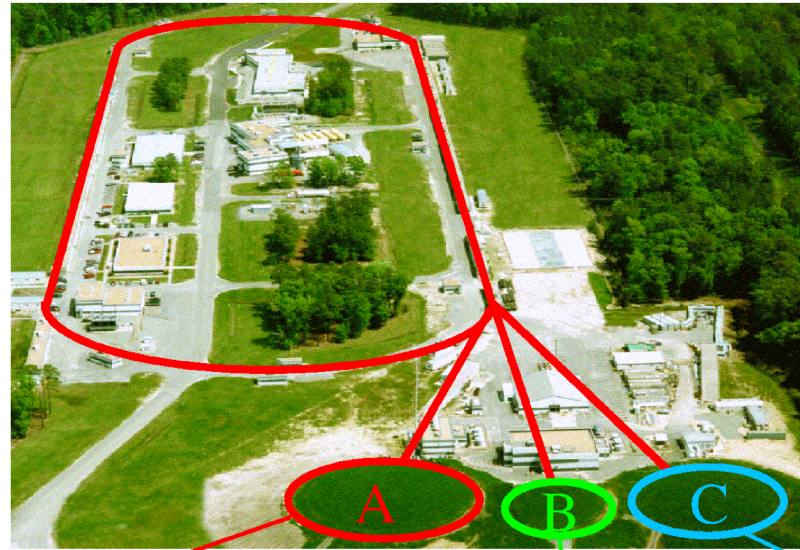
- **~ 1400 Active Users**
- **Produces ~1/3 of US PhDs in Nuclear Physics**



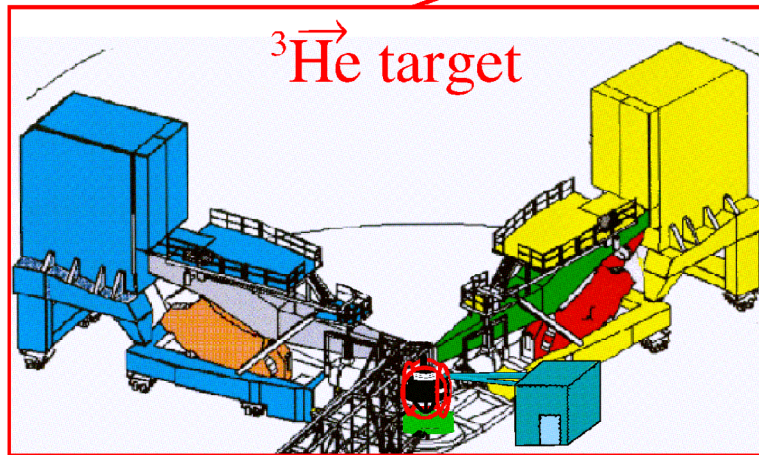
# Thomas Jefferson National Accelerator Facility

Newport News, Virginia, USA

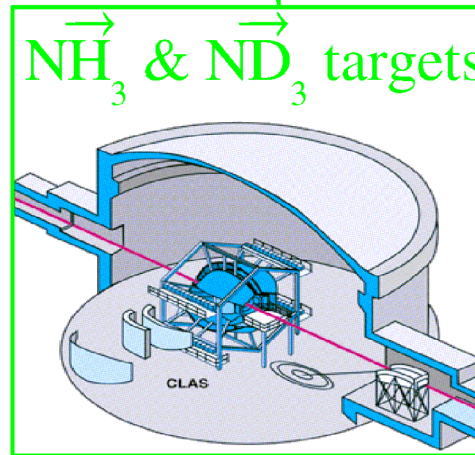
6 GeV polarized  
CW electron beam  
Pol=85%, 200 $\mu$ A  
Luminosity  $\sim 10^{39}$



Upgrading to 12 GeV  
nearly complete



Hall A: two HRS'

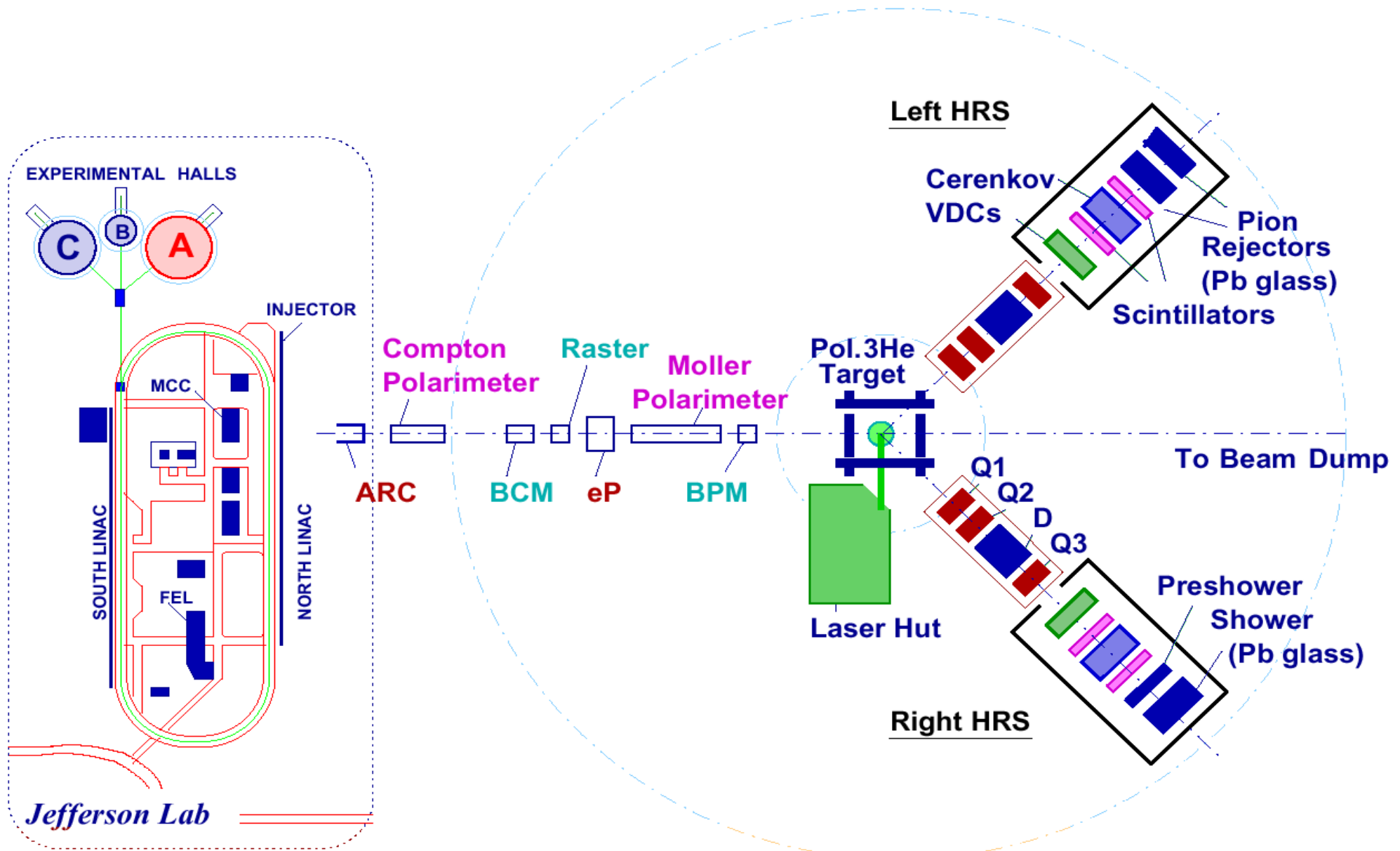


Hall B: CLAS



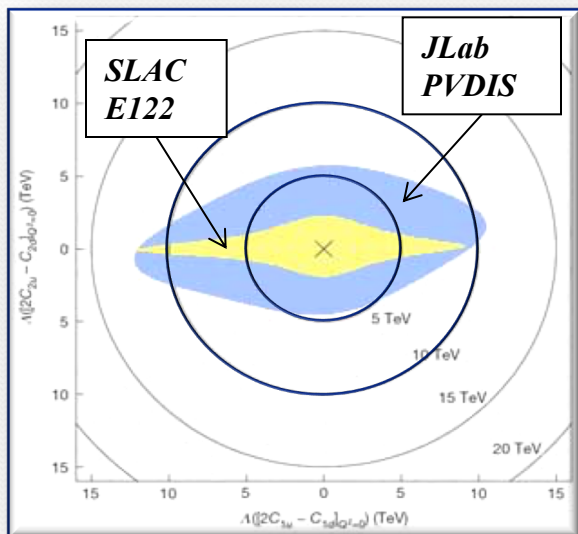
Hall C: HMS+SOS

# Jefferson Lab Hall A Experimental Setup for inclusive polarized $n$ ( $^3\text{He}$ ) Experiments

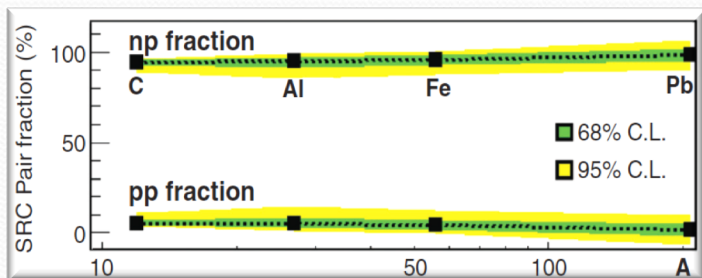


# JLab 2014

Nature 506, 67 (6 February 2014)  
Parity Violating DIS



Science 346, 614 (October 2014)  
Short Range NN Correlations



# Near-Future

Decade of Experiments Approved  
Eager to Start 12 GeV Science!

Jefferson Lab  
Thomas Jefferson National Accelerator Facility

Physics Opportunities with  
the 12 GeV Upgrade at Jefferson Lab

- **Confinement**
- **Hadron Structure**
- **Nuclear Structure**  
and Astrophysics
- **Fundamental Symmetries**

# Future

Electron Ion Collider  
The Next QCD Frontier

Electron Ion Collider:  
The Next QCD Frontier

Understanding the glue  
that binds us all

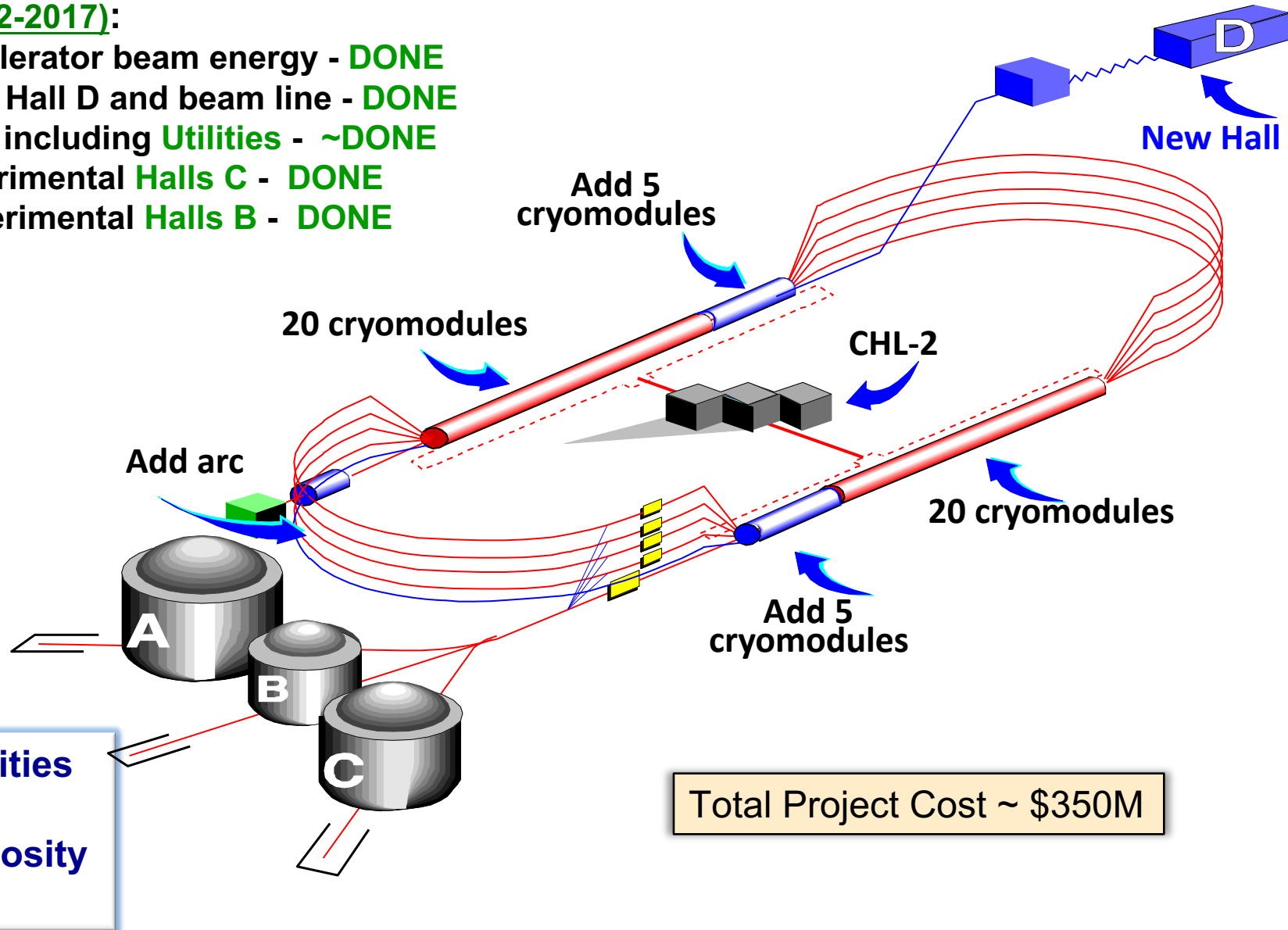
SECOND EDITION

**Role of Gluons in Nucleon and  
Nuclear Structure**

# 12 GeV Upgrade Project

## Project Scope (2012-2017):

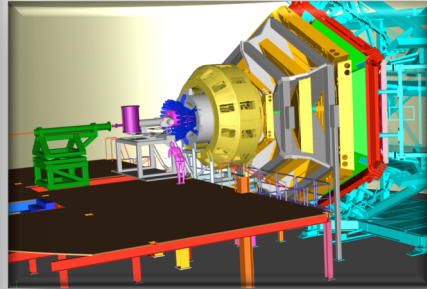
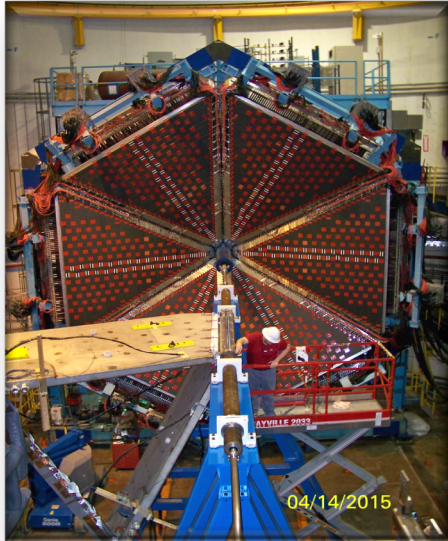
- Doubling the accelerator beam energy - **DONE**
- New experimental Hall D and beam line - **DONE**
- Civil construction including **Utilities** - **~DONE**
- Upgrades to Experimental **Halls C** - **DONE**
- Upgrades to Experimental **Halls B** - **DONE**



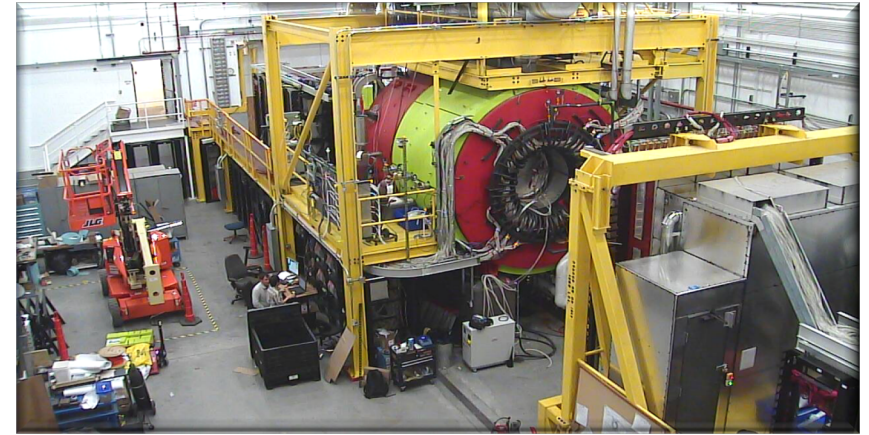
Enhanced capabilities  
in existing Halls  
Increase of Luminosity  
 $10^{35} - \sim 10^{39} \text{ cm}^{-2}\text{s}^{-1}$

# 12 GeV Scientific Capabilities

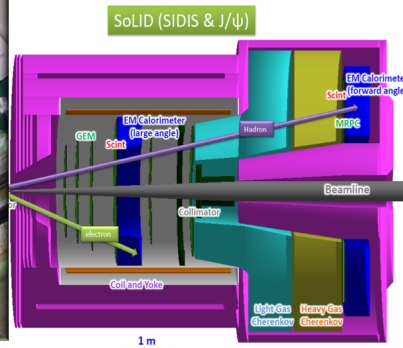
**Hall B** – understanding **nucleon structure** via generalized parton distributions



**Hall D** – exploring origin of **confinement** by studying exotic mesons



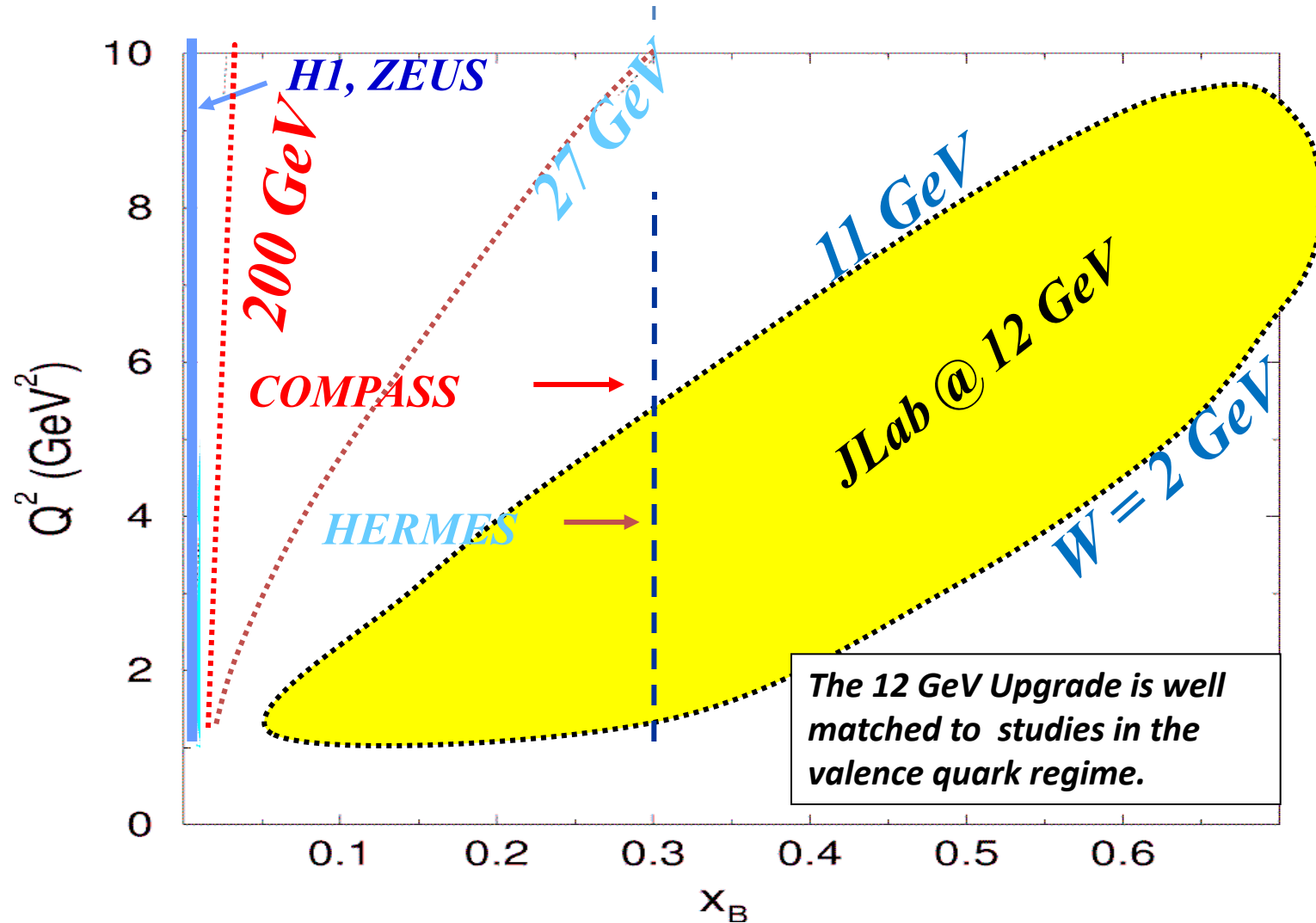
**Hall A** – form factors, future new experiments (e.g., **SoLID** and MOLLER)



**Hall C** – precision determination of **valence quark** properties in nucleons/nuclei

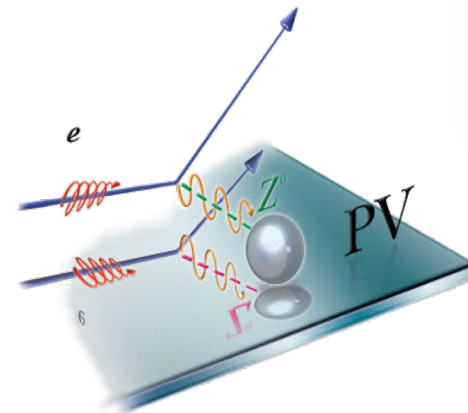
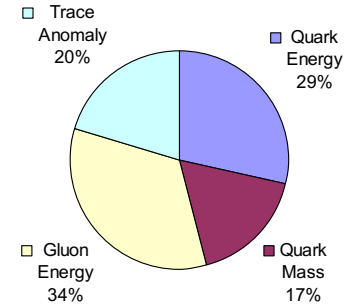


# *Kinematics Coverage of the 12 GeV Upgrade*



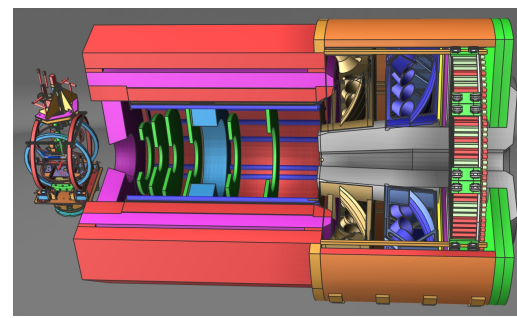
# Jefferson Lab @ 12 GeV Science Questions

- What's the origin of the proton mass?  
How can measurements help?
- Where is the missing spin in the nucleon?  
Role of orbital angular momentum?
- Can we reveal a novel landscape of nucleon substructure through 3D imaging at the femtometer scale?
- Can we discover evidence for physics beyond the standard model of particle physics?





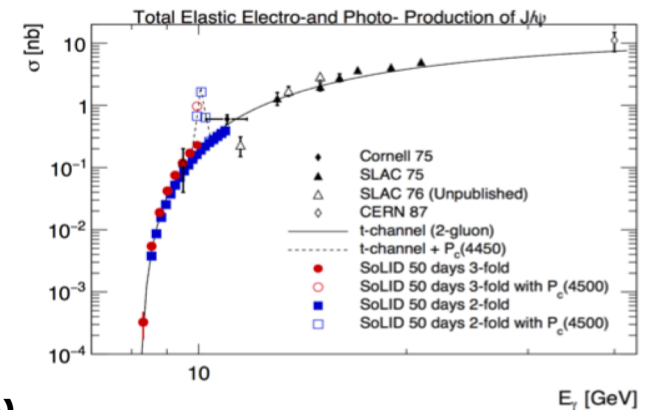
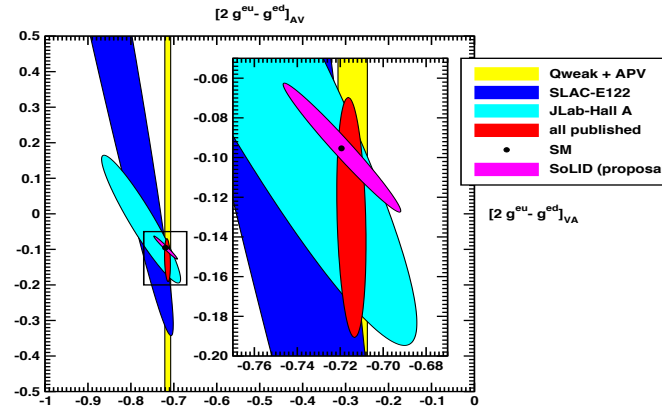
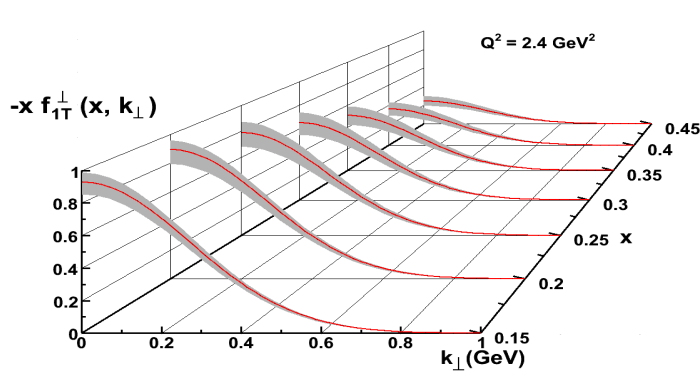
# Solenoidal Large Intensity Device (SoLID)



- Full exploitation of JLab 12 GeV Upgrade to maximize scientific return

## A Large Acceptance Detector AND Can Handle High Luminosity ( $10^{37}$ - $10^{39}$ )

- Reach ultimate precision for tomography of the nucleon
- PVDIS in high- $x$  region - providing sensitivity to new physics at 10-20 TeV
- Threshold J/Psi - probing strong color fields in the nucleon and the origin of its mass (trace anomaly)



- Strong collaboration (300 collaborators from 72 institutions, 13 countries)

- Significant international contributions
- Strong theoretical support

- 2015 LRP recommendation IV

- We recommend increasing investment in small-scale and mid-scale projects and initiatives that enable forefront research at universities and laboratories –
- **SoLID – Strongly endorsed mid-scale project**

# Electron Ion Collider

Future QCD Facility:  
Study QCD Sea and Gluons

# Electron Ion Collider

## NSAC 2007 Long-Range Plan:

“An **Electron-Ion Collider (EIC)** with **polarized** beams has been **embraced by the U.S. nuclear science community** as embodying the vision for **reaching the next QCD frontier**. EIC would provide unique capabilities for the study of QCD well beyond those available at existing facilities worldwide and complementary to those planned for the next generation of accelerators in Europe and Asia.”

## NSAC 2015 Long-Range Plan:

We recommend a high-energy high-luminosity polarized **EIC as the highest priority for new facility construction** following the completion of FRIB.

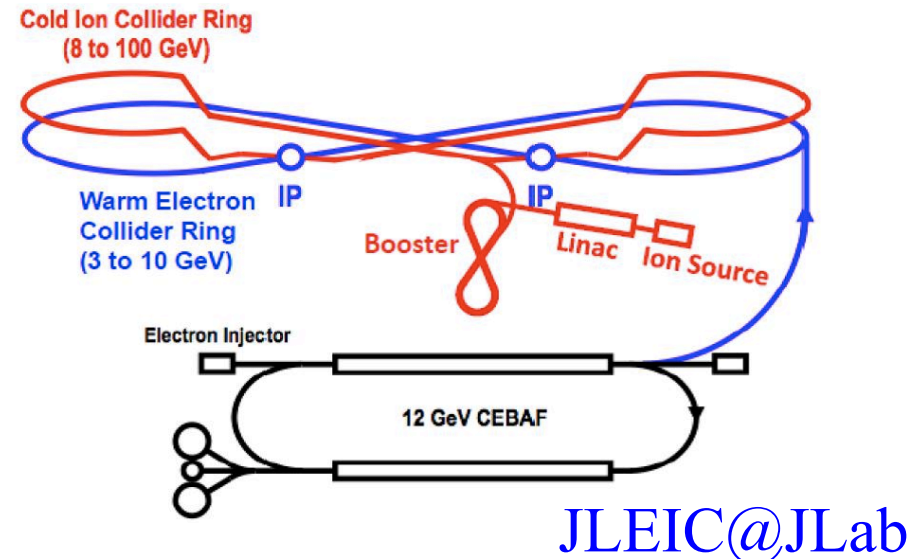
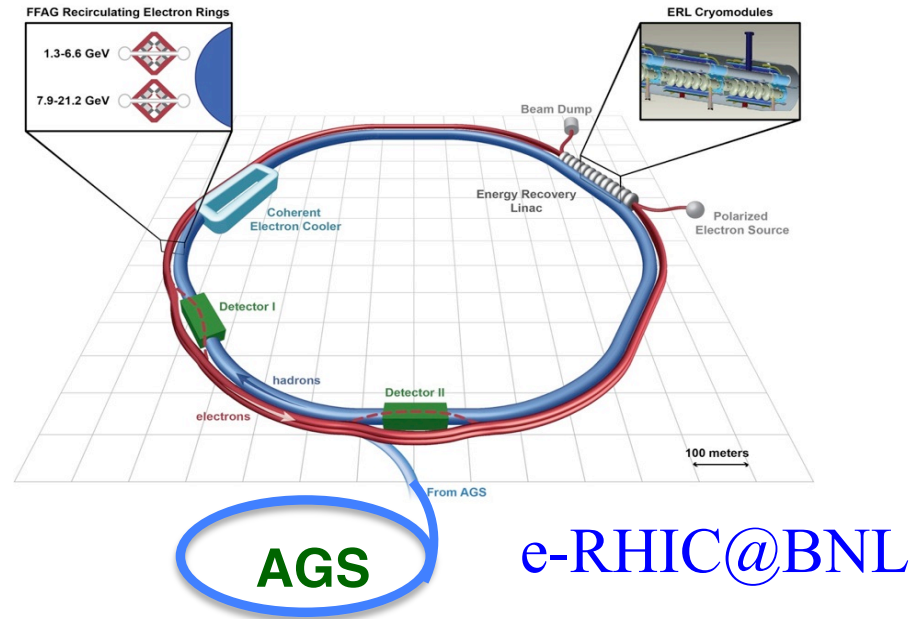
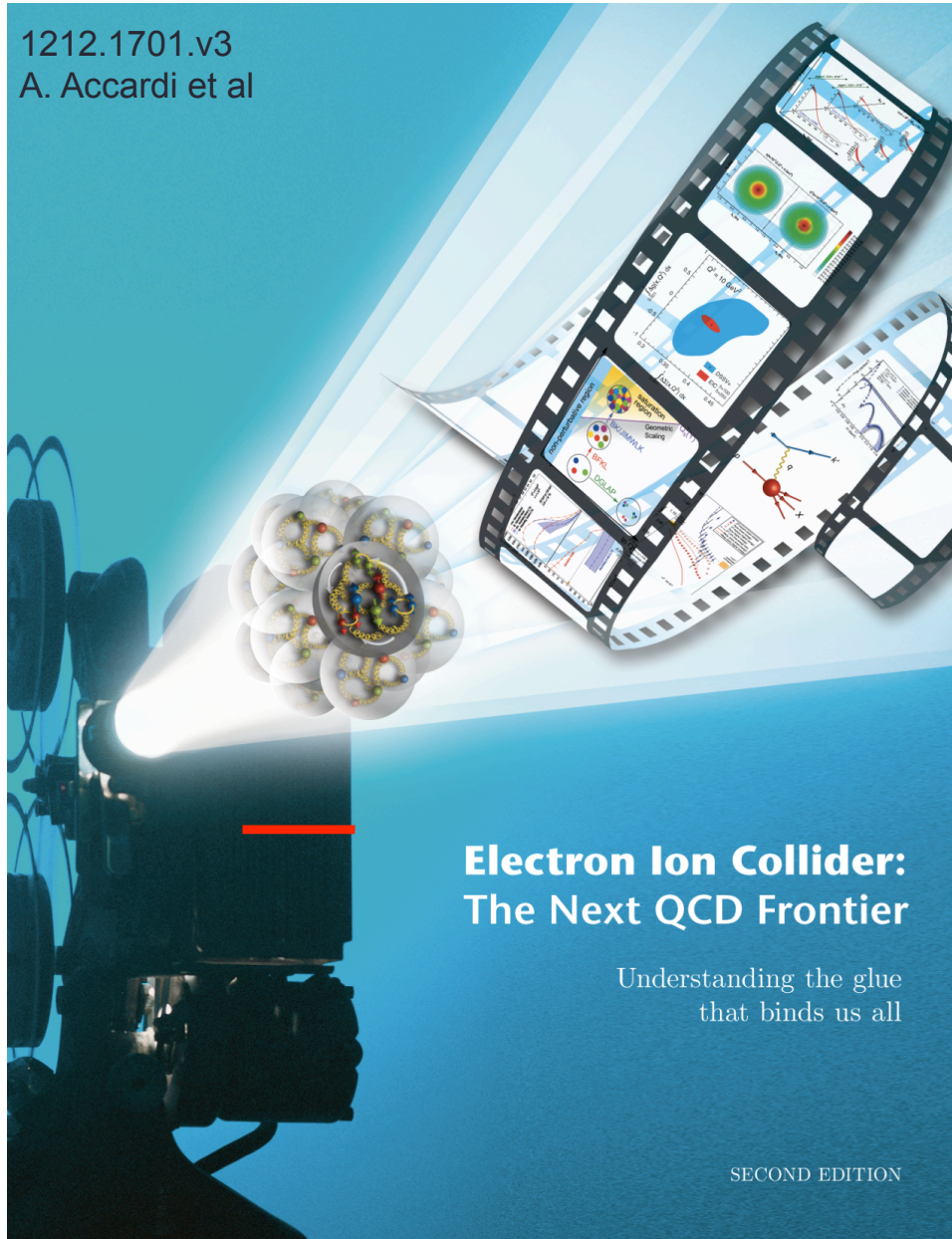
EIC Community White Paper arXiv:1212.1701v2



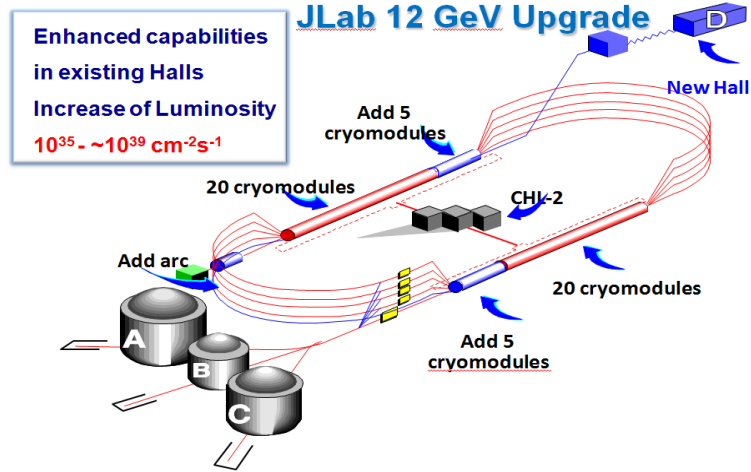
# The Electron Ion Collider

Two proposals for realization of the Science Case

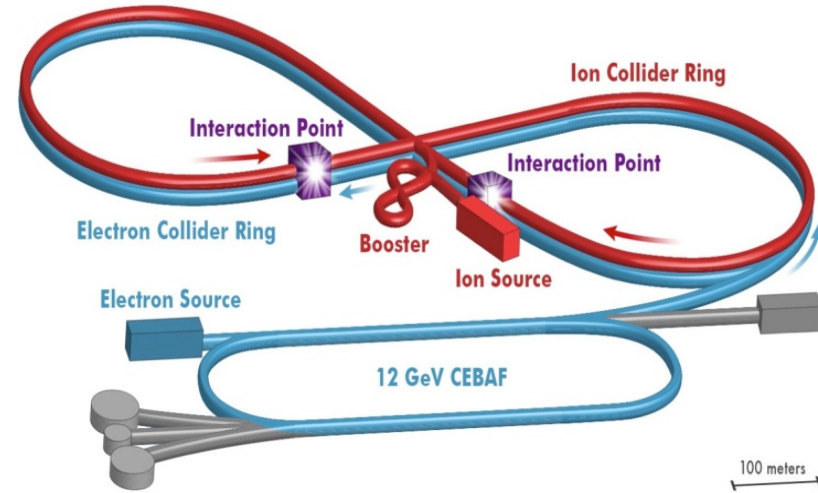
1212.1701.v3  
A. Accardi et al



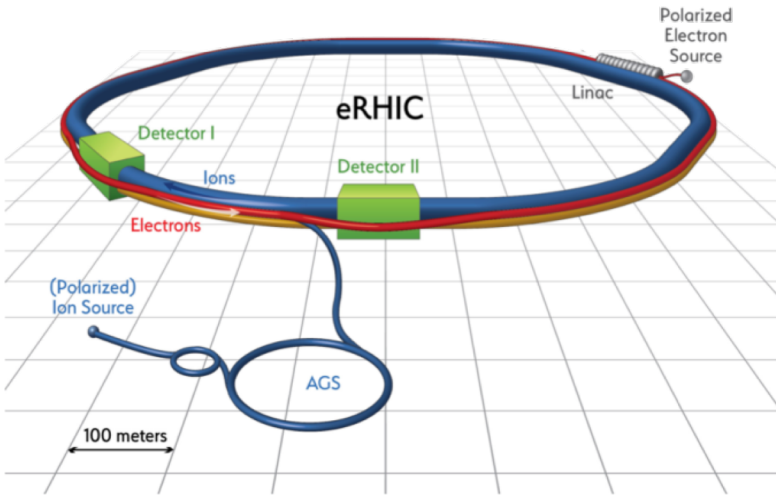
# JLab 12 and Future EIC Plan



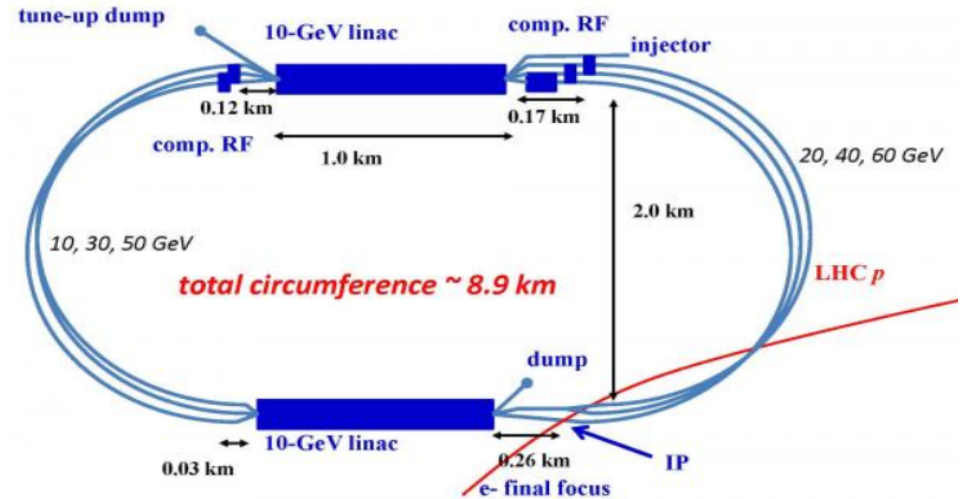
Jlab 12 upgrade (Fixed target)



JLEIC  $\sqrt{s} \sim 20$  to 70 GeV



eRHIC,  $\sqrt{s} \sim 140$  GeV

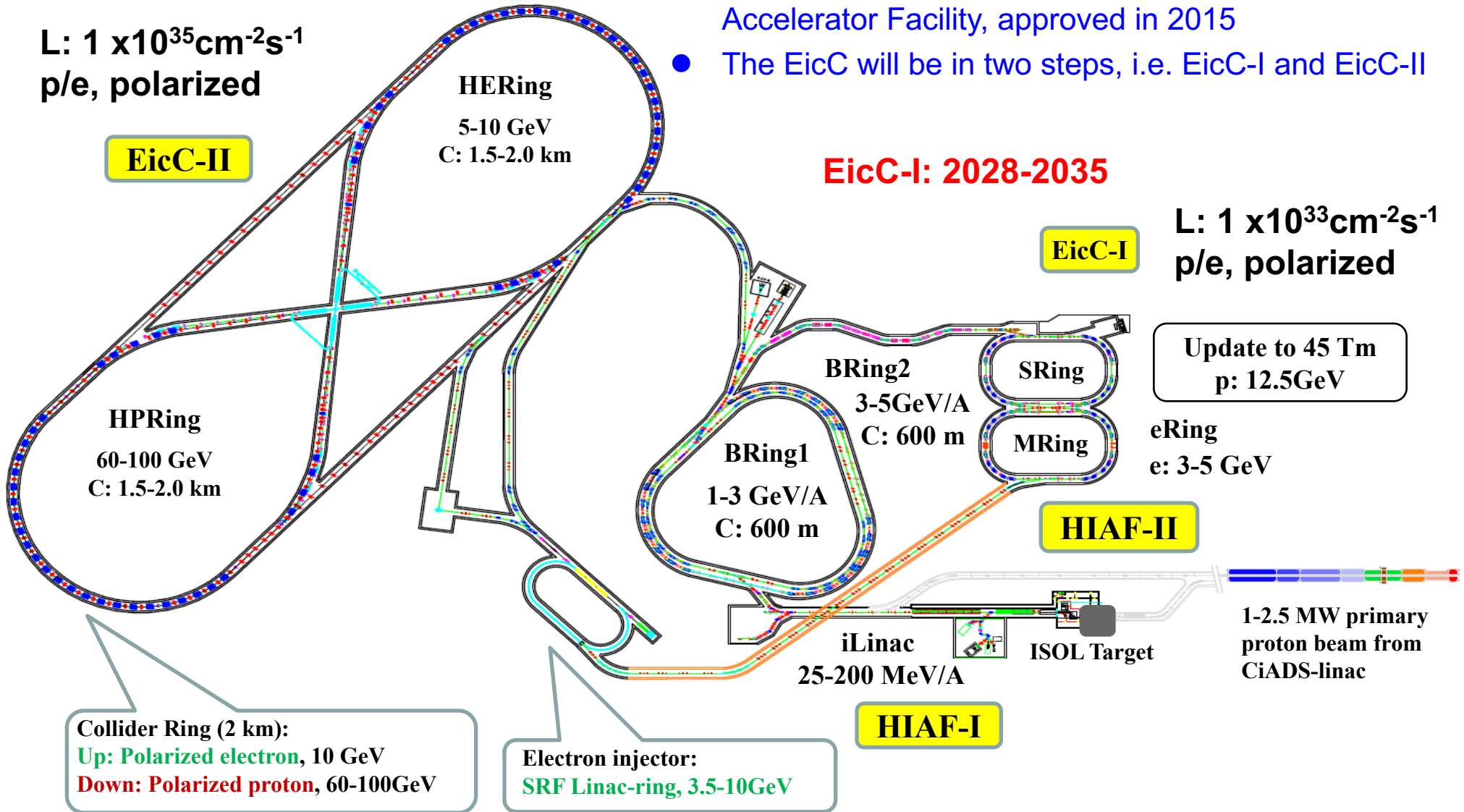


LHeC,  $\sqrt{s} : 1.3 \sim 3.5$  TeV

- Based on the HIAF (the Heavy Ion high Intensity Accelerator Facility, approved in 2015)
- The EicC will be in two steps, i.e. EicC-I and EicC-II

**L:  $1 \times 10^{35} \text{cm}^{-2} \text{s}^{-1}$**   
**p/e, polarized**

**EicC-II**

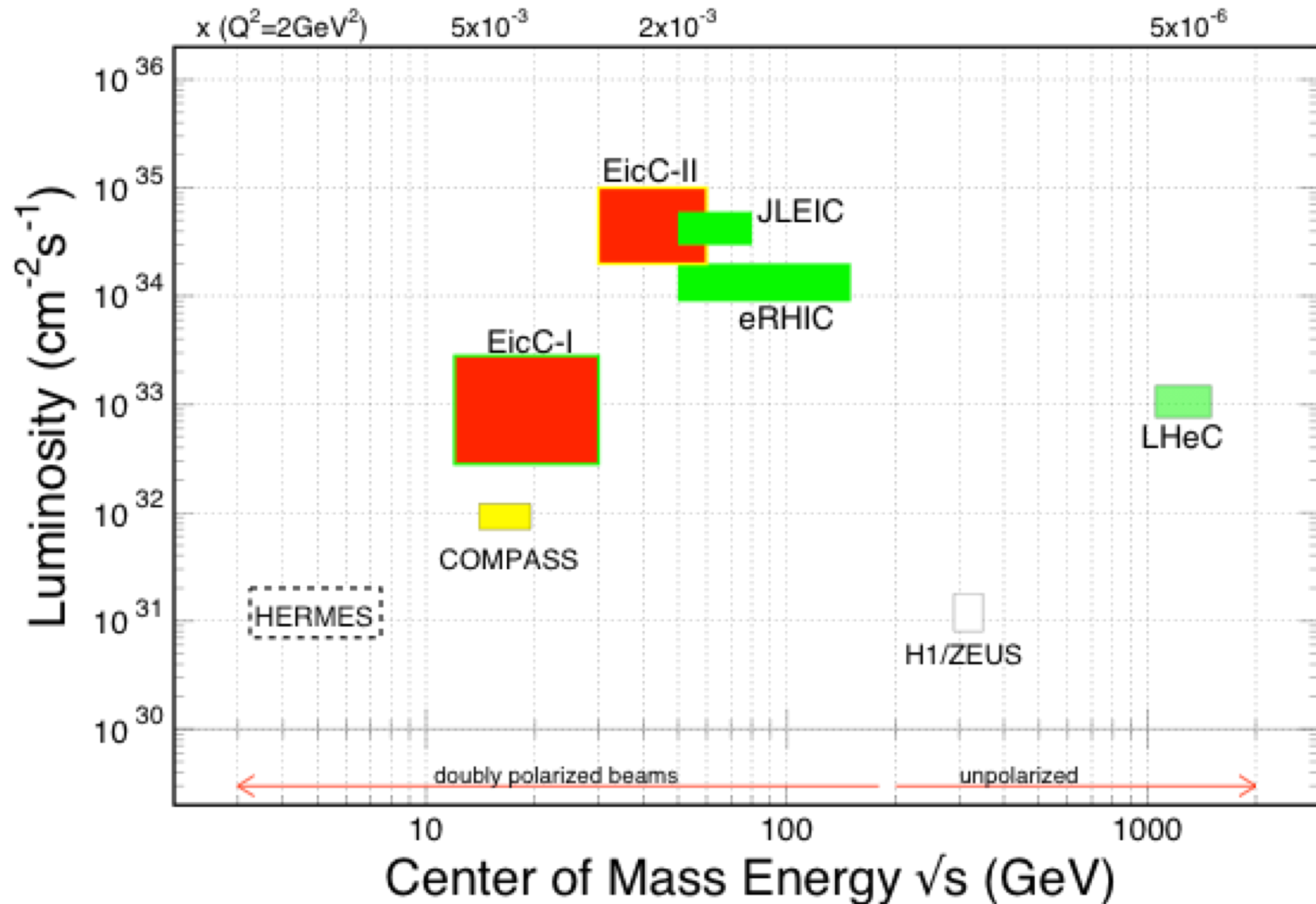


**L:  $1 \times 10^{33} \text{cm}^{-2} \text{s}^{-1}$**   
**p/e, polarized**

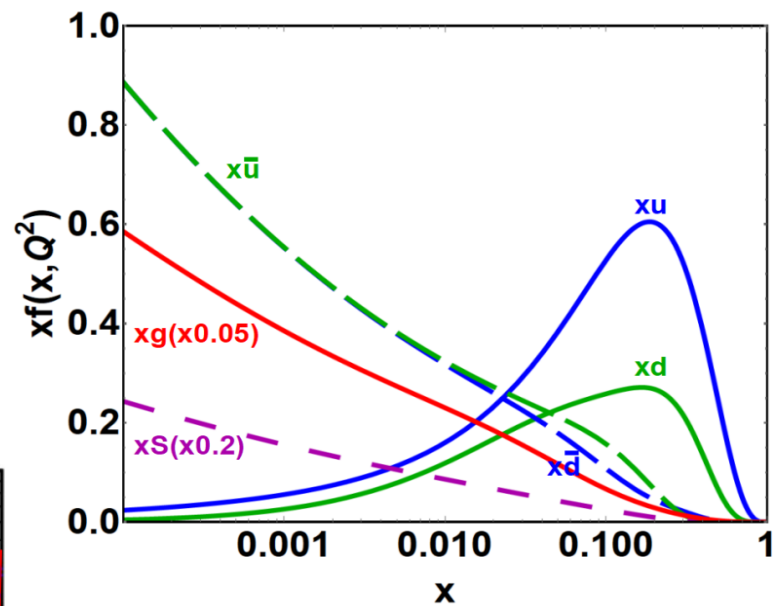
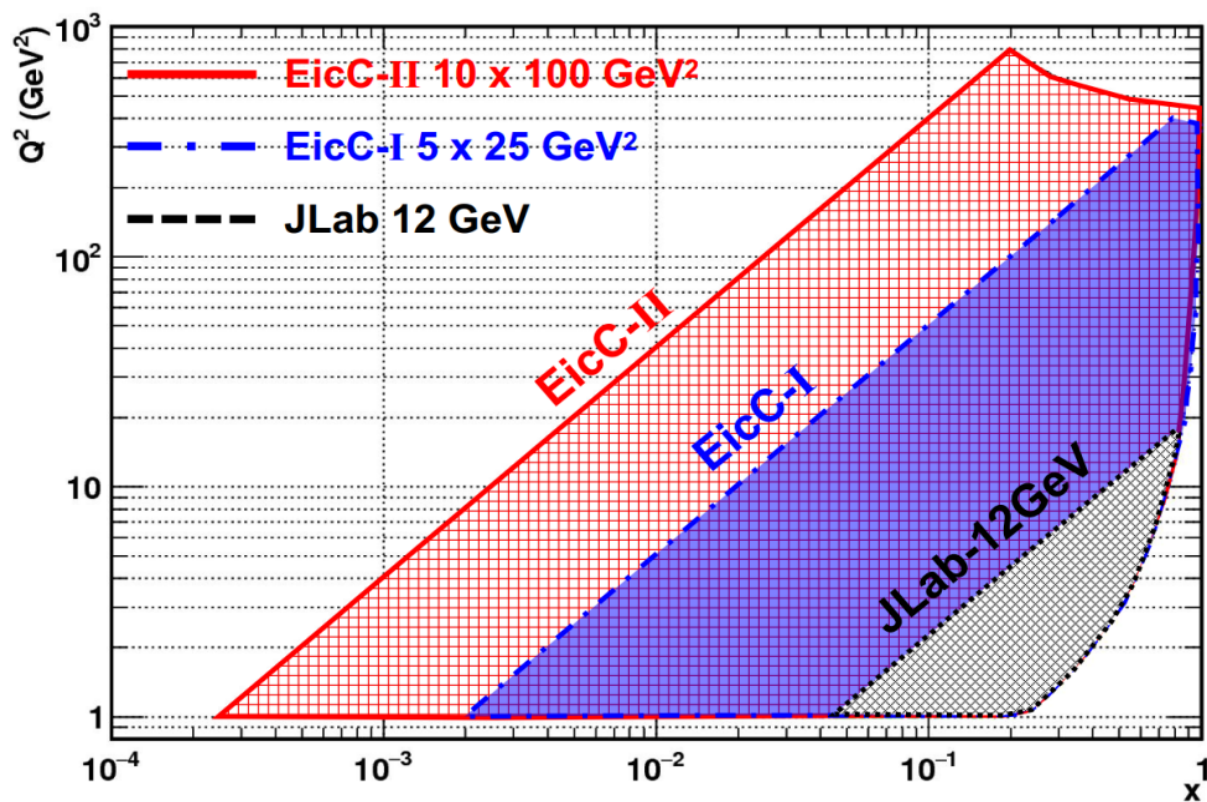
**EicC-I**

**EicC-I: 2028-2035**

# Comparisons: Luminosity and Energy



# Kinematics Coverage





# Figure of Merit Comparison

- **Figure-of Merit for double polarization experiments**

$$\text{FOM} = L * P_e^2 * P_N^2 * D^2$$

L=Luminosity, P=Polarization, D=Dilution

- **FOM Comparison of EIC@HIAF (1) with COMPASS (2)**

HIAF:  $L=1 * 10^{33}$ ,  $D=1$

COMPASS:  $L=10^{32}$ ,  $D=0.13$  ( $\text{NH}_3$  target)

Unpolarized:

$$\text{FOM}(1)/\text{FOM}(2) = L(1)/L(2) \sim 10$$

Polarized:

$$\text{FOM}(1)/\text{FOM}(2) = L(1)/L(2) * [D(1)^2 / D(2)^2] \sim 500$$

# Overview of EIC Experiments

A Key Question for EIC:

“How are the sea quarks and gluons, and their spins distributed in space and momentum inside the nucleon?”

- Spin and Flavor Structure of the Nucleon
- 3-d Structure in Momentum Space and Confined Motion of Partons inside the Nucleon
- 3-d Structure in Coordinator Space and Tomography of the Nucleon

Other Important Questions:

“Where does the saturation of gluon densities set in?”

How does the nuclear environment affect the distribution of quarks and gluons and their interactions in nuclei?”

Opportunity for Low Energy Search of Physics Beyond SM

- Parity Violating e-N

# *Summary*

- Understand strong interaction/nucleon structure: A challenge
- Review of History in Nucleon Structure Study
- Electron Scattering: A clean tool to study nucleon structure and QCD
- JLab facility and 12 GeV upgrade
- Future Electron-Ion Collider
- EIC goes into new region: understand sea quarks and gluons

# Physics with an Electron-Ion Collider

## *II: From Factors*

Jian-ping Chen (陈剑平), Jefferson Lab, Virginia, USA

Pre-Workshop Lectures, Hadron-China2018, July 25, 2018

- Electron Scattering
- Elastic Scattering: From Factors

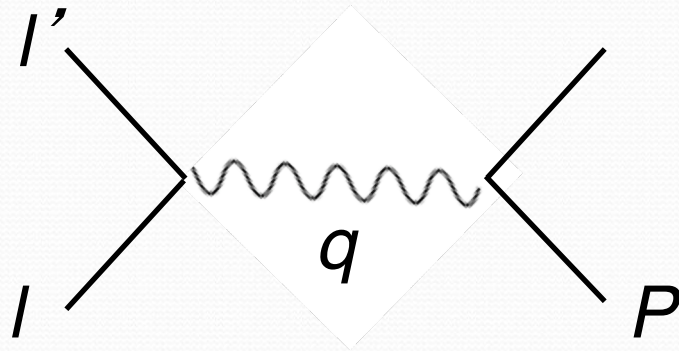
Surprise:  $G_E^p$  @ high  $Q^2$ : proton shape, 2- $\gamma$  exchange

Proton radius puzzle

# Nucleon Form Factors

**Charge and Magnetization Distributions**  
**Transverse Density**

# Elastic Electron Scattering



$$d\sigma \propto \langle |\mathcal{M}|^2 \rangle = \frac{g_e^4}{q^4} L_{\text{lepton}}^{\mu\nu} K_{\mu\nu \text{ nucleon}}$$

The lepton tensor is calculable:

$$L_{\text{lepton}}^{\mu\nu} = 2 (k^\mu k'^\nu + k^\nu k'^\mu + g^{\mu\nu} (m^2 - k \cdot k'))$$

The nucleon tensor is not; it's general (spin-independent, parity conserved) form is:

$$K_{\mu\nu \text{ nucleon}} = -K_1 g_{\mu\nu} + \frac{K_2}{M^2} p_\mu p_\nu + \frac{K_4}{M^2} q_\mu q_\nu + \frac{K_5}{M^2} (p_\mu q_\nu + p_\nu q_\mu)$$

Charge conservation at the proton vertex reduces the number of structure functions:

$$q_\mu K_{\text{nucleon}}^{\mu\nu} \rightarrow K_4 = f(K_1, K_2), \quad K_5 = g(K_2)$$

and one obtains the Rosenbluth form, with electric and magnetic form factors:

$$\frac{d\sigma}{d\Omega} = \left( \frac{\alpha}{4ME \sin^2(\theta/2)} \right)^2 \frac{E'}{E} [2K_1 \sin^2(\theta/2) + K_2 \cos^2(\theta/2)], \quad K_{1,2}(q^2)$$

# Elastic Scattering on a Proton

From relativistic quantum mechanics one can derive the the formula electron-proton scattering where one has assumed the exchange of a single virtual photon.

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \cdot \frac{E'}{E} \left[ \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta}{2} \right]$$

where  $G_E$  and  $G_M$  form factors take into account the finite size of the proton.

$$G_E = G_E(Q^2), G_M = G_M(Q^2); G_E(0)=1, G_M(0) = \mu_p$$

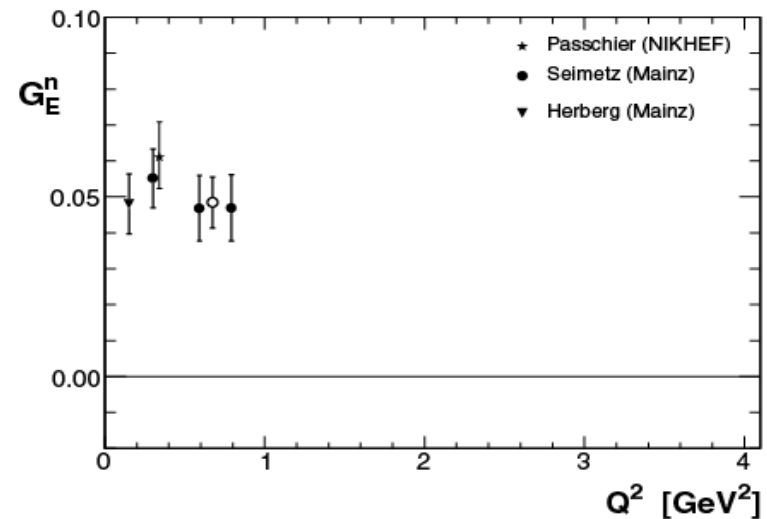
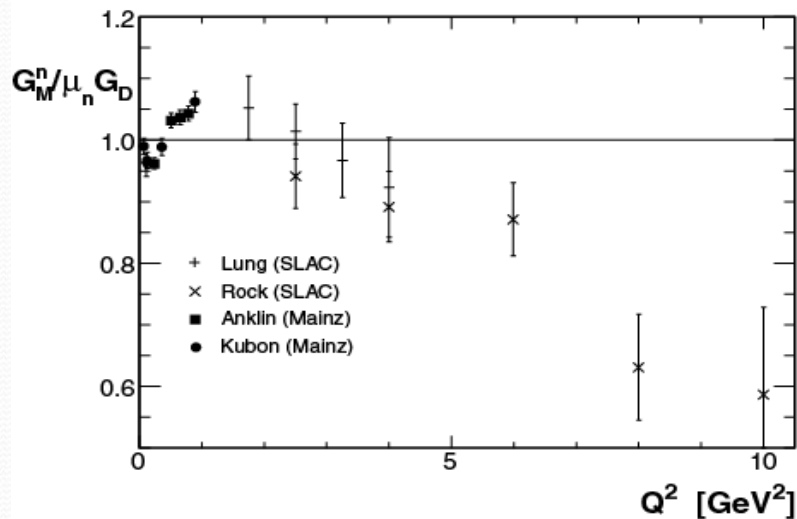
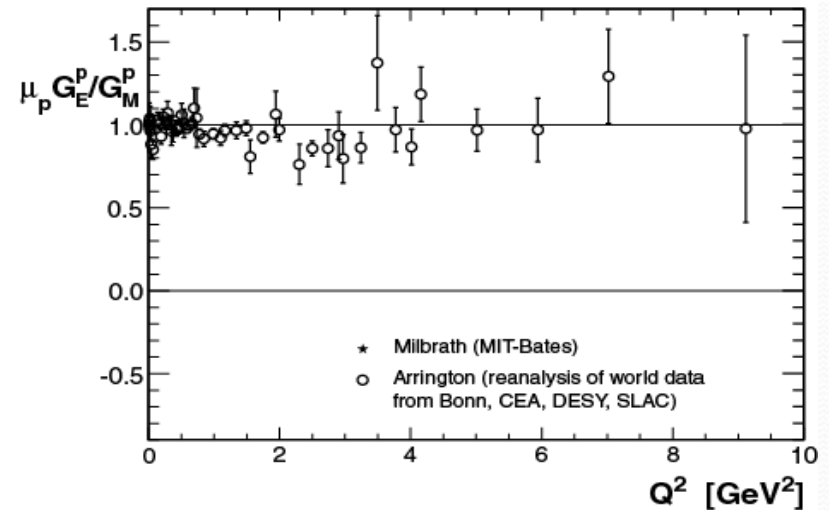
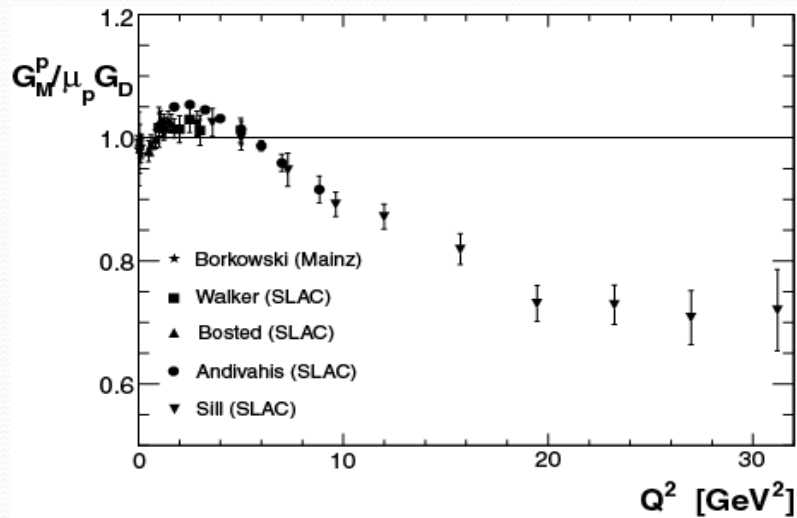
$$Q^2 = 4 E E' \sin^2(\theta/2) \text{ and } \tau = Q^2 / 4m_p^2$$

Elastic cross sections at small angles and small  $Q^2$ 's are dominated by  $G_E$  ( Prad Hall B )

Elastic cross Sections at small angles and small  $Q^2$ 's are dominated by  $G_M$  ( GMP Hall A )

For moderate  $Q^2$ 's one can separate  $G_E$  and  $G_M$  with Rosenbluth or asymmetry measurements.

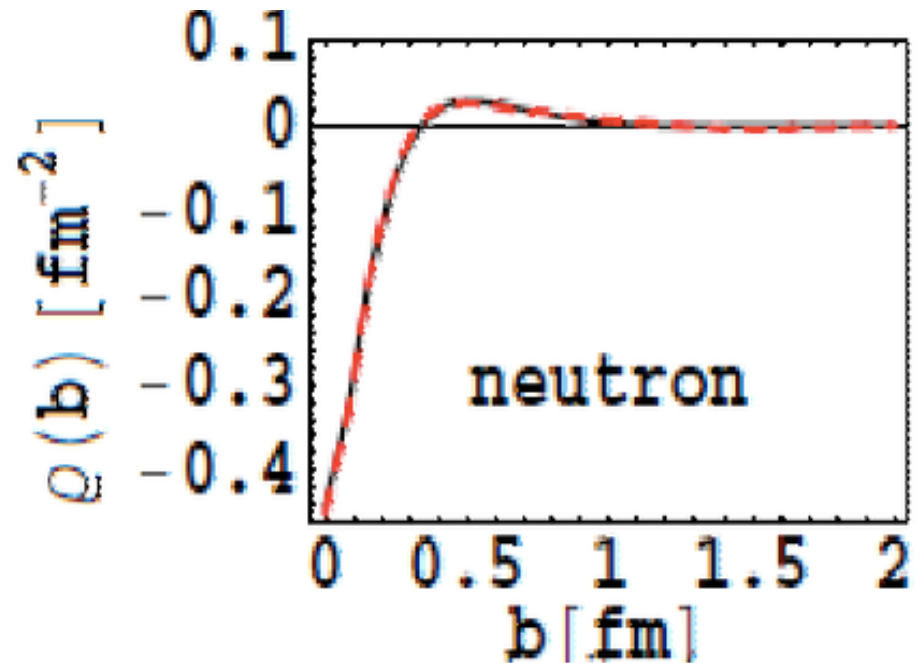
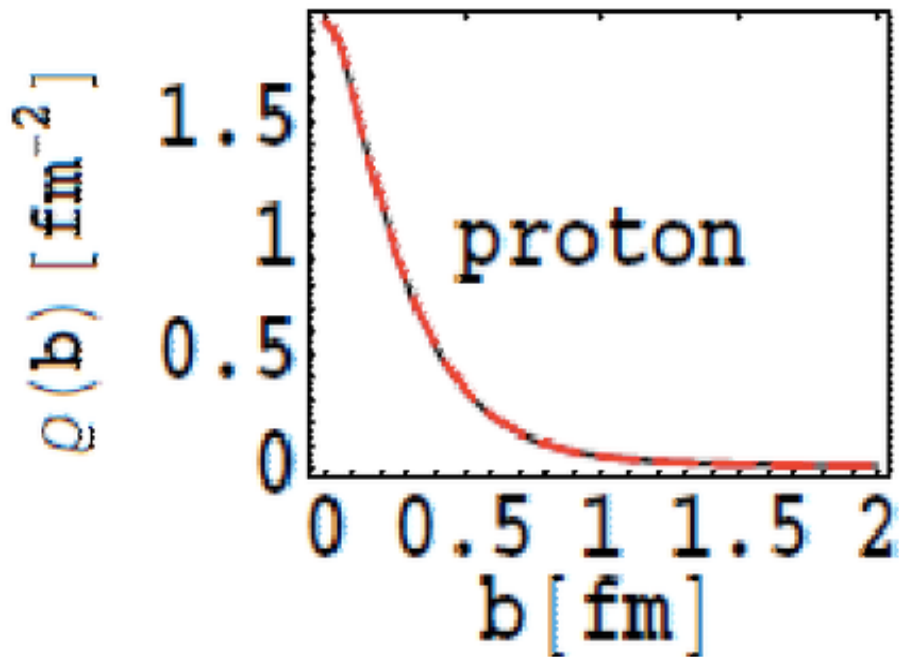
# Before JLab and Recent non-JLab Data





# Form Factors $\rightarrow$ Charge/Current Distributions (non-relativistic)

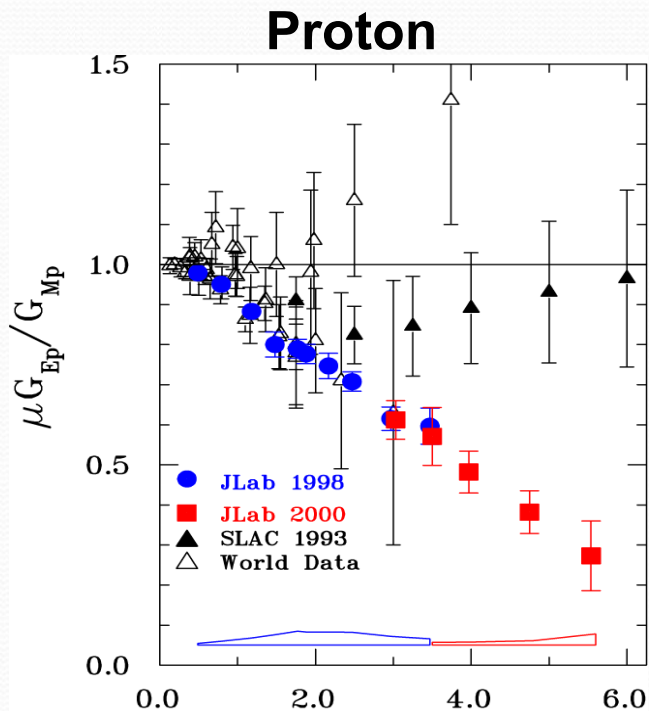
Elastic electric form factor  $\rightarrow$  Charge distributions



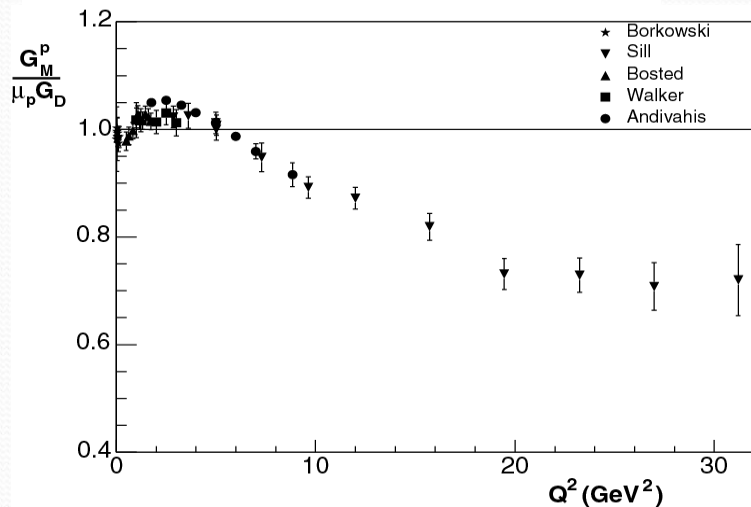
# JLab Data on EM Form Factors

## Testing Ground for Theories of Nucleon Structure

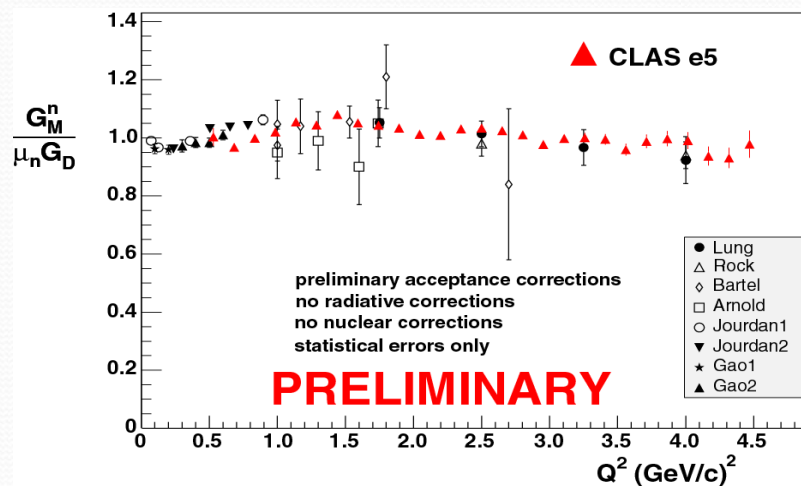
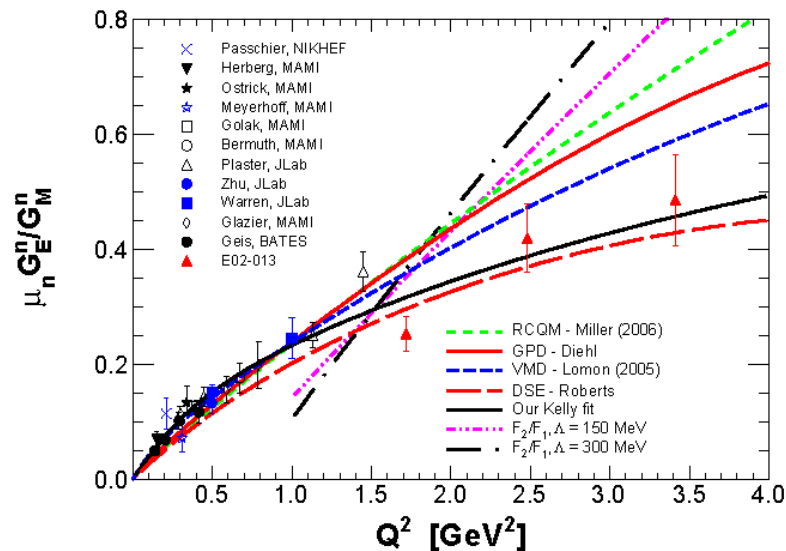
Electric



Magnetic



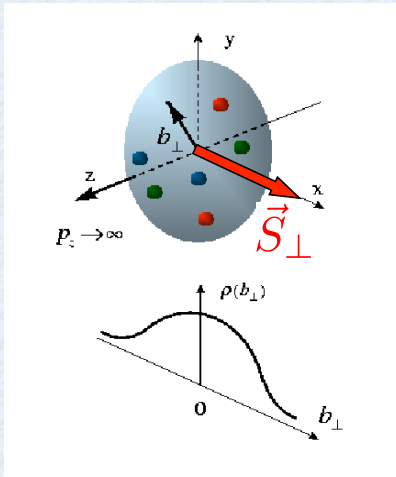
### Neutron



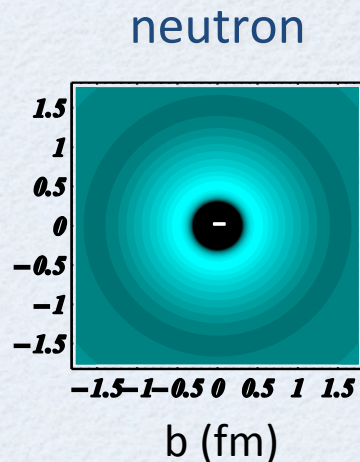
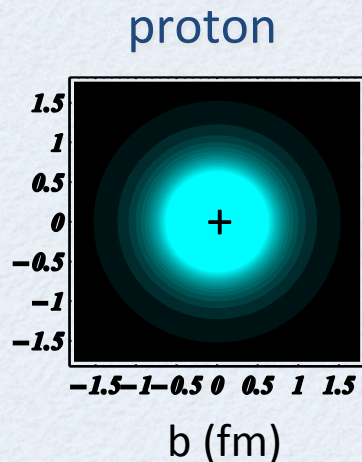
# Form factors: 2D light-front densities of hadrons

$$\rho^N(\vec{b}) = \int_0^\infty \frac{dQ}{2\pi} Q J_0(bQ) F_1(Q^2) + \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{2M_N} J_1(bQ) F_2(Q^2)$$

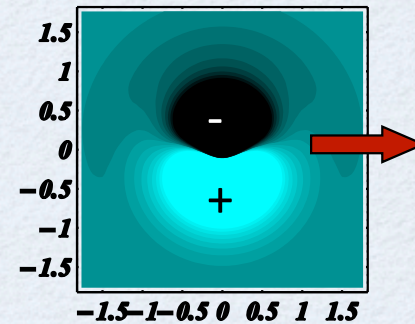
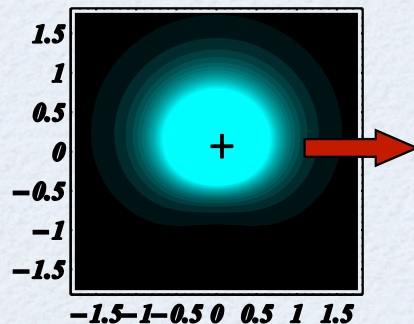
→ unpolarized Dirac FF  $F_1$   
 → transverse polarization Pauli FF  $F_2$



unpolarized charge density



density for transverse polarization



Burkardt (2000, 2003)

Miller (2007)

Carlson, Vdh (2008)

# $G_E^p$ : JLab Polarization-Transfer Data

Using Focal Plane Polarimeter in Hall A

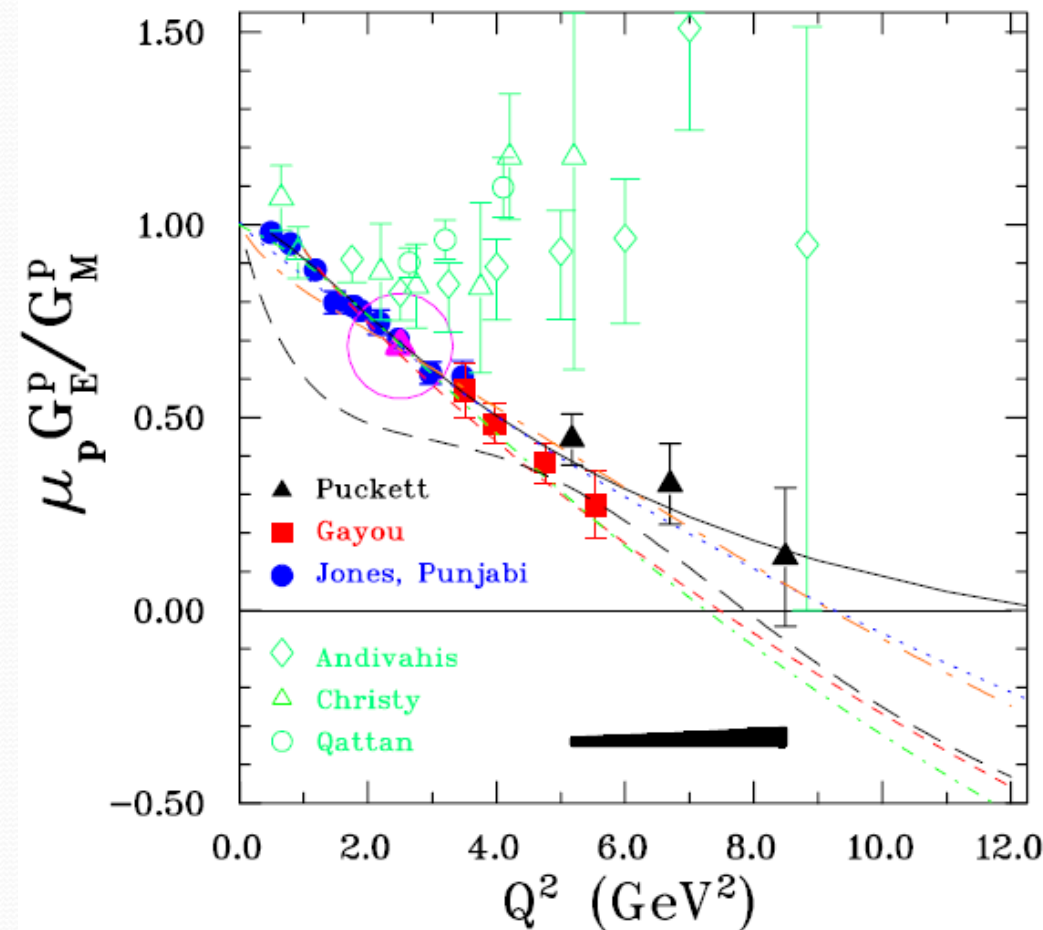
- E93-027 PRL 84, 1398 (2000)
- E99-007 PRL 88, 092301 (2002)
- E04-108, [arXiv:1005.3419v2](https://arxiv.org/abs/1005.3419v2) (2010)

Clear discrepancy between polarization transfer and Rosenbluth data

- Investigate possible theoretical sources for discrepancy  
→ likely two-photon contributions

Information on the shape of the proton and the orbital angular momentum.

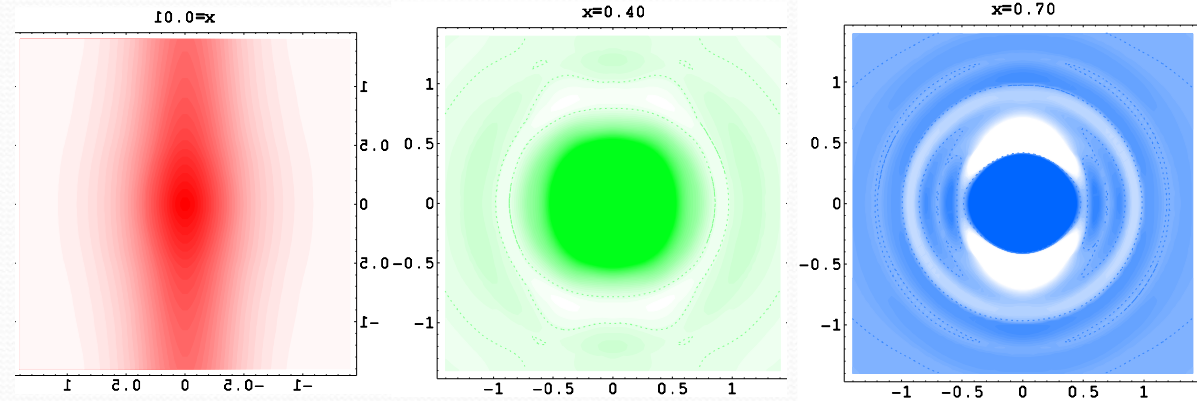
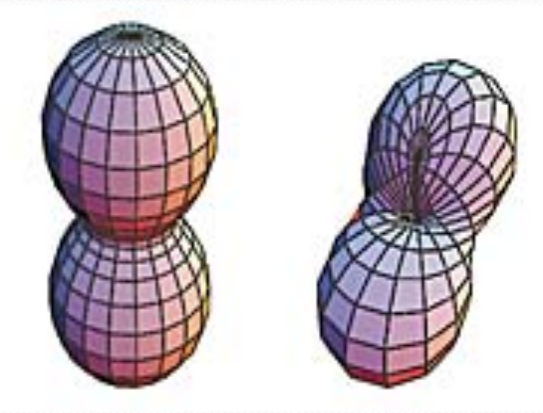
Transverse density .



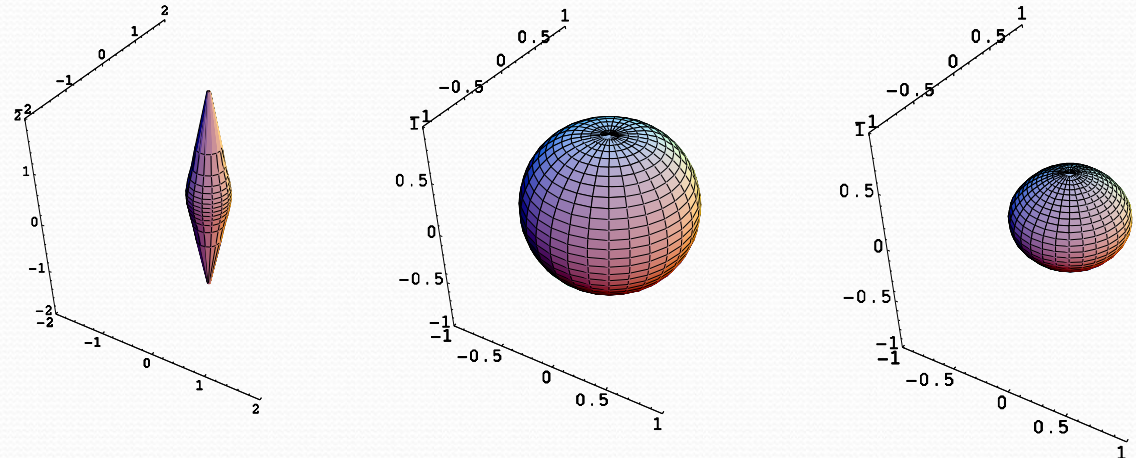
# The Proton's Shape

It's a Ball. No, It's a Pretzel.  
Must Be a Proton.  
(K. Chang, NYT, May 6, 2003)

Belitsky, Ji and Yuan: PRD 69, 074014(04)

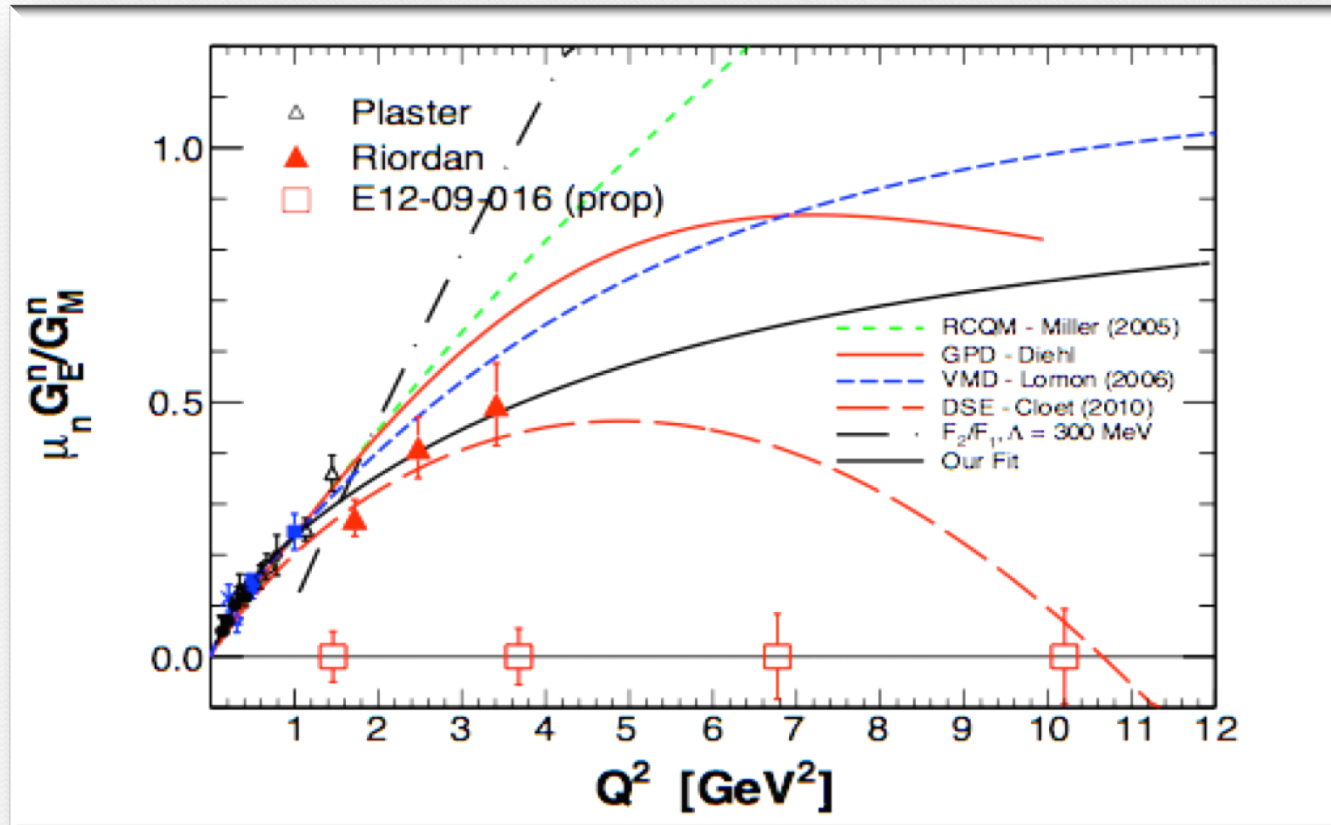


quark spin parallel to that  
of the proton (left), quark spin  
perpendicular to the proton spin  
(right).



G. Miller, PRC 68, 022201 (03)

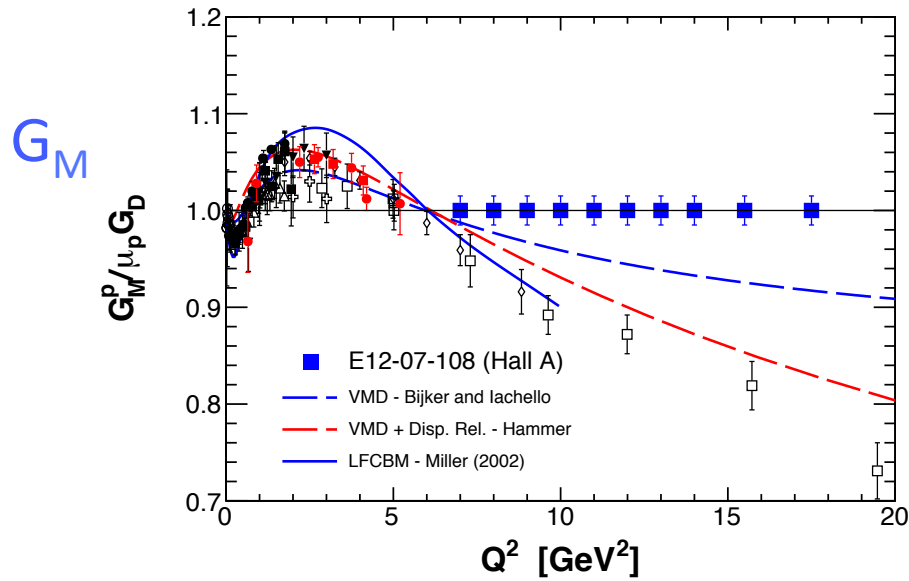
# $G_E^n$ : 6 GeV Results and 12 GeV Plan



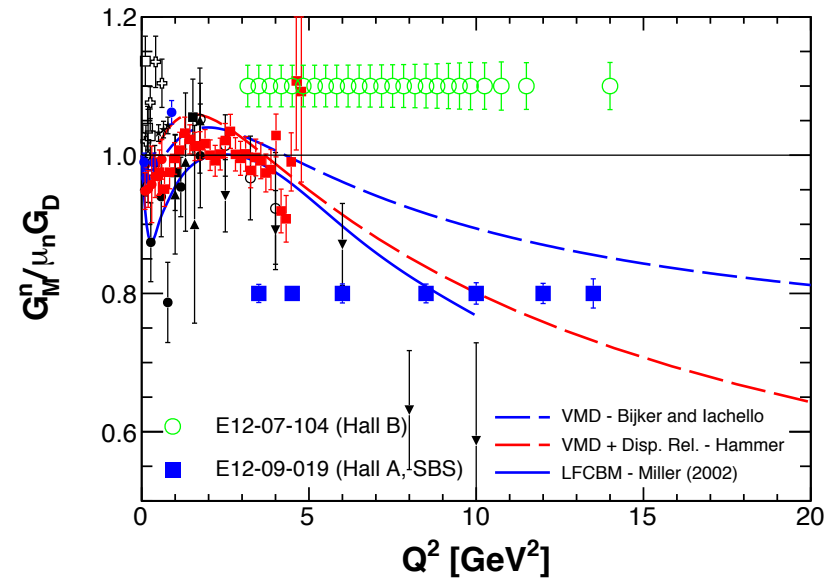
- *The dramatic turnover of the Argonne DSE model would be clearly visible.*
- *If the turnover is seen, it would provide strong evidence for the importance of diquark degrees of freedom in the nucleon form factors.*

# Planned JLab Measurements of Form Factors

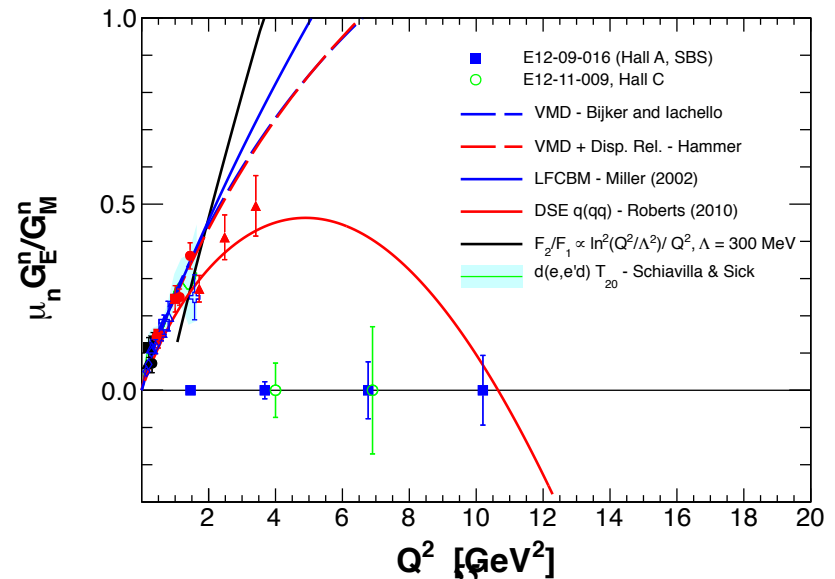
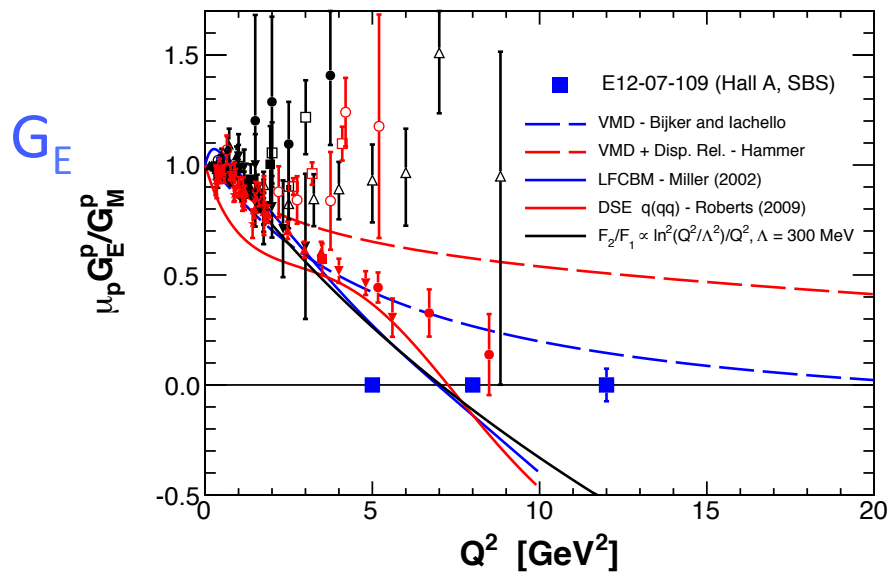
Proton



Neutron



$G_E$

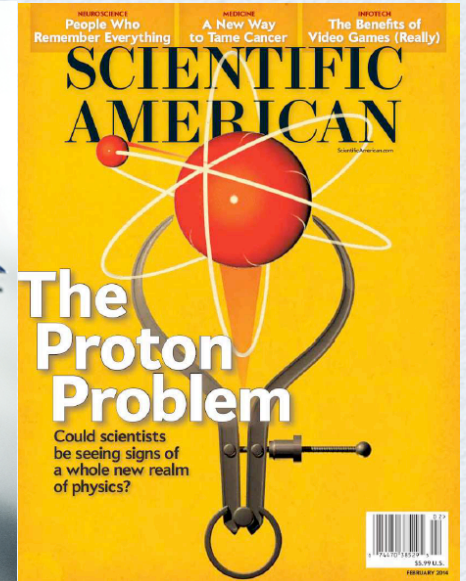
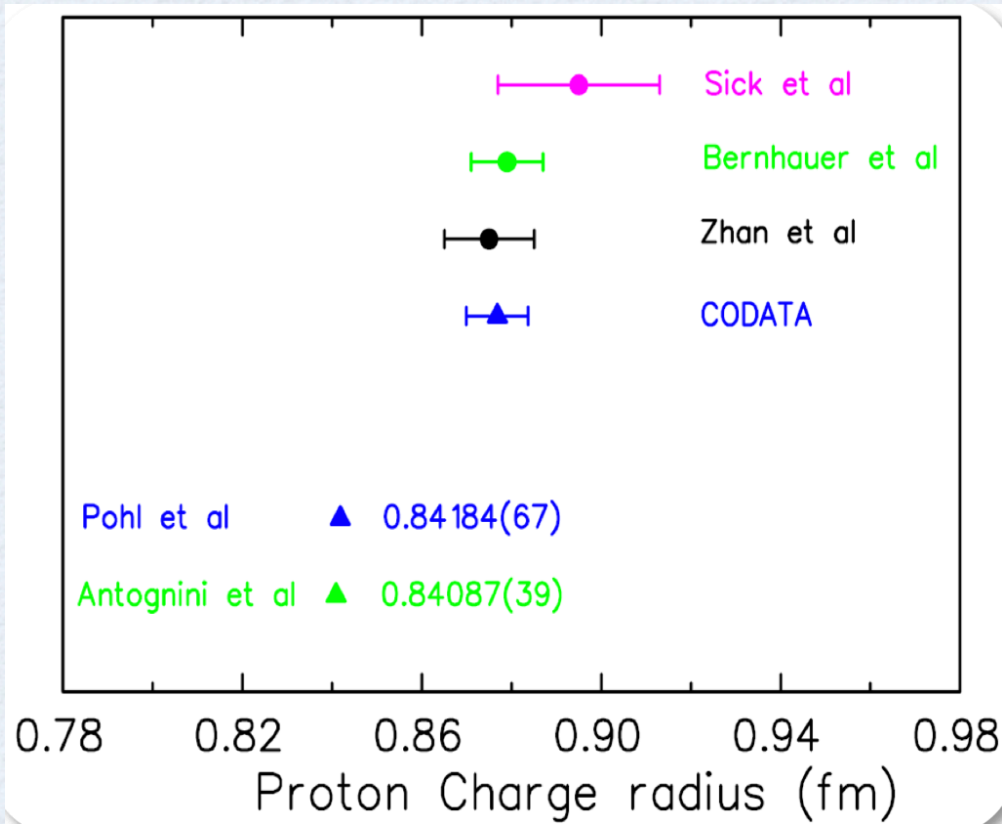


# Proton Radius Puzzle

**Electron probe vs. muon probe**



# Proton radius puzzle



**$\mu\text{H}$  data:**

$$R_E = 0.8409 \pm 0.0004 \text{ fm}$$

Pohl et al. (2010)

Antognini et al. (2013)



**$7 \sigma$  difference !?**

**ep data:**

$$R_E = 0.8775 \pm 0.0051 \text{ fm}$$



## Charge Radius of the Proton

- Proton  $G_E$  has no measured minima and it is too light for the Fourier transformation to work in a model independent way.
- Thus for the proton we make use of the fact that as  $Q^2$  goes to zero the charge radius is proportional to the slope of  $G_E$

$$G_E(Q^2) = 1 + \sum_{n \geq 1} \frac{(-1)^n}{(2n+1)!} \langle r^{2n} \rangle Q^{2n}$$

$$r_p \equiv \sqrt{\langle r^2 \rangle} = \left( -6 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \right)^{1/2}$$

*We don't measure to  $Q^2$  of zero, so this is going to be an extrapolation problem.*

# Proton radius puzzle: what's next ?

- ➔  $\mu\text{H}$  Lamb shift: muonic D, muonic  $^3\text{He}$ ,  $^4\text{He}$  have been performed
- ➔ electronic H Lamb shift: higher accuracy measurements underway
- ➔ electron scattering analysis: **Lorenz et al.**
  - radius extraction fits (use fits with correct analytical behavior:  $2\pi$  cut)
  - radiative corrections, two-photon exchange corrections

new fit  $R_E = 0.904(15)$  fm ( $4\sigma$  from  $\mu\text{H}$ ) **Lee, Arrington, Hill (2015)**

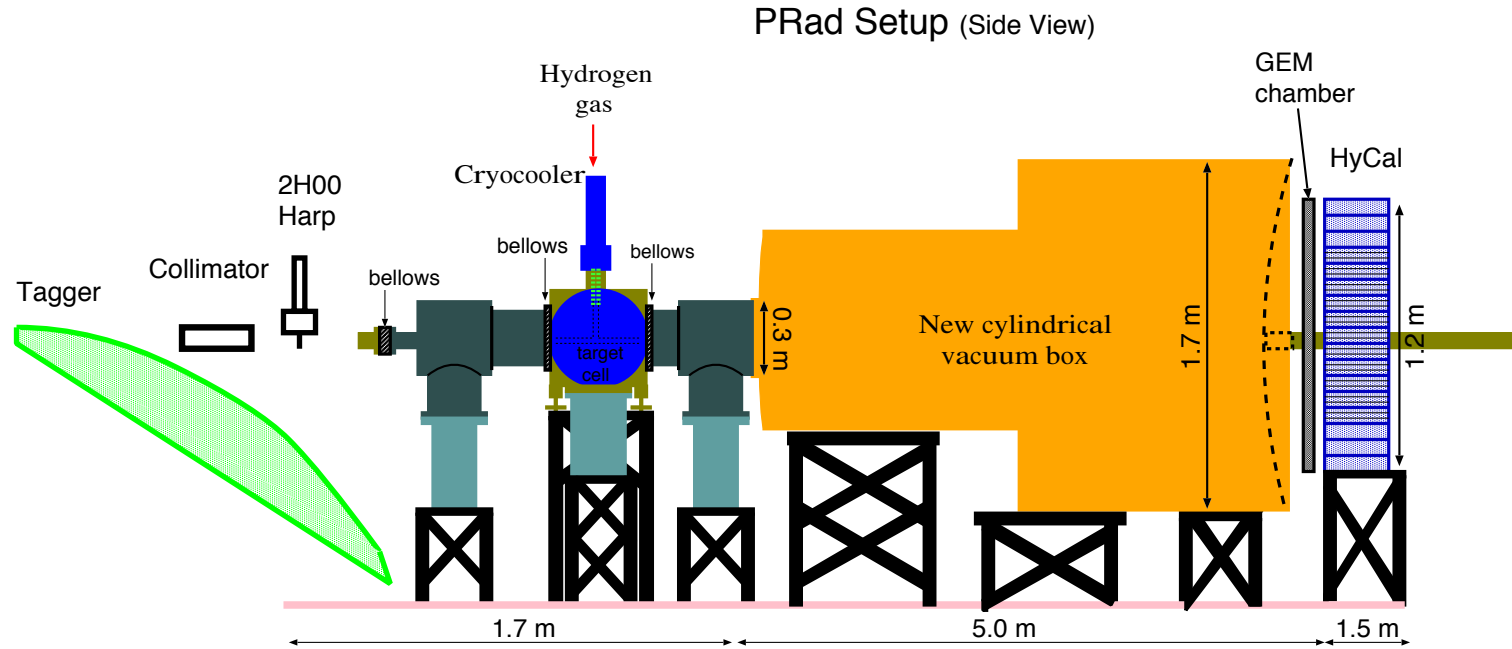
➔ electron scattering experiments:  
new  $G_{Ep}$  experiments down to  $Q^2 \approx 2 \times 10^{-4}$   $\text{GeV}^2$

- **MAMI/A1**: Initial State Radiation (2013/4)
- **JLab/Hall B**: HyCal, magnetic spectrometer-free experiment, norm to Møller (2016/7)  
see talk: H. Gao
- **MESA**: low-energy, high resolution spectrometers (2019)

➔ muon scattering experiments: **MUSE@PSI** (2017/8)

➔  $e^-e^+$  versus  $\mu^- \mu^+$  photoproduction: lepton universality test

# *PRad Experimental Setup in Hall B at JLab*



- **High resolution, large acceptance calorimeter**
- **Windowless H<sub>2</sub> gas flow target**
- **Simultaneous detection of elastic and Moller electrons**
- **GEM detectors**
- **Q<sup>2</sup> range of  $2 \times 10^{-4} - 0.14 \text{ GeV}^2$**

Future sub 1% measurements:  
(1) ep elastic scattering at Jlab (PRad)  
(2)  $\mu p$  elastic scattering at PSI - 16 U.S. institutions! (MUSE)  
(3) ISR experiments at Mainz

Ongoing H spectroscopy experiments

# Summary

- Electron Scattering to study Nucleon Structure
- Elastic: Form Factors
  - charge/current distributions
  - transverse density
  - $G_E^p$  @ large  $Q^2$  surprise  $\rightarrow$  shape of proton, 2- $\gamma$  effects
  - proton radius puzzle