



A theoretical study of

$$d^*(2380) \rightarrow d \pi \pi$$

Decay width

Yubing Dong (董宇兵)

Institute of High Energy physics (IHEP),
Chinese Academy of Sciences

Collaborators: Zongye Zhang (IHEP)
Pengnian Shen (IHEP)
Fei-Huang (UCAS)

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Contents

- 1 A Brief Introduction: Multi-quark states
Observation of $d^*(2380)$
- 2 One theoretical interpretation for the
resonance $d^*(2380)$ —Chiral quark model
- 3 Decay d^* to double pion and deuteron
- 4 Outlook and Summary

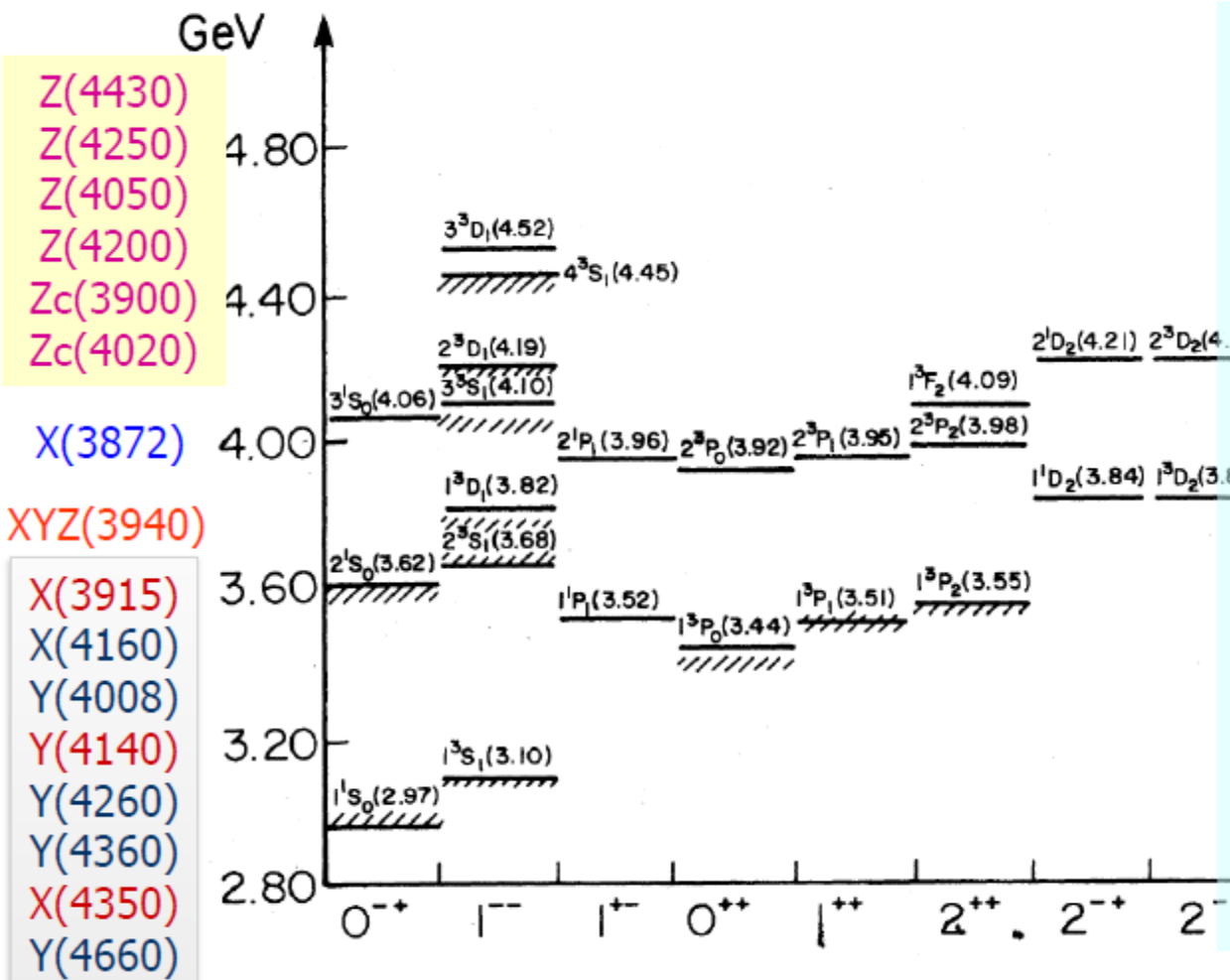
1, Introduction (Multiquark states)

The XYZ states

Four-quark

What are they ?

Potential models worked well for charmonium spectroscopy



Z(4430)
Z(4250)
Z(4050)
Z(4200)
Z_c(3900)
Z_c(4020)

X(3872)

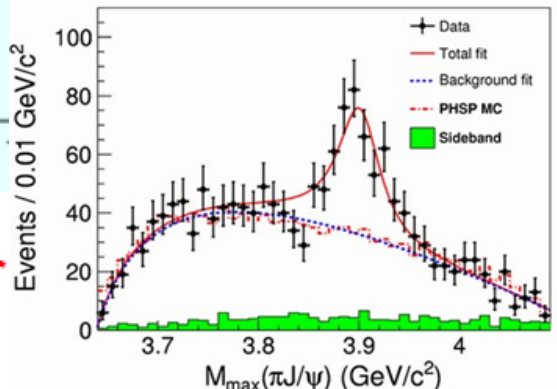
XYZ(3940)

X(3915)
X(4160)
Y(4008)
Y(4140)
Y(4260)
Y(4360)
X(4350)
Y(4660)

Courtesy of
2015/8/6
C. Z. Yuan

Not all XYZ states are char

BESIII, Belle and CLEO-c \rightarrow Z_c(3900)
 $M_{Z_c(3900)} = (3899 \pm 3.6 \pm 4) \text{ MeV}$
 $\Gamma_{Z_c(3900)} = (46 \pm 10 \pm 20) \text{ MeV}$



(New resonances, five-quark)

Observation of $J/\psi p$ resonances consistent with pentaquark states in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays

The LHCb collaboration

Abstract

Observations of exotic structures in the $J/\psi p$ channel, that we refer to as pentaquark-charmonium states, in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays are presented. The data sample corresponds to an integrated luminosity of 3 fb^{-1} acquired with the LHCb detector from 7 and 8 TeV pp collisions. An amplitude analysis is performed on the three-body final-state that reproduces the two-body mass and angular distributions. To obtain a satisfactory fit of the structures seen in the $J/\psi p$ mass spectrum, it is necessary to include two Breit-Wigner amplitudes that each describe a resonant state. The significance of each of these resonances is more than 9 standard deviations. One has a mass of $4380 \pm 8 \pm 29 \text{ MeV}$ and a width of $205 \pm 18 \pm 86 \text{ MeV}$, while the second is narrower, with a mass of $4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ and a width of $39 \pm 5 \pm 19 \text{ MeV}$. The preferred J^P assignments are of opposite parity, with one state having spin $3/2$



Five-quark

$\bar{D}\Sigma_c^*$, $\bar{D}^*\Sigma_c$, $\bar{D}^*\Sigma_c^*$ bound states

$3^- / 2, 5^+ / 2$

$P_c(4380), P_c'(4449)$

$\Lambda_c(2940)^+$

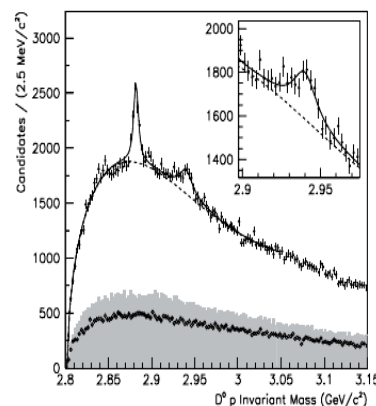
PRL 98, 012001 (2007)

PHYSICAL REVIEW LETTERS

week ending
5 JANUARY 2007

Observation of a Charmed Baryon Decaying to $D^0 p$ at a Mass Near $2.94 \text{ GeV}/c^2$

(BABAR Collaboration)



The results for the $\Lambda_c(2940)^+$ baryon are

$$m = [2939.8 \pm 1.3(\text{stat}) \pm 1.0(\text{syst})] \text{ MeV}/c^2,$$

$$\Gamma = [17.5 \pm 5.2(\text{stat}) \pm 5.9(\text{syst})] \text{ MeV}.$$

For the $\Lambda_c(2880)^+$ baryon the results are

$$m = [2881.9 \pm 0.1(\text{stat}) \pm 0.5(\text{syst})] \text{ MeV}/c^2,$$

$$\Gamma = [5.8 \pm 1.5(\text{stat}) \pm 1.1(\text{syst})] \text{ MeV}.$$

Potential models

Non relativistic QCD

Heavy quark effective theory

Heavy hadron chiral perturbation theory

QCD sum rule

Lattice calculations

- Molecule, baryonium
- tetraquark
- Hybrids
- Coupling channel...

$d^*(2380)$, six-quark

INTERNATIONAL JOURNAL OF HIGH-ENERGY PHYSICS

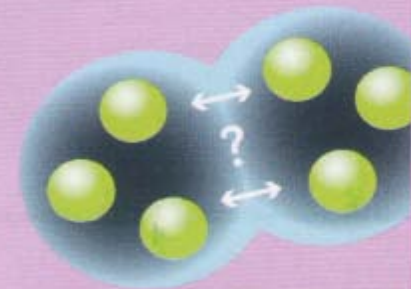
CERN COURIER

VOLUME 54 NUMBER 6 JULY/AUGUST 2014

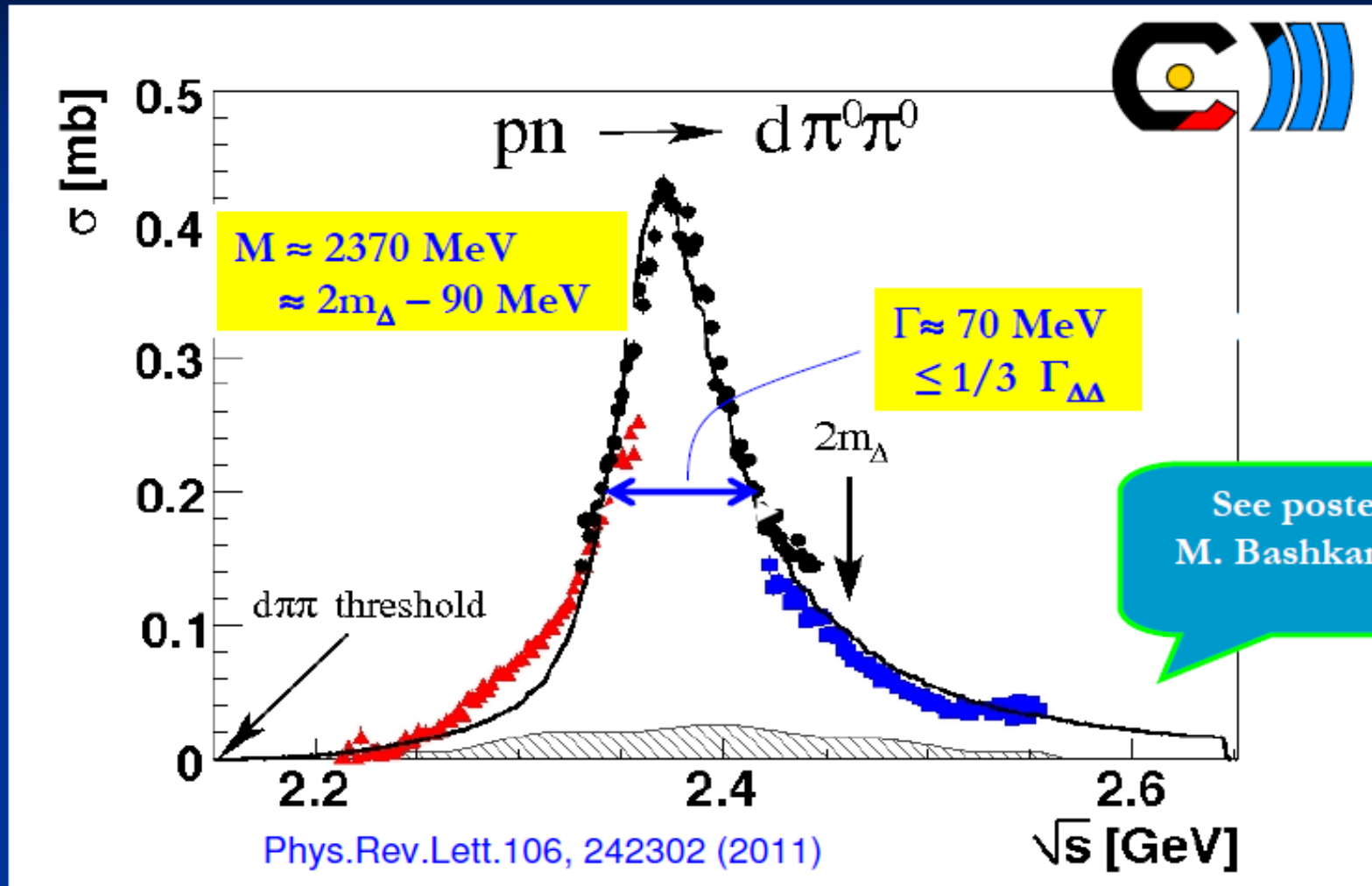
Experiments at the Jülich Cooler Synchrotron (COSY) have found compelling evidence for a new state in the two-baryon system, with a mass of 2380 MeV, width of 80 MeV and quantum numbers $I(J^P) = 0(3^+)$. The structure, containing six valence quarks, constitutes a dibaryon, and could be either an exotic compact particle or a hadronic molecule. The result answers the long-standing question of whether there are more eigenstates in the two-baryon system than just the deuteron ground-state. This fundamental question has been awaiting an answer since at least 1964, when first Freeman Dyson and later Robert Jaffe envisaged the possible existence of non-trivial six-quark configurations.

EXOTICS

COSY's new evidence for a six-quark state



The d^* Resonance $I(J^P) = 0(3^+)$



$$M_{\Delta\Delta} = 2464 \text{ MeV}$$

2015/8/6

$$M_{d^*} \approx 2380 \text{ MeV}$$

$$\Gamma_{d^*} \approx 70 \text{ MeV}$$

$$M_{\Delta N\pi} = 2310 \text{ MeV}$$

???

Properties of the $d^*(2380)$

■ Mass

$$M_{\Delta\Delta} = 2464 \text{ MeV}$$

$$M_{d^*} \approx 2380 \text{ MeV}$$

$$M_{\Delta N\pi} = 2310 \text{ MeV}$$

Far From threshold

$$\Delta E \sim 84 \text{ MeV}$$

$$\Delta E \sim 70 \text{ MeV}$$

■ Width

$$\Gamma_{\Delta} = 116 \sim 120 \text{ MeV}$$

$$\Gamma_{d^*} \approx 70 \text{ MeV (narrow)}$$

$$< \frac{1}{3} (\Gamma_{\Delta} + \Gamma_{\Delta})$$

■ Spin-parity

$$I (J^P) = 0 (3^+)$$

Quantum numbers

$$pn \rightarrow d\pi^0\pi^0$$

HADRON2015, Kunshan

2, Interpretations

- Many interpretations have been proposed
 - 1964 Dyson and Xiong: six non-strange states
 - J.J. de Swart --- Phys. Rev. D17(1978)260
 - M.Oka & K.Yazaki---PLB90(1980) 41
 - A.W. Thomas---J.Phys.G9(1983)1159
 - K.Maltman (Berkeley): Nucl.Phys.A438(1985)669
 - T.Goldman ... F. Wang Phys.Rev. C39(1989)1889
 - Zhang, and Shen et al., PRC60 (1999) 045203
 - **AFTERWARDS**
 - Bashkanov, Brodsky, and Clement: arguments (2013)
 - A. Gal et al. Nucl.Phys.A928(2014)73(Feddev+N+ Δ + π)
 - Kuklin—Russia (PRC87 (13) 025202: $d^*[d+\sigma(2\pi)]$)
 - +
- Predictions

Interpretation (argument)

Novel six-quark hidden-color dibaryon states in QCD

PLB727, 438 (2013)

M. Bashkanov^{a,*}, Stanley J. Brodsky^b, H. Clement^a

$$|\Psi_{d^*}\rangle = \sqrt{\frac{1}{5}}|\Delta\Delta\rangle + \sqrt{\frac{4}{5}}|6Q\rangle \quad \text{and}$$

$$|\Psi_{d^*}\rangle = \sqrt{\frac{4}{5}}|\Delta\Delta\rangle - \sqrt{\frac{1}{5}}|6Q\rangle.$$

Here $\Delta\Delta$ means the asymptotic $\Delta\Delta$ configuration and $6Q$ is the genuine “hidden color” six-quark configuration. The first solution denotes a S^6 quark structure (all six quarks in the S-shell), the second one a S^4P^2 configuration (4 quarks in the S-shell and 2 quarks in the P-shell). The quark structure with the large $\Delta\Delta$ coupling would correspond to a deltaron and can be excluded. Thus it is natural to assign the observed d^* resonance to the S^6 six-quark predominantly “hidden color” state, thus providing an explanation for its narrow decay width.

2, Chiral quark model

- X.Q.Yuan, Z.Y.Zhang ...P.N.Shen: Phys.Rev.C60(1999)045203

Hamiltonian of the system:

$$\mathbf{H} = \sum_i \mathbf{t}_i - \mathbf{T}_G + \sum_{i < j} \mathbf{V}_{ij} ,$$

$$\mathbf{V}_{ij} = \mathbf{V}_{ij}^{\text{conf}} + \mathbf{V}_{ij}^{\text{oge}} + \mathbf{V}_{ij}^{\text{ch}} + \mathbf{V}_{ij}^{\text{chv}}$$

$$\mathbf{V}_{ij}^{\text{ch}} = \sum_a (\mathbf{V}_{ij}^{\text{s(a)}} + \mathbf{V}_{ij}^{\text{ps(a)}}) .$$

$\Delta\Delta + CC$
channel

Results of the model

		SU(3)	Ext. SU(3) (f/g=0)	Ext. SU(3) (f/g=2/3)
Deuteron Binding energy(MeV)		2.09	2.24	2.20
Fraction of Wave Function (%)	NN (L=0)	93.68	94.66	94.71
	NN (L=2)	6.32	5.34	5.29

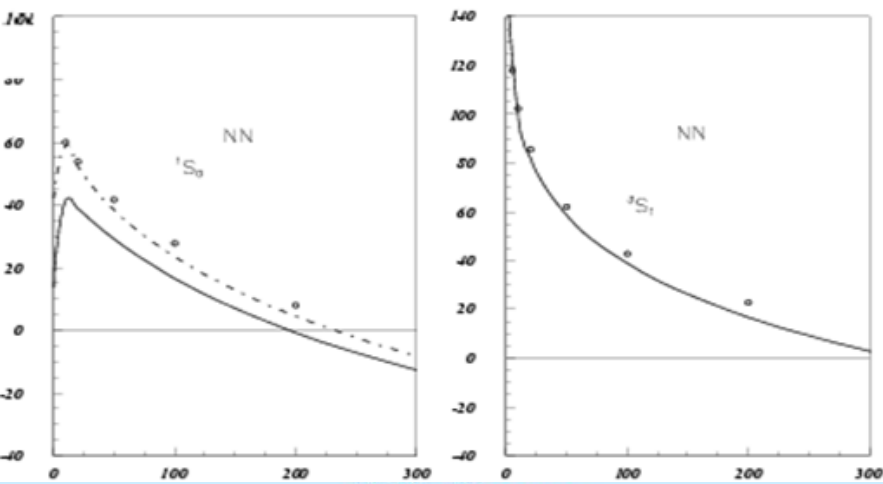
For deuteron

Results of the model

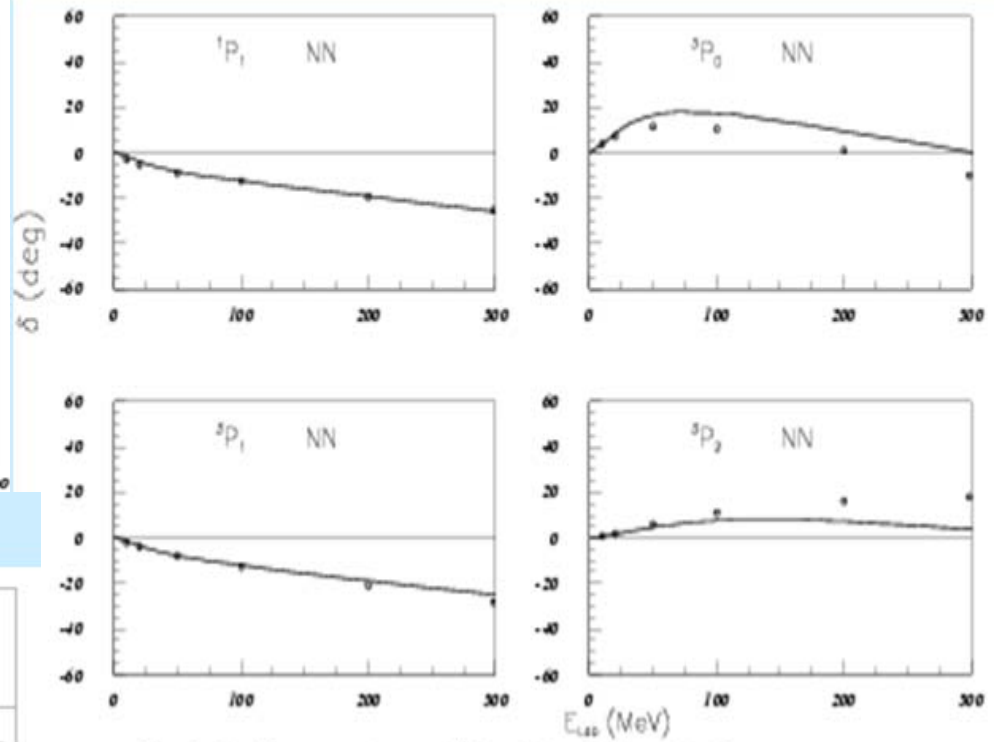
1S_0

3S_1

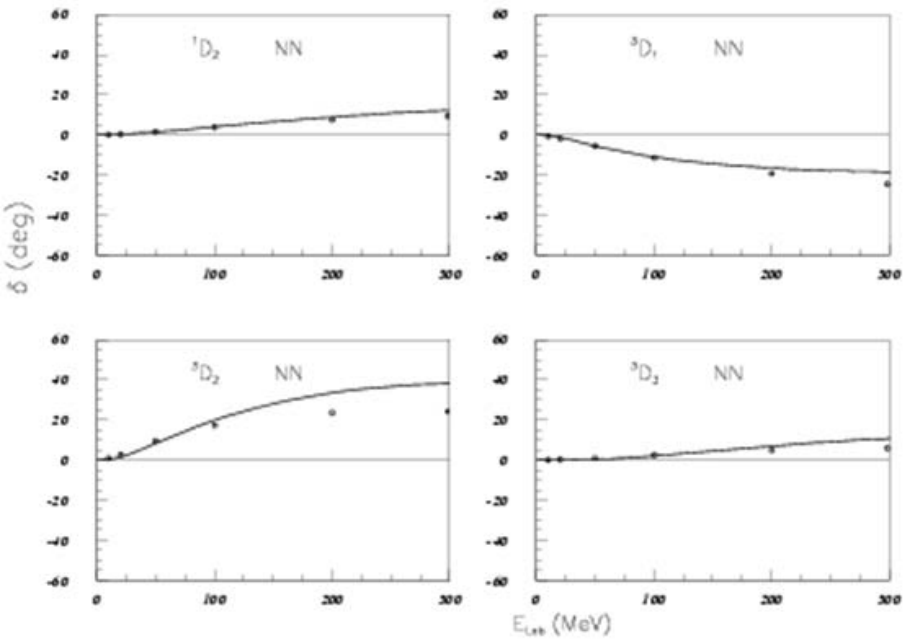
N-N P wave



N-N D wave



Phase-shift (N-N)



Results of the model (3)

TABLE III. Deltaron binding energy $B(\text{MeV})$ with different parameters. $B = -(E_{\text{deltaron}} - 2M_{\Delta})$.

	$(\Delta\Delta + CC)$		$(L=0+L=2)$	
$B(\text{OGE} + \pi, \sigma)$	79.7	97.1	97.9	113.4
$B[\text{OGE} + \text{SU}(3)]$	37.3	64.2	52.4	79.2
$b_N(\text{fm})$	0.505	0.60	0.505	0.60
$m_{\sigma}(\text{MeV})$	625	625	550	550

Phys.Rev.C60(1999)045203

$d^*(\Delta\Delta + CC (IS=03))$

→ $CC(2/3)$

New analysis

1505.05395

Appear on CPC

TABLE II. Binding energy, root-mean-square radius (RMS) of 6 quarks, and fraction of channel wave function for d^* in the chiral SU(3) quark model and extended chiral SU(3) quark model with ratios of tensor coupling to vector coupling $f/g=0$ and $f/g=2/3$ for vector meson fields.

	$\Delta\Delta (L=0,2)$			$\Delta\Delta - CC (L=0,2)$		
	SU(3)	Ext. SU(3) ($f/g=0$)	Ext. SU(3) ($f/g=2/3$)	SU(3)	Ext. SU(3) ($f/g=0$)	Ext. SU(3) ($f/g=2/3$)
Binding energy (MeV)	28.96	62.28	47.90	47.27	83.95	70.25
RMS of $6q$ (fm)	0.96	0.80	0.84	0.88	0.76	0.78
Fraction of $(\Delta\Delta)_{L=0}$ (%)	97.18	98.01	97.71	33.11	31.22	32.51
Fraction of $(\Delta\Delta)_{L=2}$ (%)	2.82	1.99	2.29	0.62	0.45	0.51
Fraction of $(CC)_{L=0}$ (%)				66.25	68.33	66.98
Fraction of $(CC)_{L=2}$ (%)				0.02	0.00	0.00

Wave function(1)

Pauli principle

$$\Psi_{6q} = (\mathbf{1}_{(1)} - \mathbf{9P}_{36(2)}) [\phi_{\Delta}\phi_{\Delta}\eta_{\Delta\Delta}(\mathbf{r})]_{\text{SIC}=30(00)} \\ + (\mathbf{1}_{(3)} - \mathbf{9P}_{36(4)}) [\phi_{C}\phi_{C}\eta_{CC}(\mathbf{r})]_{\text{SIC}=30(00)}$$

$$\chi_{\Delta\Delta}(\mathbf{r}) \equiv \langle \phi_{\Delta}(\xi_1, \xi_2) \phi_{\Delta}(\xi_4, \xi_5) | \Psi_{6q} \rangle ,$$

$$\chi_{CC}(\mathbf{r}) \equiv \langle \phi_{C}(\xi_1, \xi_2) \phi_{C}(\xi_4, \xi_5) | \Psi_{6q} \rangle ,$$

➔ Relative Wave functions

★ Quark's Degrees of freedom
are integrated out.
Equivalent to hadronization

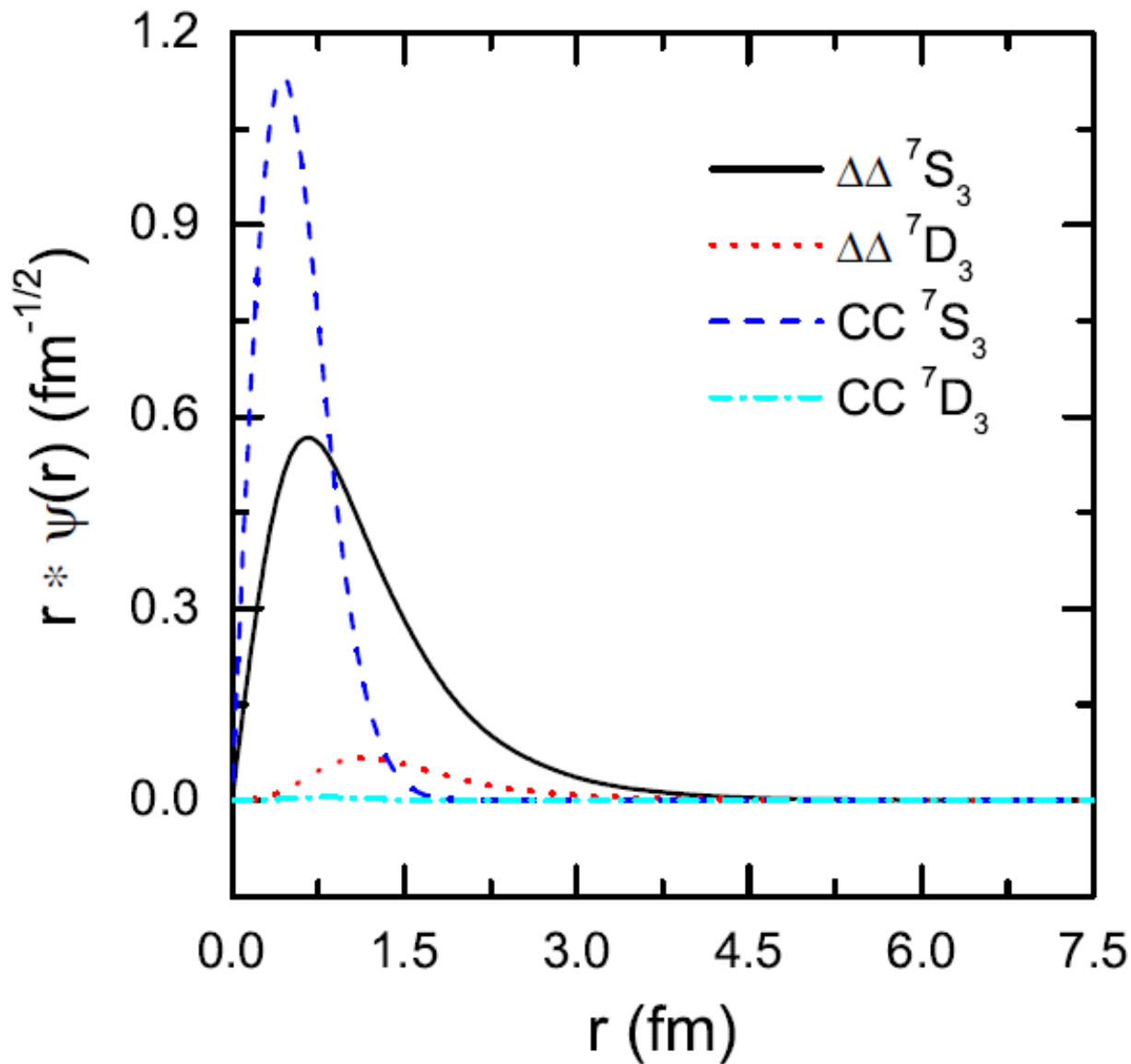
$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(\mathbf{r}) + |CC\rangle \chi_{CC}(\mathbf{r})$$

Two channels
Model space

Resonating group
method (RGM)

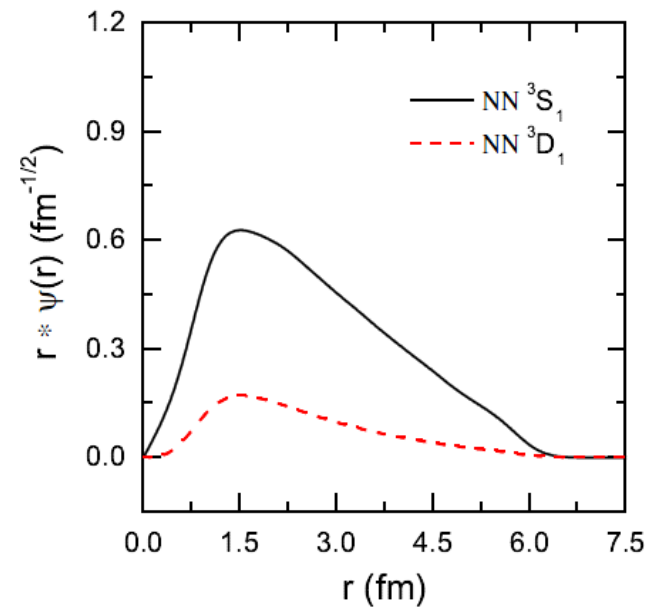
Orthogonal states
Anti-symmetrize
effect

d^* Wave function



D-wave is small,
and the system
looks compact

d^* :rms:(0.76~0.8)fm



(a) Deuteron

Deuteron, rms~2fm

3, Model calculation of

$$d^* \rightarrow d + \pi^0 + \pi^0$$

a, Quark model for $\Delta \rightarrow \pi + N$

Wave functions of Δ and N

$$|N\rangle = \frac{1}{\sqrt{2}}[\chi_\rho \psi_\rho + \chi_\lambda \psi_\lambda] \Phi_N(\vec{\rho}, \vec{\lambda}) \quad |\Delta\rangle = \chi_s \psi_s \Phi_\Delta(\vec{\rho}, \vec{\lambda})$$

Interaction of $qq\pi$

$$\mathcal{H}_{qq\pi} = g_{qq\pi} \vec{\sigma} \cdot \vec{k}_\pi \tau \cdot \phi \frac{1}{(2\pi)^{3/2} \sqrt{2\omega_\pi}},$$

$$M \rightarrow 3 \langle N\pi | \mathbf{H}_{qq\pi} | \Delta \rangle$$

$$\langle S_\alpha | \frac{\sigma_3}{2} | S_\beta \rangle = \frac{\sqrt{3}}{6} \begin{bmatrix} \sqrt{5} & 0 & -2 \\ 0 & 3 & 0 \\ 2\sqrt{2} & 0 & -1 \end{bmatrix},$$

$$\Gamma_{\Delta \rightarrow \pi N} = \frac{4}{3\pi} k_\pi^3 (g_{qq\pi} I_0)^2 \frac{\omega_N}{M_\Delta},$$

Simon Capstick, PRD46,2864

b, application of wave functions to

$$d^* \rightarrow d + \pi^0 + \pi^0$$

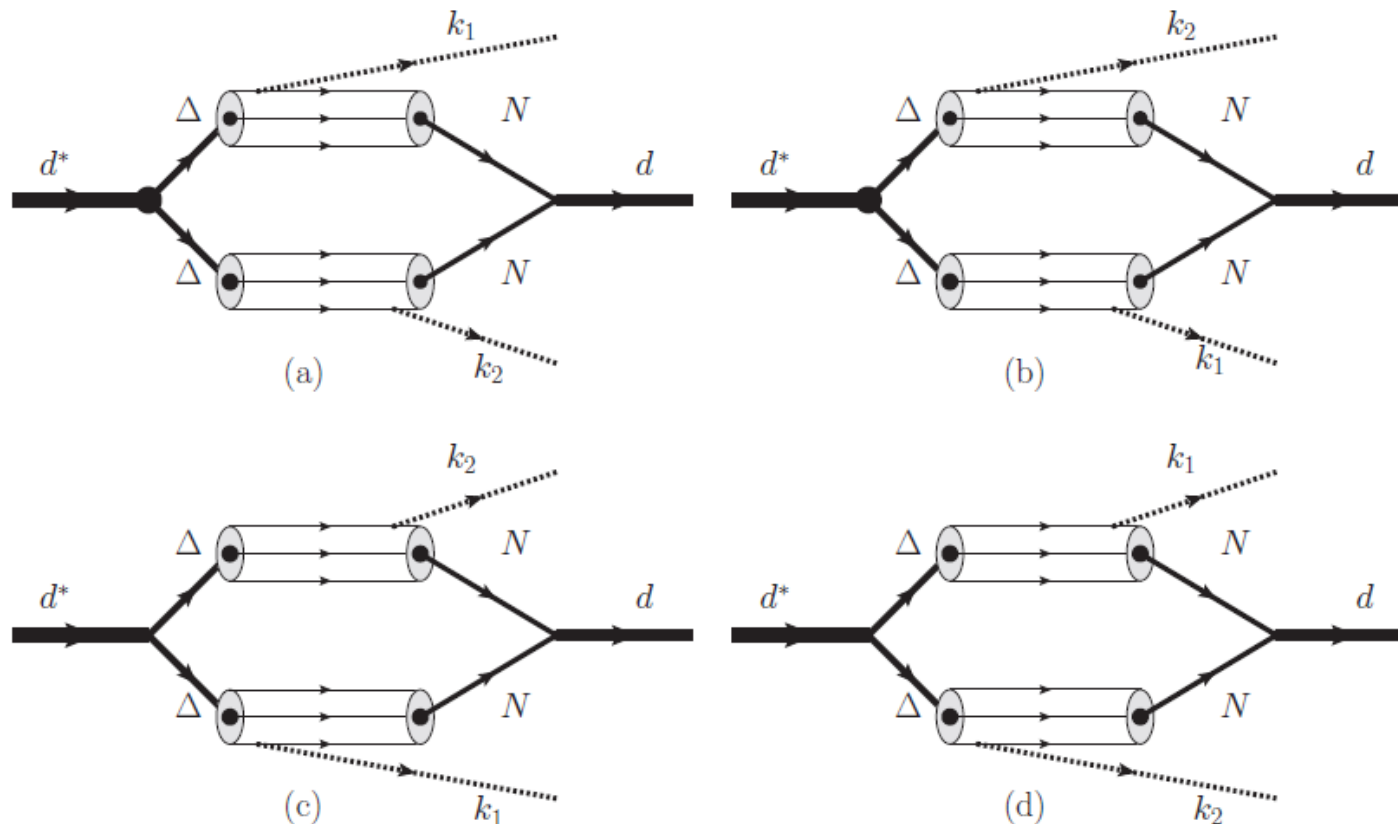


FIG. 1. Four possible emission paths in the decay of the d^* resonance composed of the $\Delta\Delta$ structure only. Two pions with momenta of \vec{k}_1 and \vec{k}_2 are emitted from one of the three quarks in two Δ s, respectively.

$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(\mathbf{r}) + |CC\rangle \chi_{CC}(\mathbf{r})$$

$$\begin{aligned}
\mathcal{M}_{if}^{\pi^0\pi^0} &\sim \int d^3q \left[\frac{\chi_d^*(\vec{q} - \frac{1}{2}\vec{k}_{12})}{E_\Delta(q) - E_N(q - k_1) - \omega_1} \right. \\
&\quad + \frac{\chi_d^*(\vec{q} + \frac{1}{2}\vec{k}_{12})}{E_\Delta(q) - E_N(q - k_2) - \omega_2} \\
&\quad + \frac{\chi_d^*(\vec{q} + \frac{1}{2}\vec{k}_{12})}{E_\Delta(-q) - E_N(-q - k_1) - \omega_1} \\
&\quad \left. + \frac{\chi_d^*(\vec{q} - \frac{1}{2}\vec{k}_{12})}{E_\Delta(-q) - E_N(-q - k_2) - \omega_2} \right] \chi_{d^*}(\vec{q})
\end{aligned}$$

$$\Gamma = \int \frac{1}{2!} d^3k_1 d^3k_2 d^3p_D 2\pi \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{p}_D) \delta(E_{k_1} + E_{k_2} + E_{p_D}^D - M_{d^*}) |\overline{\mathcal{M}}_{if}|^2$$

Constraint: the experimental data show that the angle between the two outgoing pions is almost zero, namely, the pions are propagating in the same direction

$$\longrightarrow \vec{k}_1 \parallel \vec{k}_2 \parallel \hat{z}$$

Wave functions (Model space ($\Delta\Delta$ +CC))

$$\Psi_d = \left[\phi_N(\xi_1, \xi_2) \phi_N(\xi_4, \xi_5) \chi_d(R) + \phi_C^d(\xi_1, \xi_2) \phi_C^d(\xi_4, \xi_5) \chi_{CC}^d(R) \right] \zeta_{(SI)=(10)},$$

$$d^* \quad \Delta\Delta \sim 1/3 \\ \quad \quad \quad CC \sim 2/3$$

$$\Psi_{d^*} = \left[\phi_\Delta(\xi_1, \xi_2) \phi_\Delta(\xi_4, \xi_5) \chi_{\Delta\Delta}(R) + \phi_C^{d^*}(\xi_1, \xi_2) \phi_C^{d^*}(\xi_4, \xi_5) \chi_{CC}^{d^*}(R) \right] \zeta_{(SI)=(30)},$$

$$\text{deuteron: } CC \sim 0$$

$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(r) + |CC\rangle \chi_{CC}(r)$$

Overlap of the two WFs also reduces spatial integral

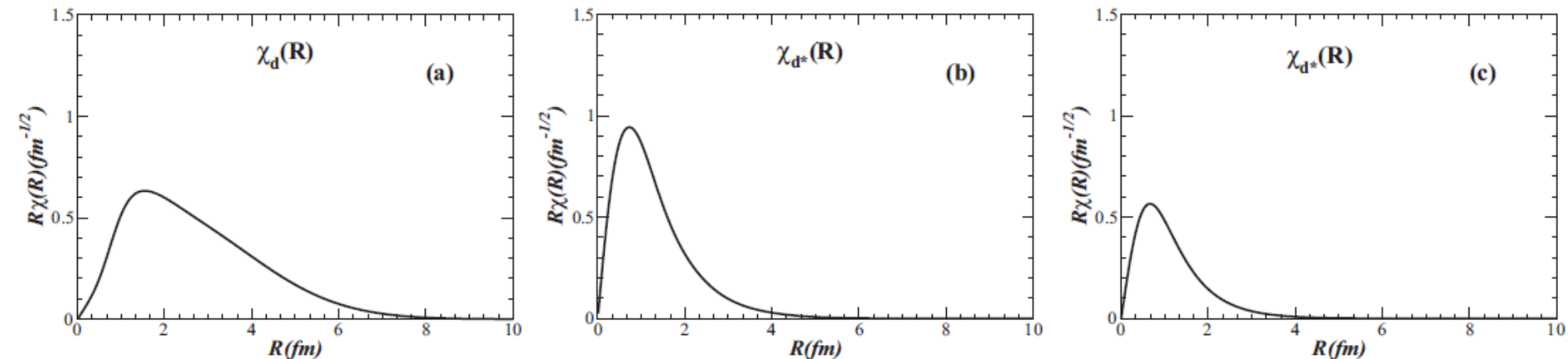


FIG. 2. Relative wave functions in the S wave in the extended chiral $SU(3)$ quark model: (a) for deuteron, (b) for $\chi_{\Delta\Delta}$ in the single $\Delta\Delta$ channel case for $d^*(2380)$, and (c) for $\chi_{\Delta\Delta}$ in the coupled $\Delta\Delta$ and CC channel case for $d^*(2380)$.

Numerical results

M_{d^*} (MeV)	Ours			Expt.	
Mode	Single channel $\Delta\Delta$ 2374	Two channels $\Delta\Delta + CC$ 2380		[4,20,21,23]	2375
	Γ (MeV)	B_r	Γ (MeV)	B_r	Γ (MeV)
$d^* \rightarrow d\pi^0\pi^0$	16.6	13.3%	9.2	14(1)%	10.2
$d^* \rightarrow d\pi^+\pi^-$	30.1	24.3%	16.8	23(2)%	16.7
$d^* \rightarrow pn\pi^0\pi^0$	14.1	11.3%	7.8	12(2)%	8.7
$d^* \rightarrow pn\pi^+\pi^-$	34.6	27.8%	19.2	30(4)%	21.8
$d^* \rightarrow pp\pi^0\pi^-$	7.06	5.65%	3.9	6(1)%	4.4
$d^* \rightarrow nn\pi^+\pi^0$	7.06	5.65%	3.9	6(1)%	4.4
$d^* \rightarrow pn$	8.24	12.0%	8.3	12(3)%	8.7
Total	117.7	99.9%	69.1	103(14)%	74.9

Two decay modes calculated

$d^* \rightarrow d\pi\pi$ (neutral)
 $d^* \rightarrow d\pi\pi$ (charged)

$\Delta E \sim 70$ MeV

The estimated decay widths of the two channel agree well with the data

* Unusual narrow width of $d^*(2380)$ is understood

* Binding energy of d^*

$$\Gamma_d \approx 70 \text{ MeV}$$

$$< \frac{1}{3} (\Gamma_\Delta + \Gamma_\Delta)$$

Discussions(1)

1, Contributions from $\Delta\Delta$ ($\sim 1/3$) component is considered

2, $(CC)_{00}$ ($\sim 2/3$): six-quark compact system does not involve in the decay process

3, Isospin breaking,
Due to the mass difference of charged and neutral pions.

$$\frac{\Gamma(d^* \rightarrow d\pi^+\pi^-)}{\Gamma(d^* \rightarrow d\pi^0\pi^0)} \sim 1.8$$

4, Single channel $\Delta\Delta$ widths larger than the data

5, Dynamical effect due to the wave function is obtained (few tens of MeV)

Discussion(2) other modes

$M_{d^*}(\text{MeV})$	Ours			Expt.	
	Single channel $\Delta\Delta$ 2374	Two channels $\Delta\Delta + \text{CC}$ 2380		[4,20,21,23] 2375	
Mode	$\Gamma(\text{MeV})$	\mathcal{B}_r	$\Gamma(\text{MeV})$	\mathcal{B}_r	$\Gamma(\text{MeV})$
$d^* \rightarrow d\pi^0\pi^0$	16.6	13.3%	9.2	14(1)%	10.2
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$d^* \rightarrow pp\pi^0\pi^-$	7.06	5.65%	3.9	6(1)%	4.4
$d^* \rightarrow nn\pi^+\pi^0$	7.06	5.65%	3.9	6(1)%	4.4
$d^* \rightarrow pn$	8.24	12.0%	8.3	12(3)%	8.7
Total	117.7	99.9%	69.1	103(14)%	74.9



are estimated according to the cross section ratios

Other modes

$$d^* \rightarrow d\pi^0\pi^0, \sigma \sim 0.27\text{mb}$$

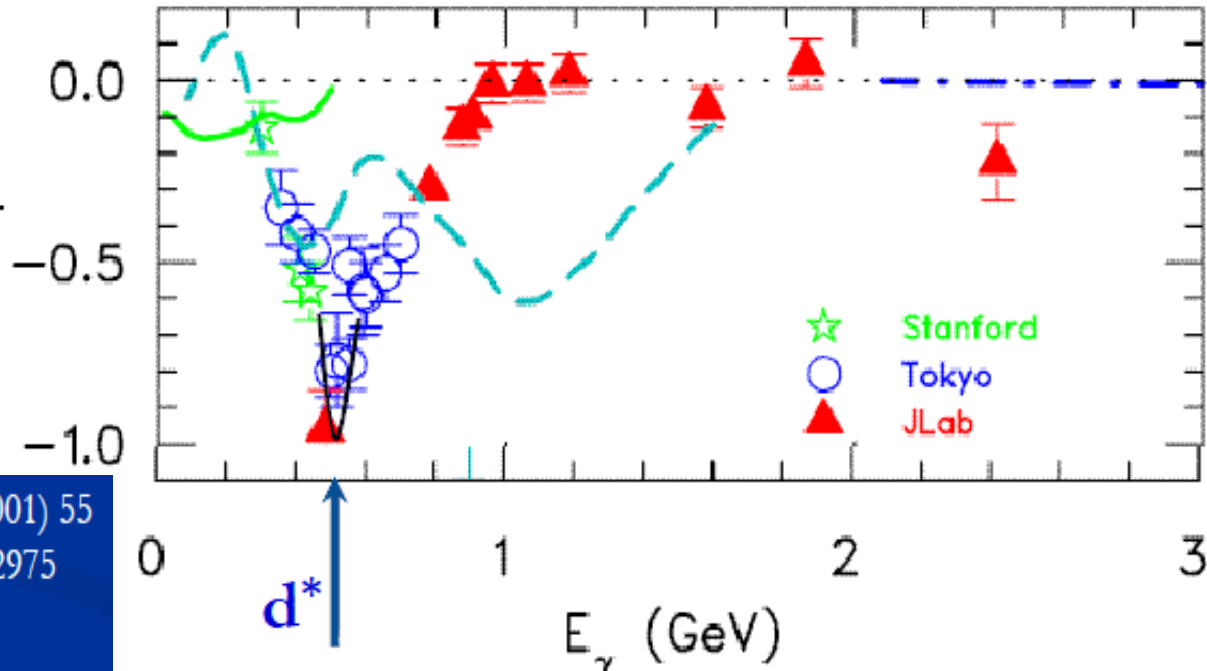
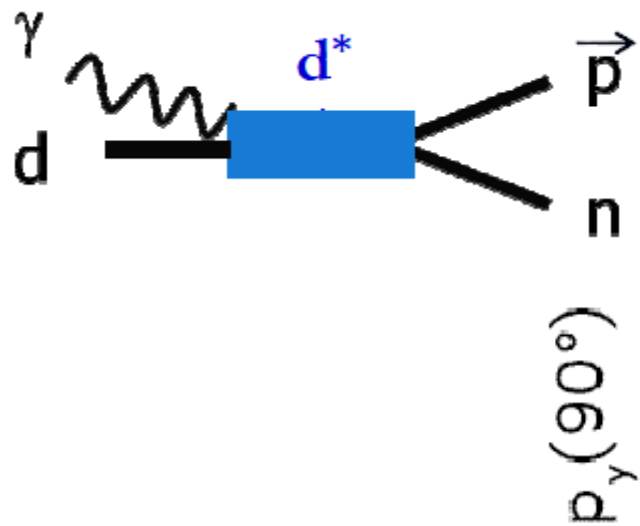
$$d^* \rightarrow np\pi^0\pi^0, \sigma \sim 0.27\text{mb}$$

$$d^* \rightarrow pp\pi^0\pi^-, \sigma \sim 0.10\text{mb}$$

Table 1: Experimental branching ratios of the d^* resonance into its decay channels based on eqs. (3) and (12) and the peak cross sections given under (i) and (ii).

decay channel	branching ratio	derived from
np	12(3) %	measurement, Ref. [8]
$d\pi^0\pi^0$	14(1) %	measurement, Ref. [3]
$d\pi^+\pi^-$	23(2) %	measurement, Ref. [3]
$pn\pi^+\pi^-$	30(4) %	measurement, Ref. [6]
$pn\pi^0\pi^0$	12(2) %	measurement, Ref. [5]
$pp\pi^0\pi^-$	6(1) %	measurement, Ref. [4]
$nn\pi^+\pi^0$	6(1) %	isospin symmetry
$(NN\pi)_{I=0}$	0(14) %	estimate, see text

4.1, Outlook



R. Gilman and F. Gross AIP Conf. Proc. 603 (2001) 55
K. Wijesooriya et al., Phys. Rev. Lett. 86 (2001) 2975

T. Kamae, T. Fujita Phys. Rev. Lett. 38 (1977) 471

H. Ikeda et al., Phys. Rev. Lett. 42 (1979) 1321

Possible in
Jefferson Lab and Mainz

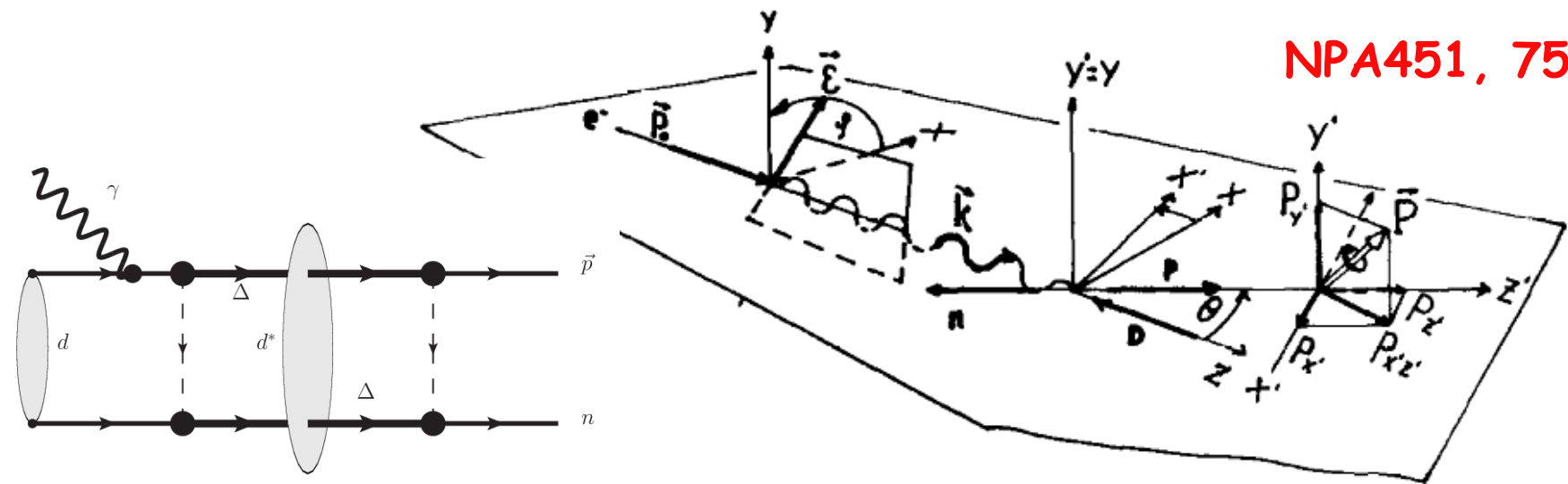


Fig. 1. Coordinate system for the double-polarization experiment in $\gamma d \rightarrow pn$. \mathbf{P}_0 : initial electron momentum; $\boldsymbol{\varepsilon}$: photon linear polarization vector; \mathbf{k} : photon momentum; \mathbf{p} : proton polarization.

$$P_y = \frac{(d\sigma/d\Omega)^+ - (d\sigma/d\Omega)^-}{(d\sigma/d\Omega)^+ + (d\sigma/d\Omega)^-}$$

is the recoil-proton polarization with unpolarized photon and deuteron: $(d\sigma/d\Omega)^{+(-)}$ is the differential cross section for the reaction, where the proton spin is directed along (against) the vector $\mathbf{k} \times \mathbf{p}$;

$$F_{i\pm} = \langle \lambda_p, \lambda_n | T | \lambda_\gamma, \lambda_d \rangle$$

$$\left(\frac{d\sigma}{d\Omega} \right)_0 = \frac{\alpha}{192\pi E^2} \frac{p}{\omega} f(\theta),$$

$$\begin{aligned}
 F_{1\pm} &= \langle \pm \frac{1}{2}, \pm \frac{1}{2} | T | 1, 1 \rangle, & F_{2\pm} &= \langle \pm \frac{1}{2}, \pm \frac{1}{2} | T | 1, 0 \rangle, & f(\theta) &= \sum_{i=1}^6 [|F_{i+}|^2 + |F_{i-}|^2] \equiv \sum_{i=1}^6 \sum_{\pm} |F_{i\pm}|^2, \\
 F_{3\pm} &= \langle \pm \frac{1}{2}, \pm \frac{1}{2} | T | 1, -1 \rangle, & F_{4\pm} &= \langle \pm \frac{1}{2}, \mp \frac{1}{2} | T | 1, 1 \rangle, \\
 F_{5\pm} &= \langle \pm \frac{1}{2}, \mp \frac{1}{2} | T | 1, 0 \rangle, & F_{6\pm} &= \langle \pm \frac{1}{2}, \mp \frac{1}{2} | T | 1, -1 \rangle, & P_y &= 2 \operatorname{Im} \sum_{i=1}^3 \sum_{\pm} \pm F_{i\pm}^* F_{(i+3)\mp} / f(\theta),
 \end{aligned}$$

4.2, Summary(1)

- 1, Interpretation of $d^*(2380)$ in our chiral quark-model
- 3, Novel structure of CC component is explicitly shown
- 2, Decay widths of $d^* \rightarrow d+2\pi$ are successfully estimated (Dynamical effect)
 - * unusual narrow width is obtained
 - * the approach can simultaneously give the binding energy +widths of the system

4.2, Summary (2)

- 4, Future applications ($\gamma d \rightarrow \vec{p}n$, polarizations)
- 5, Other observations of the resonances at Jefferson, Mainz, and Belle.
- Thanks for your attention!