

THE G_2^p EXPERIMENT

A Measurement of Proton g_2 Structure Function
and the Longitudinal-Transverse Spin Polarizability

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On behalf of the g_2^p collaboration

Hadron 2013, Huangshan, China



g₂^P Collaboration

▪ Spokepeople

- Alexandre Camsonne (Jlab)
- Jian-Ping Chen (JLab)
- Don Crabb (UVA)
- Karl Slifer (UNH)

• Post Docs

- Kalyan Allada (Jlab)
- Elena Long (UNH)
- James Maxwell (UNH)
- Vince Sulkosky (MIT)
- Jixie Zhang (Jlab)

▪ PhD Student

- Toby Badman (UNH)
- Melissa Cummings (W&M)
- Chao Gu (UVa)
- Min Huang (Duke)
- Jie Liu (UVa)
- Pengjia Zhu (USTC)
- Ryan Zielinski (UNH)

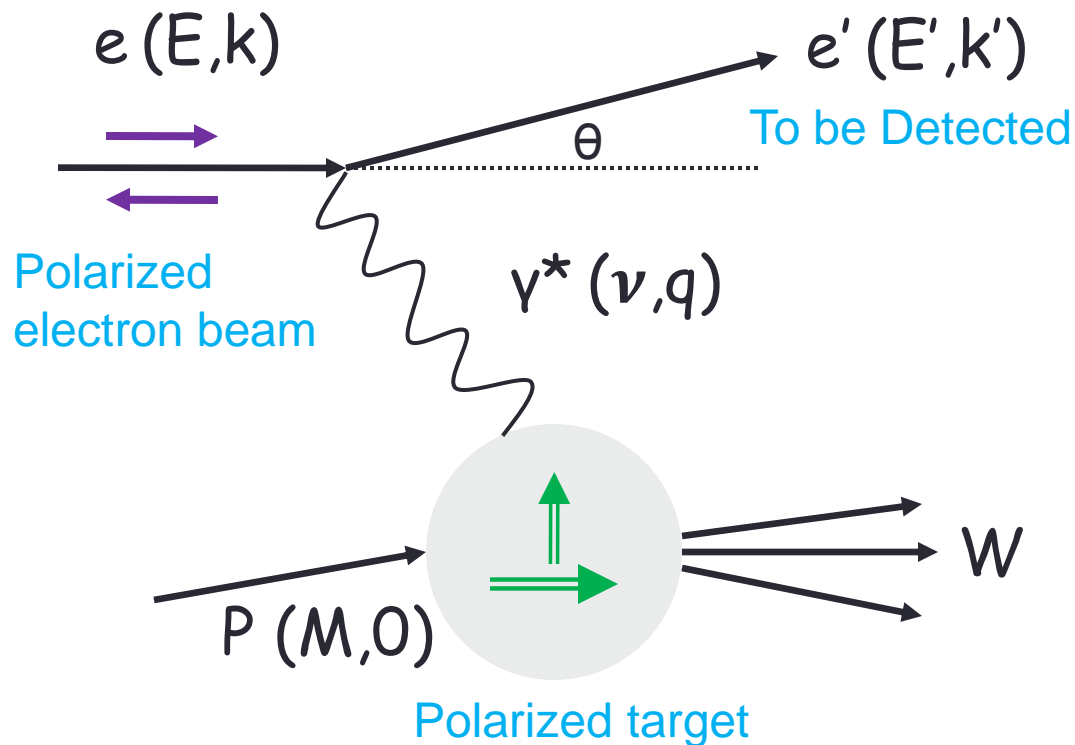
▪ Institutions

- 20 Institutions/Collaborators

Outline

- Introduction
- Physics Motivation
- Experiment Setup
- Kinematics and Projection
- Summary

Inclusive Electron Scattering

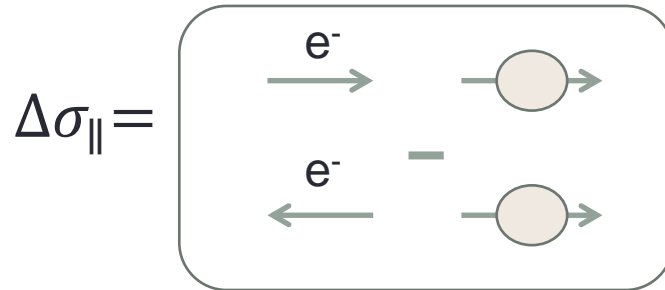


- Invariant Mass
 $W^2 = M^2 + 2M\nu - Q^2$
- Four momentum transfer squared
 $Q^2 = -q^2$
- Bjorken variable
 $x = Q^2/2M\nu$ fixed target

For point-like target

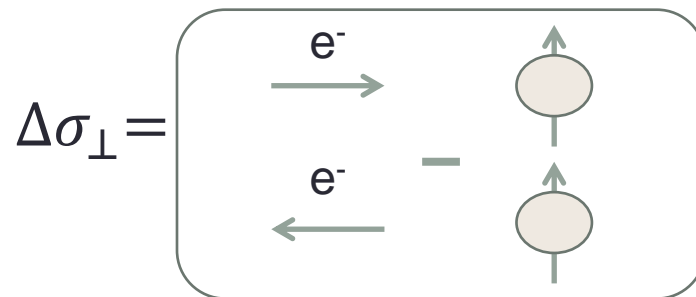
$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_{\text{Mott}} \left[\frac{1}{\nu} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2 \frac{\theta}{2} + \gamma g_1(x, Q^2) + \delta g_2(x, Q^2) \right]$$

g_1, g_2 : polarized nucleon spin structure functions

To get g_2^p 

Hall B EG4 measure g_1^p ,
 g_2^p experiment has one
 measurement to cross
 check

$$= \frac{4\alpha^2 E'}{M\nu Q^2 E} [(E + E' \cos\theta) g_1 - 2Mx g_2]$$



g_2^p experiment measure,
 g_2^p essential contribution to
 $\Delta\sigma_{\perp}$ in this kinematic region

$$= \frac{4\alpha^2 E'}{M\nu Q^2 E} \left[\sin\theta \left(g_1 + \frac{2E}{\nu} g_2 \right) \right]$$

Motivation

- Measure the proton spin structure function g_2 in the **low Q^2 region** ($0.02 < Q^2 < 0.2 \text{ GeV}^2$) for **the first time**
- Extract δ_{LT} to provide a benchmark test of χ PT calculations
- Opportunity to test the Burkhardt-Cottingham sum rule
- Crucial inputs for hydrogen hyperfine splitting and proton charge radius measurements

g_2 Structure Function

□ At high to intermediate Q^2

- g_2 can be separated into leading and higher-twist components

$$g_2(x, Q^2) = g_2^{ww}(x, Q^2) + \overline{g_2}(x, Q^2)$$

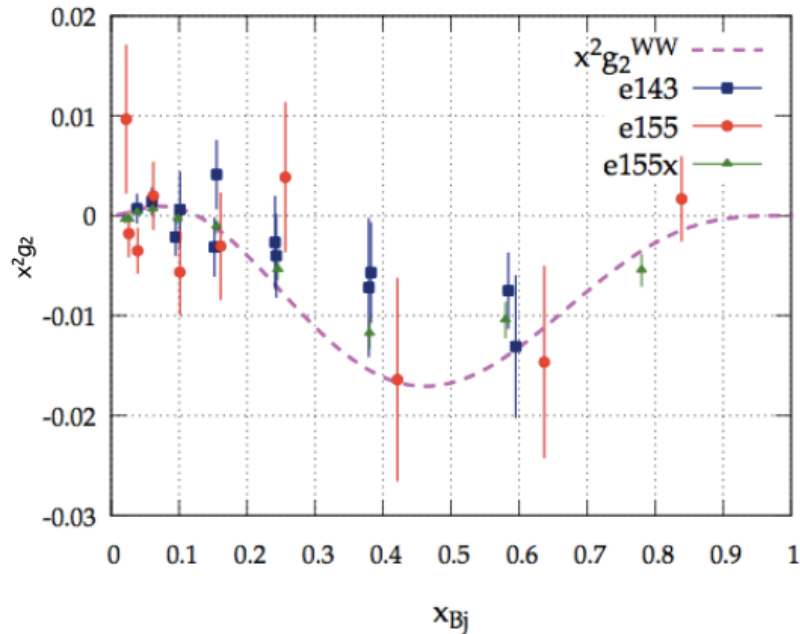
- g_2 leading twist related to g_1 by Wandzura-Wilczek relation

$$g_2^{ww}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 \frac{dy}{y} g_1(y, Q^2)$$

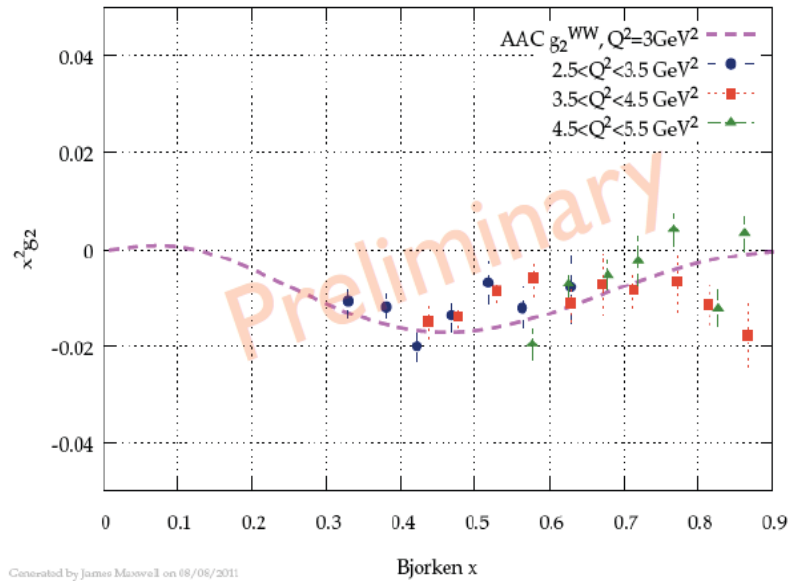
Good approximation as, $Q^2 \rightarrow \infty$

- g_2 exhibits strong deviations from this leading twist behavior at typical JLab kinematics
- $g_2 - g_2^{ww}$: a clean way to access **higher-twist contribution**, quantify **q-g** correlations.

g_2^p Existing Data

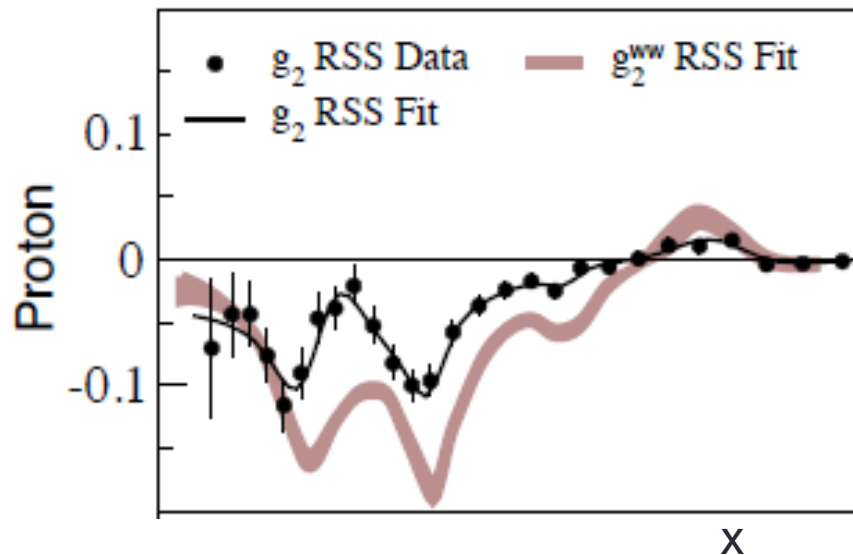


Proton g_2 Data from SLAC
 Averaged $Q^2 \approx 5 \text{ GeV}^2$



Proton g_2 Data from Jlab SANE
 $Q^2 \approx 2.5 - 5.5 \text{ GeV}^2$

g_2^p Existing Data



Proton g_2 Data from Jlab RSS
 $Q^2 = 1.3 \text{ GeV}^2$

K. Slifer O. Rondon et al.
 PRL, 105(2010)101601

Precision Measurement of $g_2^p(x, Q^2)$:
 Can search for higher twist effects

BC Sum Rule

- BC Sum Rule:

$$\int_0^1 g_2(x, Q^2) dx = 0$$

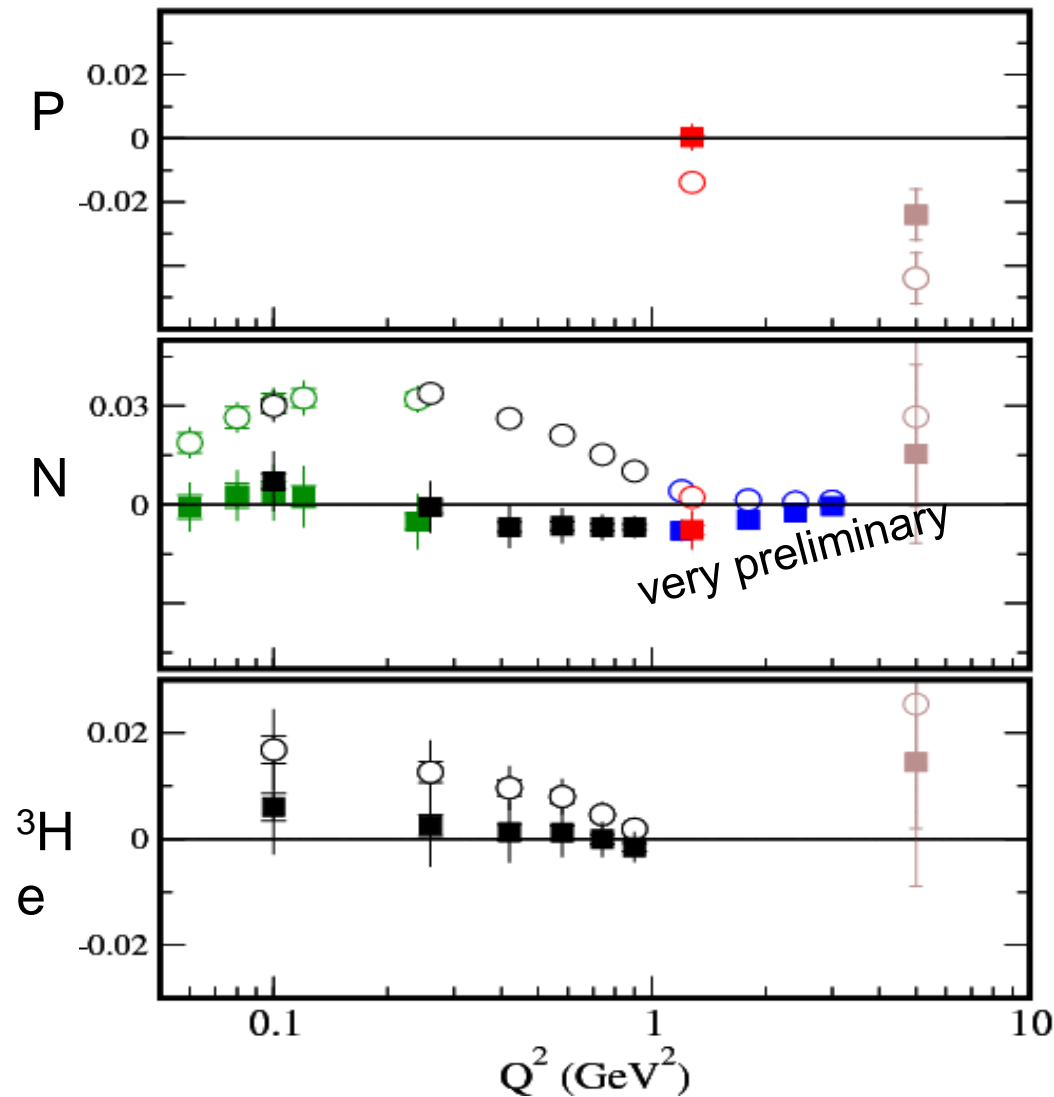
H. Burkhardt and W. N. Cottingham, *Annals. Phys.*, 56(1970)453

- BC Sum Rule will fail if g_2 :
 - exhibits non-Regge behavior at low x
 - exhibits a delta function at $x=0$

R. L. Jaffe and X.-D. Ji, *Phys. Rev. D*, 43(1991)724

- Experiment test:
 - BC = Measured +low_x+Elastic

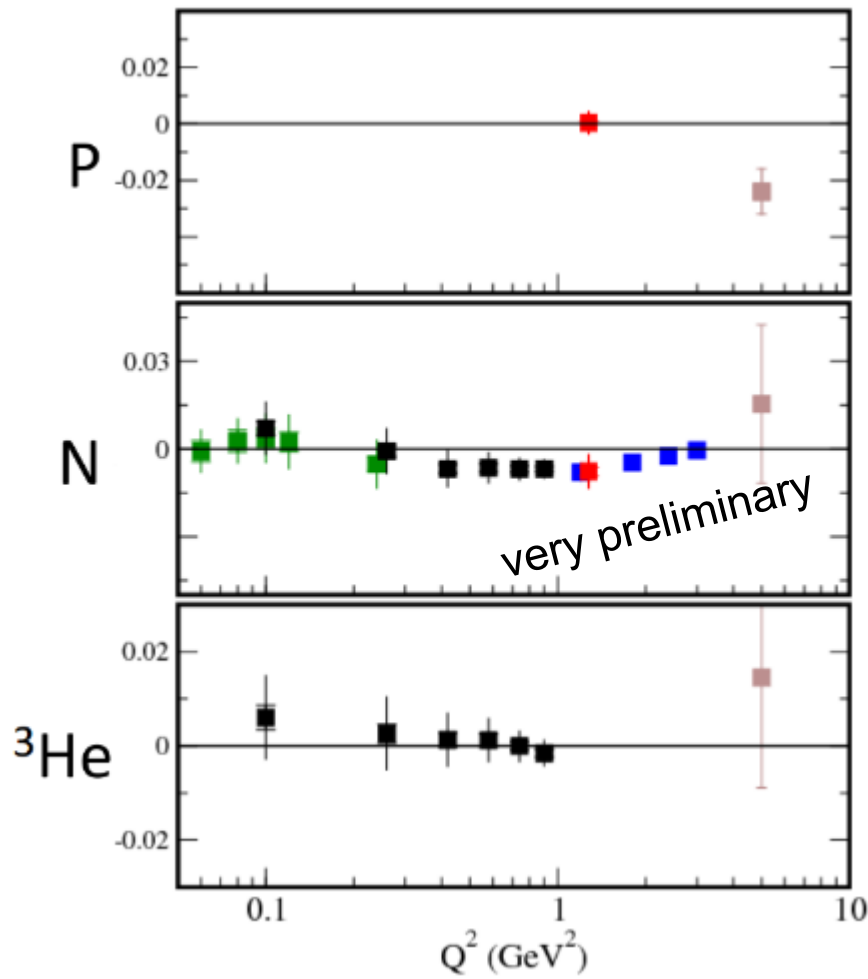
BC Sum Rule



- SLAC E155x
- Hall C RSS
- Hall A E94-010
- Hall A E97-110 (preliminary)
- Hall A E01-012 (preliminary)

- Open symbols: measured
- Full symbols: include unmeasured estimation
- low_x: unmeasured, assume Leading Twist behavior
- Elastic: From well known form factors (<5%)

BC Sum Rule



$$\int_0^1 g_2(x, Q^2) dx = 0$$

- Violation suggested for proton at large Q^2
- Found within error for ³He
- Within error for neutron, but barely in vicinity of $Q^2 \approx 1 \text{ GeV}^2$
- Mostly unmeasured for proton

Generalized Spin Polarizabilities

- Generalized Spin Polarizabilities:
how nucleons respond to virtual photons
- Relate to doubly-virtual Compton scattering, with assumption:
appropriate convergence and unsubtracted dispersion relation

- Generalized forward spin polarizability $\gamma_0(Q^2)$

$$\gamma_0(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} dx x^2 \left[g_1(x, Q^2) - \frac{4M^2 x^2}{Q^2} g_2(x, Q^2) \right]$$

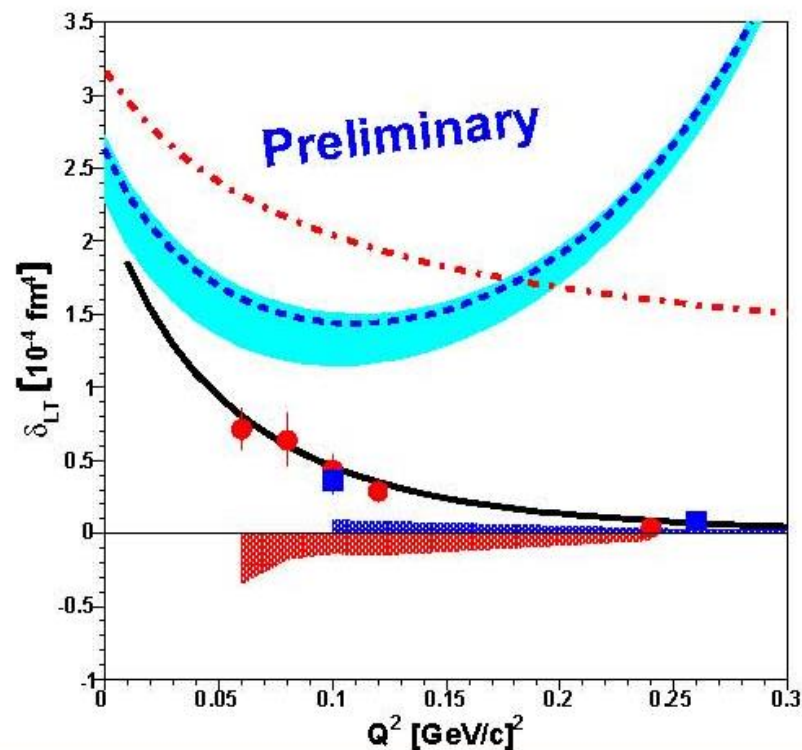
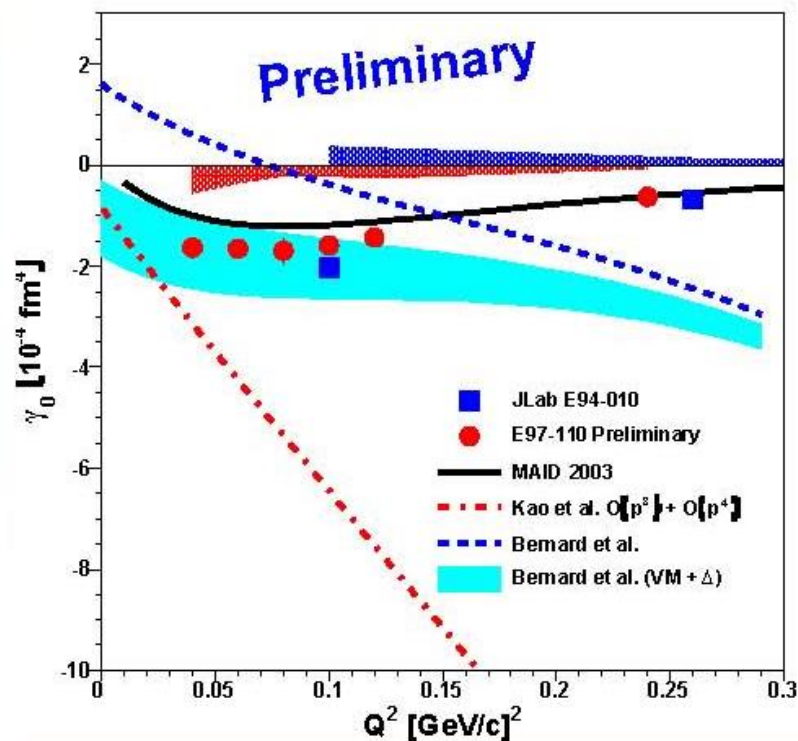
- Generalized longitudinal-transverse spin polarizability $\delta_{LT}(Q^2)$

$$\delta_{LT}(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} dx x^2 \left[g_1(x, Q^2) + g_2(x, Q^2) \right]$$

- Can be calculated via Chiral Perturbation Theory

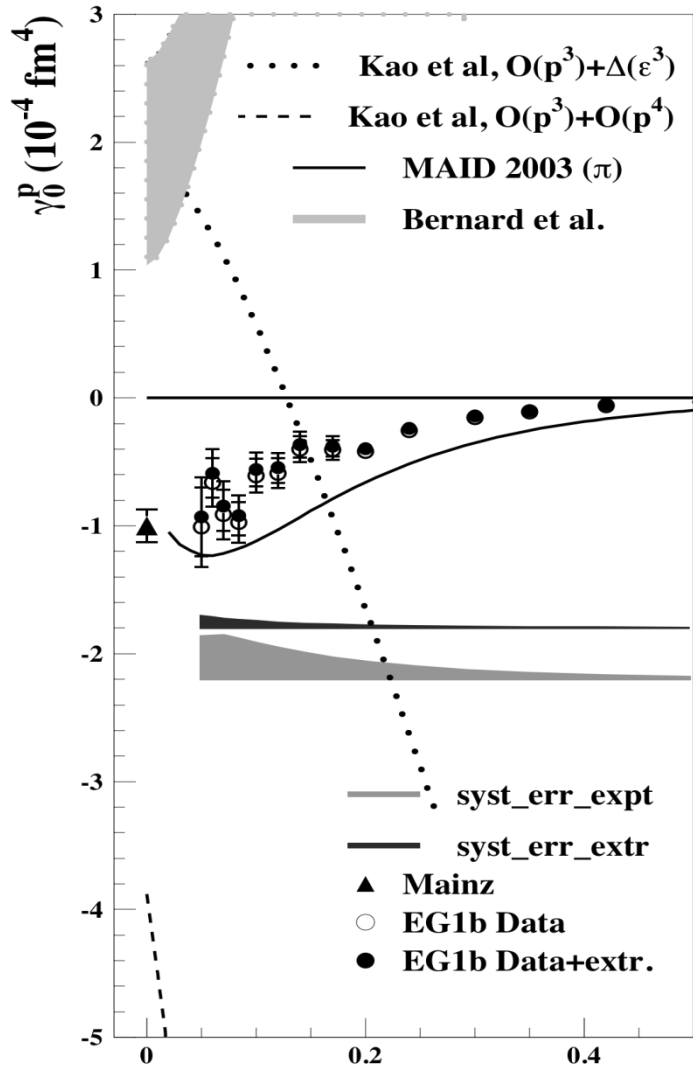
δ_{LT} Puzzle for Neutron

- δ_{LT} is **insensitive** to Δ resonance, more suitable than γ_0 to test χ PT
- **Significant disagreement** between data and both χ PT calculations for δ_{LT}
- Good agreement with MAID model predictions



Plots courtesy of V. Sulkosky : Preliminary E97-110 and Published E94-010

Proton Spin Polarizabilities

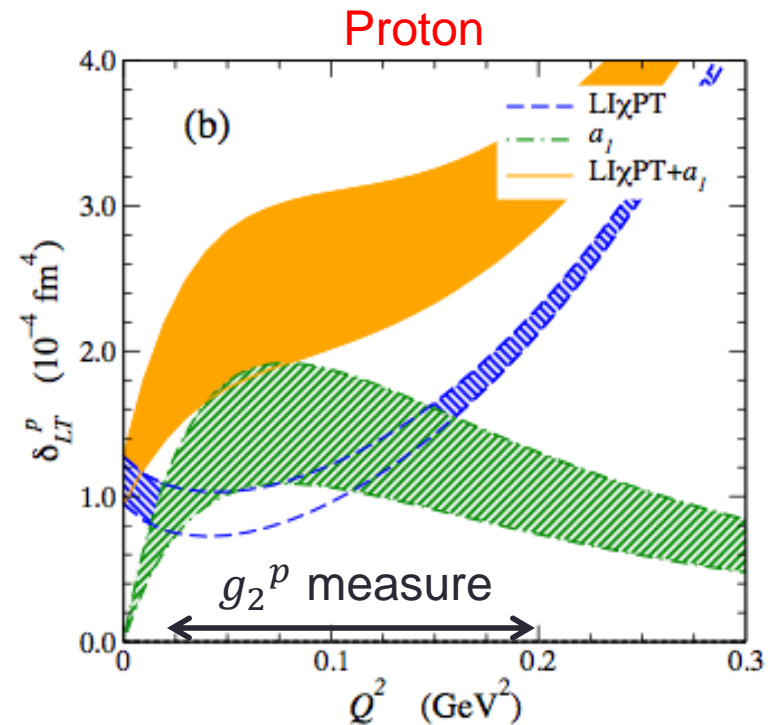
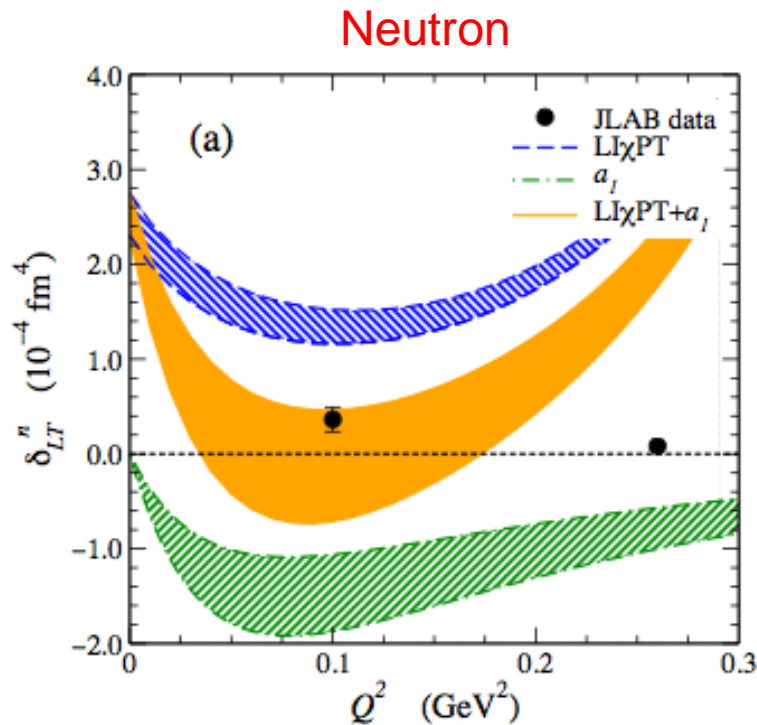


- χ^{PT} calculations still fails for proton γ_0
- γ_0 sensitive to resonance
- No data yet on proton δ_{LT} polarizability
- This experiment will provide proton δ_{LT} data

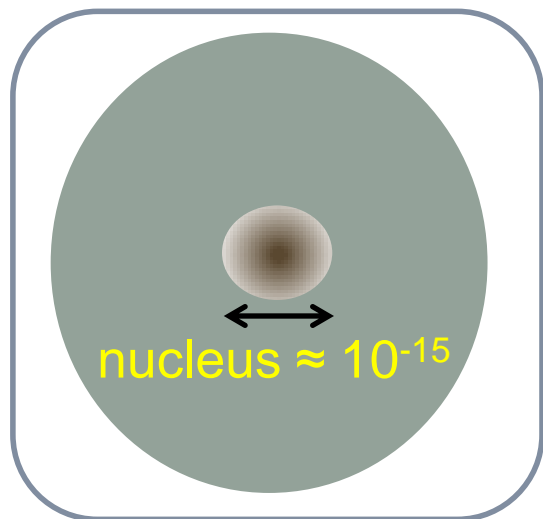
PLB672, 12 (2009)

δ_{LT} Puzzle

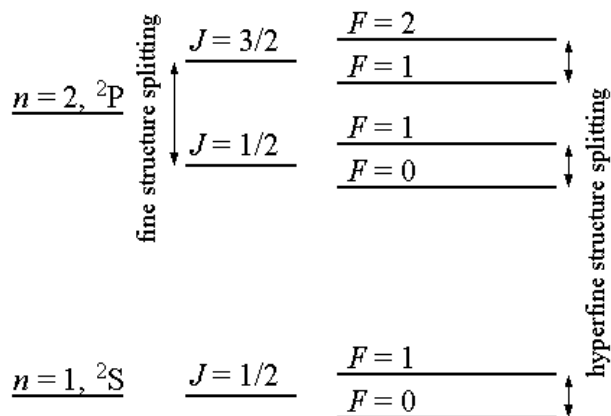
- **New calculation result:** Kochelev & Oh. arXiv:1103.4892
- Include the axial-anomaly $a_1(1260)$ meson contribution
- Improves agreement with neutron
- Need data on proton δ_{LT} polarizability



Hydrogen Hyperfine Structure



$I = 1/2$



- Hydrogen hyperfine splitting in the ground state has been measured to a relative high accuracy of 10^{-13}

$$\begin{aligned} \Delta E &= 1420.405\,751\,766\,7(9) \text{ MHz} \\ &= (1 + \delta)E_F \end{aligned}$$

$$\delta = (\delta_{QED} + \delta_R + \delta_{small}) + \Delta_S$$

- Δ_S : proton structure function correction
 - depends on ground state and excited properties of the proton
 - largest uncertainty

Hydrogen Hyperfine Structure

$$\Delta_S = \Delta_Z + \Delta_{pol}$$

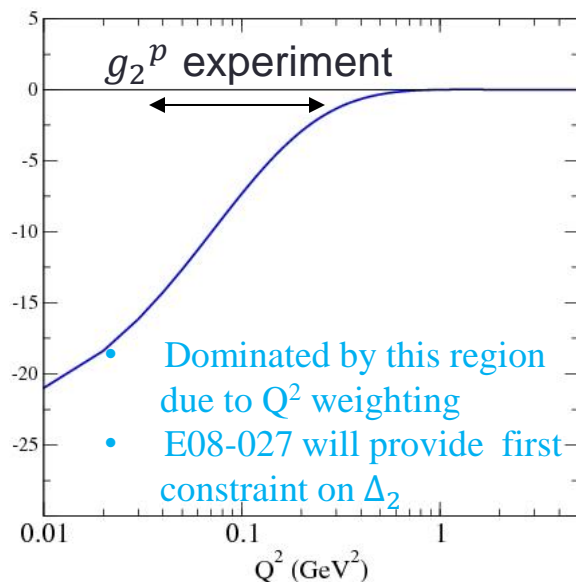
Elastic Scattering

$$D_Z = -41.0 \pm 0.5 \text{ ppm}$$

involves contributions $\Delta_{pol} \approx 1.3 \pm 0.3 \text{ ppm}$
where the proton is excited

$$\Delta_{pol} = \frac{\alpha m_e}{\pi g_p m_p} [\Delta_1 + \Delta_2]$$

Integrand of Δ_2



Δ_1 : involves Pauli form factor and the g_1 structure function

Δ_2 : depends on g_2 structure function

$$\Delta_2 = -24 m_p^2 \int_0^\infty \frac{dQ^2}{Q^4} [B_2(Q^2)]$$

$$B_2(Q^2) = \int_0^{x_{th}} dx \beta_2(\tau) g_2(x, Q^2)$$

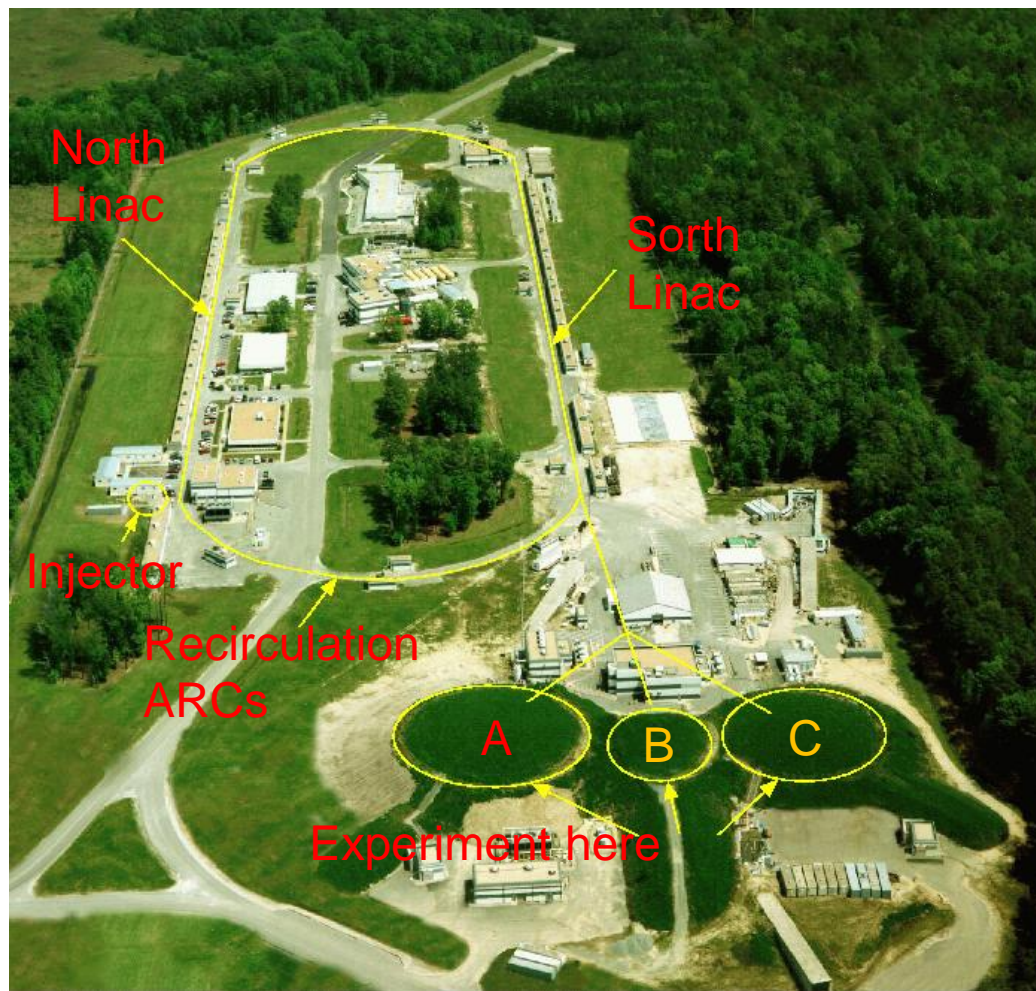
$$\beta_2(\tau) = 1 + 2\tau - 2\sqrt{\tau(\tau + 1)}$$

Proton Radius Puzzle

- Two ways to measure:
- Atomic physics:
 - energy splitting of the $2S_{1/2} - 2P_{1/2}$ level (Lamb shift)
 - The result from Lamb shift in muonic hydrogen is much more precise
[R. Pohl et.al., Nature, July 20102](#)
- Nuclear Physics:
 - $\frac{dG_{E(M)}(Q^2)}{Q^2}$ defines radius at $Q^2 = 0$
- Not agree with each other, around $\sim 6\%$
- Main uncertainties originates from the proton polarizability and different values of the Zemach radius

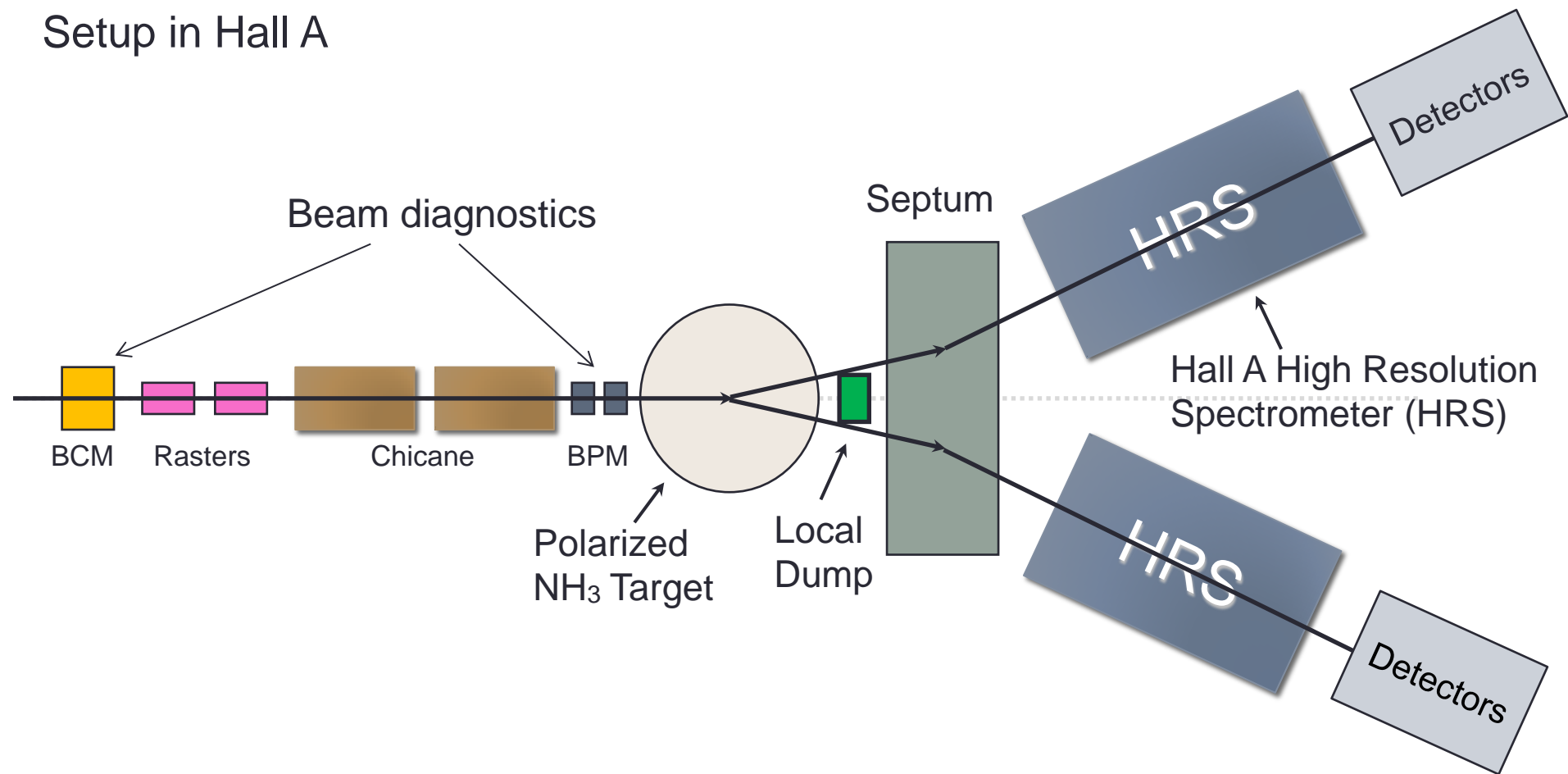
Experiment Setup

- g_2^p experiment took data in Jefferson Lab Hall A from Feb 29th to May 18th 2012



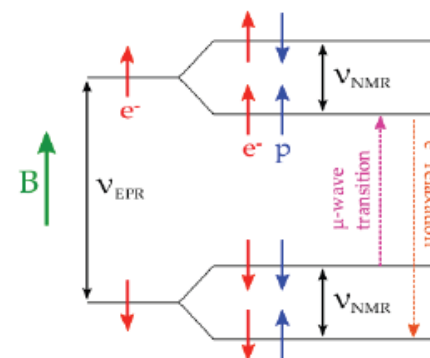
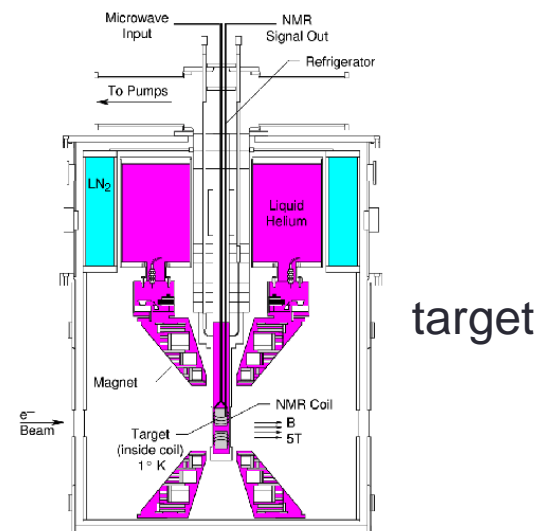
Experiment Setup

Setup in Hall A



Experiment Setup

- Polarized NH_3 target (2.5T/5T)
 - Upstream chicane: to provide a incident angle beam,
 - Downstream local dump: some energy/target settings, beam cannot go into hall dump, to be deposited in local dump directly
- Low current polarized beam
 - Upgrades existing beam diagnostics to work at 50 nA
- Lowest possible Q^2 in the resonance region
 - Use septum magnets to bend the small scattering angle electrons, to access a lower Q^2
 - Detector package has a minimum angle limit at 12.5°

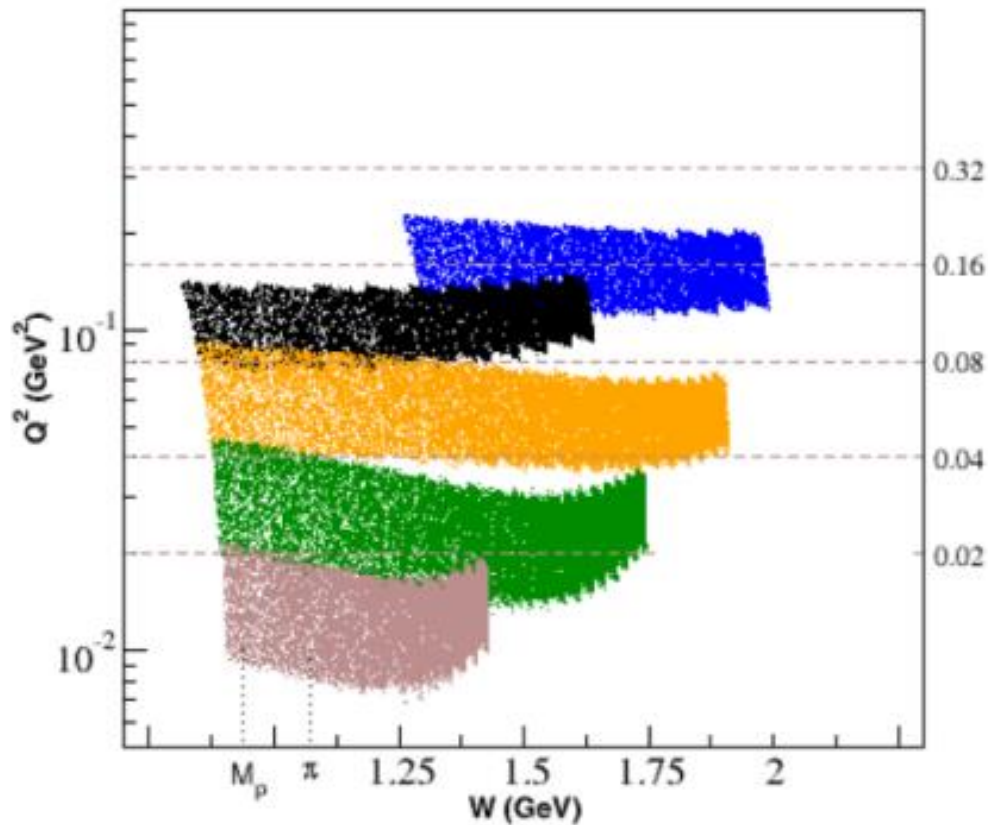


Dynamic nuclear polarization

Kinematics Coverage

$$0.02 < Q^2 < 0.2 \text{ GeV}^2$$

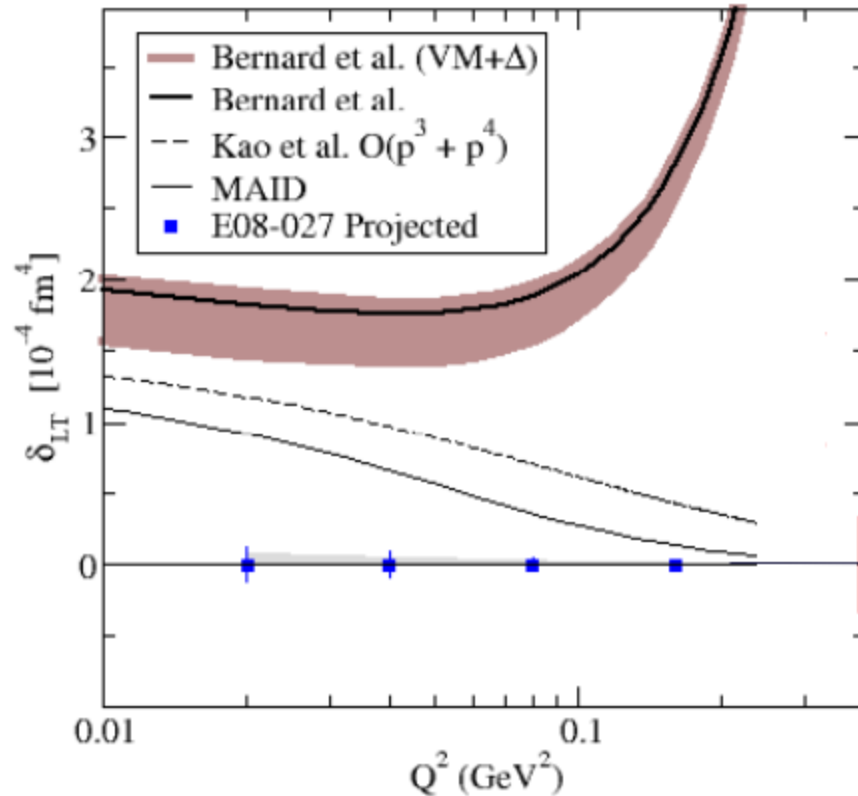
$$M_p < W < 2 \text{ GeV}$$



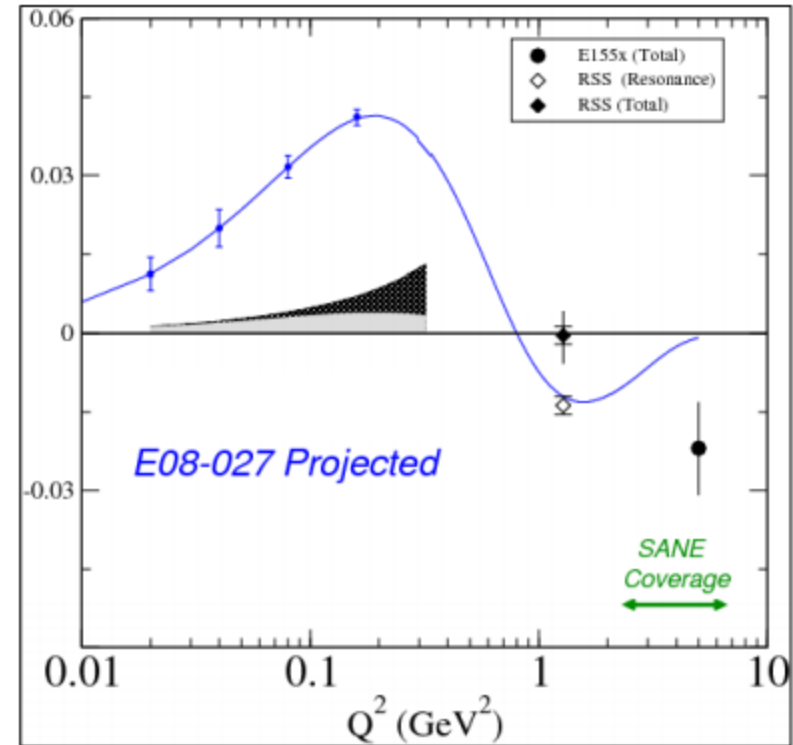
Beam Energy /GeV	Target Field /T
2.254	2.5
1.706	2.5
1.158	2.5
2.254	5.0
3.352	5.0

Kinematics and Projection

LT Spin Polarizability



BC Sum Integral Γ_2

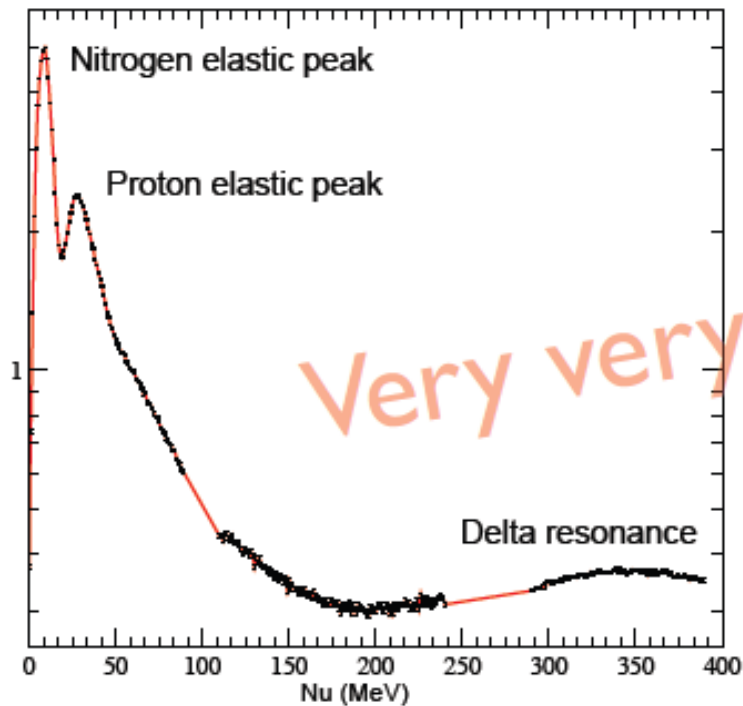


$$\delta_{LT}(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} dx x^2 [g_1(x, Q^2) + g_2(x, Q^2)]$$

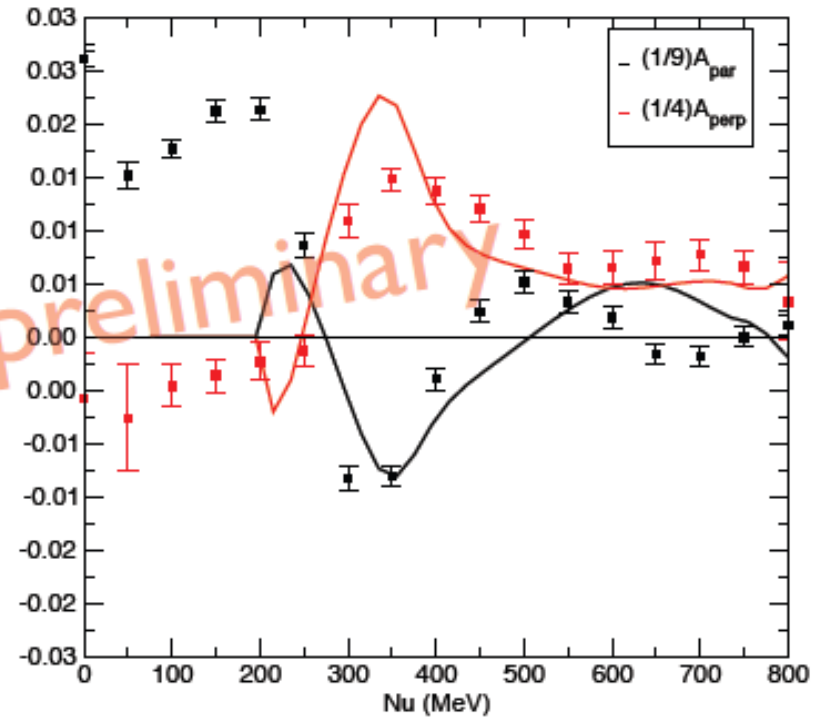
$$\int_0^1 g_2(x, Q^2) dx = 0$$

Online Results

E=2254MeV Normalized Yield

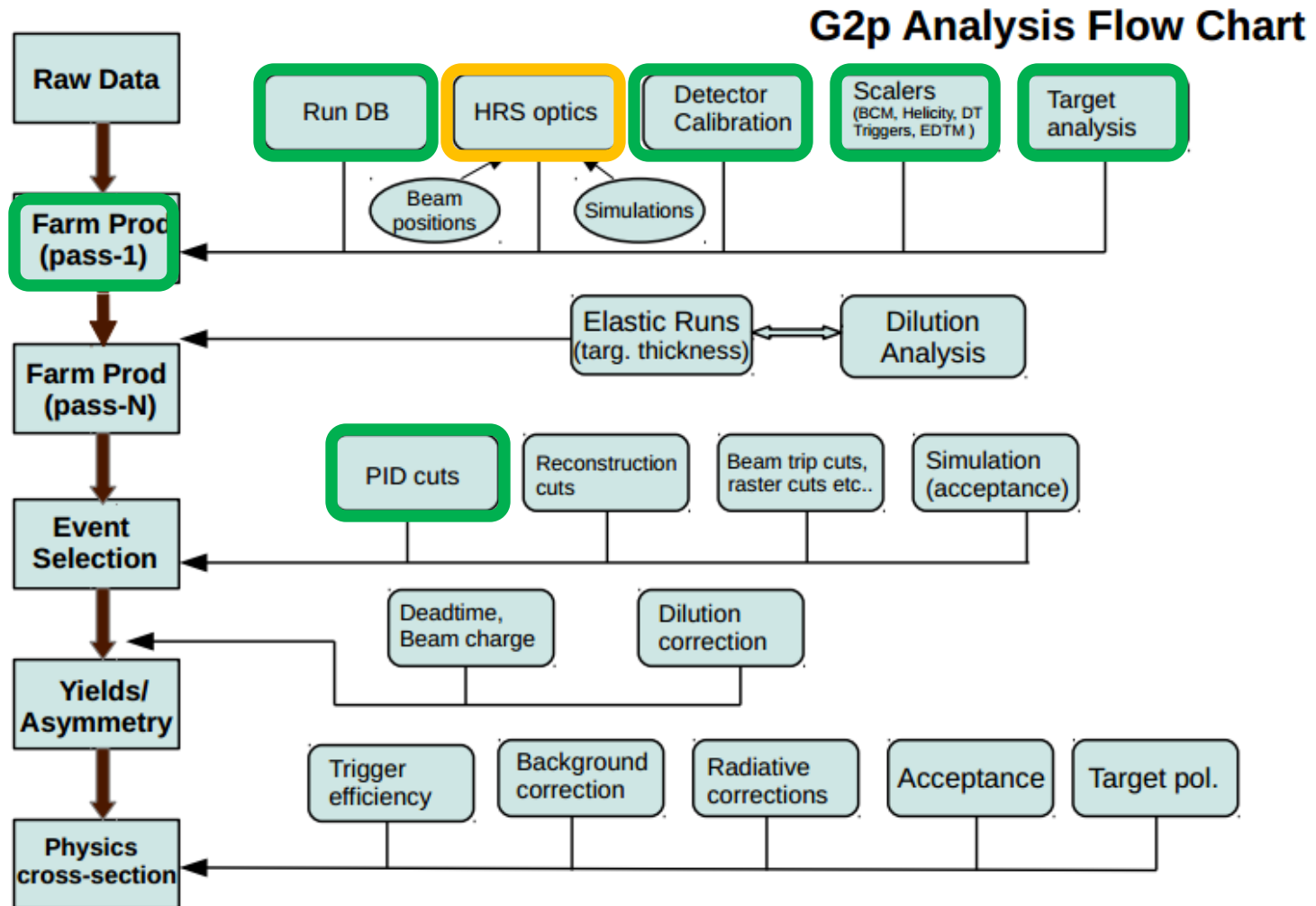


E=2254MeV Asymmetry



$$\sigma_{\perp} = \sigma_{total} * A_{\perp}$$

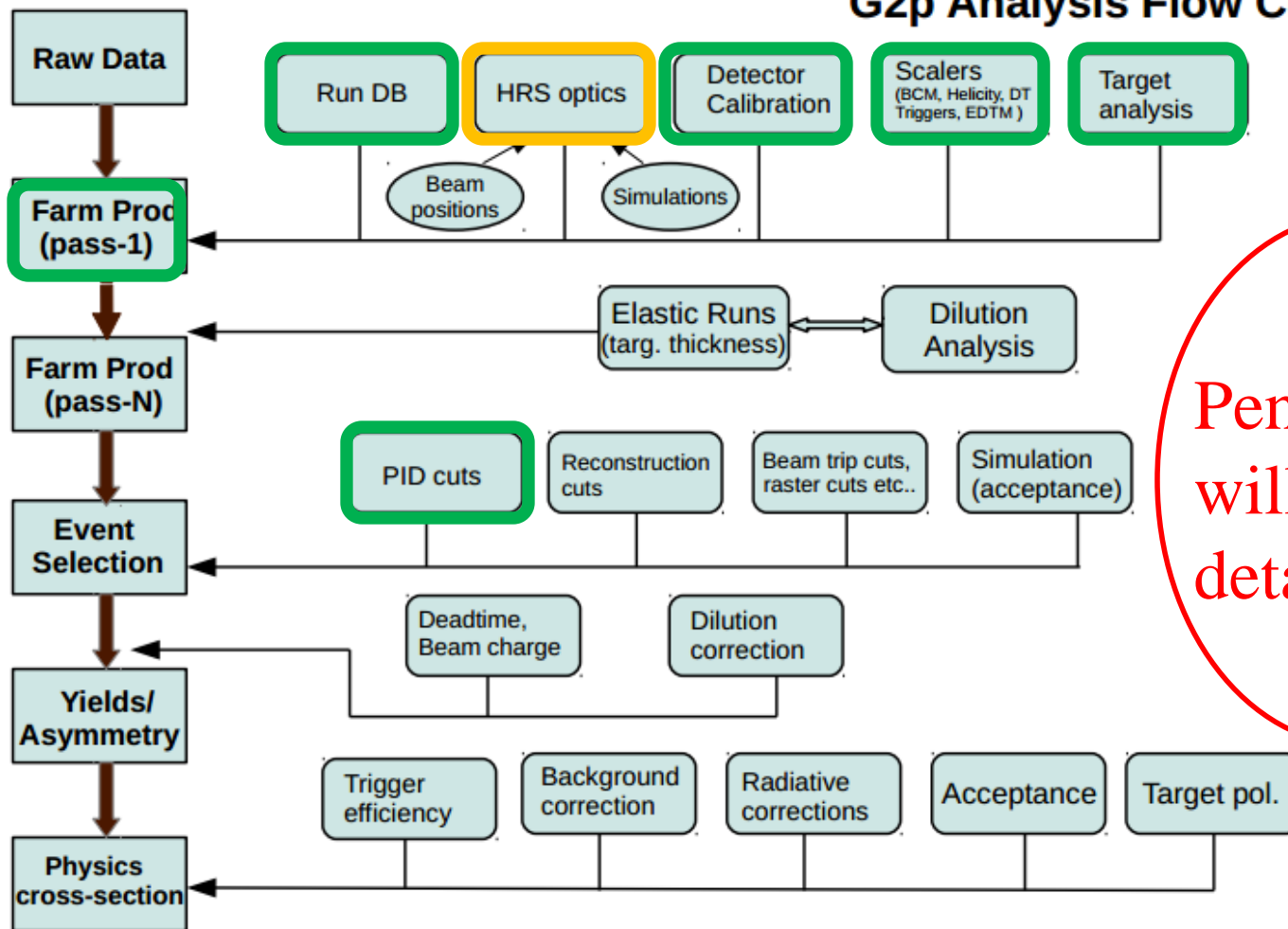
Analysis



Kalyan Allada
JLab

Analysis

G2p Analysis Flow Chart



Pengjia Zhu will talk in details

Kalyan Allada
JLab

Summary

- The g_2^p experiment took data successfully covering $M_p < W < 2$ GeV, $0.02 < Q^2 < 0.2$ GeV²
- Will provide a precision measurement of g_2^p in the low Q^2 region for the first time
- Will extract δ_{LT} to provide a benchmark test of χ PT calculations
- Results will shed light on several physics puzzles

Thanks!