



Hard Exclusive Processes : Perspectives

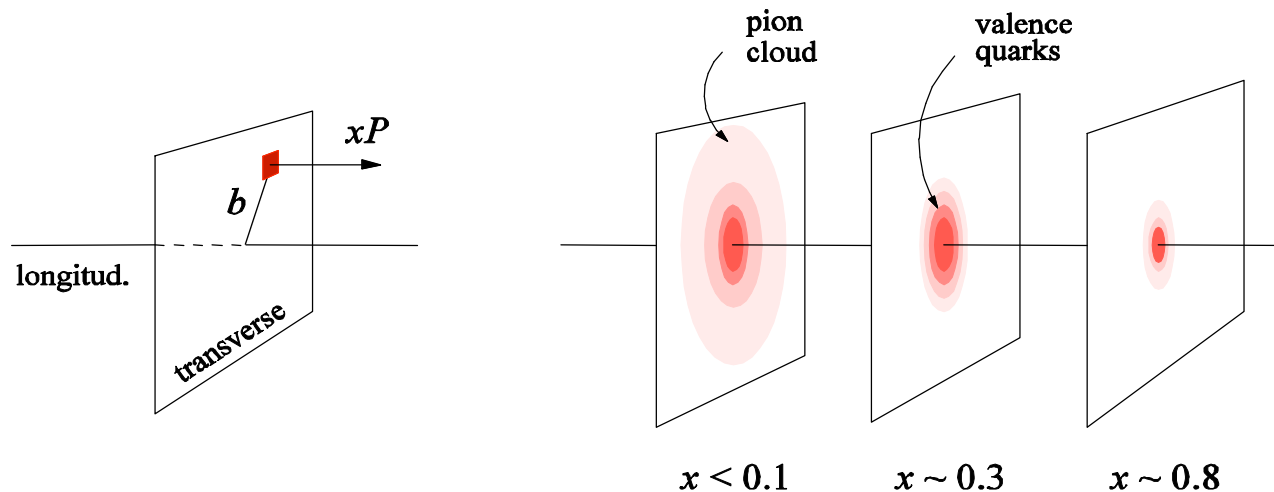
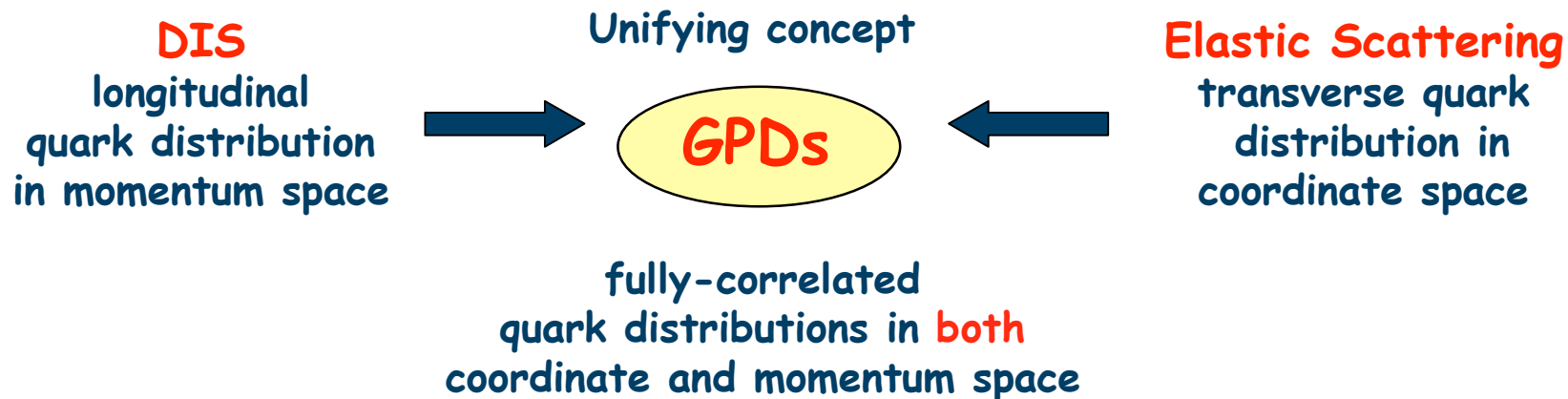
Marc Vanderhaeghen

Johannes Gutenberg Universität, Mainz

4th Workshop on "Exclusive Reactions at High
Momentum Transfer", Jefferson Lab

May 18 - 21, 2010

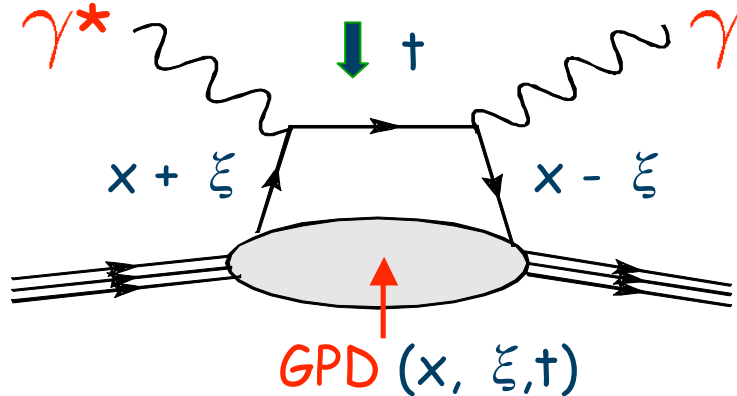
Generalized Parton Distributions (GPDs) : 3D picture of nucleon



Burkardt (2000, 2003),
Belitsky, Ji, Yuan (2004)

QCD factorization : tool to access GPDs

$Q^2 \gg 1 \text{ GeV}^2$

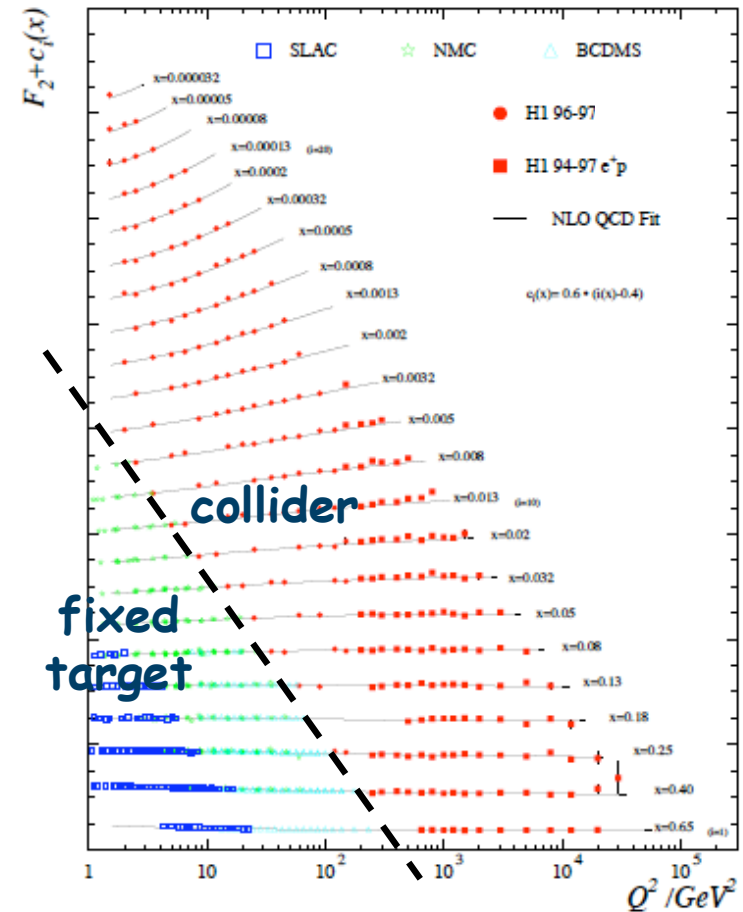


➔ at large Q^2 : **QCD factorization theorem** :
 hard exclusive process described by **GPDs**
 model independent !

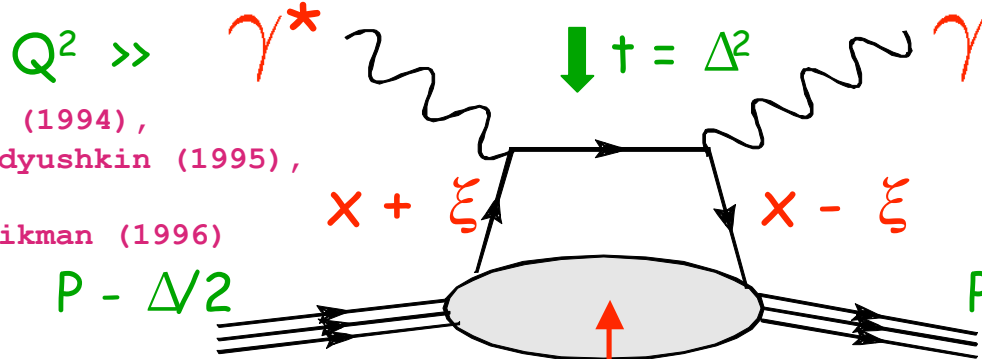
Müller et al. (1994),
 Ji (1995), Radyushkin (1995),
 Collins, Frankfurt, Strikman (1996)

➔ **KEY** Q^2 leverage required to test
QCD scaling

world data on proton F_2



Generalized Parton Distributions



Müller et al. (1994),
 Ji (1995), Radyushkin (1995),
 Collins,
 Frankfurt, Strikman (1996)

low $-t$ process :
 $-t \ll Q^2$

$P - \Delta/2$ $P + \Delta/2$

GPD (x, ξ, t)

$$\Delta^+ = - (2 \xi) P^+$$



light-cone dominance, $n^\mu(1, 0, 0, -1) / (2 P^+)$

$$\frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle P + \frac{\Delta}{2} | \bar{q} \left(-\frac{y}{2} \right) \gamma \cdot n q \left(\frac{y}{2} \right) | P - \frac{\Delta}{2} \rangle_{y^+=0, y_\perp=0}$$

$$= \bar{N} \left\{ H(x, \xi, t) \gamma \cdot n + E(x, \xi, t) i\sigma^{\mu\nu} \frac{\Delta_\nu}{2M} n_\mu \right\} N$$

$$\frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle P + \frac{\Delta}{2} | \bar{q} \left(-\frac{y}{2} \right) \gamma \cdot n \gamma_5 q \left(\frac{y}{2} \right) | P - \frac{\Delta}{2} \rangle_{y^+=0, y_\perp=0}$$

$$= \bar{N} \left\{ \tilde{H}(x, \xi, t) \gamma \cdot n \gamma_5 + \tilde{E}(x, \xi, t) \gamma_5 \frac{\Delta^\mu}{2M} n_\mu \right\} N$$

known information on GPDs

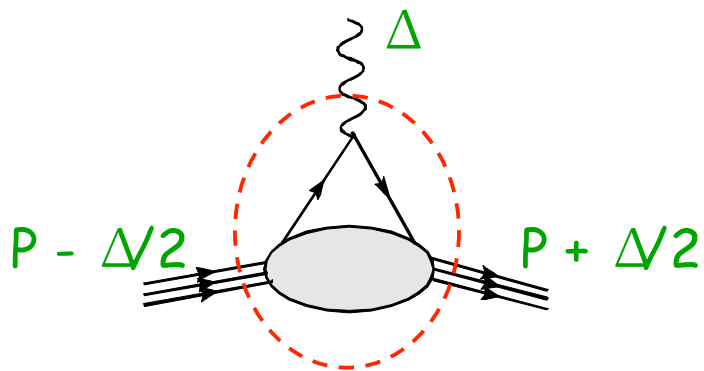
→ forward limit : ordinary **parton distributions**

$$H^q(x, \xi = 0, t = 0) = q(x) \quad \text{unpolarized quark distr}$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x) \quad \text{polarized quark distr}$$

E^q, \tilde{E}^q : do NOT appear in DIS → new information

→ first moments : nucleon **electroweak form factors**



ξ -independence :
Lorentz invariance

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t) \quad \text{Dirac}$$

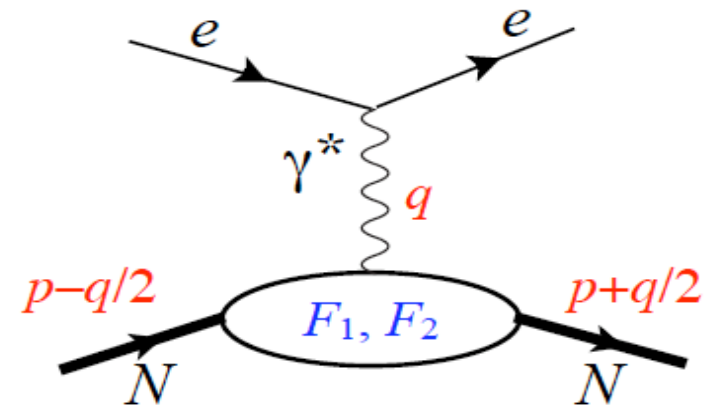
$$\int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t) \quad \text{Pauli}$$

$$\int_{-1}^1 dx \tilde{H}^q(x, \xi, t) = G_A^q(t) \quad \text{axial}$$

$$\int_{-1}^1 dx \tilde{E}^q(x, \xi, t) = G_P^q(t) \quad \text{pseudo-scalar}$$

spin-1/2 electromagnetic form factors

- Elastic $e p \rightarrow e p$ scattering is like an electron microscope to investigate nucleon structure
- In 1-photon exchange approximation : nucleon structure parameterized by 2 form factors



$$A_{\lambda\lambda'}^{\mu} = \langle p + \frac{1}{2}q, \lambda' | J^{\mu}(0) | p - \frac{1}{2}q, \lambda \rangle$$

$$= \bar{u}(p + \frac{1}{2}q, \lambda') \left[F_1(Q^2) \gamma^{\mu} + F_2(Q^2) \frac{i}{2m} \sigma^{\mu\nu} q_{\nu} \right] u(p - \frac{1}{2}q, \lambda)$$

Dirac **Pauli**

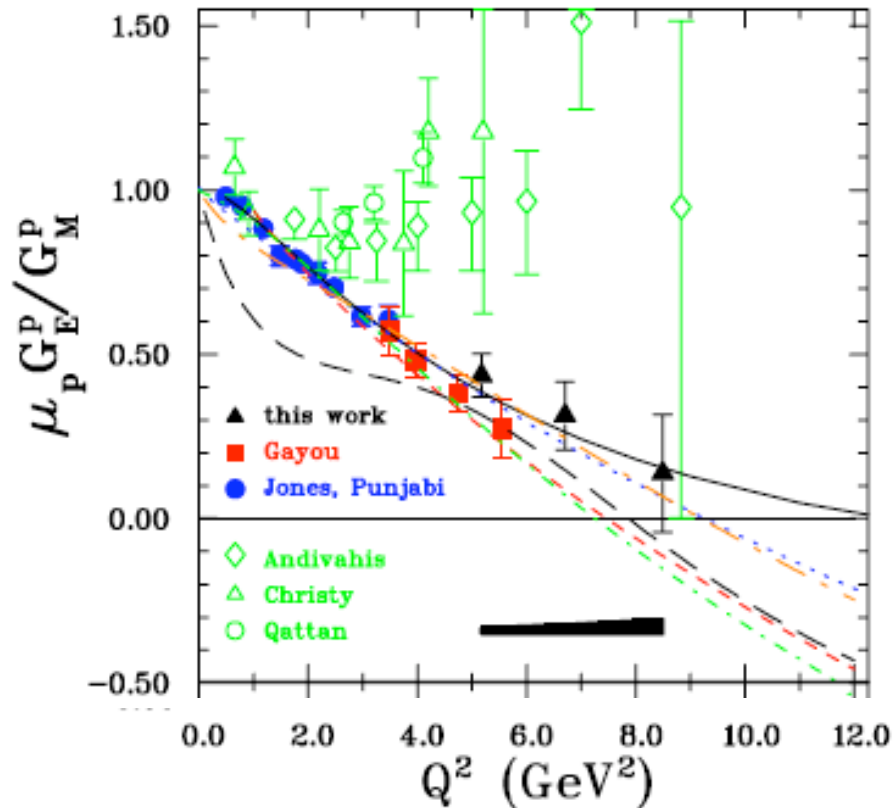
F_1 helicity conserving , F_2 helicity flip form factors

- Alternatively, the Sachs form factors

$$G_E(Q^2) = F_1(Q^2) - \tau F_2(Q^2), \quad G_M(Q^2) = F_1(Q^2) + F_2(Q^2), \quad \text{with } \tau = Q^2/4 m^2$$

Traditionally : it is assumed that in the Breit frame, and for non-relativistic systems with $m \gg Q$, G_E and G_M are 3-dim Fourier transforms of charge- and current distributions.

Nucleon e.m. Form Factors : new experiments

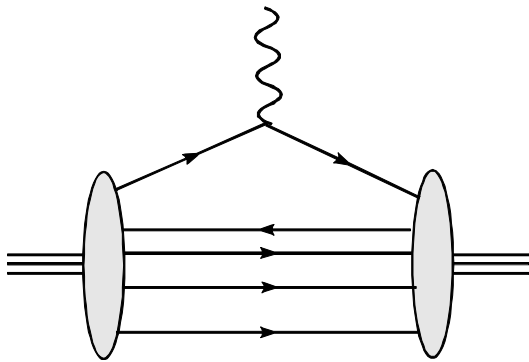
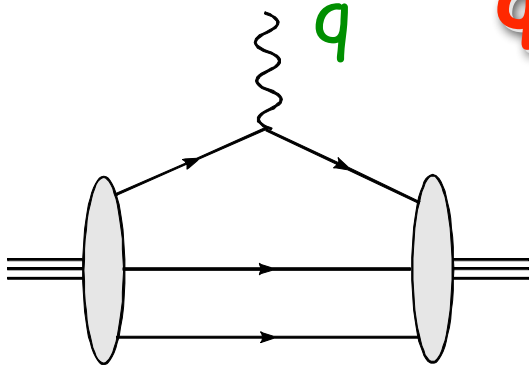


see talks :
Puckett, De Jager



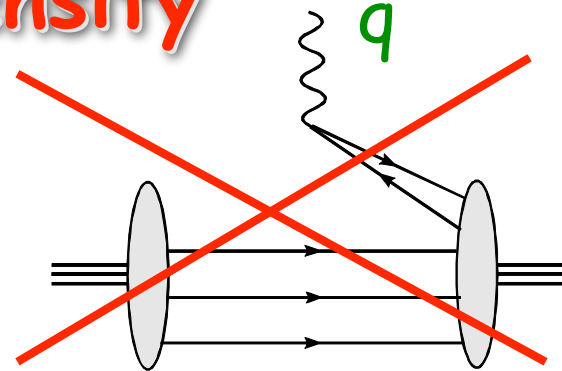
Spin-1/2 transverse densities

interpretation of Form Factor as quark density



overlap of wave function
Fock components with
same number of quarks

interpretation as
probability/charge density



overlap of wave function Fock
components with different
number of constituents

NO probability/charge
density interpretation

absent in a LIGHT-FRONT frame !

$$q^+ = q^0 + q^3 = 0$$

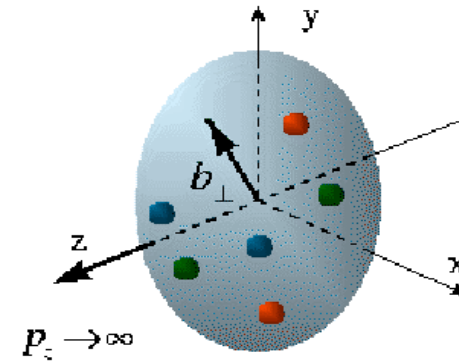
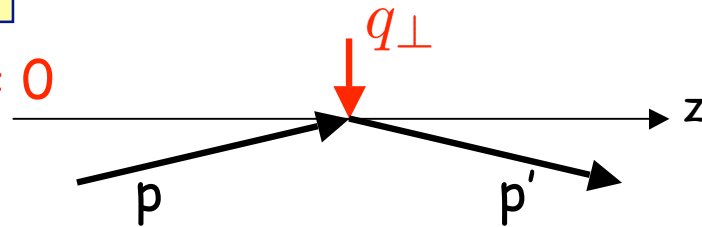
quark transverse charge densities in nucleon (I)

light-front



$$q^+ = q^0 + q^3 = 0$$

$$Q^2 \equiv \vec{q}_\perp^2$$

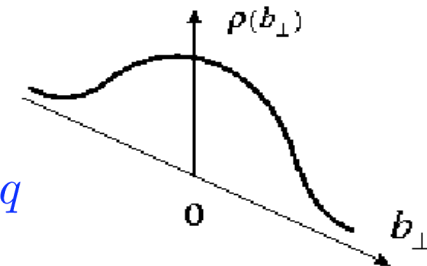


photon only couples to forward moving quarks



quark charge density operator

$$J^+ \equiv J^0 + J^3 = \bar{q}\gamma^+q = 2q_+^\dagger q_+, \quad \text{with} \quad q_+ \equiv \frac{1}{4}\gamma^-\gamma^+q$$



★ longitudinally polarized nucleon

$$\begin{aligned} \rho_0^N(\vec{b}) &\equiv \int \frac{d^2\vec{q}_\perp}{(2\pi)^2} e^{-i\vec{q}_\perp \cdot \vec{b}} \frac{1}{2P^+} \langle P^+, \frac{\vec{q}_\perp}{2}, \lambda | J^+(0) | P^+, -\frac{\vec{q}_\perp}{2}, \lambda \rangle \\ &= \int_0^\infty \frac{dQ}{2\pi} Q J_0(bQ) F_1(Q^2) \end{aligned}$$

Miller
(2007)

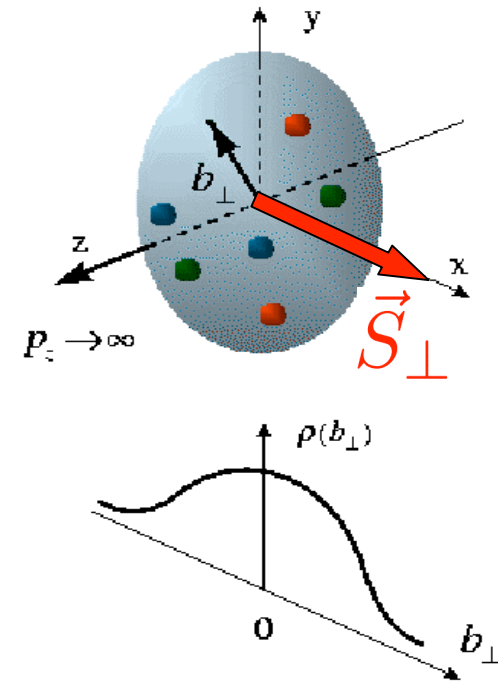
quark transverse charge densities in nucleon (II)

★ transversely polarized nucleon

transverse spin $\vec{S}_\perp = \cos \phi_S \hat{e}_x + \sin \phi_S \hat{e}_y$

e.g. along x-axis : $\phi_S = 0$

$$\vec{b} = b (\cos \phi_b \hat{e}_x + \sin \phi_b \hat{e}_y)$$

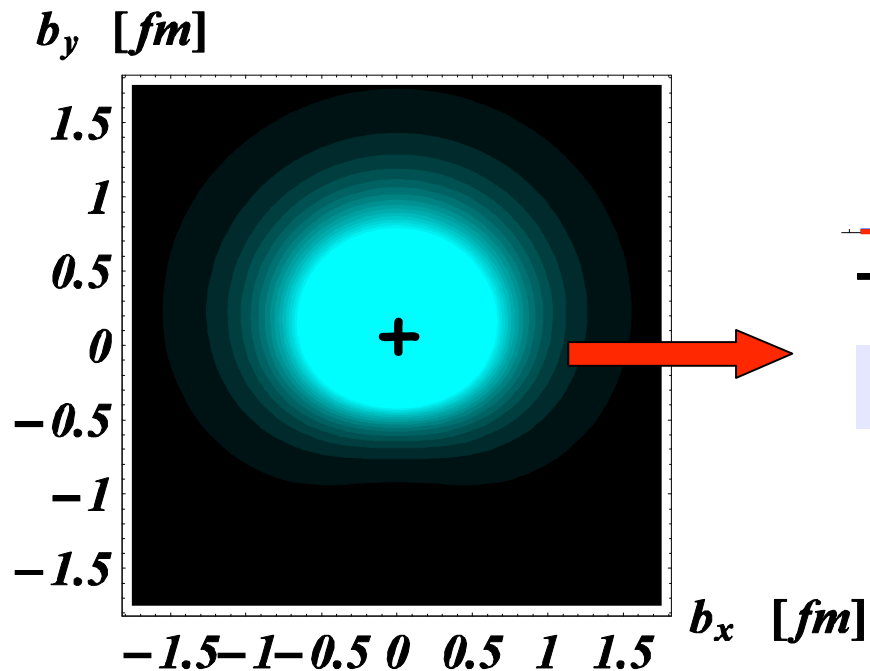
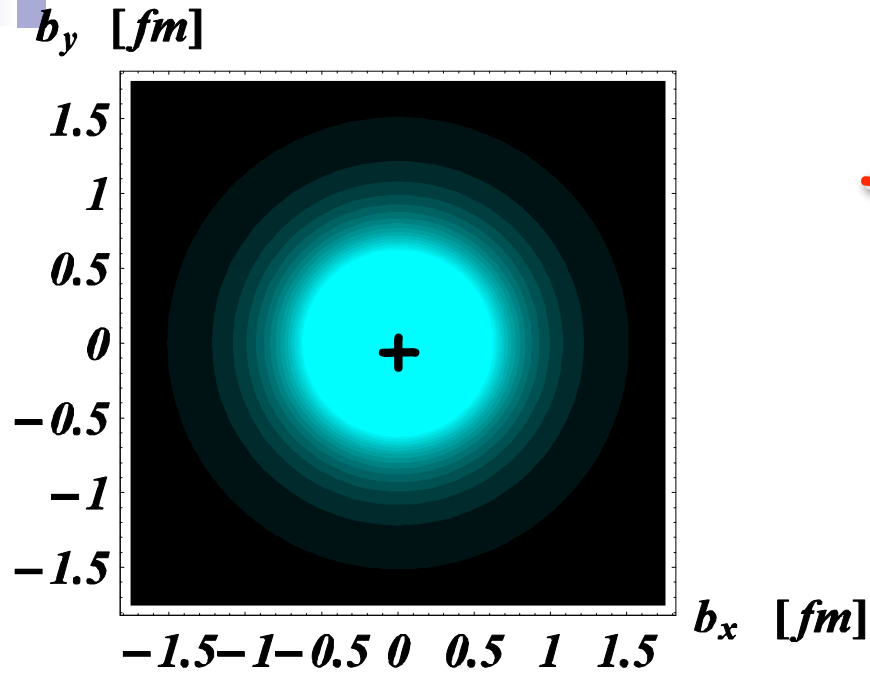


$$\begin{aligned} \rho_T^N(\vec{b}) &\equiv \int \frac{d^2 \vec{q}_\perp}{(2\pi)^2} e^{-i \vec{q}_\perp \cdot \vec{b}} \frac{1}{2P^+} \langle P^+, \frac{\vec{q}_\perp}{2}, s_\perp = +\frac{1}{2} | J^+(0) | P^+, -\frac{\vec{q}_\perp}{2}, s_\perp = +\frac{1}{2} \rangle \\ &= \rho_0^N(b) + \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{2M_N} J_1(bQ) F_2(Q^2) \end{aligned}$$

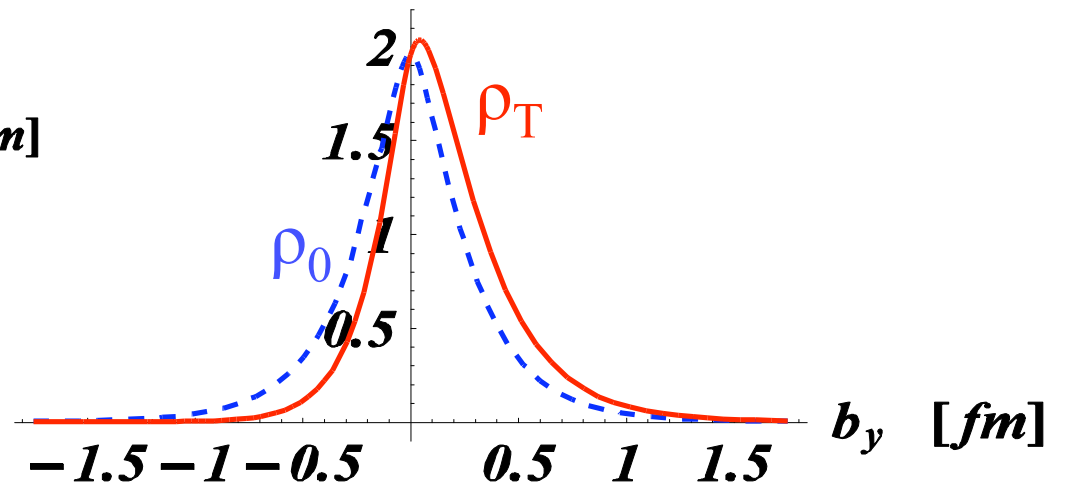
dipole field pattern

Carlson, Vdh (2007)

empirical quark transverse densities in proton



ρ_0^P, ρ_T^P [$1/\text{fm}^2$]

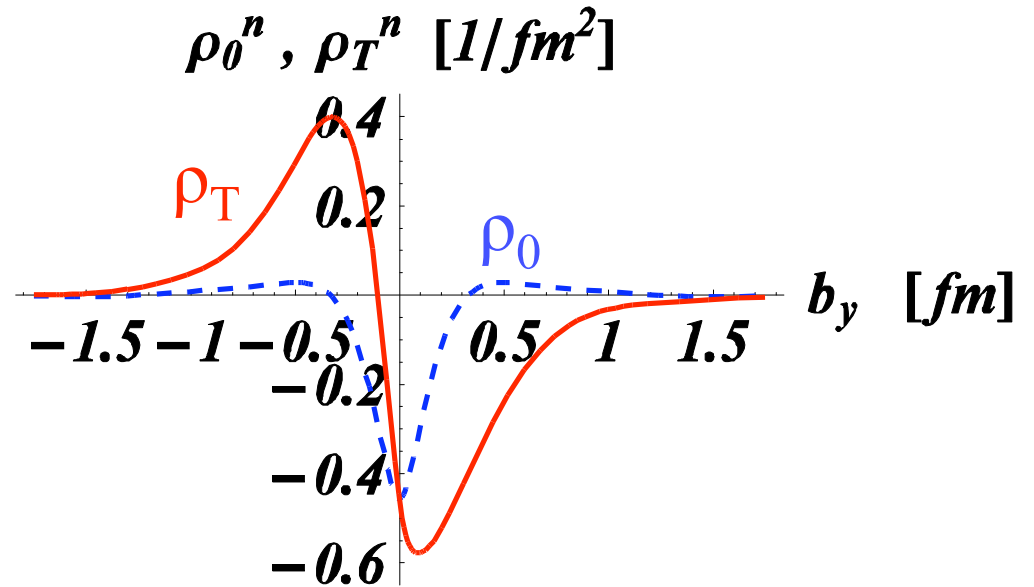
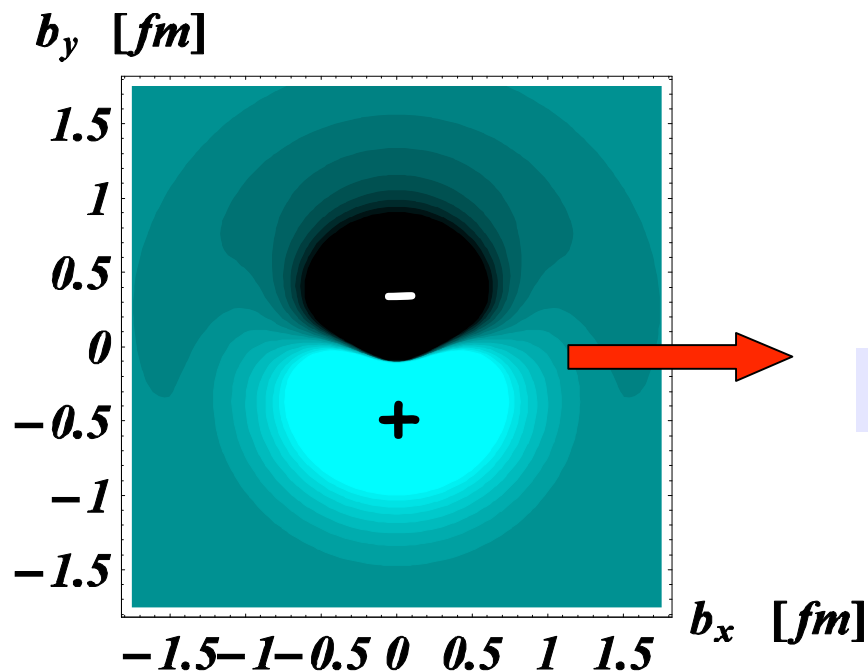
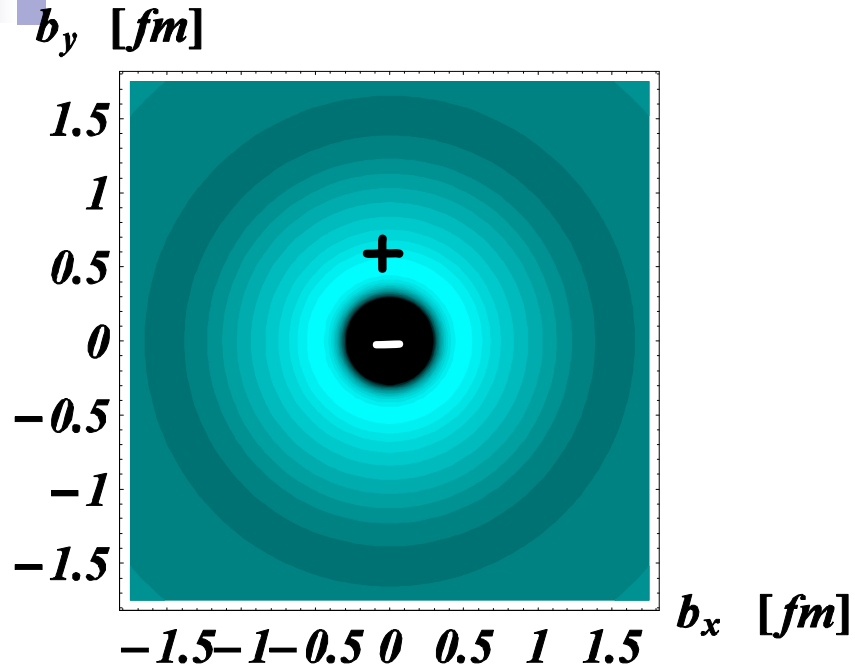


induced EDM : $d_y = F_{2p}(0) \cdot e / (2 M_N)$

data : Arrington, Melnitchouk, Tjon (2007)

densities : Miller (2007); Carlson, Vdh (2007)

empirical quark transverse densities in neutron



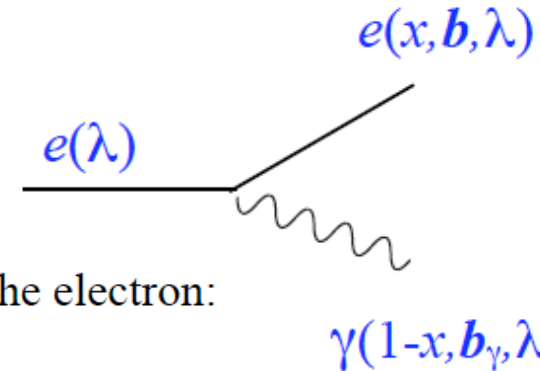
induced EDM : $d_y = F_{2n}(0) \cdot e / (2 M_N)$

data: Bradford, Bodek, Budd, Arrington (2006)

densities : Miller (2007); Carlson, Vdh (2007)

transverse densities of $e\gamma$ Fock state in electron

Hoyer, Kurki (2009)



The wave functions give the densities of the $|e\gamma\rangle$ Fock state of the electron:

$$\rho_0(x, \mathbf{b}) = \frac{\alpha m^2}{2\pi^2} \left[\frac{1+x^2}{1-x} K_1^2(mb) + (1-x) K_0^2(mb) \right]$$

LC Wavefunction :

Brodsky, Drell (1980)

$$\rho_x(x, \mathbf{b}) = \rho_0(x, \mathbf{b}) + \frac{\alpha m^2}{\pi^2} x \sin(\phi_b) K_0(mb) K_1(mb)$$

from which the Pauli form factor is obtained (exact at order α)

$$F_2(Q^2) = \frac{4\alpha m^3}{\pi Q} \int_0^1 dx x \int_0^\infty db b J_1(bQ) K_0(mb) K_1(mb)$$

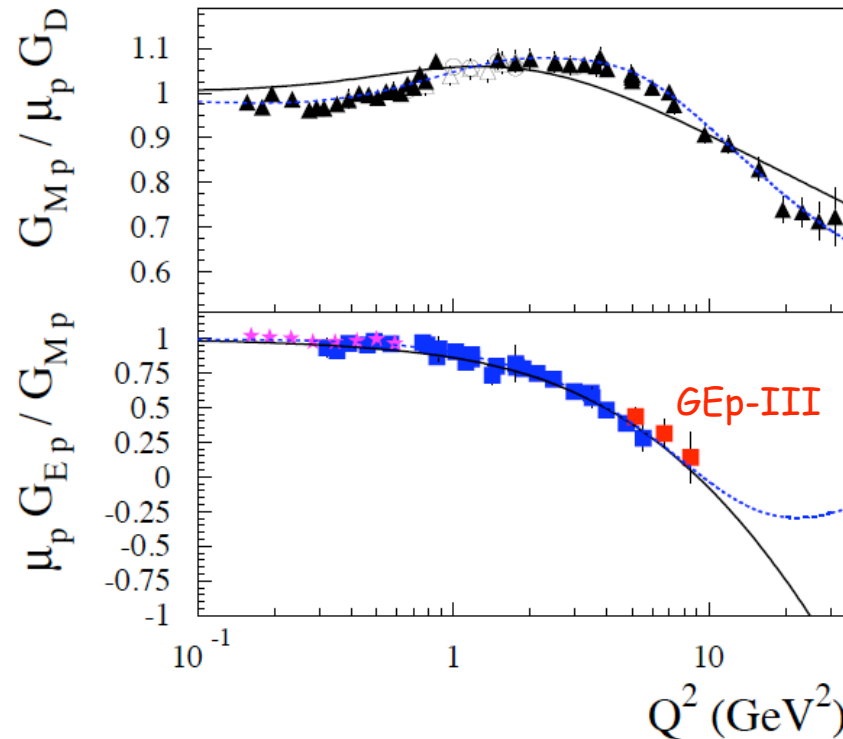
x- and b-dependence factorizes

$$= \frac{2\alpha m^2}{\pi} \frac{1}{Q\sqrt{Q^2+4m^2}} \log \left[\frac{1}{2m} \left(\sqrt{Q^2+4m^2} + Q \right) \right]$$

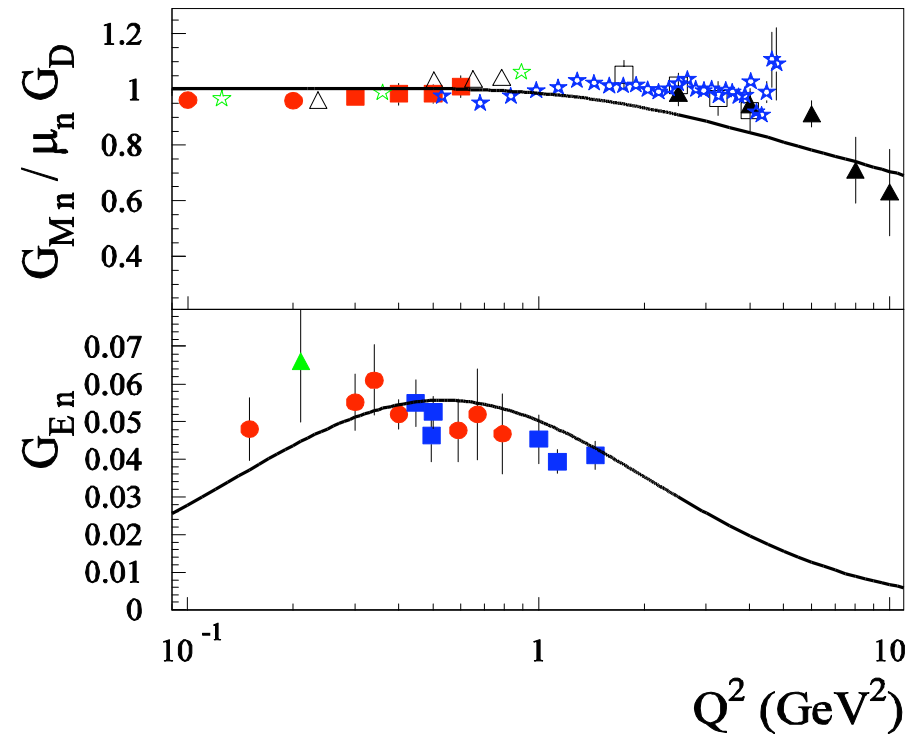
Exact expression from loop integral

electromagnetic form factors

PROTON



NEUTRON



→ modified Regge GPD parameterization

3-parameter fit $\left\{ \begin{array}{l} 1 : \text{Regge slope} \rightarrow \text{proton Dirac (Pauli) radius} \\ 2, 3 : \text{large } x \text{ behavior of GPD } E^u, E^d \rightarrow \text{large } Q^2 \text{ behavior of } F_{2p}, F_{2n} \end{array} \right.$

Guidal, Polyakov, Radyushkin, Vdh (2005)

also Diehl, Feldmann, Jakob, Kroll (2005)

connection large Q^2 of FF \leftrightarrow large x of GPD

$$\begin{aligned} I &= \int_0^1 dx (1-x)^\nu e^{\alpha' Q^2 (1-x) \ln x} = \int_0^1 dx e^{\nu \ln(1-x) + \alpha' Q^2 (1-x) \ln x} \\ &= \int_0^1 dx e^{f(x, Q^2)} \end{aligned}$$

at large Q^2 : integral dominated by maximum of $f(x, Q^2)$, remainder region is exp. suppressed (method of steepest descent)

$f(x, Q^2)$ reaches maximum for : $x = x_0 \simeq 1 - \frac{\nu}{\alpha' Q^2}$

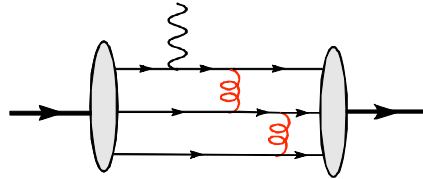
"Drell-Yan-West" relation for PDF/GPD :

at large Q^2 : I is dominated by its behavior around $x \rightarrow 1$

$$I \simeq e^{f(x_0, Q^2)} \left(\frac{2}{f''(x_0, Q^2)} \right)^{1/2} \frac{\sqrt{\pi}}{2} \sim \left(\frac{1}{\alpha' Q^2} \right)^{(\nu+1)/2}$$

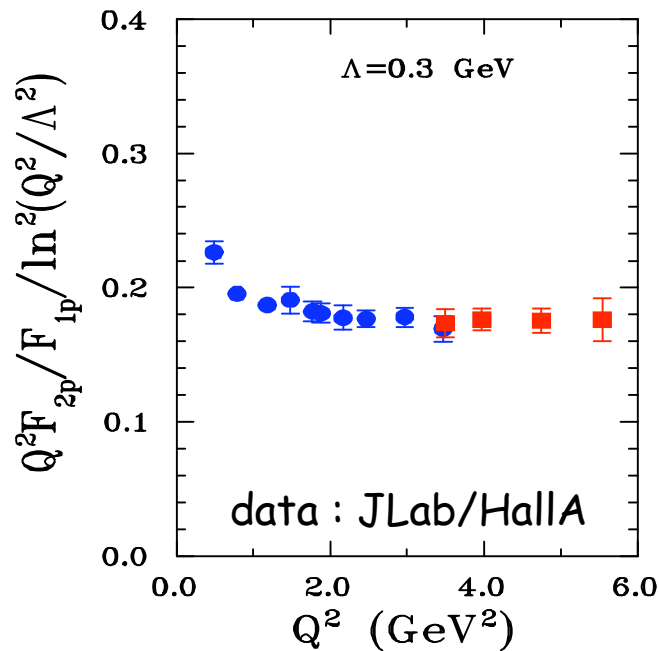
proton Dirac & Pauli FFs : $\begin{cases} G_M = F_1 + F_2 \\ G_E = F_1 - \left(\frac{Q^2}{4M_N^2}\right) F_2 \end{cases}$

PQCD



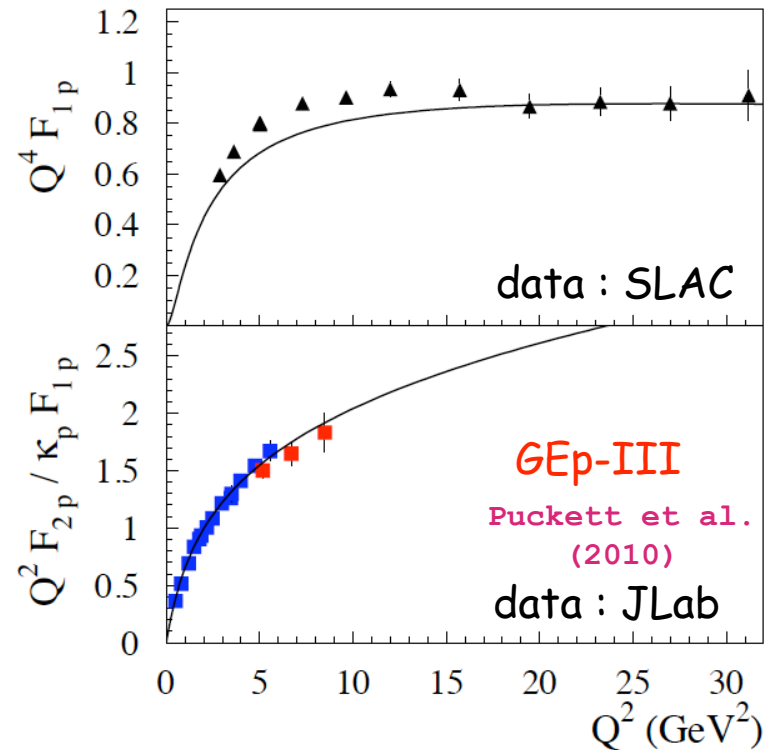
GPD framework

$$\frac{F_{2p}}{F_{1p}} \sim \frac{\ln^2(Q^2/\Lambda^2)}{Q^2}$$



Beltisky, Ji, Yuan (2003)

modified Regge GPD model



Guidal, Polyakov, Radyushkin, Vdh (2005)

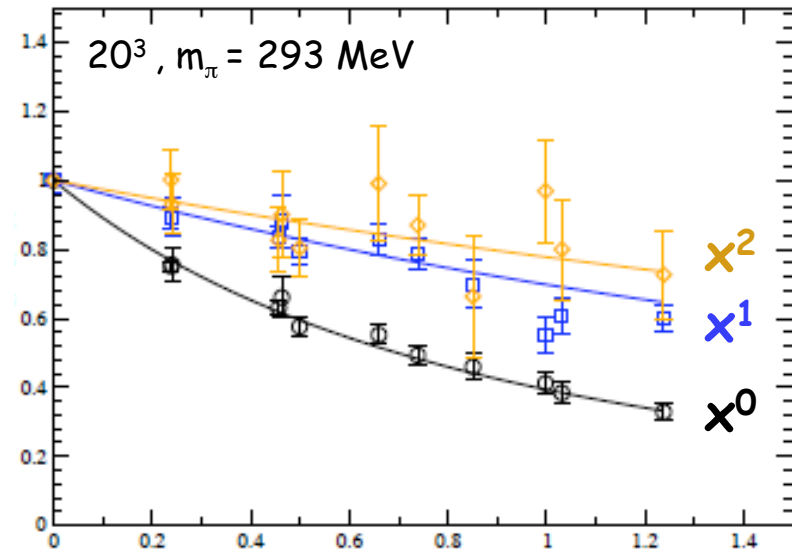
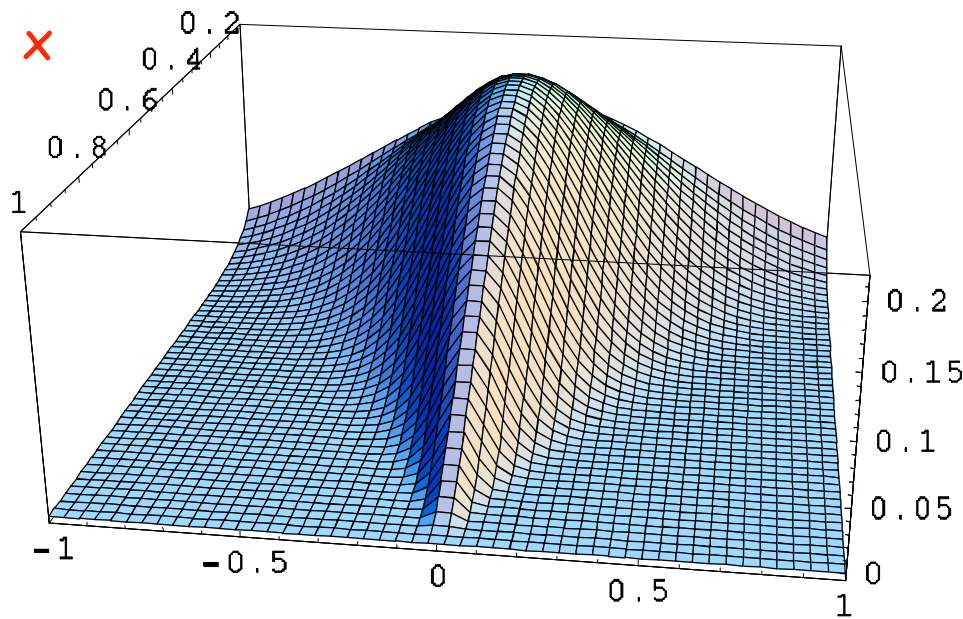
GPDs : transverse image of nucleon

GPDs : quark distributions w.r.t.
longitudinal momentum x and
transverse position b_{\perp}

lattice QCD : moments of GPDs

$$H^u(x, b_{\perp})$$

x^n moment of H^{u-d}



b_{\perp} (fm)

Fourier transform

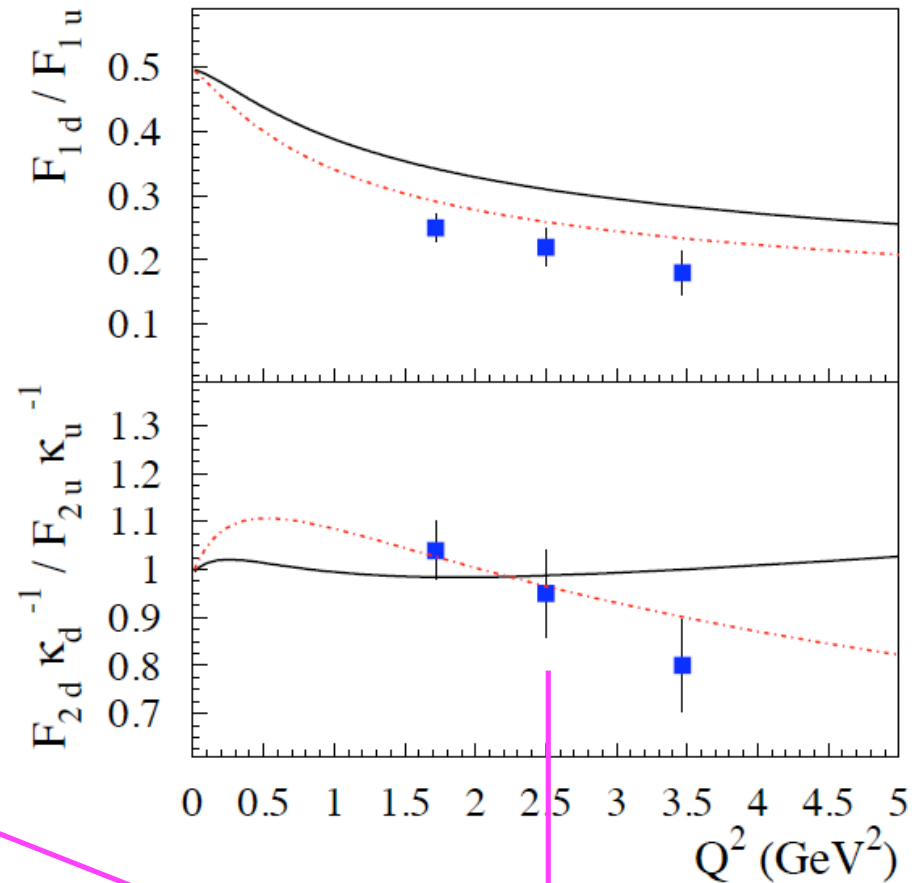
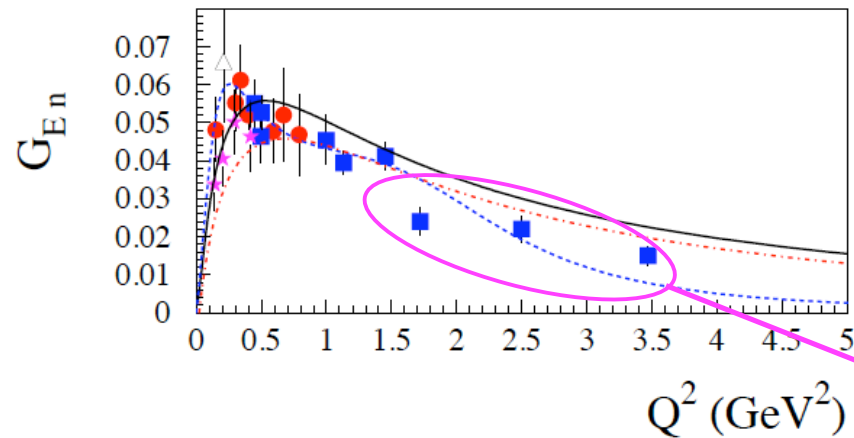
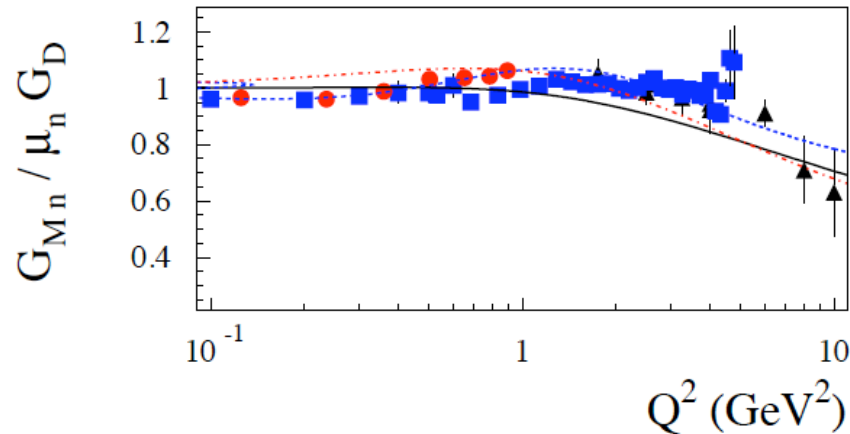
$-t$ (GeV²)

Guidal, Polyakov, Radyushkin, Vdh (2005),

Diehl, Feldmann, Jakob, Kroll (2005)

LHPC Coll.

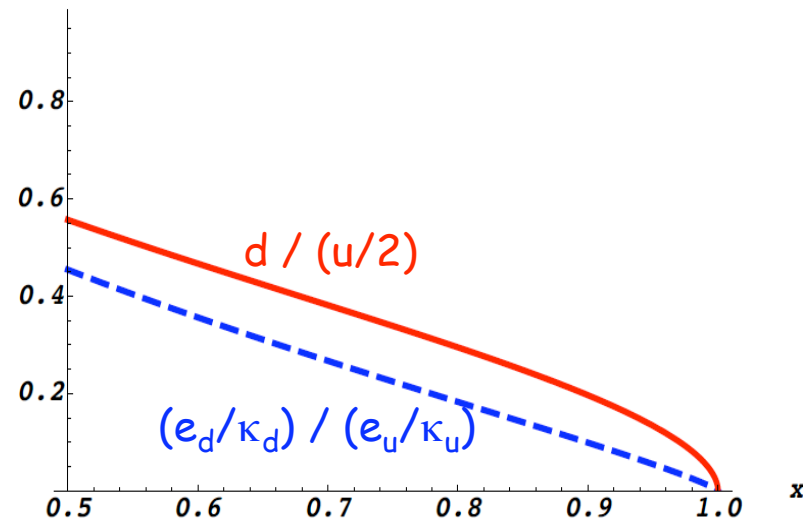
neutron e.m. form factors



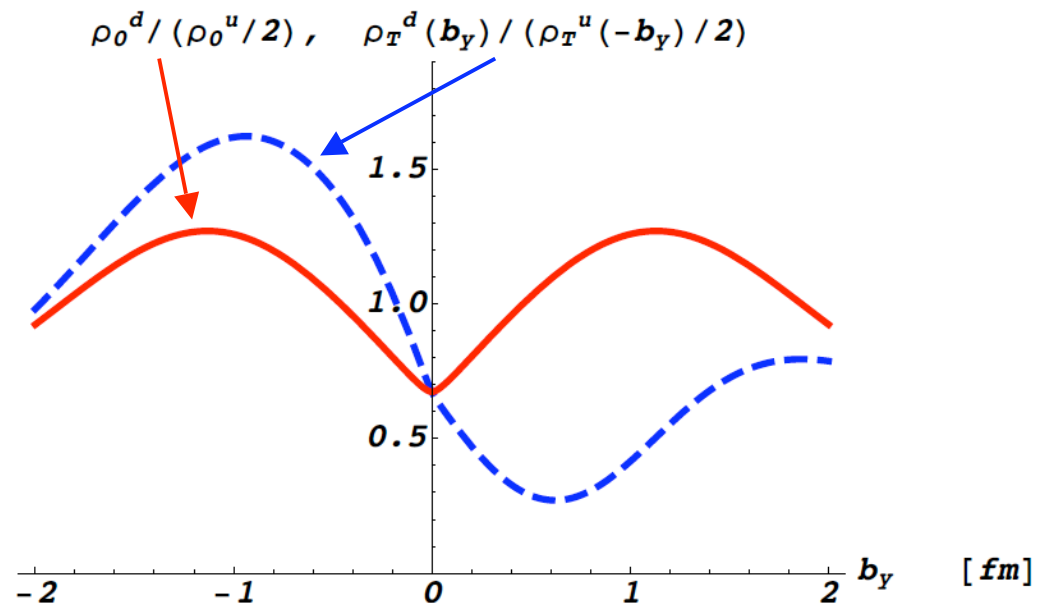
- Phenomenological fit : Bradford et al.
- modified Regge GPD parameterization (3 parameters)
- .-.- modified Regge GPD parameterization (6 parameters)

Jlab/HallA E02-013
preliminary

d/u quark densities



d-quark distr. : further spread out in proton than u-quark distr.
 Opposite behavior for neutron



GPDs : total angular momentum sum rule

→ total angular momentum $J^q = \frac{1}{2} \Delta q + L^q$ ← quark **orbital** angular momentum

x. Ji
(1997)

$$2 J^q = M_2^q + \int_{-1}^1 dx x E^q(x, 0, 0)$$

with known $M_2^q = \int_0^1 dx x [q(x) + \bar{q}(x)]$

→ Valence parametrization for GPD E^q :

PROTON	M_2^q	$2 J^q$ GPD model	$2 J^q$ Lattice (LHPC) (4 GeV ²)
u	0.37	0.58	≈ 0.47
d	0.20	-0.06	≈ 0.00
s	0.04	0.04	
u + d + s	0.61	0.56	

lattice : full QCD,
no disconnected diagrams so far
see talk : Hägler

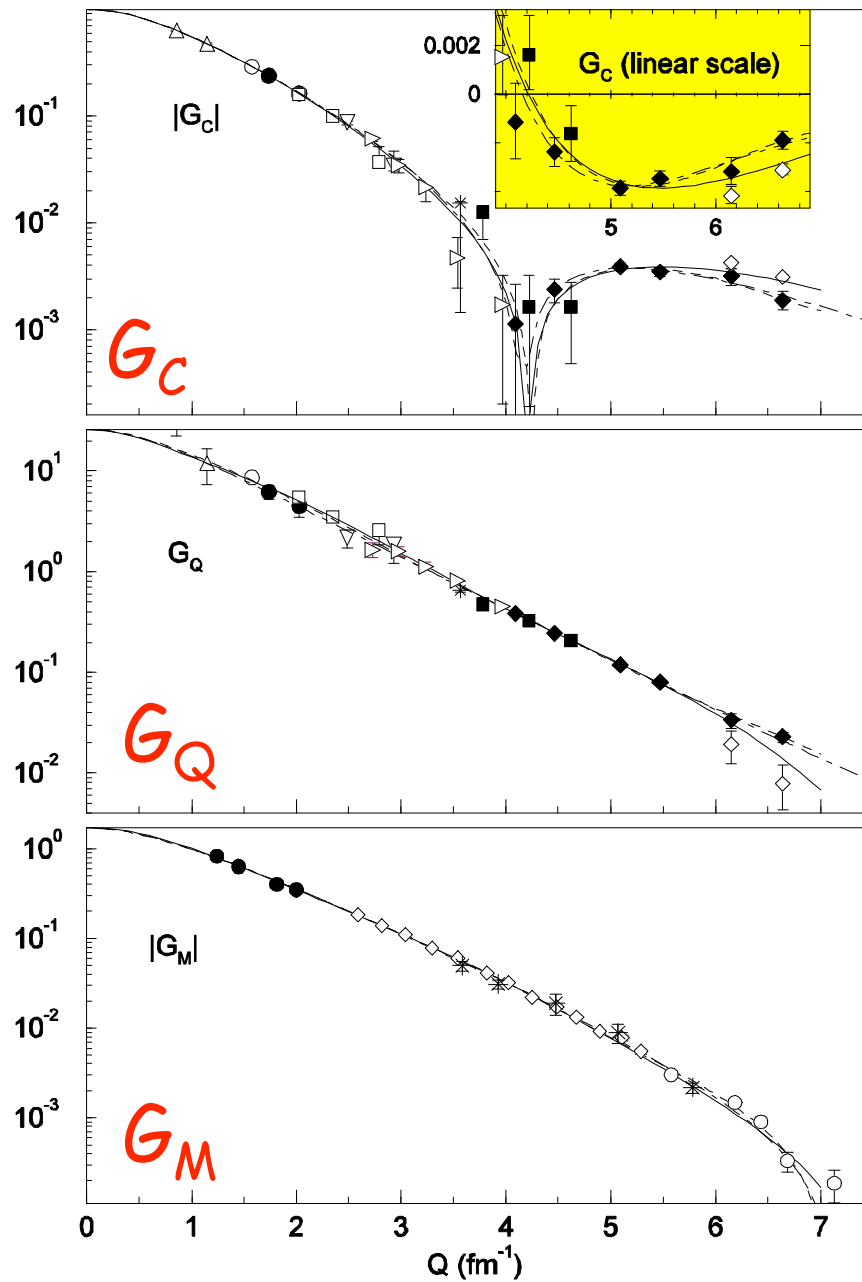


Higher Spin transverse densities

deuteron e.m. FFs

separated data (measuring t_{20})
up to about 2 GeV^2

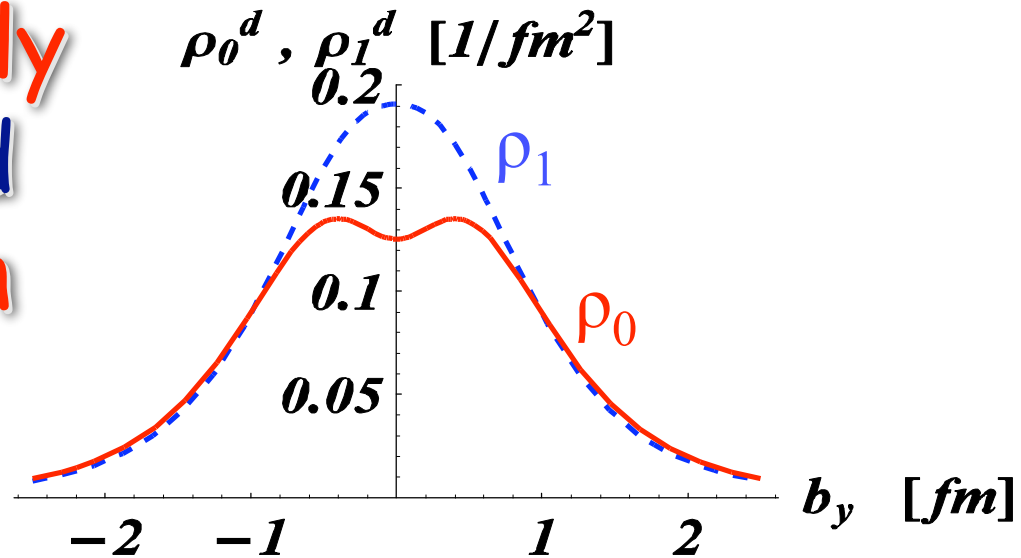
Abbott et al. (2000)



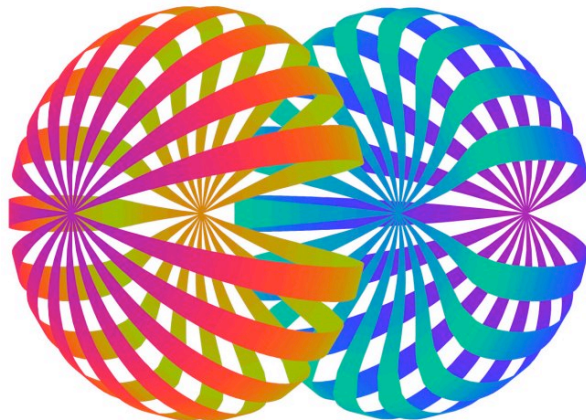
$$G_M(0) = 1.71$$

$$G_Q(0) = 25.84(3)$$

longitudinally polarized deuteron



$\lambda = \pm 1$



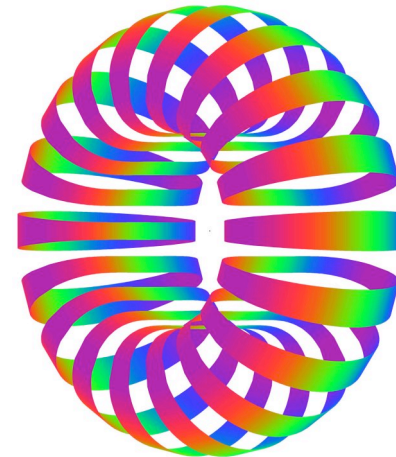
deuteron equidensity
surfaces

$$(\rho_d = 0.24 \text{ fm}^{-3})$$

from Argonne v_{18} :

Forest et al. (1996)

$\lambda = 0$



transversely polarized deuteron

$$Q_{s_{\perp}}^d \equiv e \int d^2\vec{b} (b_x^2 - b_y^2) \rho_{T s_{\perp}}^d(\vec{b})$$

$$Q_1^d = -\frac{1}{2} Q_0^d = \frac{1}{2} \{ [G_M(0) - 2] + [G_Q(0) + 1] \} \left(\frac{e}{M_d^2} \right)$$

experiment :

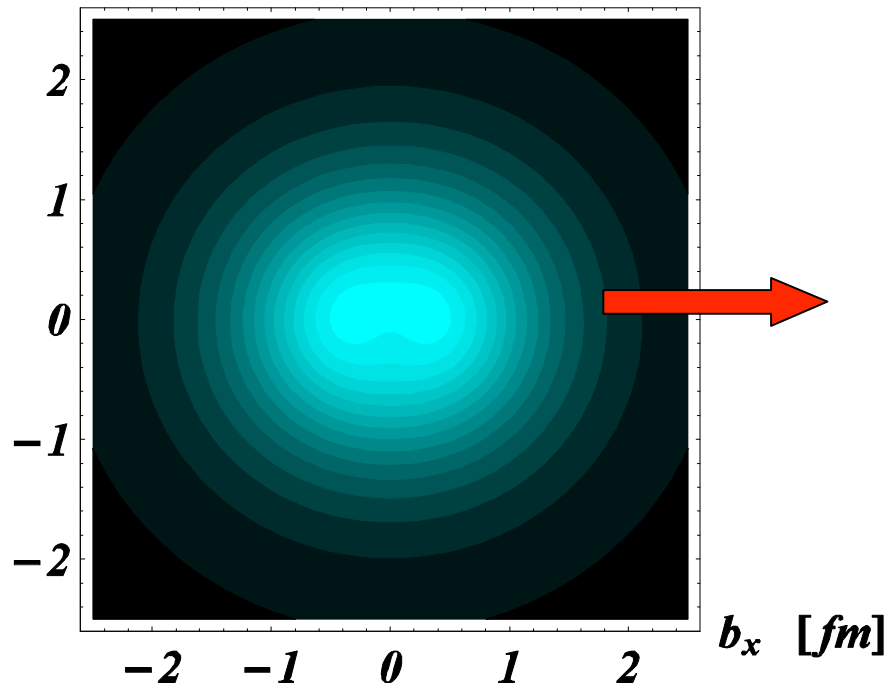
$$G_M(0) = 1.71$$

$$G_Q(0) = 25.84(3)$$

$$s_{\perp} = +1$$

$$Q_1^d > 0$$

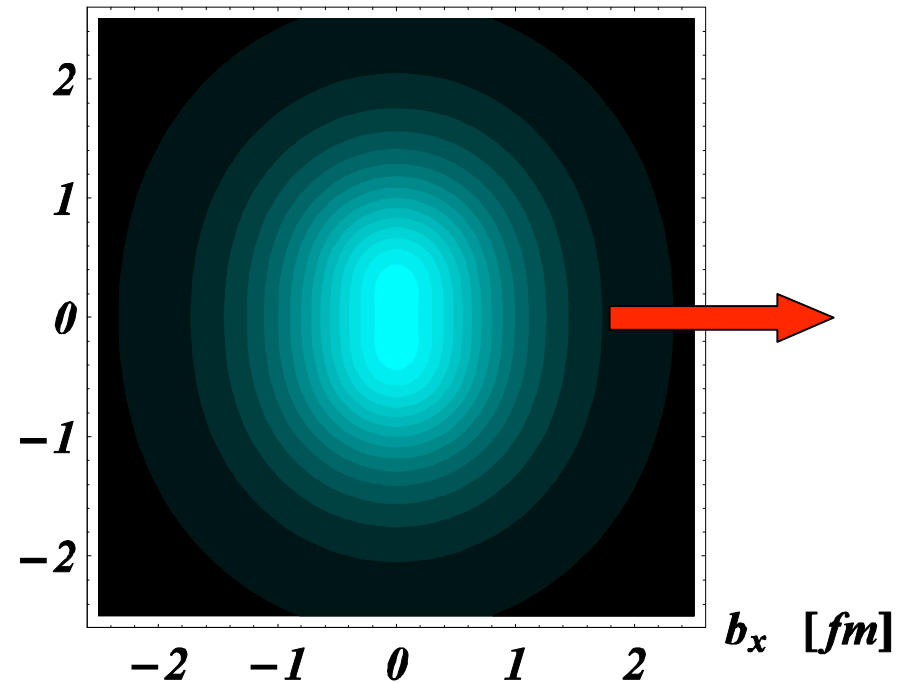
b_y [fm]



$$s_{\perp} = 0$$

$$Q_0^d < 0$$

b_y [fm]



E.M. moments of W bosons

for spin-1 point particle

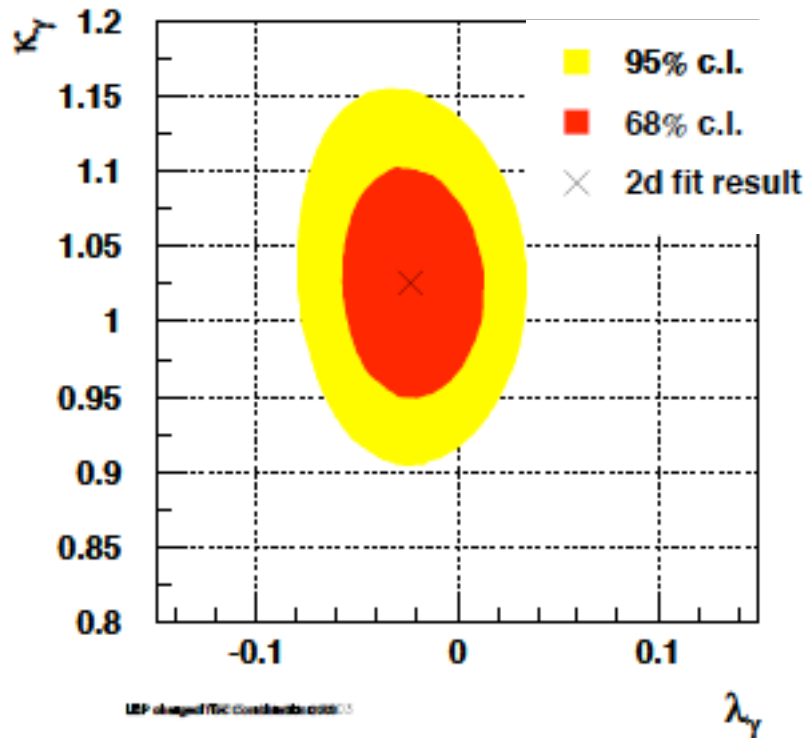
$$G_M(0) = 2 \text{ and } G_Q(0) = -1$$

$$\mu = \frac{e}{2M_W} \{2 + (\kappa - 1) + \lambda\}$$

$$Q = -\frac{e}{M_W^2} \{1 + (\kappa - 1) - \lambda\}$$

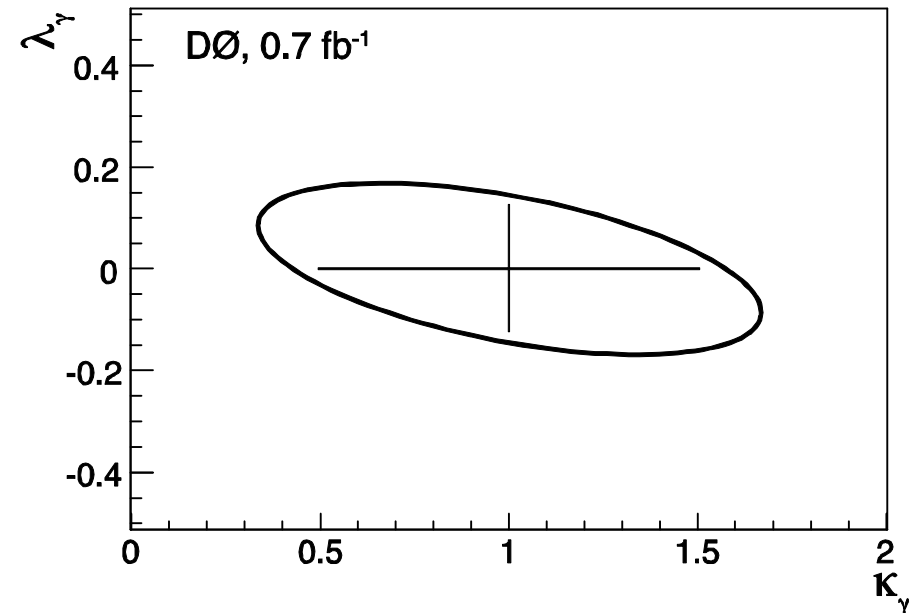
LEP Electroweak working group

hep-ex/0612034



DØ Collaboration

PRL100, 241805 (2008)



natural values for e.m. moments of point particle with spin j

Lorcé (2008)

see talk : Lorcé

$$G_{E0}(0) = 1$$

$$G_{M1}(0) = 2j$$

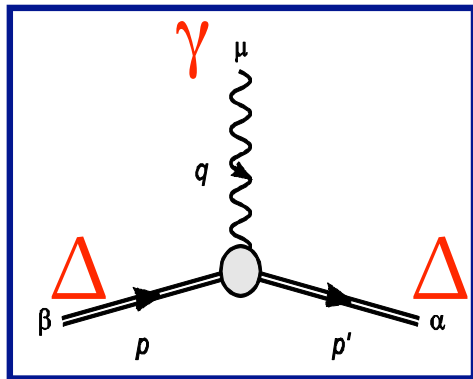
$$G_{E2}(0) = -j(2j - 1)$$

$$G_{M3}(0) = -\frac{1}{3}j(2j - 1)(2j - 2)$$

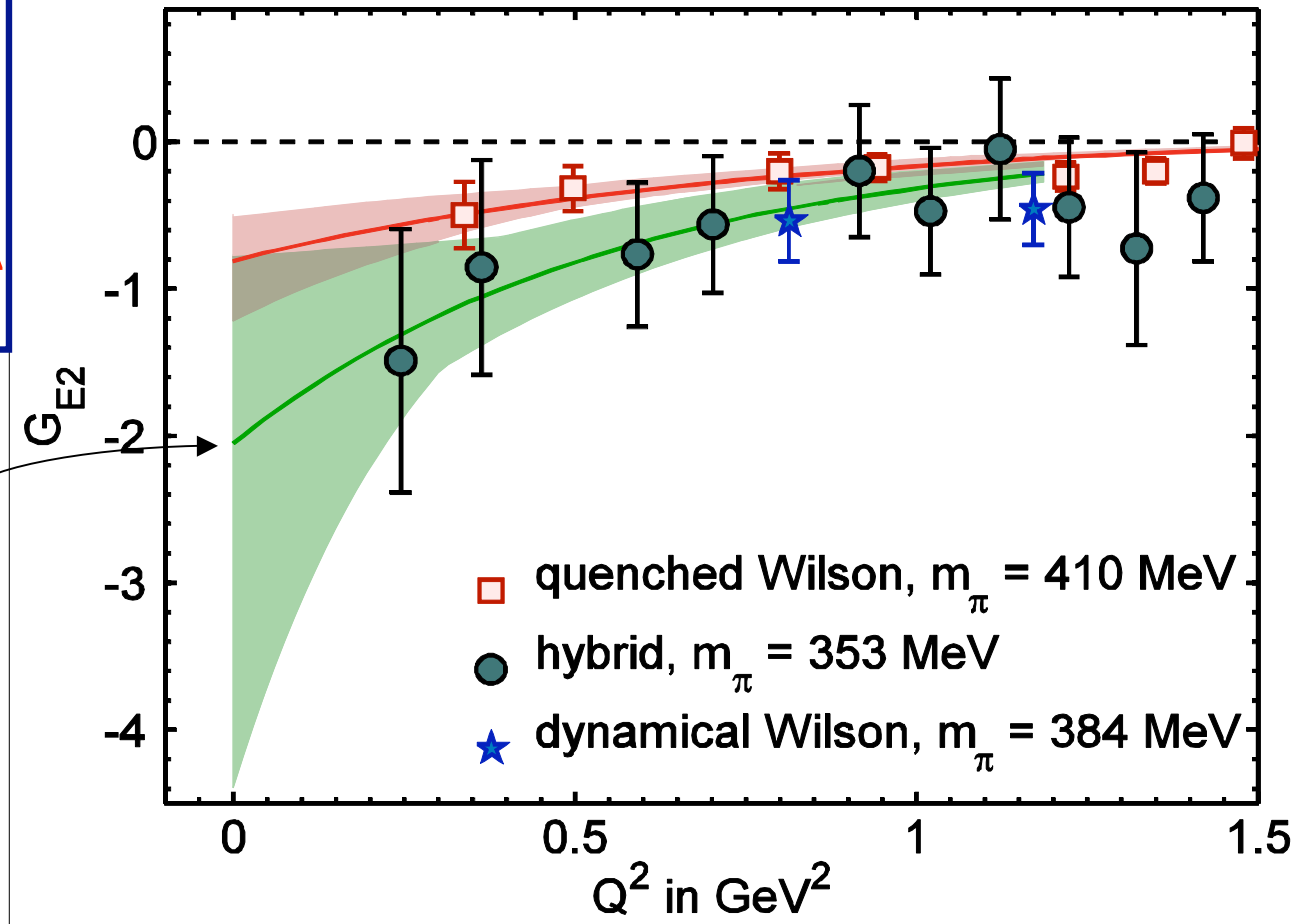
j	$G_{E0}(0)$	$G_{M1}(0)$	$G_{E2}(0)$	$G_{M3}(0)$	$G_{E4}(0)$	$G_{M5}(0)$	$G_{E6}(0)$
0	1	0	0	0	0	0	0
1/2	1	1	0	0	0	0	0
1	1	2	-1	0	0	0	0
3/2	1	3	-3	-1	0	0	0
2	1	4	-6	-4	1	0	0
5/2	1	5	-10	-10	5	1	0
3	1	6	-15	-20	15	6	-1
...							

 transverse charge densities depend only on anomalous values
 of e.m. moments  reflect internal structure

Hadron shape : e.m. Δ to Δ transition



$C0$, $M1$,
 $C2$, $M3$
 transitions



lattice analysis :

quark transverse charge densities in $\Delta(1232)$

$$\rho_{T s_{\perp}}^{\Delta}(\vec{b}) \equiv \int \frac{d^2 \vec{q}_{\perp}}{(2\pi)^2} e^{-i \vec{q}_{\perp} \cdot \vec{b}} \frac{1}{2P^+} \langle P^+, \frac{\vec{q}_{\perp}}{2}, s_{\perp} | J^+(0) | P^+, -\frac{\vec{q}_{\perp}}{2}, s_{\perp} \rangle$$

$$Q_{s_{\perp}}^{\Delta} \equiv e \int d^2 \vec{b} (b_x^2 - b_y^2) \rho_{T s_{\perp}}^{\Delta}(\vec{b})$$

$$Q_{\frac{3}{2}}^{\Delta} = -Q_{\frac{1}{2}}^{\Delta} = \frac{1}{2} \{2 [G_{M1}(0) - 3e_{\Delta}] + [G_{E2}(0) + 3e_{\Delta}]\} \left(\frac{e}{M_{\Delta}^2} \right) \quad s_{\perp} = +3/2$$

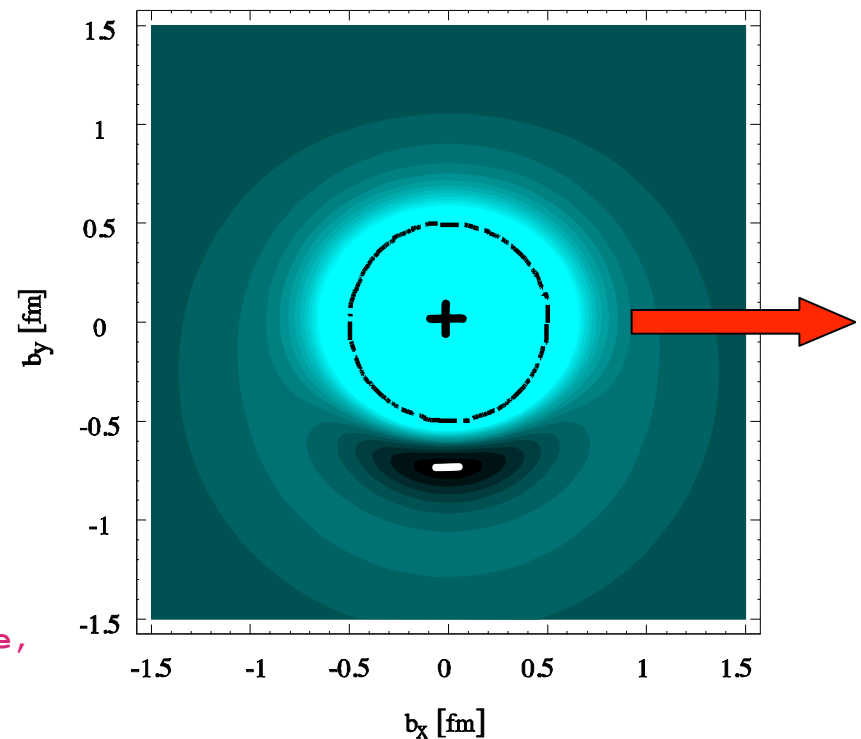
for spin-3/2 point particle

$$G_{M1}(0) = 3e_{\Delta} \quad \text{and} \quad G_{E2}(0) = -3e_{\Delta}$$

transverse charge densities
depend only on anomalous
values of e.m. moments
-> reflect internal structure

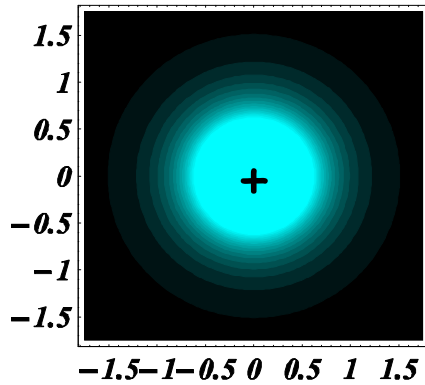
lattice analysis :

Alexandrou, Korzec, Koutsou, Leontiou, Lorcé, Negele,
Pascalutsa, Tsapalis, Vdh (2008)

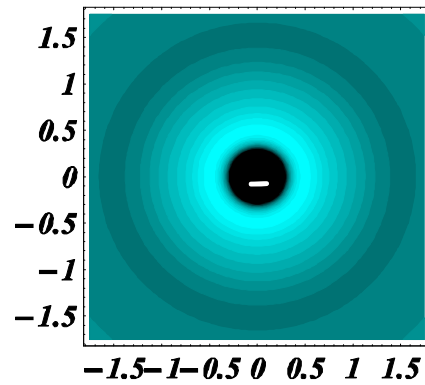


empirical transverse transition densities

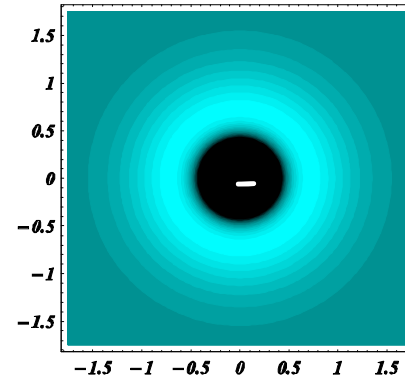
p



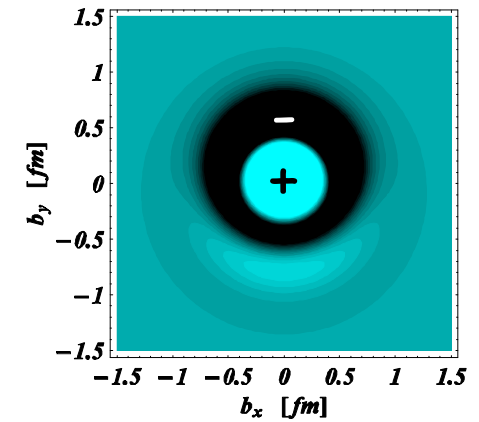
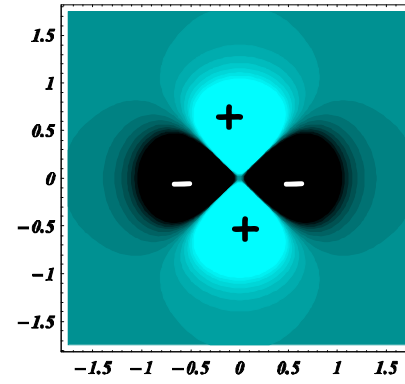
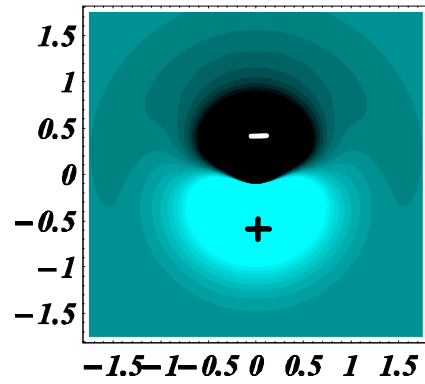
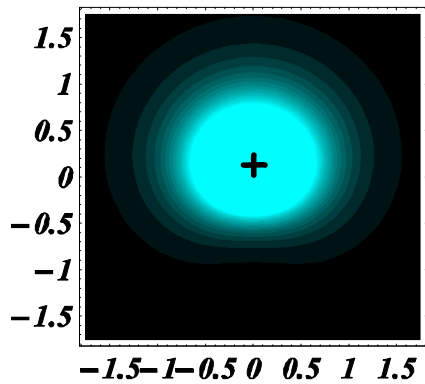
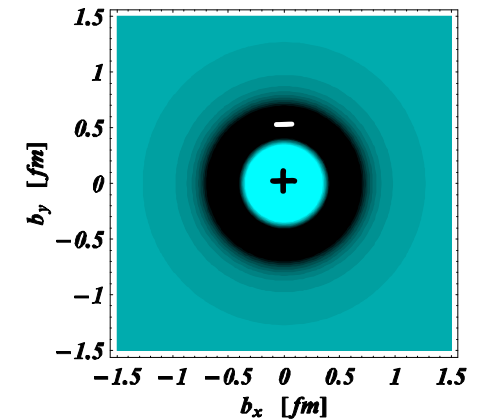
n



p \rightarrow Δ^+ (1232)



p \rightarrow N^* (1440)



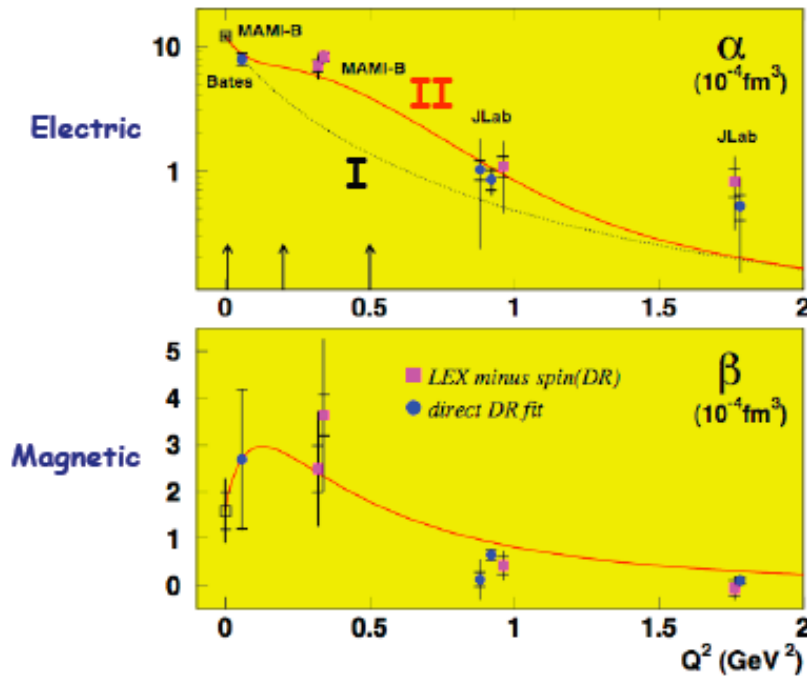
Carlson, Vdh (2007)

quadrupole
pattern

Tiator, Vdh (2008)

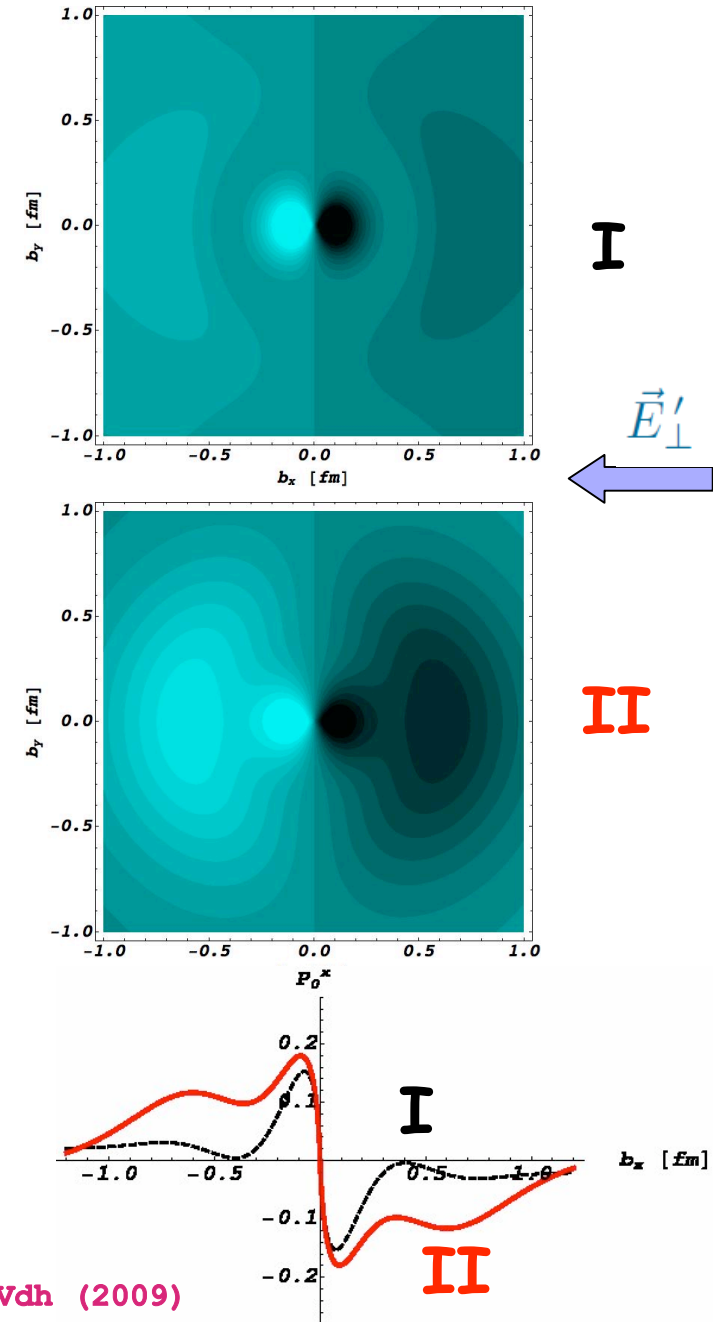
induced polarization in proton

$$\begin{aligned} \vec{P}_0(\vec{b}) &= \int \frac{d^2\vec{q}_\perp}{(2\pi)^2} e^{-i\vec{q}_\perp \cdot \vec{b}} \vec{P}_0(\vec{q}_\perp) \\ &= \hat{b} \int_0^\infty \frac{dQ}{(2\pi)} Q J_1(bQ) A(Q^2) \end{aligned}$$



see talk : Lorcé

Gorchtein, Lorcé, Pasquini, Vdh (2009)

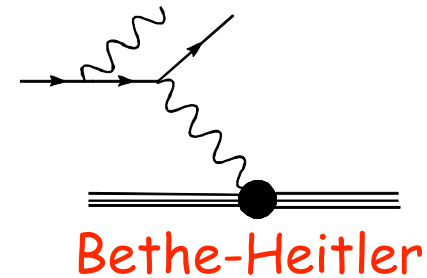
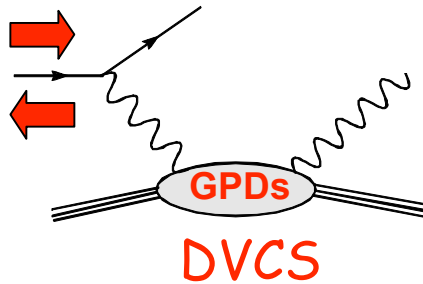




DVCS Observables

★ First observation of DVCS asymmetries in 2000

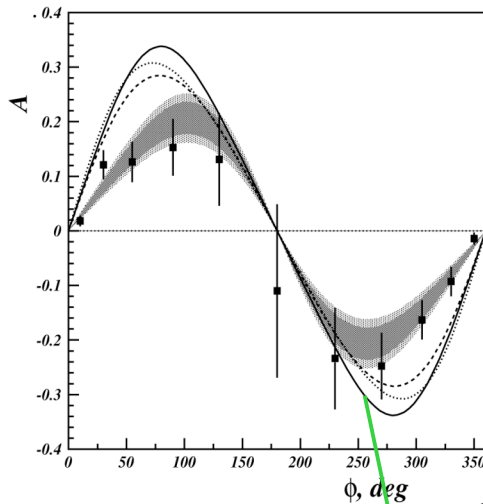
$$A_{LU} = \frac{(BH) * \text{Im}(DVCS) * \sin \Phi}{(BH^2 + DVCS^2)}$$



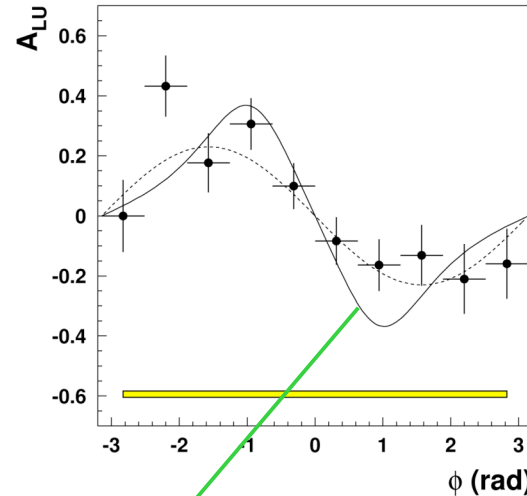
CLAS



$Q^2 = 1.25 \text{ GeV}^2$,
 $x_B = 0.19$,
 $-t = 0.19 \text{ GeV}^2$



PRL 87:182002 (2001)



PRL 87:182001 (2001)

HERMES



$Q^2 = 2.6 \text{ GeV}^2$,
 $x_B = 0.11$,
 $-t = 0.27 \text{ GeV}^2$

twist-2 + twist-3

Vdh, Guichon, Guidal (1999)

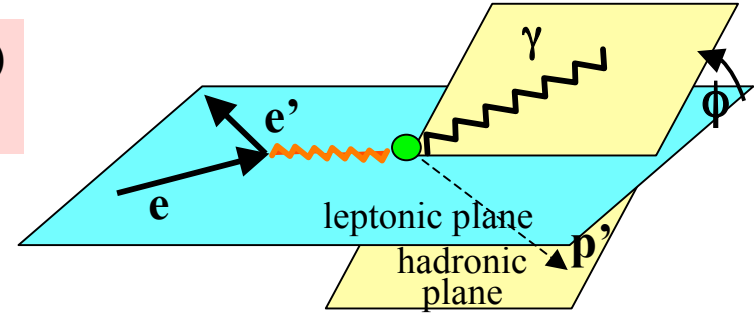
Kivel, Polyakov, Vdh (2000)

Extracting GPDs from DVCS observables

$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

$$\xi = x_B / (2 - x_B)$$

$$k = -t / 4M^2$$



Polarized **beam**, unpolarized **proton** target:

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im} \{ F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E \} d\phi$$

Kinematically suppressed

$$\rightarrow H_p, \tilde{H}_p, E_p$$

Unpolarized beam, **longitudinal proton** target:

$$\Delta\sigma_{UL} \sim \sin\phi \operatorname{Im} \{ F_1 \tilde{H} + \xi(F_1 + F_2)(H + \dots) \} d\phi$$

$$\rightarrow H_p, \tilde{H}_p$$

Unpolarized beam, **transverse proton** target:

$$\Delta\sigma_{UT} \sim \sin\phi \operatorname{Im} \{ k(F_2 H - F_1 E) + \dots \} d\phi$$

$$\rightarrow H_p, E_p$$

Polarized **beam**, unpolarized **neutron** target:

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im} \{ F_1 H + \xi(F_1 + F_2) \tilde{H} - kF_2 E \} d\phi$$

$$\rightarrow H_n, \tilde{H}_n, E_n$$

Suppressed because $F_1(t)$ is small

Suppressed because of **cancellation** between PPD's of **u** and **d** quarks

$$H_p(x, \xi, t) = 4/9 H_u(x, \xi, t) + 1/9 H_d(x, \xi, t)$$

$$H_n(x, \xi, t) = 1/9 H_u(x, \xi, t) + 4/9 H_d(x, \xi, t)$$

In hard exclusive process @ leading twist :
 one accesses 8 GPD quantities
 Observables : Compton Form Factors

$$P \int_0^1 dx [H(x, \xi, t) - H(-x, \xi, t)] C^+(x, \xi), \quad (1)$$

$$P \int_0^1 dx [E(x, \xi, t) - E(-x, \xi, t)] C^+(x, \xi), \quad (2)$$

$$P \int_0^1 dx [\tilde{H}(x, \xi, t) + \tilde{H}(-x, \xi, t)] C^-(x, \xi), \quad (3)$$

$$P \int_0^1 dx [\tilde{E}(x, \xi, t) + \tilde{E}(-x, \xi, t)] C^-(x, \xi), \quad (4)$$

$$H(\xi, \xi, t) - H(-\xi, \xi, t), \quad (5)$$

$$E(\xi, \xi, t) - E(-\xi, \xi, t), \quad (6)$$

$$\tilde{H}(\xi, \xi, t) + \tilde{H}(-\xi, \xi, t), \quad (7)$$

$$\tilde{E}(\xi, \xi, t) + \tilde{E}(-\xi, \xi, t) \quad (8)$$

with

$$C^\pm(x, \xi) = \frac{1}{x - \xi} \pm \frac{1}{x + \xi} \quad (9)$$

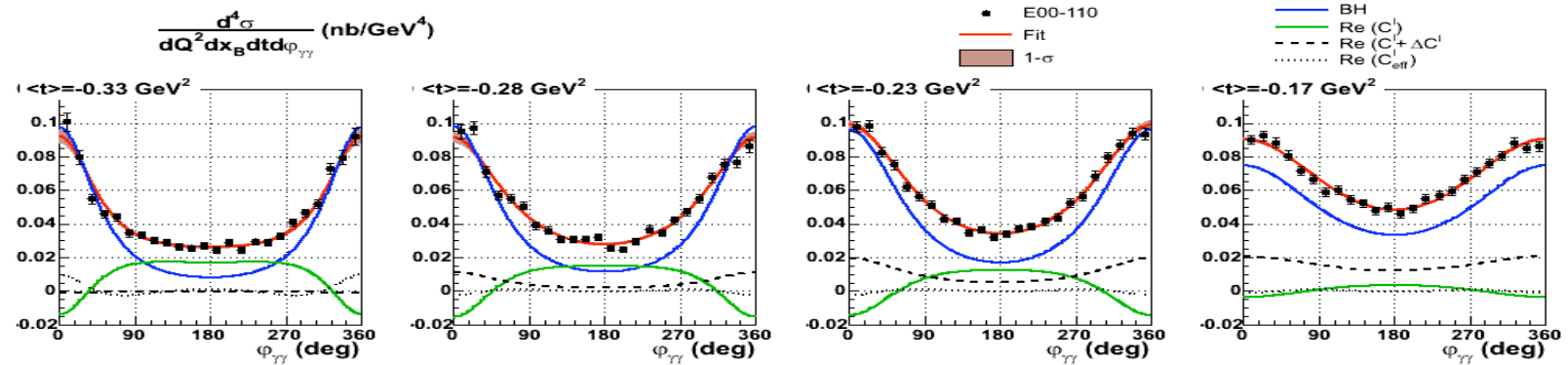
which we can call, respectively, in a symbolic notation,
 $Re(H)$, $Re(E)$, $Re(\tilde{H})$, $Re(\tilde{E})$, $Im(H)$, $Im(E)$, $Im(\tilde{H})$
 and $Im(\tilde{E})$.

DVCS : observables

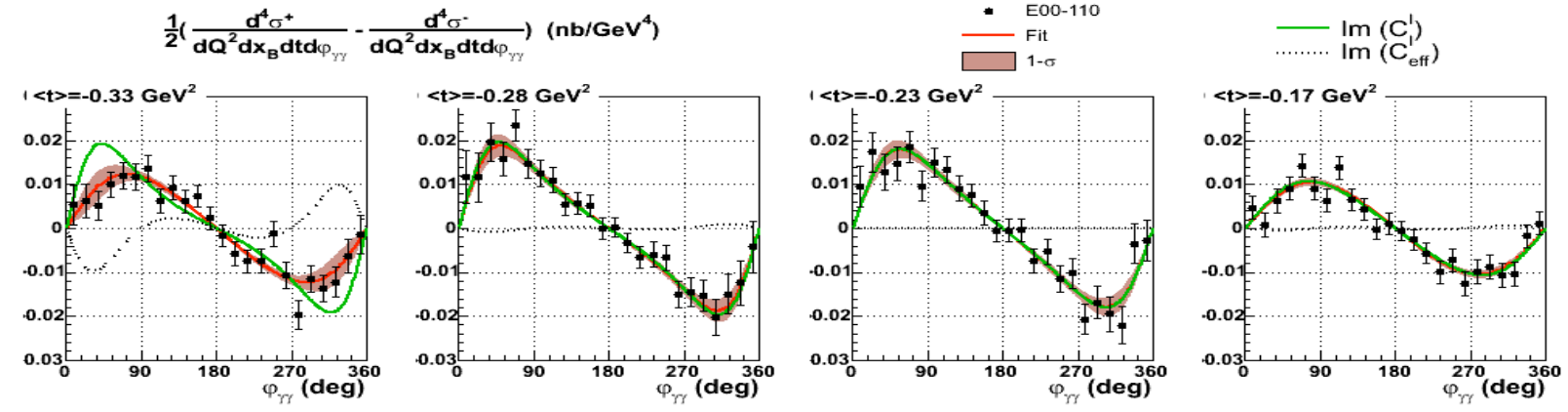
Jlab/Hall A

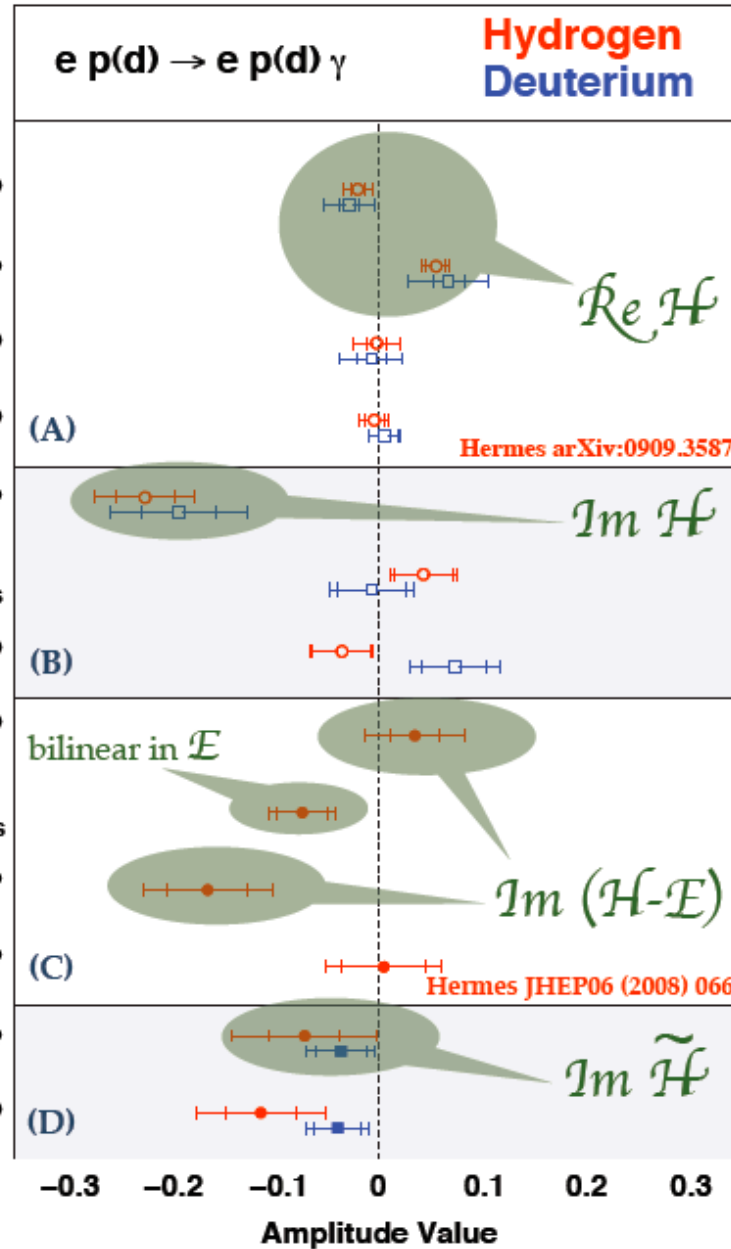


Unpolarized cross sections



Difference of polarized cross sections





DVCS : asymmetries

beam charge asymmetry

beam spin asymmetry

T target spin asymmetry

L target spin asymmetry

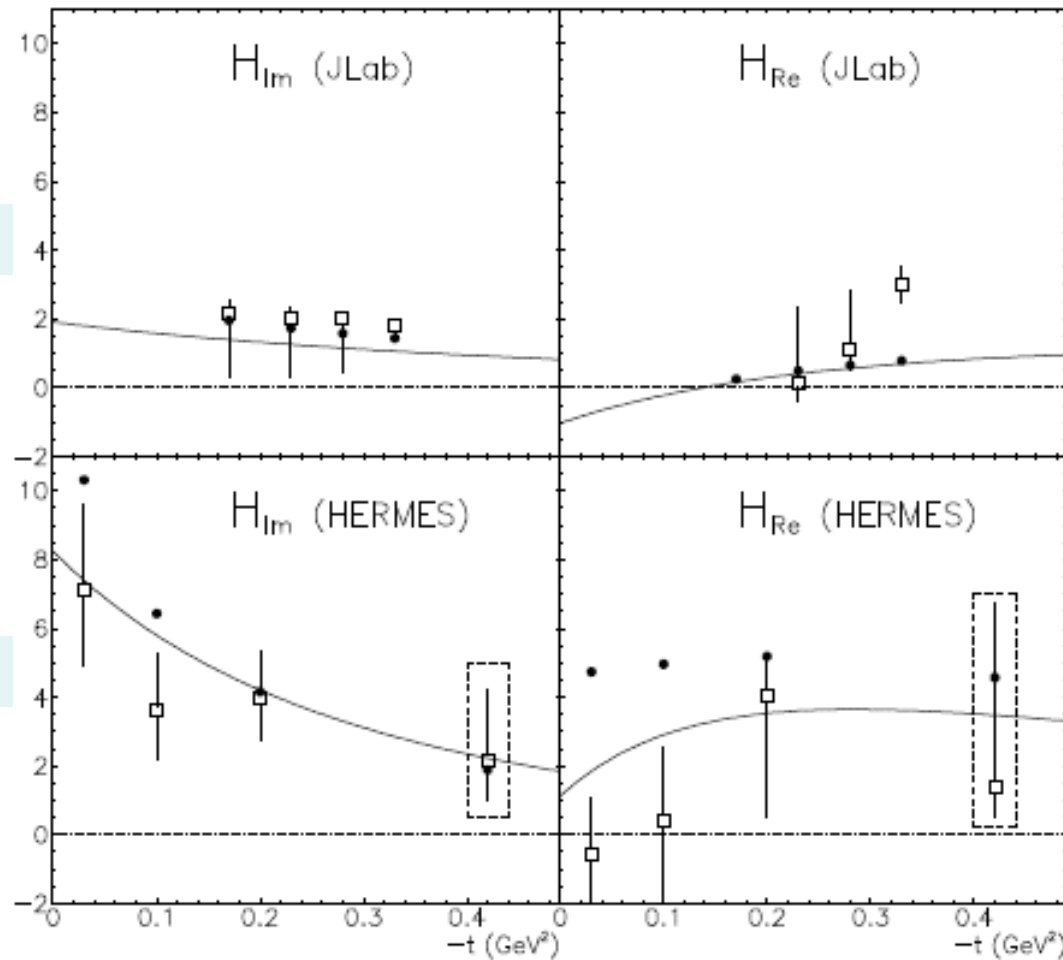
CFF from DVCS : model independent fit extractions (I)

JLab

$x_B=0.36, Q^2=2.3$

HERMES

$x_B=0.09, Q^2=2.5$



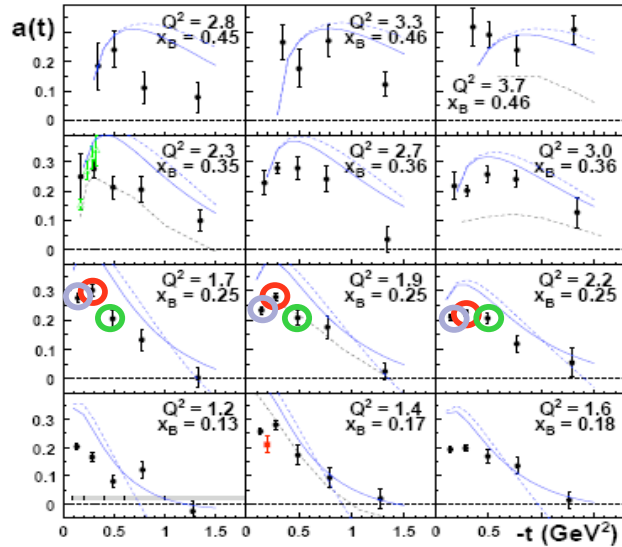
as energy increases:

- ➔ « Shrinkage » of $\text{Im}(H)$
- ➔ $\text{Im}(H) > \text{Re}(H)$
- ➔ different t -behavior for $\text{Im}(H)$ & $\text{Re}(H)$

solid circles :
VGG (1998)

model dependent
fit of
D. Muller,
K. Kumericki (2009)

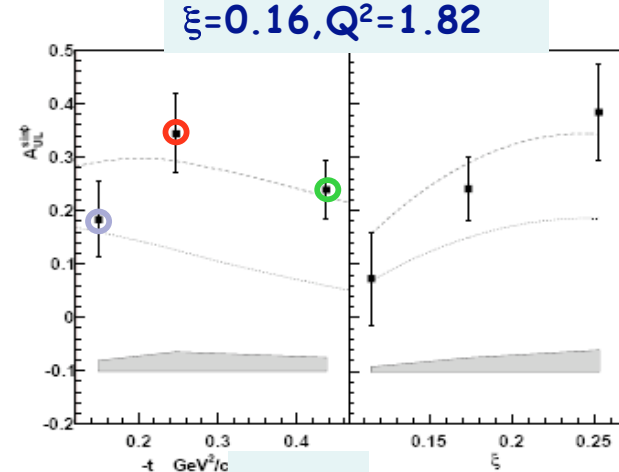
CFF from DVCS : fits (II)



Jlab/CLAS

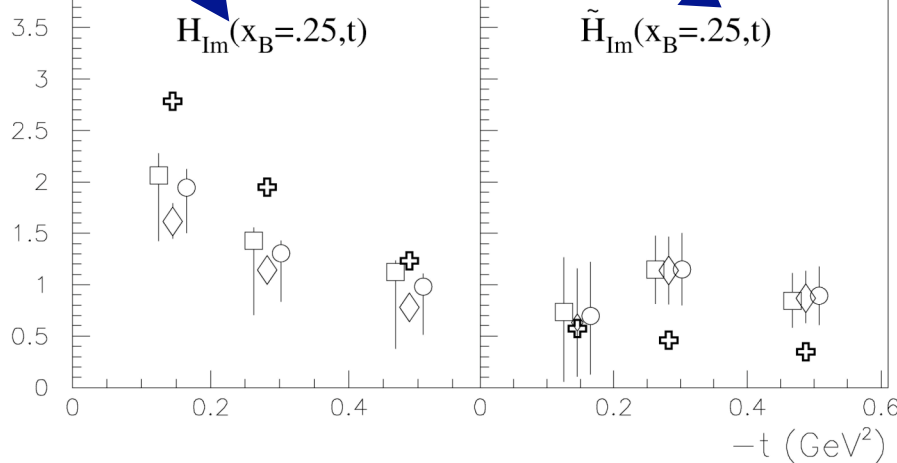
← Girod et al. (2006)

Chen et al. → (2008)



A_{UL}

A_{LU}

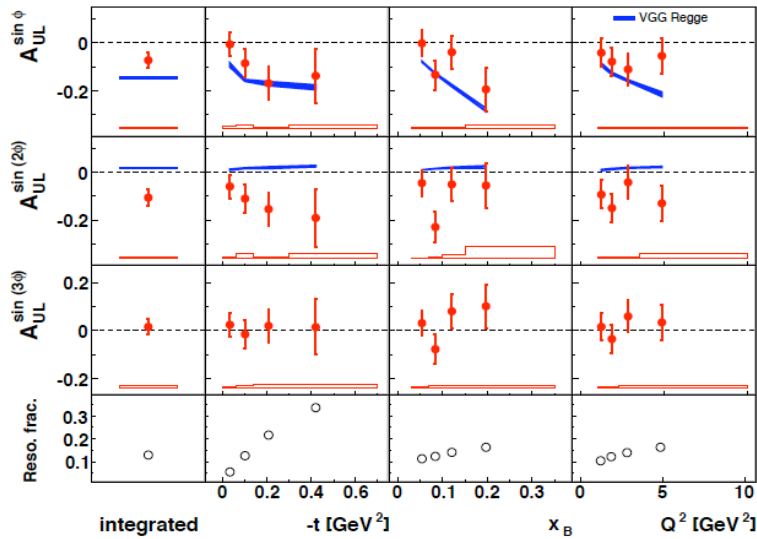


- Fit with **7 CFFs** (bounds 5xVGG CFFs)
- Fit with **7 CFFs** (bounds 3xVGG CFFs)
- ◇ Fit with **ONLY \tilde{H} and H CFFs**
- ⊕ **VGG prediction**

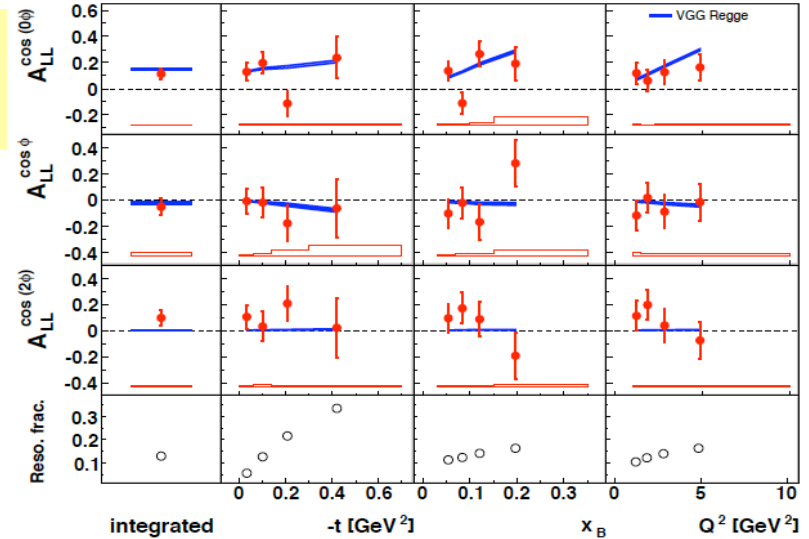
Guidal (2010)

arXiv:1003.0307 [hep-ph]

CFF from DVCS : fits (III)

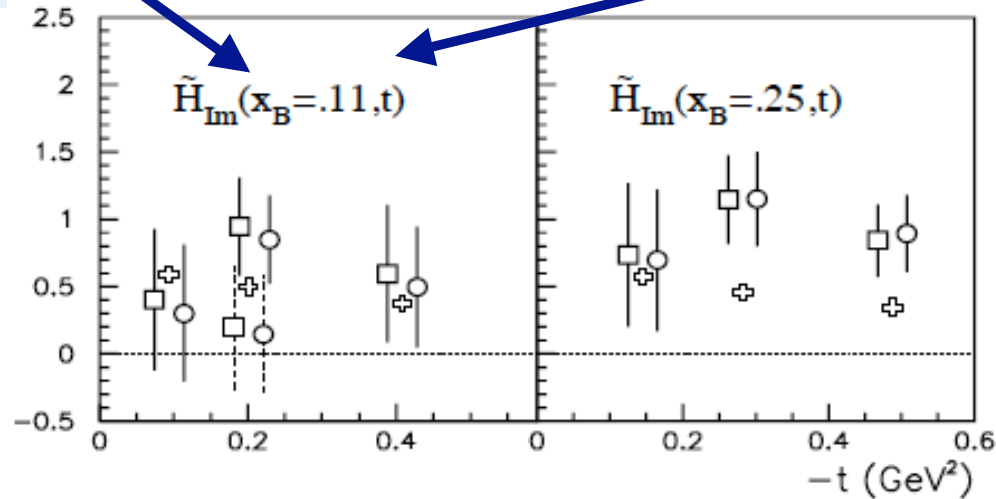


HERMES
(2010)



A_{UL}

A_{LL}



Guidal (2010)

open crosses :
VGG (1998)

Dispersion Relations for DVCS

→ once subtracted **fixed- t** dispersion relation in variable x

$$ReA(\xi, t) = \Delta(t) + \frac{2}{\pi} PV \int_0^1 \frac{dx}{x} \frac{ImA(x, t)}{(\xi^2/x^2 - 1)}$$

↑
subtraction constant

↙ accessible through spin asymmetries

→ link with twist-2 GPD : $ImA(x, t) = \pi H^{(+)}(x, x, t)$

$$ReA(\xi, t) = \Delta(t) - PV \int_0^1 dx H^{(+)}(x, x, t) \left[\frac{1}{x - \xi} + \frac{1}{x + \xi} \right]$$

DR for DVCS amplitudes (in terms of GPDs)

see talk : Mueller

Anikin, Teryaev (2007)

Diehl, Ivanov (2007)

Polyakov, Vdh (2008)

Kumericki-Passek, Mueller, Passek (2008)

Goldstein, Liuti (2009) ...

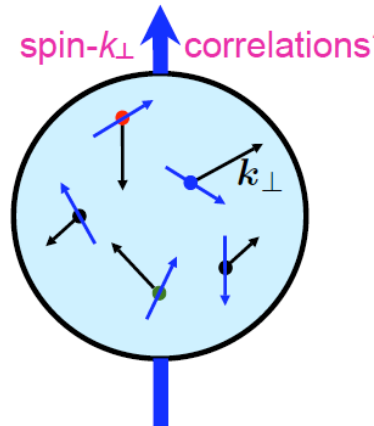
DR for 12 VCS amplitudes : Drechsel, Gorchtein, Metz, Pasquini, Vdh (2000)

Transverse Momentum Dependent Parton distributions

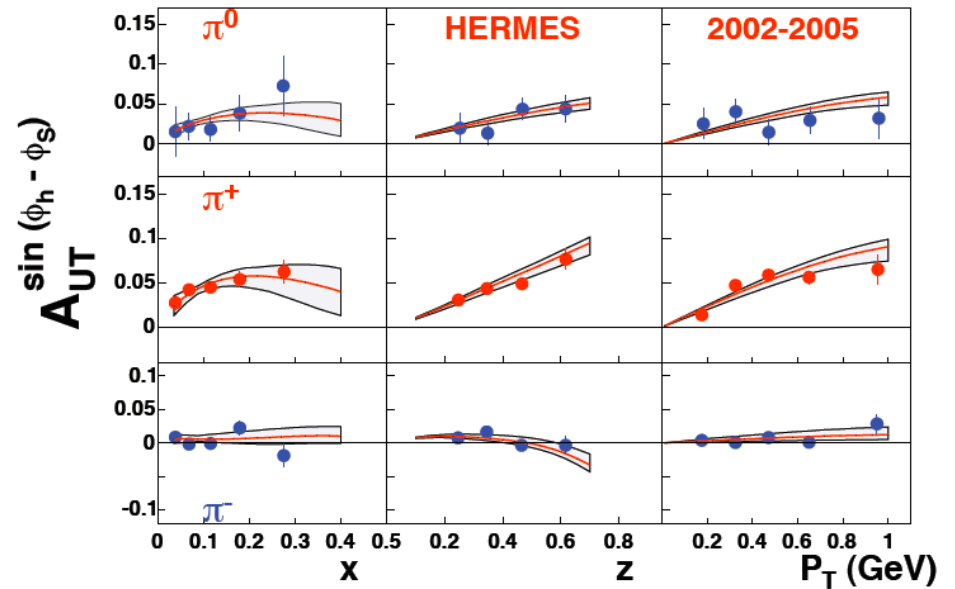
Quark distribution functions

		quark		
		U	L	T
n o e - c u n	U	f_1		h_1^\perp -
	L		g_1 -	h_{1L}^\perp -
	T	f_{1T}^\perp -	g_{1T}^\perp -	h_1 - h_{1T}^\perp -

Sivers DF

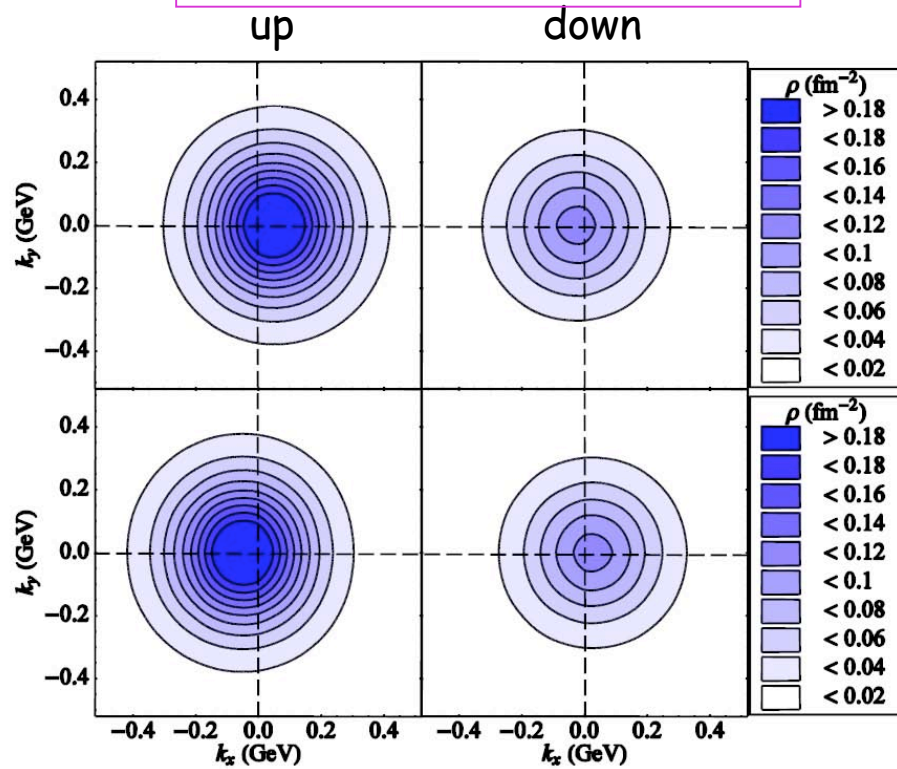


accessible in
semi-inclusive DIS



theory curves : Anselmino et al. (2009)

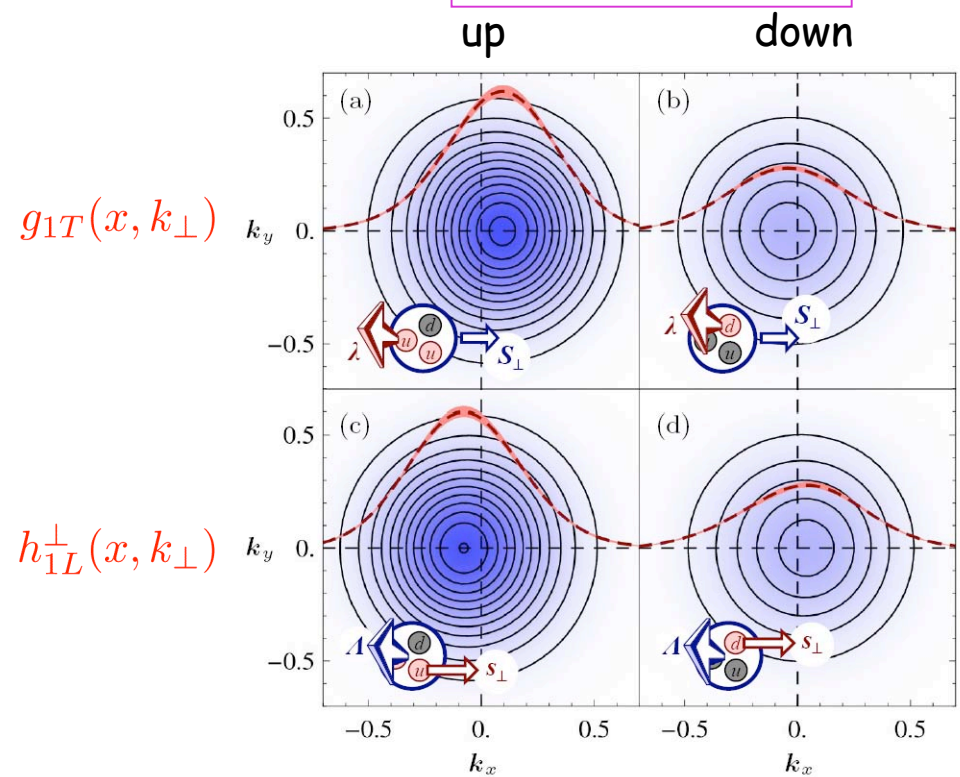
Light-cone quark model



BP, Cazzaniga, Boffi, PRD78 (2008)

$$\langle k_x^u \rangle = 55.8 \text{ MeV} \quad \langle k_x^d \rangle = -27.9 \text{ MeV}$$

Lattice QCD



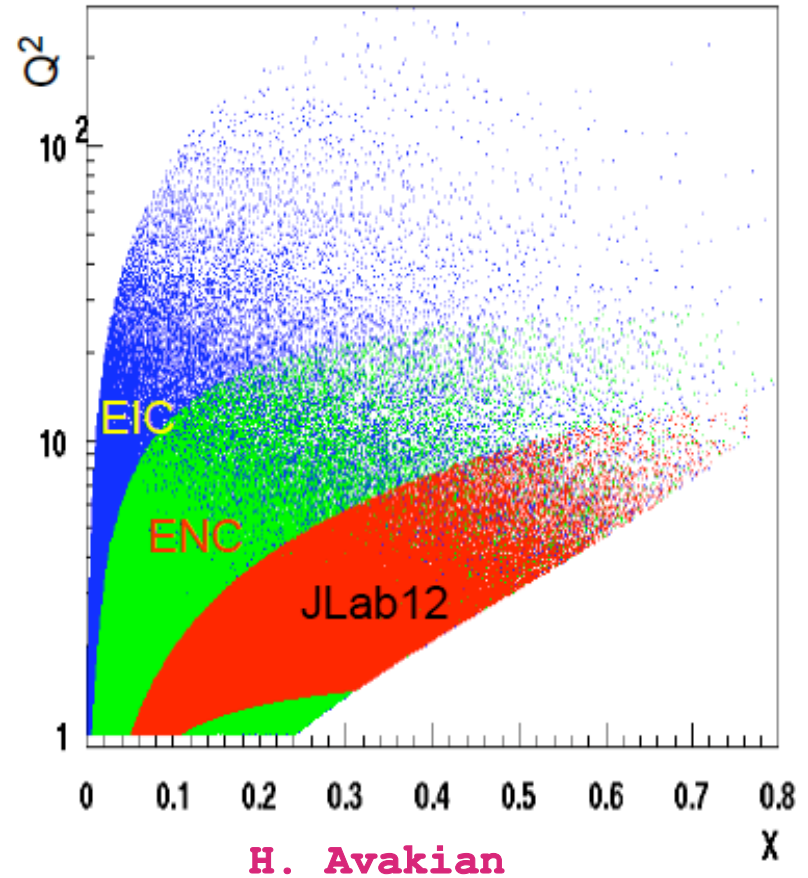
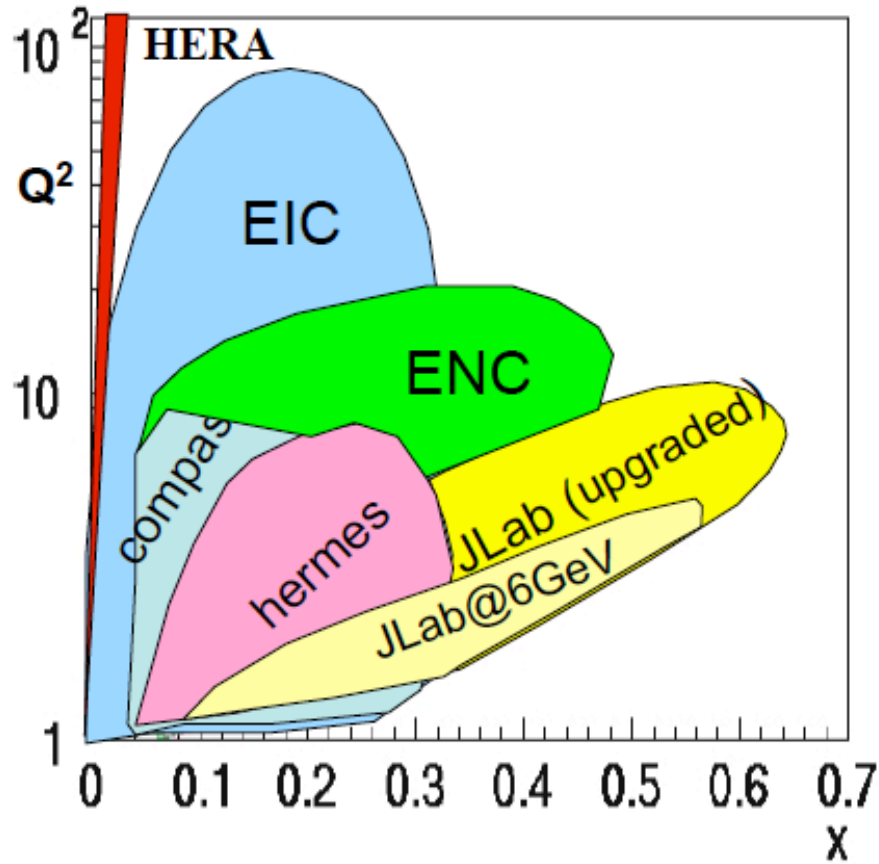
Haegler, Musch, Negele, Schaefer, Europhys. Lett. 88 (2009)

$$\langle k_x^u \rangle = 67(5) \text{ MeV} \quad \langle k_x^d \rangle = -30(5) \text{ MeV}$$

❖ g_{1T}, h_{1L}^\perp ~~↔~~ GPDs \Rightarrow genuine effect of intrinsic transverse momentum of quarks

see talks : Pasquini, Musch

The Energy / Luminosity Frontier



Hard exclusive reactions :
high energy and high luminosity required + polarization