

Measurement of Collins Asymmetries in e^+e^- Annihilation at Belle

Workshop on Exclusive Reactions at

High Momentum Transfer

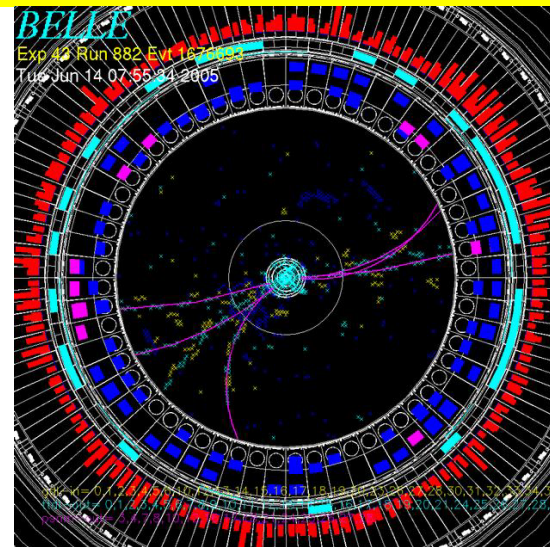
May 24th , Thonon-les-Bains Laboratory

[Sandorfi](talks/Sandorfi.pdf)

D. Gabbert
M. G. Perdekamp
K. Hasuko
S. Lange
M. Leitgab
D. Mertens
A. Ogawa
R. Seidl
V. Siegle

Illinois and RBRC
Illinois and RBRC
RIKEN and RBRC
Frankfurt
Illinois
Illinois
BNL and RBRC
Illinois and RBRC
RBRC

for the Belle Collaboration



○ Motivation

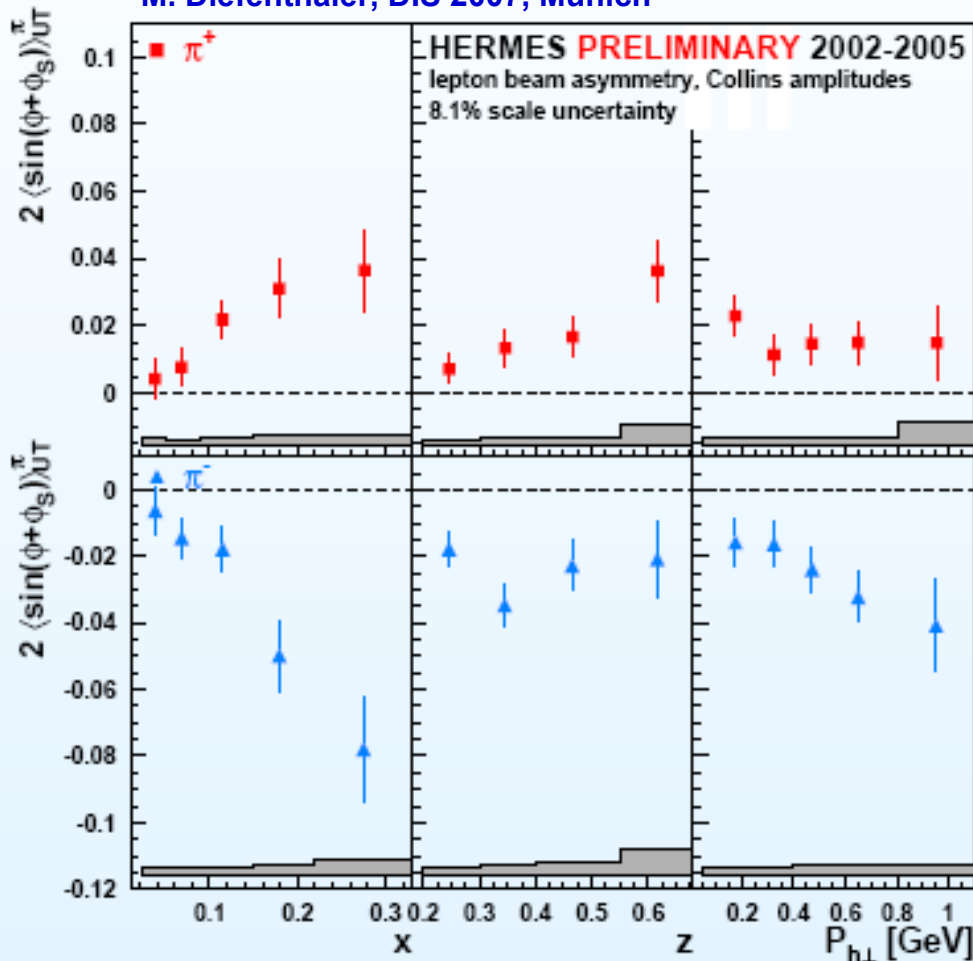
- Collins FF for global QCD analysis of single transverse asymmetries in pp and SIDIS

○ Collins Asymmetries from e^+e^-

- LEP first work on Delphi data in the 90s:
Efremov, Smirnova, Tkatchev and Bonivento, Matteuzzi, Kotzinian
- Experimental technique
- Results

Motivation Transversity Quark Distributions from Collins- and Interference-Fragmentation

New HERMES results for Collins Asymmetries
M. Diefenthaler, DIS 2007, Munich



Collins- and IFF- asymmetries in SIDIS and pp are of the form

$$\sim \text{Transversity}(x) \times \text{CFF}(z)$$

$$\sim \text{Transversity}(x) \times \text{IFF}(z)$$

Collins- and IFF- asymmetries in e^+e^- are of the form

$$\sim \text{CFF}(z_1) \times \text{CFF}(z_2)$$

$$\sim \text{IFF}(z_1) \times \text{IFF}(z_2)$$

→ global QCD analysis



Extract Transversity Distributions

SIDIS \Rightarrow

transversity \times Collins

transversity \times IFF

HERMES, COMPASS,

JLAB, EIC

Factorization

+

Universality ?!

$e^+e^- \Rightarrow$ Collins \times Collins

Interference FF

\times Interference FF

Belle

Transversity
Tensor Charge

RHIC / GSI

pp \Rightarrow

A_N for inclusive hadrons, Jets

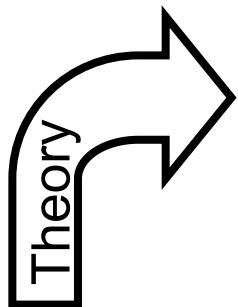
A_T in Jets : transversity \times Collins

transversity \times IFF

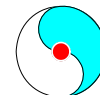
GSI

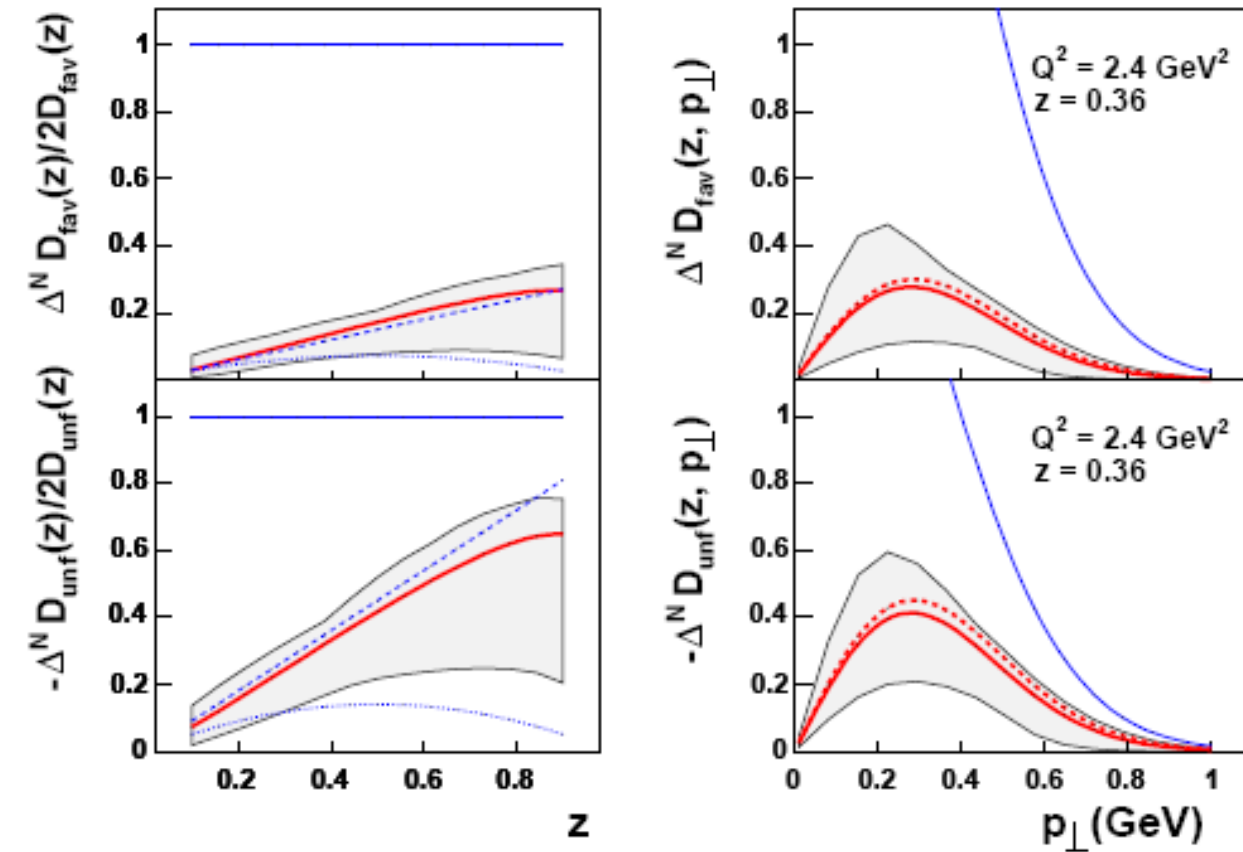
A_{TT} Drell Yan :

transversity \times transversity



Lattice QCD: Tensor Charge





Fit includes:

HERMES SIDIS
+ COMPASS SIDIS
+ Belle e^+e^-

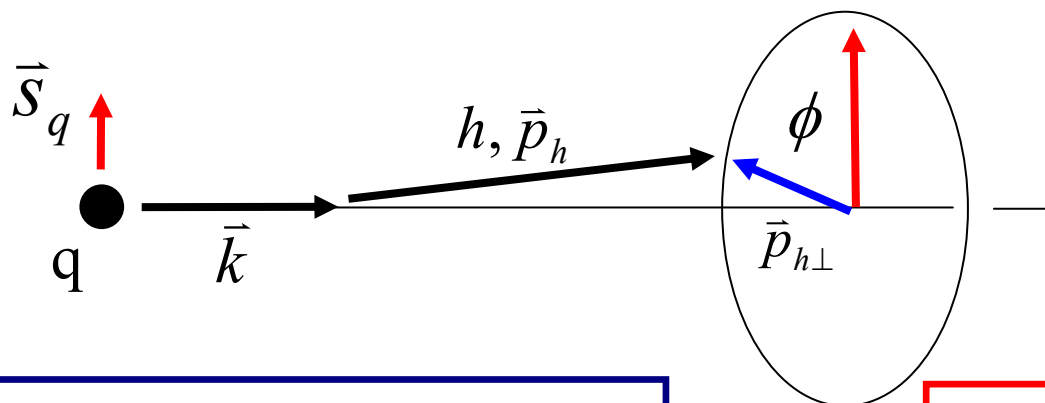
→ transversity dist.
+ Collins FF

Measurement of Collins Asymmetries In e^+e^- at KEK B with the Belle

Phys.Rev.Lett.96:232002,2006
and update at Spin 2006 in Kyoto

Collins Effect in Quark Fragmentation

J.C. Collins, Nucl. Phys. B396, 161(1993)



\vec{k} : quark momentum
 \vec{s}_q : quark spin
 \vec{p}_h : hadron momentum
 $\vec{p}_{h\perp}$: transverse hadron momentum
 $z_h = E_h/E_q$
 $= 2 E_h/\sqrt{s}$: relative hadron momentum

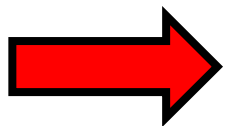
Collins Effect:
 Fragmentation of a transversely polarized quark q into spin-less hadron h carries an azimuthal dependence:
 $\propto (\vec{k} \times \vec{p}_{h\perp}) \cdot \vec{s}_q$
 $\propto \sin \phi$

Number density for finding hadron h from a transversely polarized quark, q :

$$D_{q\uparrow}^h(z, \vec{p}_{h\perp}) = \underbrace{D_1^{q,h}(z)}_{\text{unpolarized FF}} + \underbrace{H_1^{\perp q,h}(z, p_{h\perp}^2)}_{\text{Collins FF}} \frac{(\hat{k} \times \vec{p}_{h\perp}) \cdot \vec{s}_q}{zM_h}$$

Collins FF in e^+e^- : Need Correlation between Hemispheres !

- Quark spin direction unknown: measurement of Collins function in one hemisphere is not possible $\sin \varphi$ modulation will average out.
- Correlation between two hemispheres with $\sin \varphi_i$ Collins single spin asymmetries results in $\cos(\varphi_1 + \varphi_2)$ modulation of the observed di-hadron yield.



Measurement of azimuthal correlations for pion pairs around the jet axis in two-jet events!



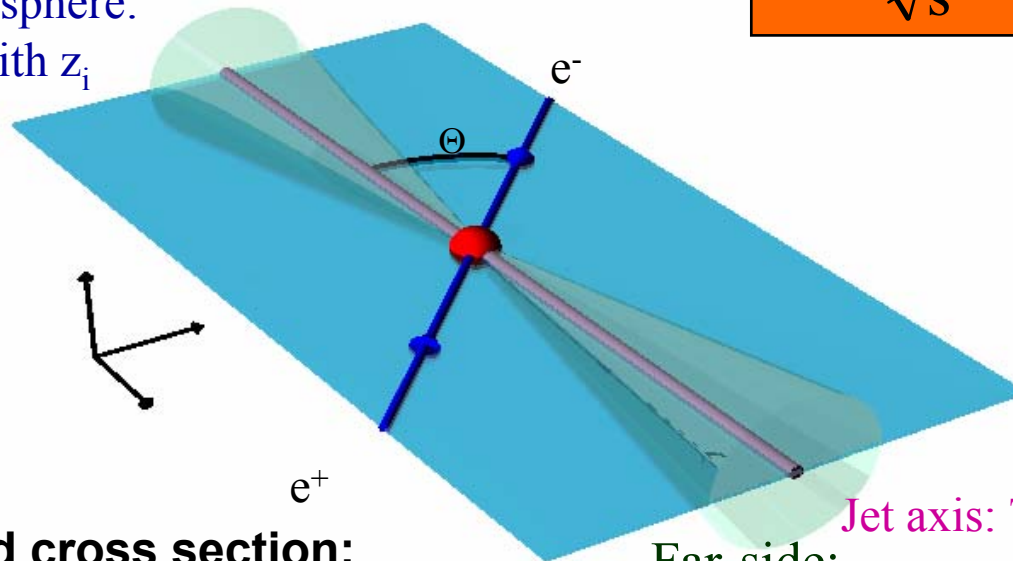
Event Structure at Belle

e^+e^- CMS frame:

$$z = \frac{2E_h}{\sqrt{s}}, \quad \sqrt{s} = 10.52 \text{ GeV}$$

Near-side Hemisphere:

$h_i, i=1, N_n$ with z_i



$$\langle N_{h+,-} \rangle = 6.4$$

Spin averaged cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2} = \frac{3\alpha^2}{Q^2} A(y) \sum_{a, \bar{a}} e_a^2 D_1(z_1) \bar{D}_1(z_2)$$

$$A(y) = \left(\frac{1}{2} - y + y^2 \right)^{(cm)} = \frac{1}{4} (1 + \cos^2 \Theta)$$

Far-side:

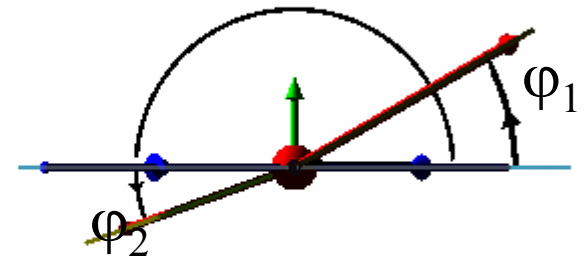
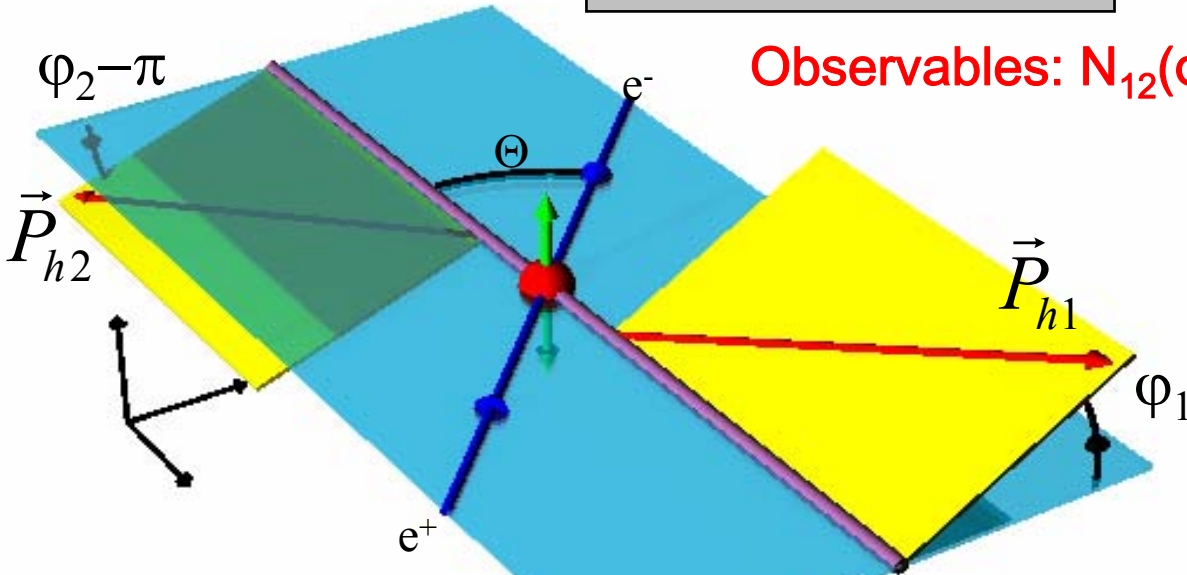
$h_j, j=1, N_f$ with z_j

Jet axis: Thrust

Collins Fragmentation: Angles and Cross Section $\cos(\phi_1 + \phi_2)$ Method

e^+e^- CMS frame:

Observables: $N_{12}(\phi_1 + \phi_2)$, $A_{12}(z_1, z_2)$



2-hadron inclusive transverse momentum dependent cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2q_T} = \dots B(y) \cos(\phi_1 + \phi_2) H_1^{\perp[1]}(z_1) \bar{H}_1^{\perp[1]}(z_2)$$

$$B(y) = y(1-y)^{\text{cm}} = \frac{1}{4} \sin^2 \Theta$$

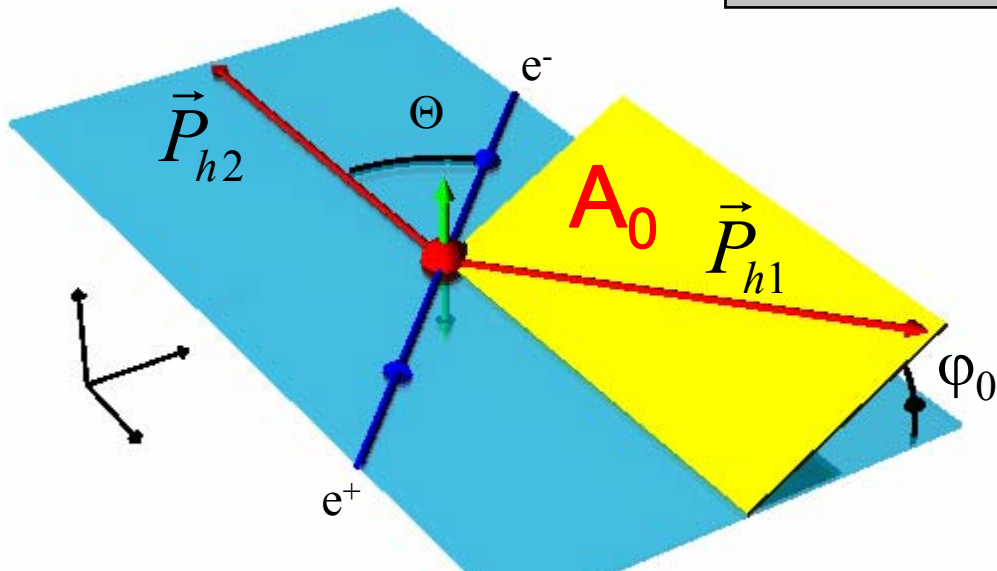
Net anti-alignment of
transverse quark spins



Collins Fragmentation: Angles and Cross Section $\cos(2\phi_0)$ Method

Observables: $N_0(\phi_0)$, $A_{12}(z_1, z_2)$

e^+e^- CMS frame:



- Independent of thrust-axis
- Convolution integral I over transverse momenta involved

[Boer, Jakob, Mulders:
NPB504(1997)345]

2-hadron inclusive transverse momentum dependent cross section:

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2q_T} = \dots B(y) \cos(2\phi_0) I \left[\left(2\hat{h} \cdot k_T \hat{h} \cdot p_T - k_T \cdot p_T \right) \frac{H_1^\perp \bar{H}_1^\perp}{M_1 M_2} \right]$$

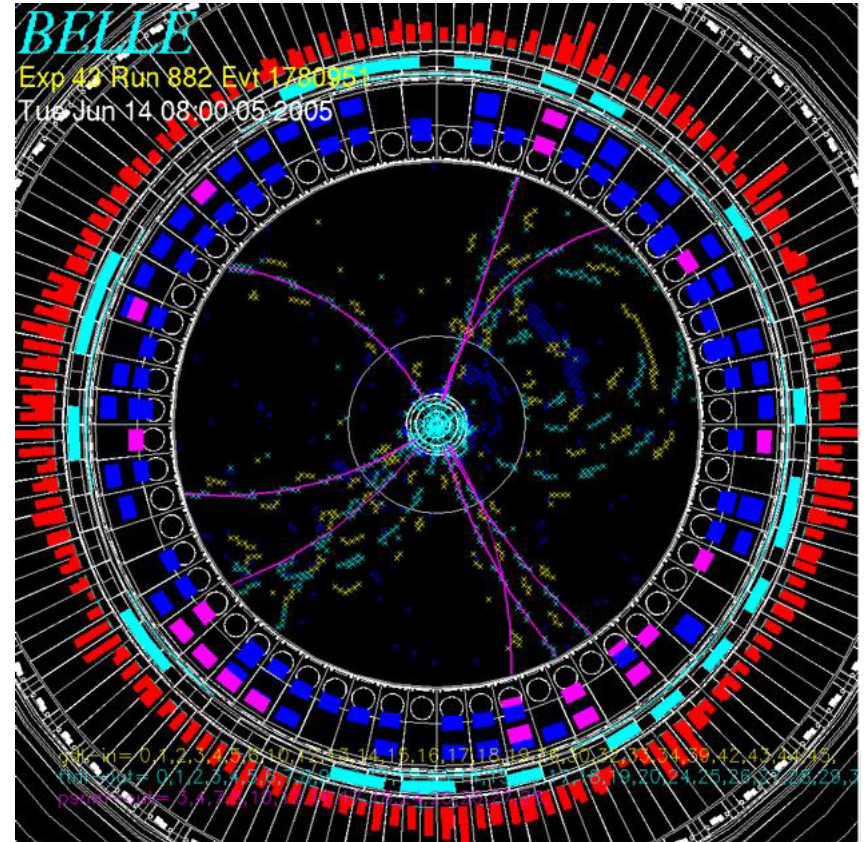
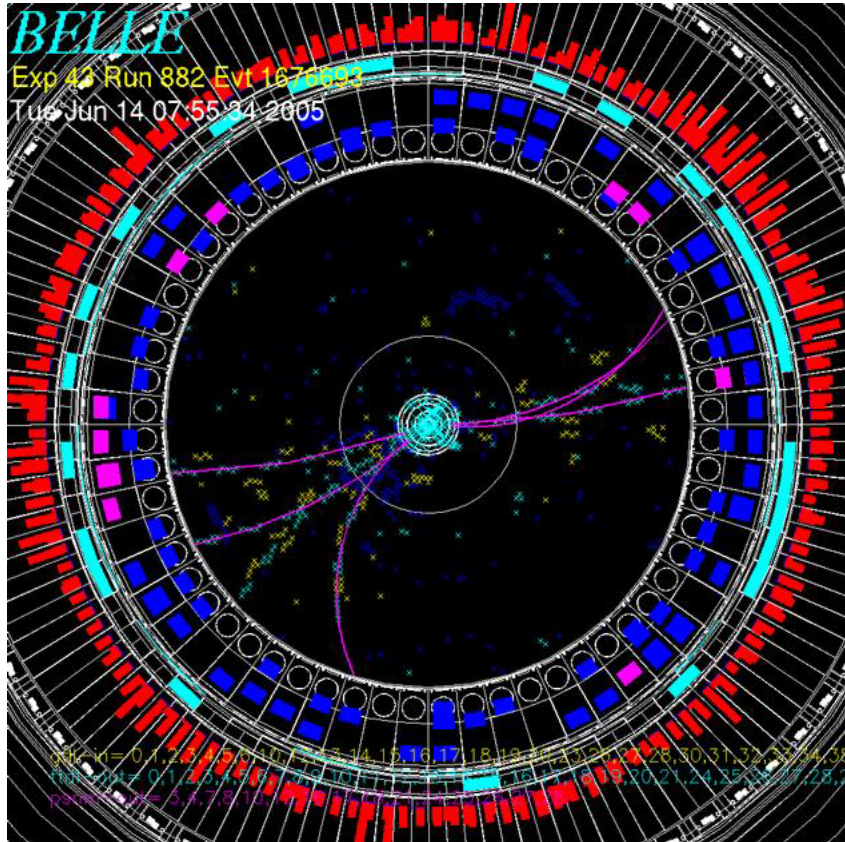
$$B(y) = y(1-y) \stackrel{\text{cm}}{=} \frac{1}{4} \sin^2 \Theta$$

Net anti-alignment of
transverse quark spins



Hadronic Events observed with Belle

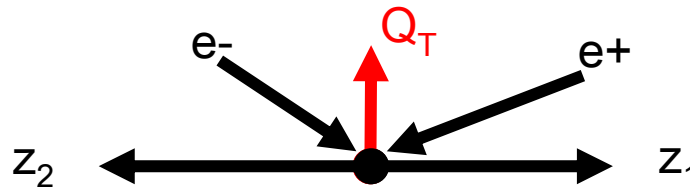
→ 1.5×10^9 hadronic events in analysis



On resonance: 547fb^{-1} , $\sqrt{s}=10.52 \text{ GeV}$ (*published*)
Off resonance: 29fb^{-1} , $\sqrt{s}=10.58 \text{ GeV}$ (*preliminary*)

Gluon Emission

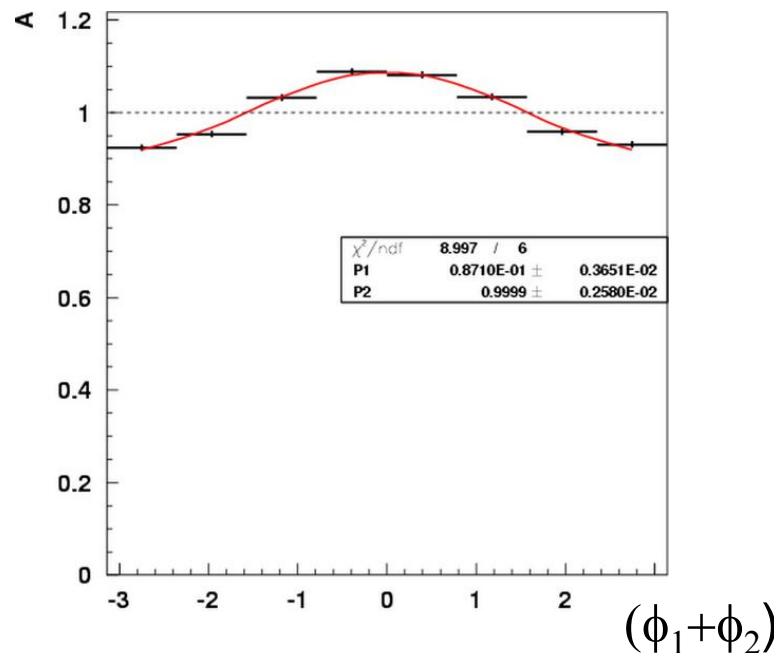
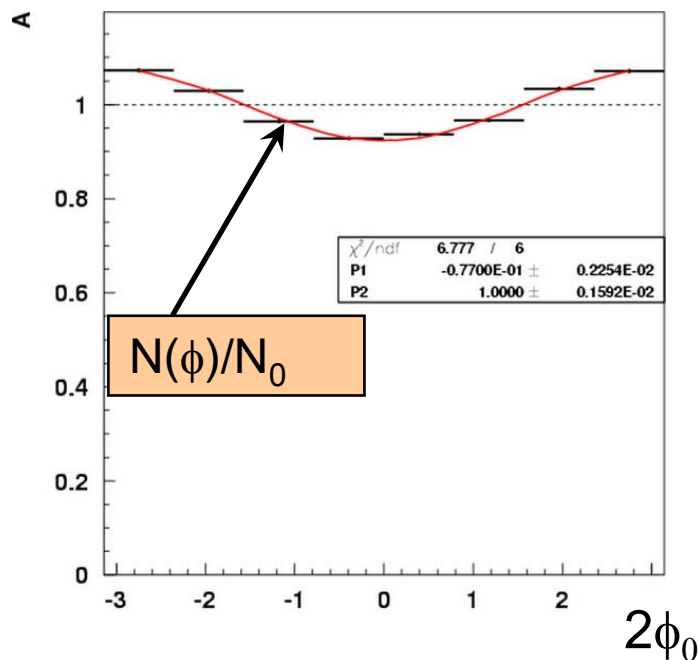
$$\frac{dN}{d\Omega dz_1 dz_2 dq_T} \propto \sum \left[\frac{q_T^2}{Q^2 + Q_T^2} \sin^2 \theta \cos(2\phi_0) D_1(z_1) \bar{D}_1(z_2) \right]$$



Frame:

$$\vec{p}_1 = -\vec{p}_2$$

Examples of Fits to Azimuthal Asymmetries



$$\frac{N(\phi)}{N_0} = \frac{aD_1\overline{D_1} + \cos(2\phi) (bH_1\overline{H_1} + cD_1\overline{D_1})}{aD_1\overline{D_1}} = P2 + P1 \cos(2\phi)$$

D_1 : spin averaged fragmentation function,

H_1 : Collins fragmentation function

Method to eliminate gluon contributions: Double ratios for unlike- and like sign pions

Double ratio method:

$$R := \frac{\frac{N^{Unlike}(\phi)}{N_0^{Unlike}}}{\frac{N^{Like}(\phi)}{N_0^{Like}}} \approx 1 + F \left(\frac{H_1^{\perp, fav}(z)}{D_1^{fav}(z)}, \frac{H_1^{\perp, unfav}(z)}{D_1^{unfav}(z)} \right) + \mathcal{O}(F(Q_T)^2)$$

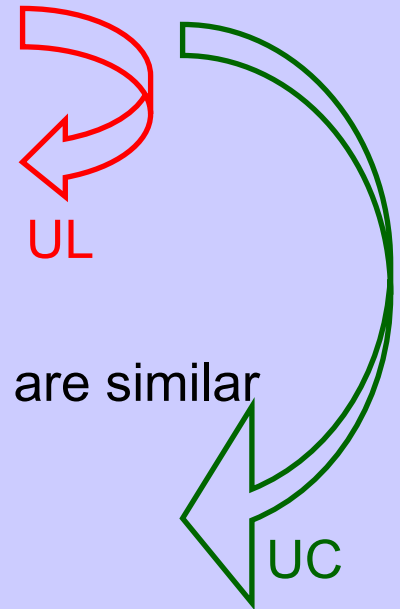
$$F \sim \frac{\sin^2(\theta)}{1 + \cos^2(\theta)} \left[\frac{\sum_q e^2 (H^{Fav} \cdot \bar{H}^{Fav} + H^{Unf} \cdot \bar{H}^{Unf})}{\sum_q e^2 (D^{Fav} \cdot \bar{D}^{Fav} + D^{Unf} \cdot \bar{D}^{Unf})} \right] \cos(\phi_0)$$

$$\longleftrightarrow A_0(z_1, z_2) \longrightarrow$$

Two Double Ratios

Double ratios unlike/like-sign not very sensitive in separating favored and disfavored Collins functions → look at unlike-sign/charge-sum

- Unlike-sign pion pairs (U):
(favored x favored + unfavored x unfavored)
- Like-sign pion pairs (L):
(favored x unfavored + unfavored x favored)
- $\pi^\pm\pi^0$ pairs
(favored + unfavored) x (favored + unfavored)
- A. Efremov et al. ([hep-ph/0603054]): charged $\pi\pi$ pairs are similar (and easier to handle) (C):
(favored + unfavored) x (favored + unfavored)

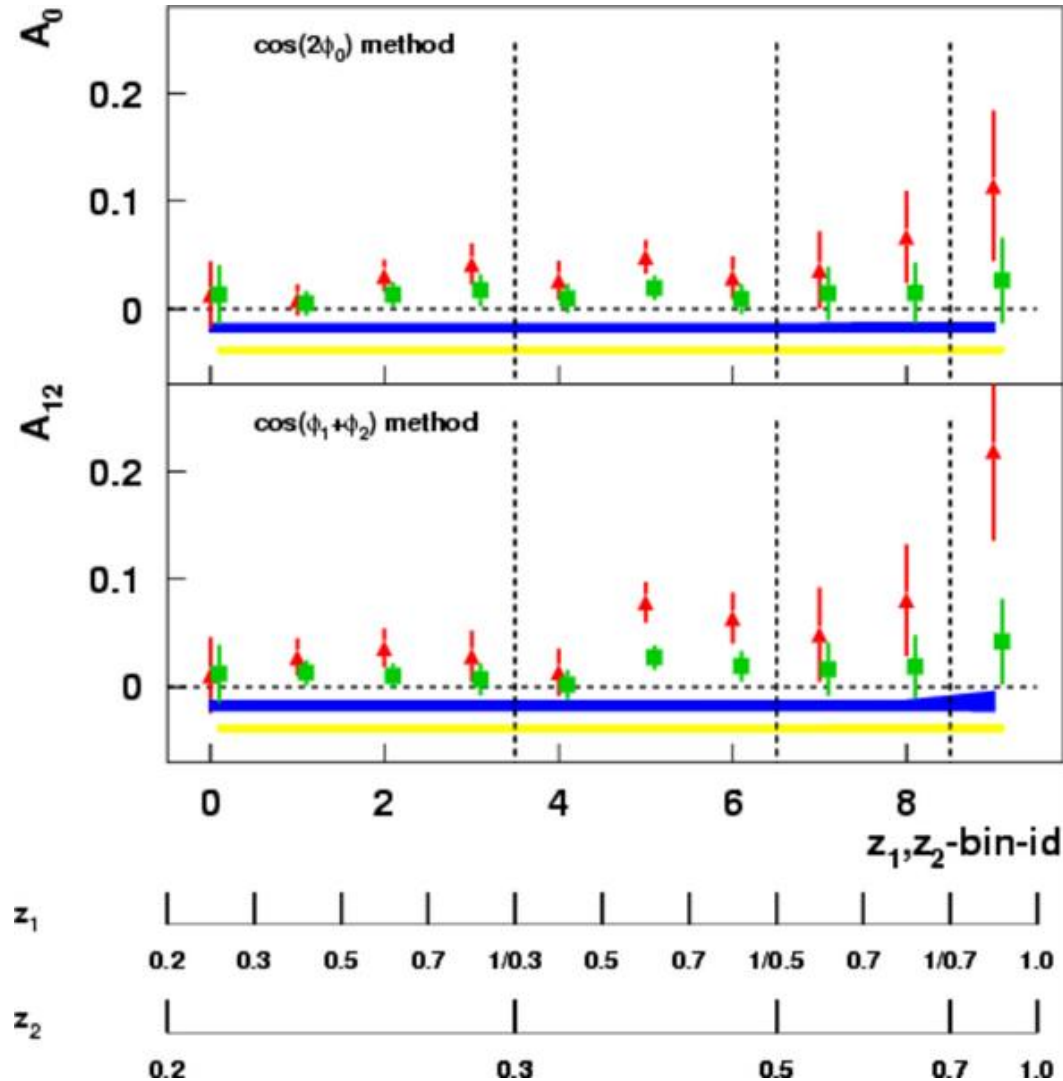


Observables:

$$\begin{array}{c}
 A_{12}(\text{UL}), A_{12}(\text{UC}) \\
 A_0(\text{UL}), A_0(\text{UC})
 \end{array}$$

published and input to fit by Anselmino et al.

- Significant non-zero asymmetries
- Rising behavior vs. z
- **UL/C** asymmetries about 40-50% of **UL/L** asymmetries
- First direct measurements of the Collins function
- UL/L data published

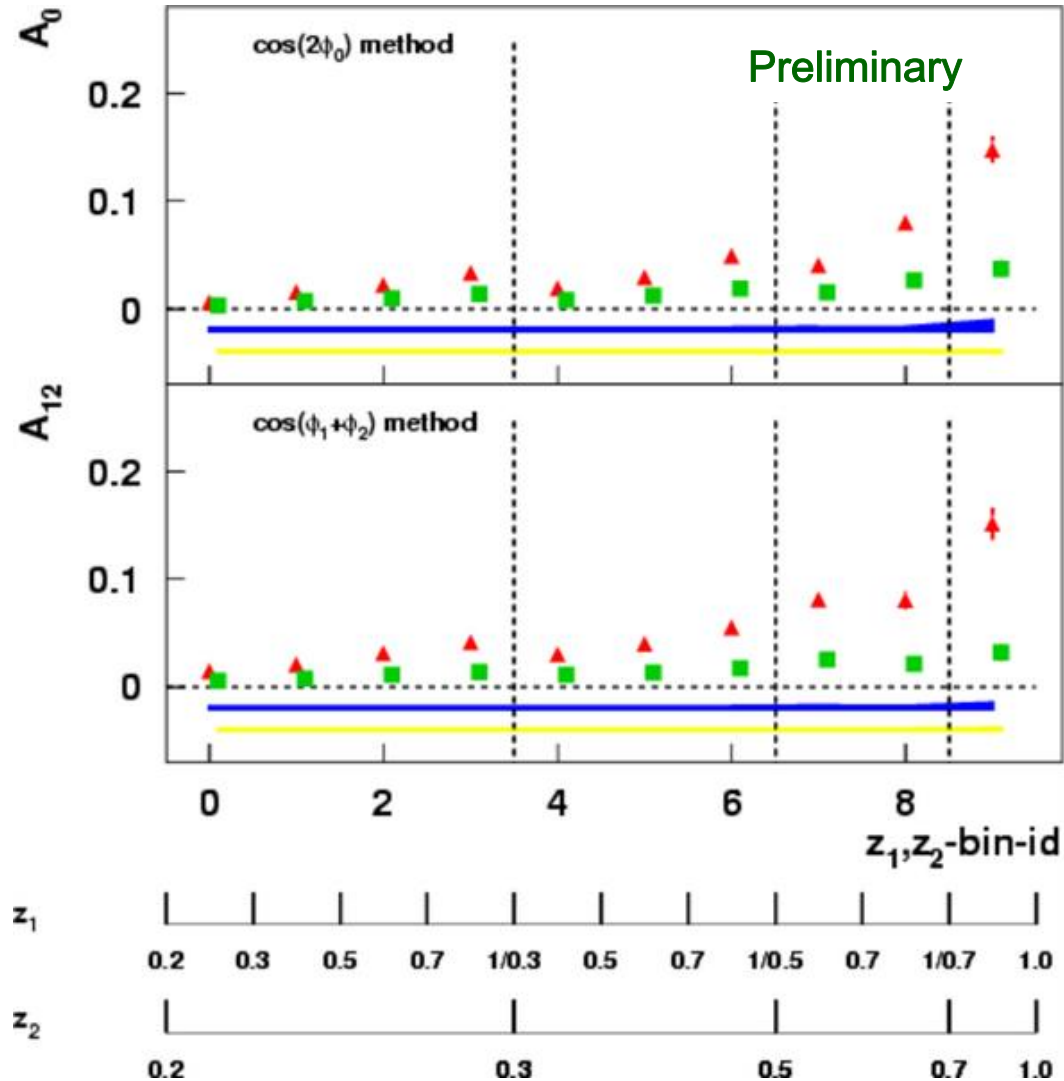


$A_0(\text{UL/L})$	$(3.06 \pm 0.57 \pm 0.55)\%$
$A_{12}(\text{UL/L})$	$(4.26 \pm 0.68 \pm 0.68)\%$
$A_0(\text{UL/C})$	$(1.27 \pm 0.49 \pm 0.35)\%$
$A_{12}(\text{UL/C})$	$(1.75 \pm 0.59 \pm 0.41)\%$



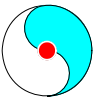
Preliminary Charm Corrected Results for $e^+ e^- \rightarrow \pi \pi X$ (547 fb^{-1} , on-resonance)

- Significance largely increased
- Behavior unchanged
- Reduced systematics
- Precise measurements of the Collins function



Integrated results:

$A_0(\text{UL/L})$	$(2.67 \pm 0.10 \pm 0.26)\%$
$A_{12}(\text{UL/L})$	$(3.55 \pm 0.08 \pm 0.15)\%$
$A_0(\text{UL/C})$	$(1.11 \pm 0.11 \pm 0.22)\%$
$A_{12}(\text{UL/C})$	$(1.46 \pm 0.09 \pm 0.13)\%$



Summary and Outlook

Summary:

- Observation of large azimuthal asymmetries in light quark fragmentation. Updated statistics:

$$\int L dt = 29 \text{ fb}^{-1} \rightarrow 547 \text{ fb}^{-1}$$

- Double ratios reliably cancel contributions from detector acceptance and gluon radiation.

important input for the transverse spin physics programs at RHIC, HERMES, COMPASS and JLab

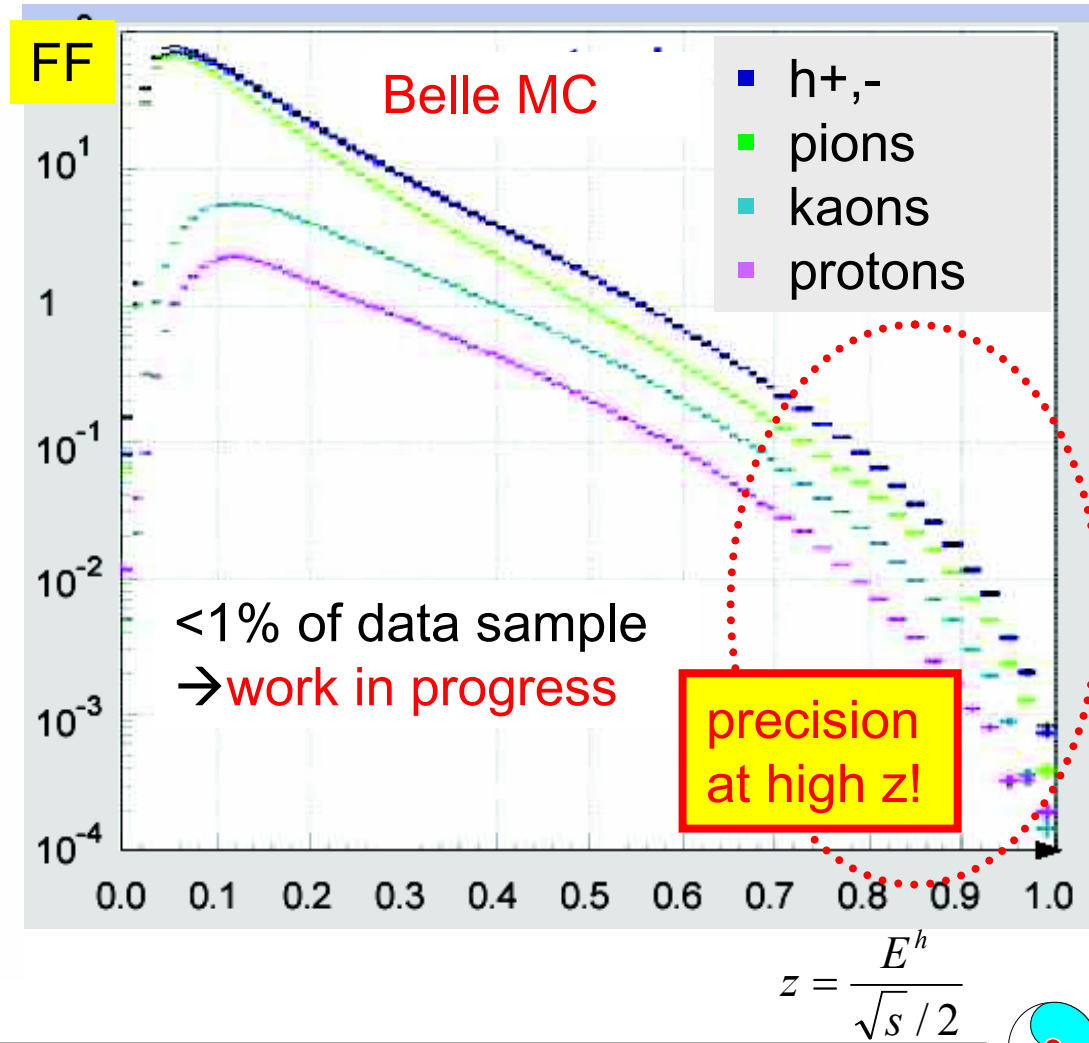
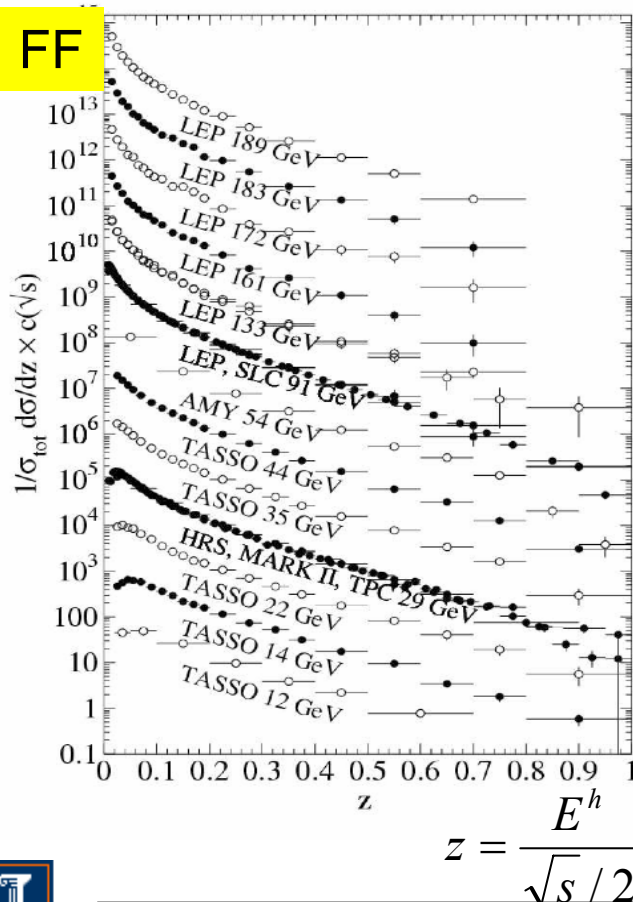
Outlook:

- Future spin dependent FFs:
 - update Collins FF
 - measure p_T dependence
 - interference fragmentation
 - Collins FF for VMs
 - Lambdas
- Precision measurement of spin averaged fragmentation functions as input to RHIC program with inclusive hadrons and future precision measurements in SIDIS.

Input also for precision measurements of quark helicity distributions in SIDIS, in particular at a possible future electron-polarized proton collider.

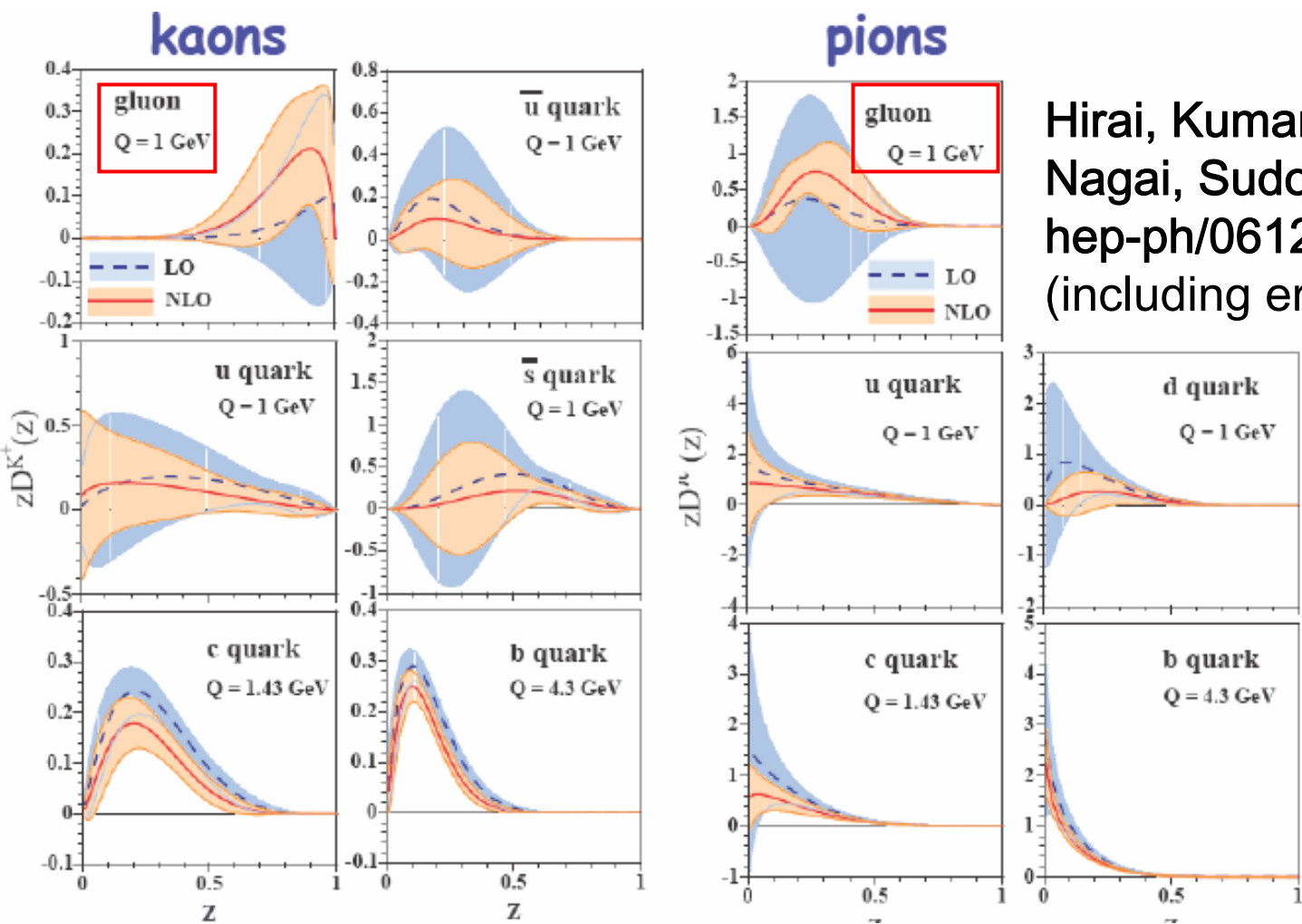
Impact on the Knowledge of FFs

Belle: Charged $h^{+/-}$, pions, kaons, protons



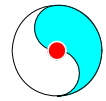


What is Known Experimentally ?



Hirai, Kumano,
Nagai, Sudo
hep-ph/0612009
(including errors!)

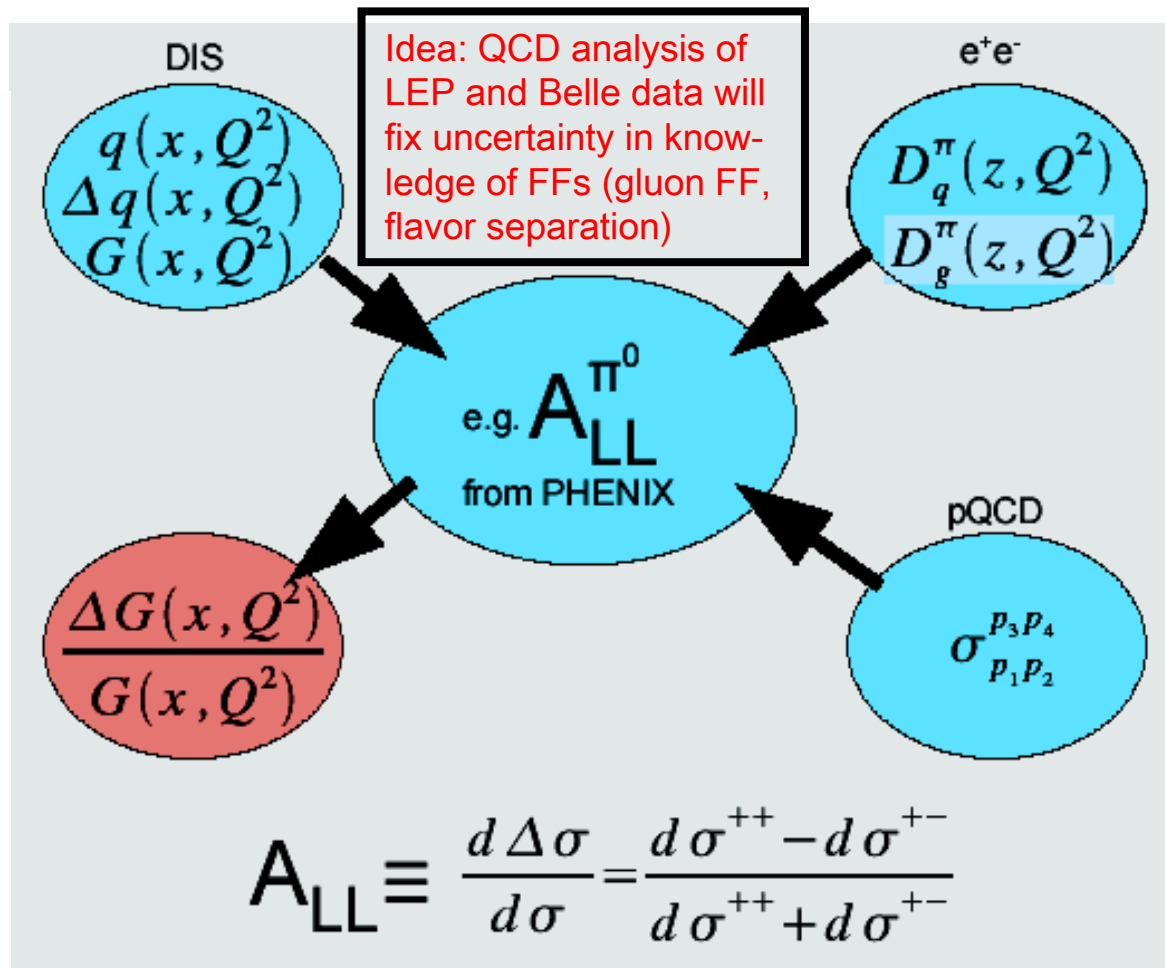
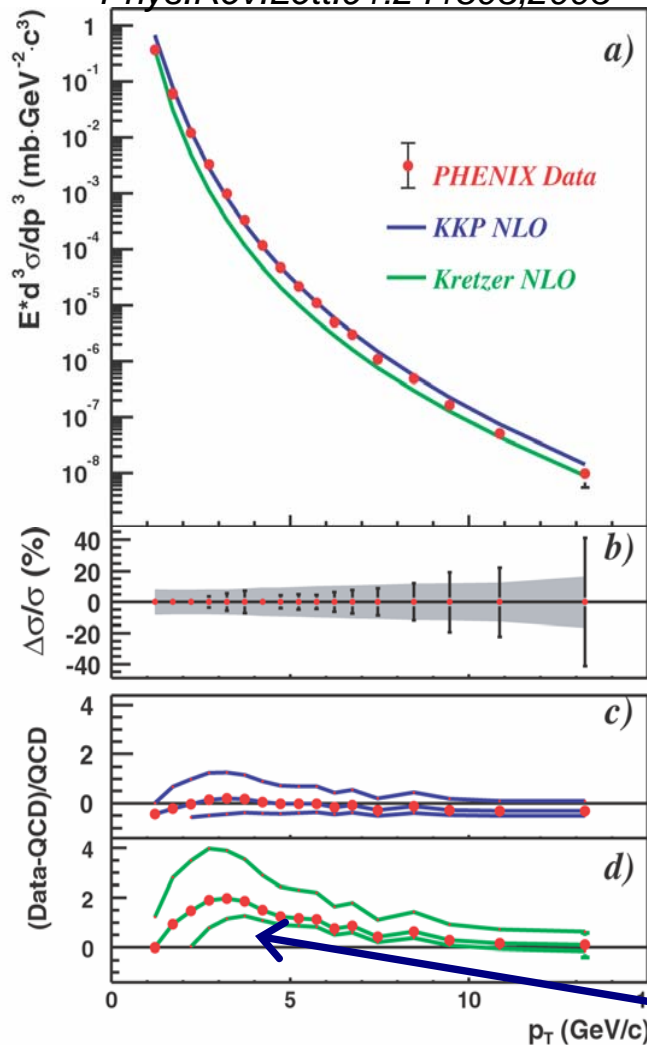
Earlier work:
Kretzer
Binnewies, Potter, Albino
Kniehl, Kramer, Potter
Albino, Kniehl, Kramer



Motivation I ΔG from QCD Analysis of A_{LL} for inclusive hadrons: $\pi^{0,+,-}, \eta, K^{+,-}$

PHENIX π^0 cross section at $|\eta| < 0.35$

Phys.Rev.Lett.91:241803,2003



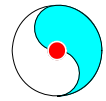
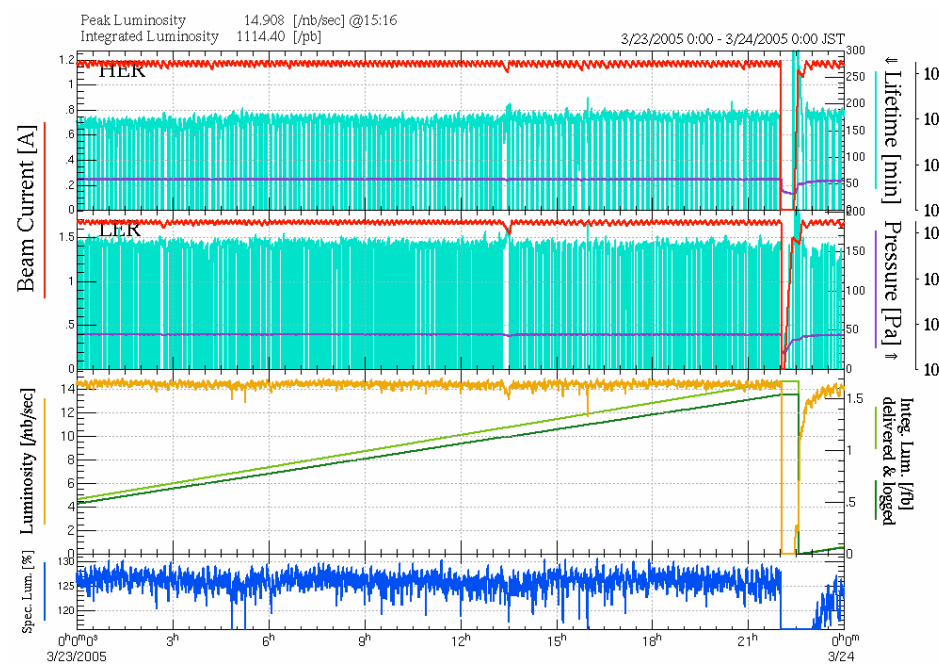
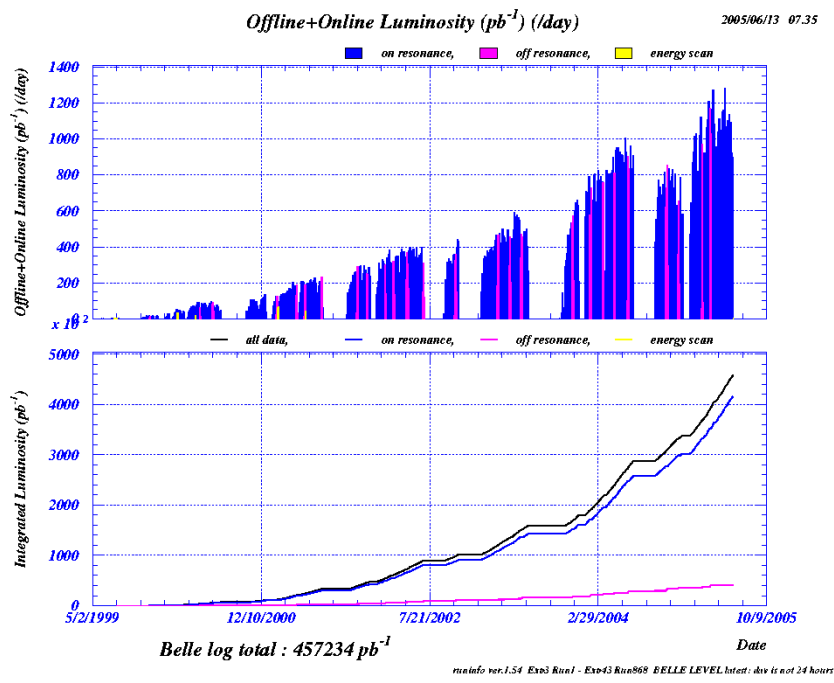
Deviation connected to uncertainties in FFs \rightarrow gluon FF!

Why is the Collins Fragmentation Function Interesting?

- o Very basic QCD process: Fundamental test case for any approach to solve QCD at soft scales.
- o Tests of universality and factorization between $e+e^-$, DIS and p-p collisions
- o Symmetry properties
- o Evolution is fundamental QCD prediction
- o Connection between microscopic and macroscopic observables:

→ Probe/analyzer for transverse quark spin
critical input for transverse proton spin program
at DESY, CERN, JLab and RHIC







KEKB: $L > 1.6 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$!!

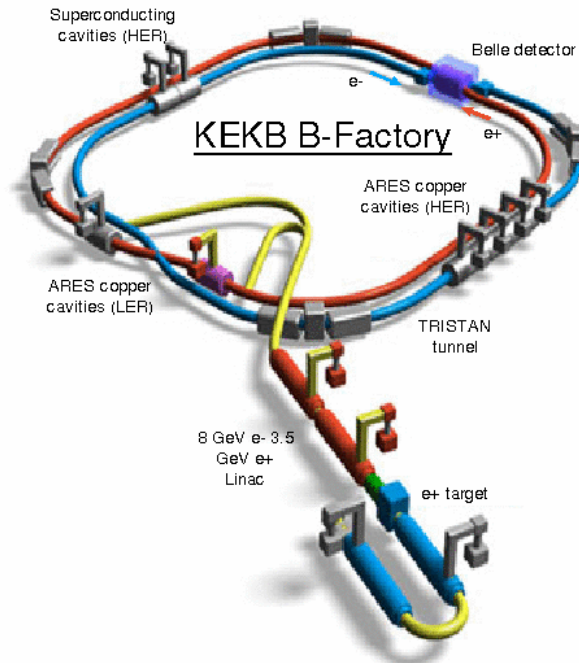
→ 1.5×10^9 hadronic events in analysis

- KEBB

- Asymmetric collider
- $8\text{GeV } e^- + 3.5\text{GeV } e^+$
- $\sqrt{s} = 10.58\text{GeV}$ ($Y(4S)$)
- $e^+e^- \rightarrow Y(4S) \rightarrow B \bar{B}$
- Off-resonance: 10.52 GeV
- $e^+e^- \rightarrow q \bar{q}$ (u,d,s,c)
- **Integrated Luminosity: $> 600 \text{ fb}^{-1}$**
- **$> 60\text{fb}^{-1} \Rightarrow$ off-resonance**

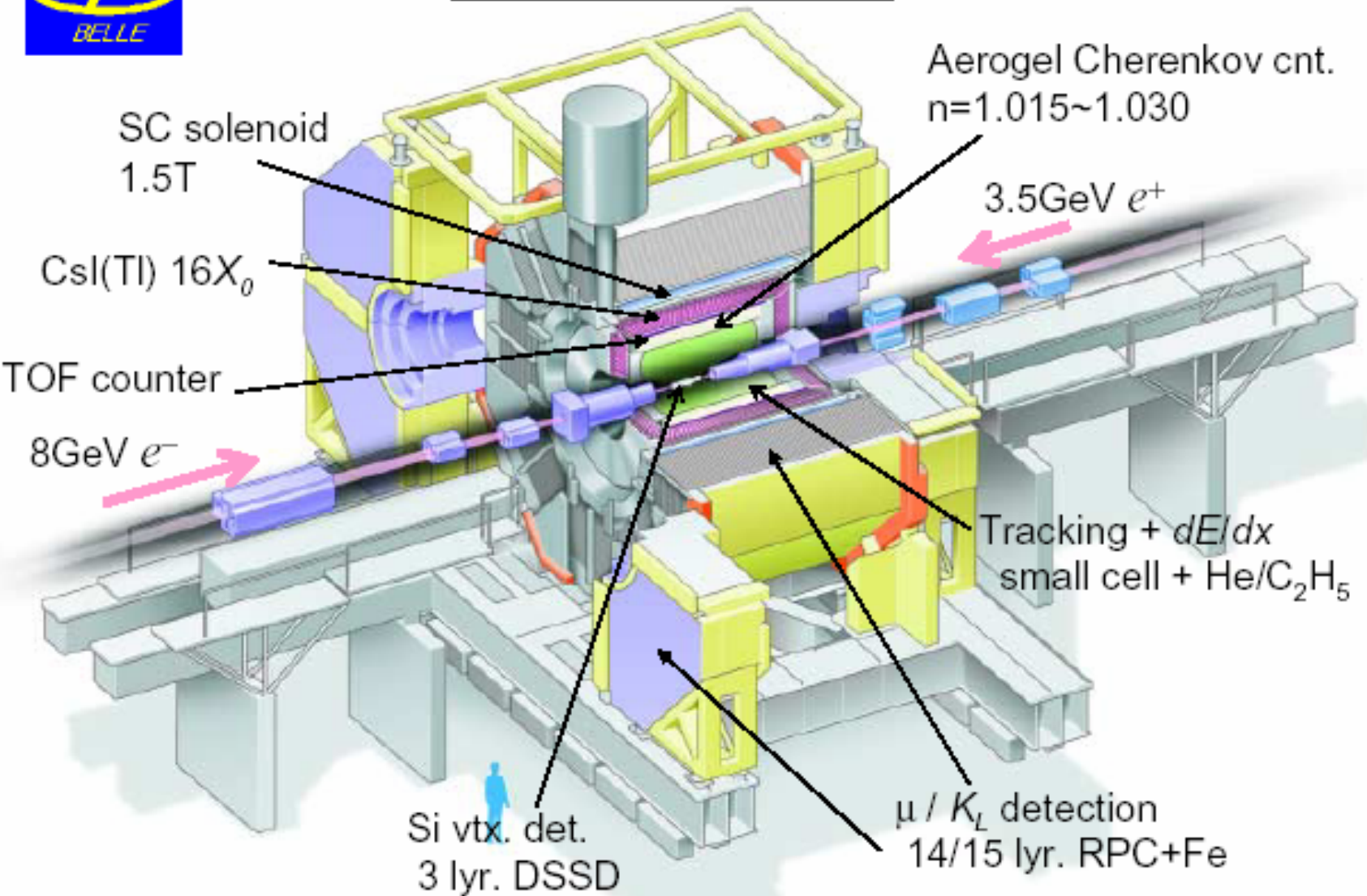
- Average Trigger rates:

$Y(4S) \rightarrow B\bar{B}$	11.5 Hz
$q \bar{q}$	28 Hz
$\mu\mu + \tau\tau$	16 Hz
<i>Bhabha</i>	4.4 Hz
2γ	35 Hz

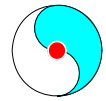




Belle Detector



Good tracking and particle identification!

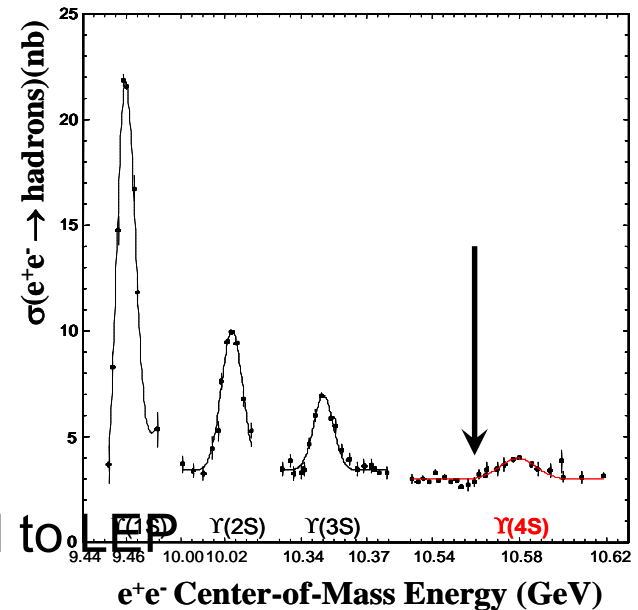


Belle is Well Suited for FF Measurements:

- Good detector performance (acceptance, momentum resolution, pid)
- Jet production from light quarks
→ off-resonance (60 MeV below resonance)
(~10% of all data)
- Intermediate Energy
→ Sufficiently high scale ($Q^2 \sim 110 \text{ GeV}^2$)
- can apply pQCD
→ Not too high energy ($Q^2 \ll M_Z^2$)
- avoids complication from Z interference
- Sensitivity = $A^2 \sqrt{N} \sim \times 25 \text{ (100)}$ compared to

$$\frac{A_{\text{Belle}}}{A_{\text{LEP}}} \sim \times 2 \text{ (A scales as } \ln Q^2)$$

$$\frac{\int L_{\text{Belle}} dt}{\int L_{\text{LEP}} dt} \sim \times 46 \text{ (600)}$$



Total number of hadronic events $\sim 1.5 \times 10^9$

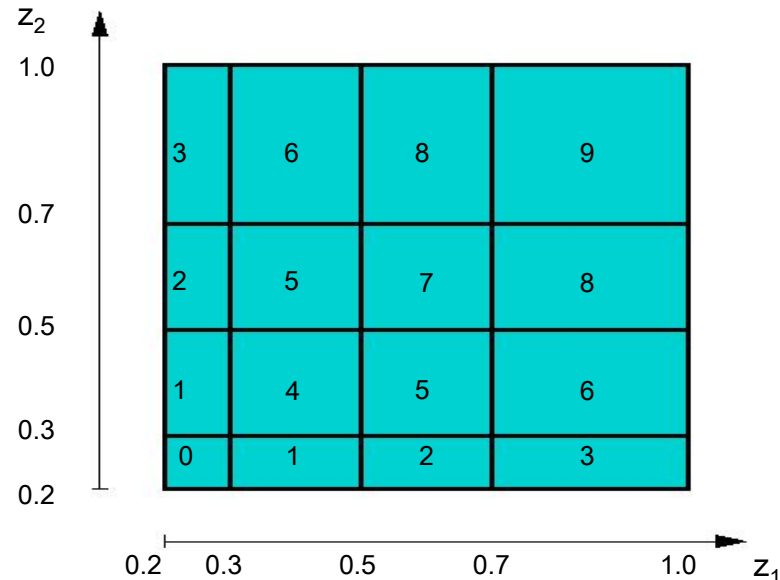
Applied Cuts, Binning

- Originally off_resonance data, now also on_resonance data (29.1 \rightarrow 547 fb⁻¹)
- Track selection:
 - pT > 0.1 GeV
 - vertex cut: dr < 2 cm, |dz| < 4 cm
- Acceptance cut
 - $-0.6 < \cos\theta_i < 0.9$
- Event selection:
 - Ntrack ≥ 3
 - Thrust > 0.8
 - $Z_1, Z_2 > 0.2$

- Hemisphere cut

$$(P_{h2} \cdot \hat{n}) \hat{n} \cdot (P_{h1} \cdot \hat{n}) \hat{n} < 0$$

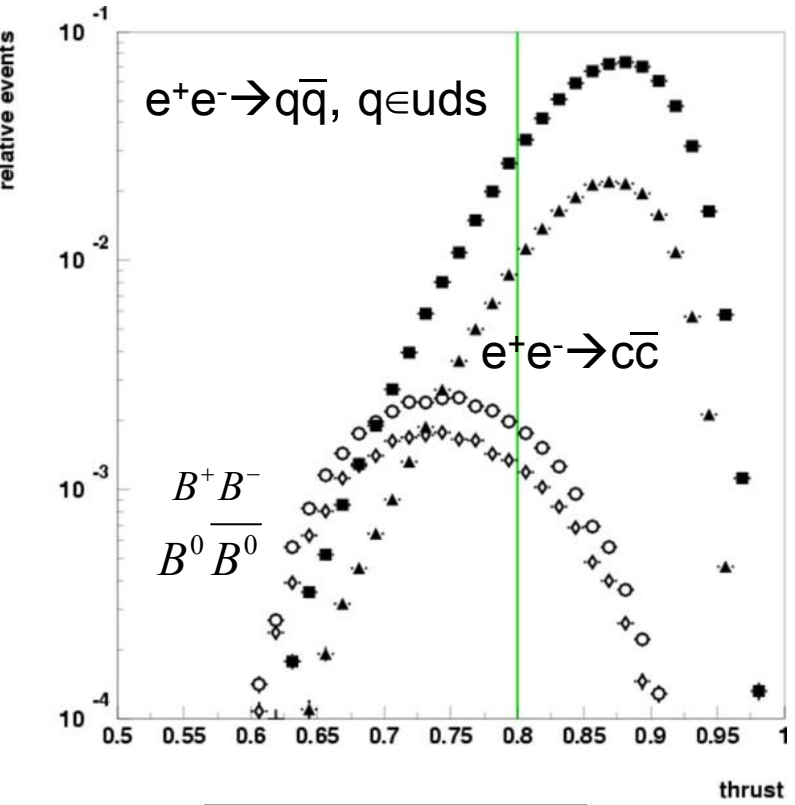
- $Q_T < 3.5$ GeV
- Pion PID selection



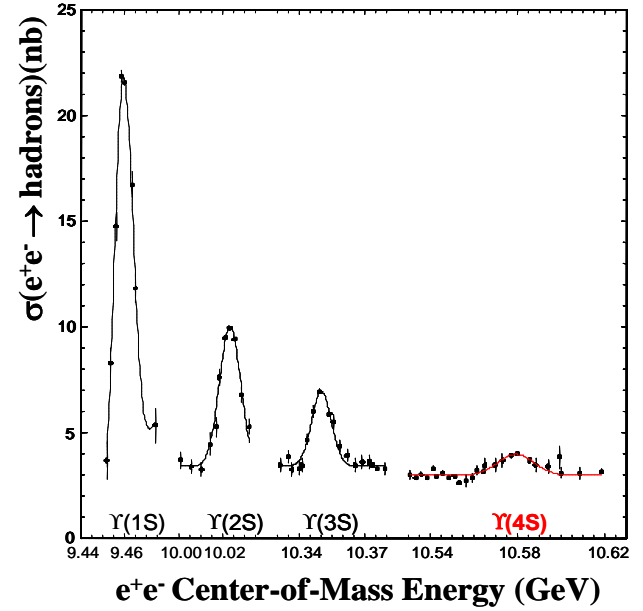
- $\cos 2\phi$ moments have two contributions:
 - Collins → Can be isolated either by subtraction or double ratio method
 - Radiative effects → Cancels exactly in subtraction method, and in LO of double ratios
- Beam Polarization zero? → $\cos(2\phi)$ asymmetries for jets or $\gamma\gamma$
- False asymmetries from weak decays → Study effect in τ decays, constrain through D tagging
- False asymmetries from misidentified hemispheres → Q_T or polar angle cut
- False asymmetries from acceptance → Cancels in double ratios, can be estimated in charge ratios, fiducial cuts
- Decaying particles → lower z cut



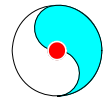
Why is it Possible to Include Data on Resonance? Different Thrust Distributions



$$\text{thrust} = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$



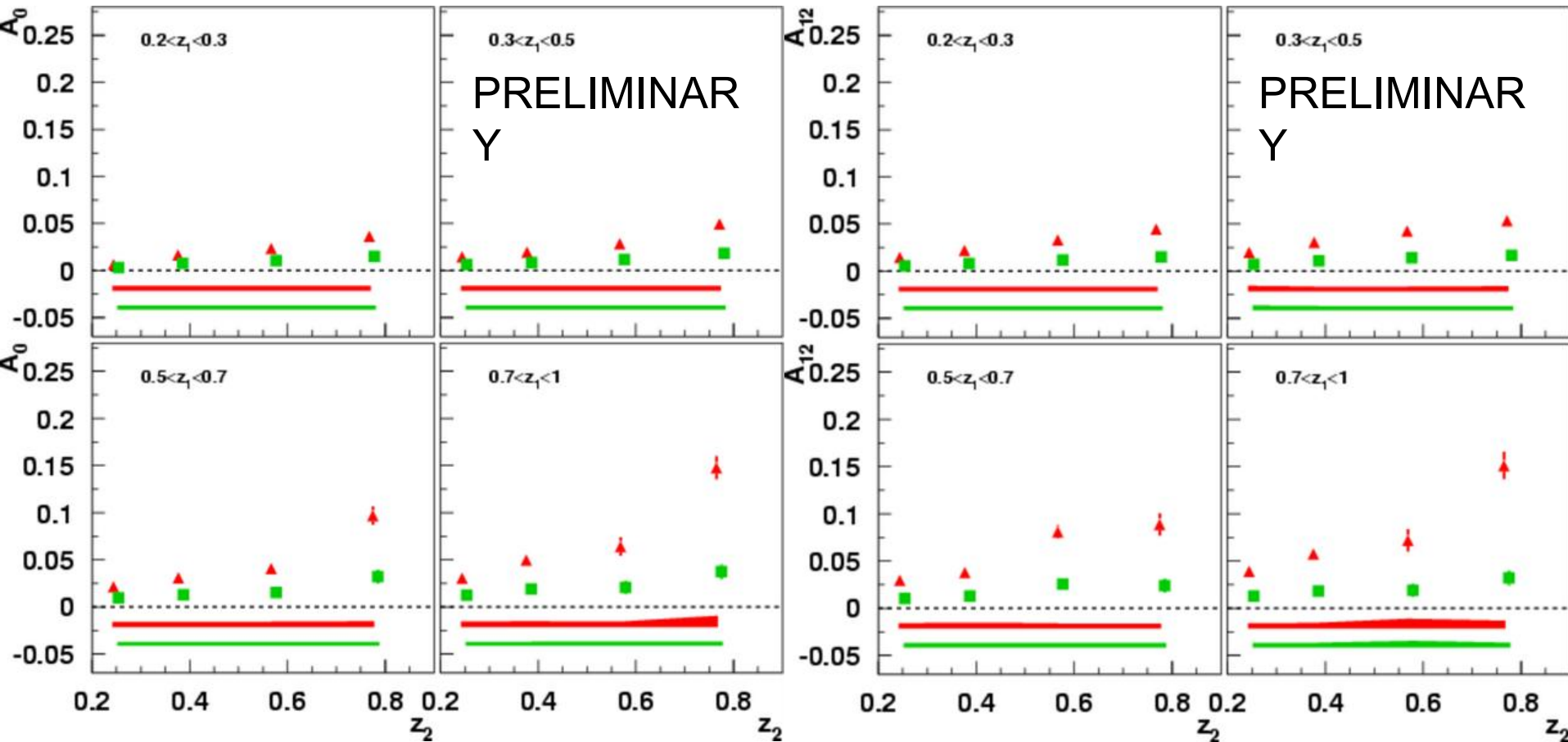
- small B contribution (<1%) in high thrust sample
- >75% of X-section continuum under Y (4S) resonance
- 29 fb⁻¹ → 547 fb⁻¹
- many systematic errors reduce with more statistics
- Charm-tagged Data sample also increases



Collins Asymmetries I: 4x4 z_1, z_2 binning

$A_0(\cos(2\phi_0))$ moments

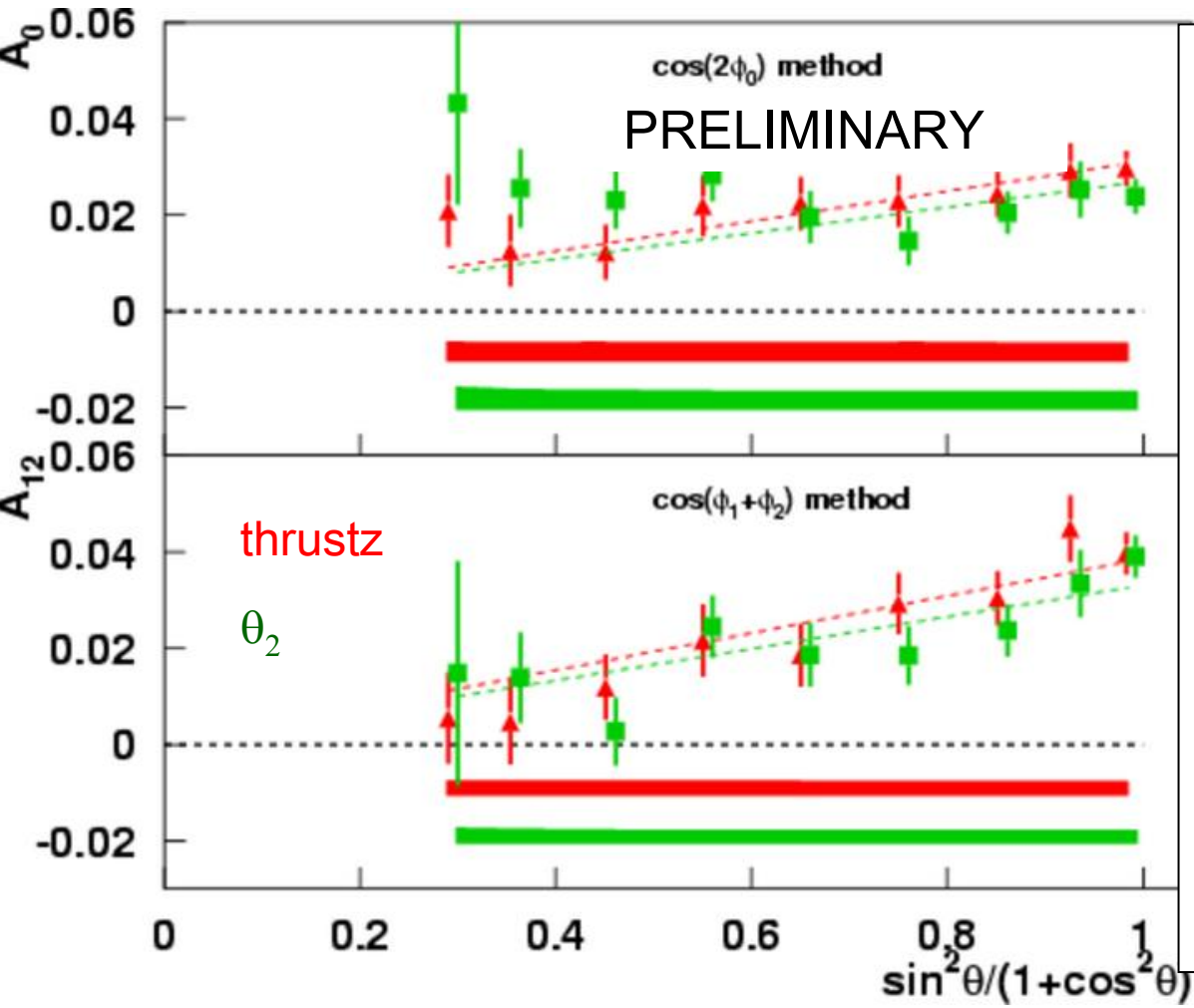
$A_{12}(\cos(\phi_1 + \phi_2))$ moments



- 547 fb⁻¹ charm corrected data sample,
- **UL** and **UC** double ratios



Collins Asymmetries II: $\sin^2 \theta / (1 + \cos^2 \theta)$ Binning (UL)

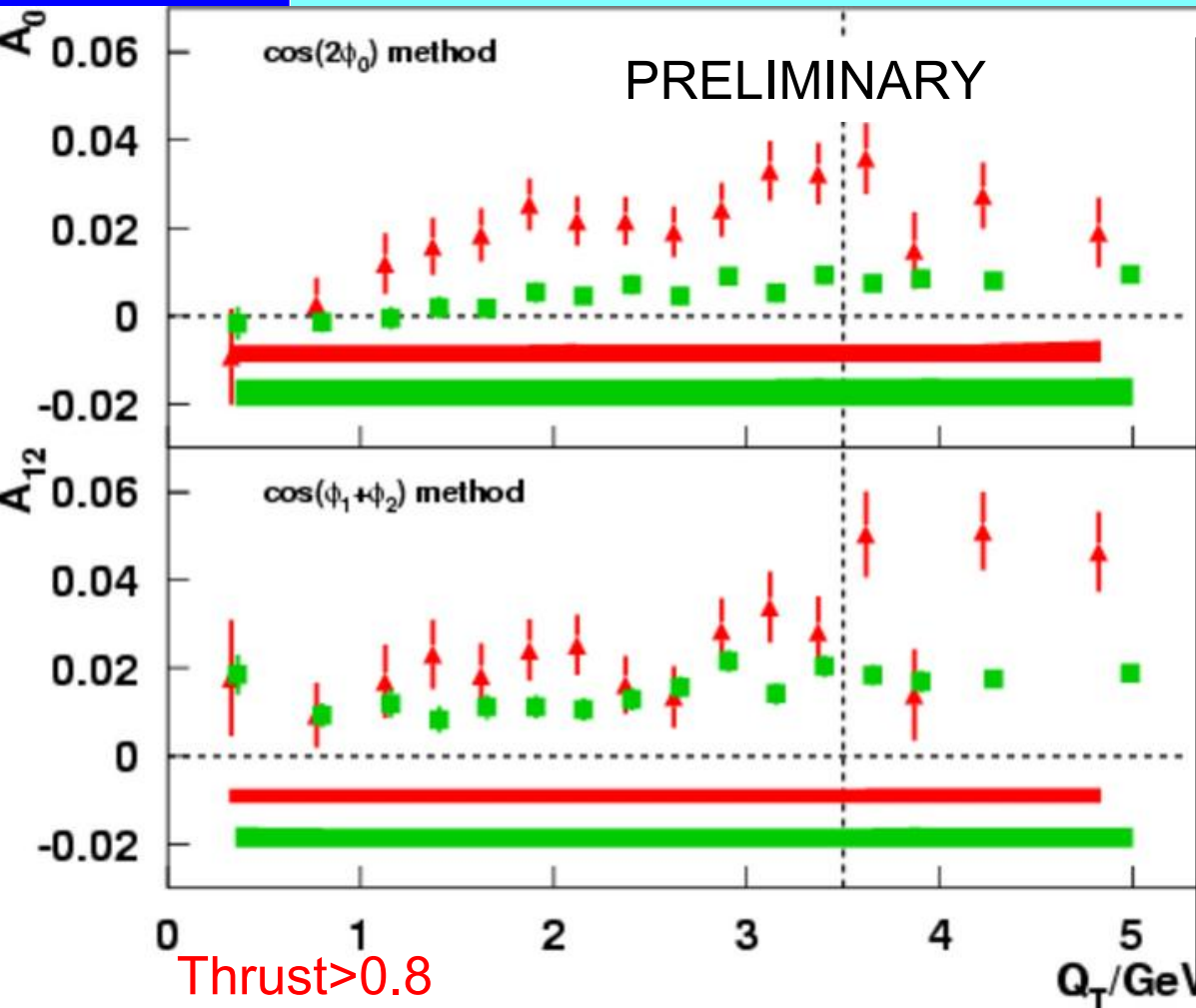


- Nonzero quark polarization $\sim \sin^2 \theta$
- Unpolarized denominator $\sim 1 + \cos^2 \theta$
- Clear linear behavior seen when using either thrust_z or 2nd hadron as polar angle
- Better agreement for thrust axis (\sim approximate quark axis)
- UC plots similar





Collins Asymmetries III: Q_T Binning (UL)



- Reduced asymmetries in low thrust sample
- At low thrust significant B contribution
(for $t < 0.8$ ~20 % B
for $t > 0.8$ < 1 % B)
- A_{12} thrust axis dependent
- High Q_T (>3.5 GeV) asymmetries from beam related BG
- UC plots similar



Improved Systematic Errors (UC)

- Tau contributions
- PID systematics*
- MC double ratios
- Charged ratios ($\pi^+\pi^+ / \pi^-\pi^-$)
- Higher order terms
- Double ratio-subtraction method

Reweighting asymmetries:

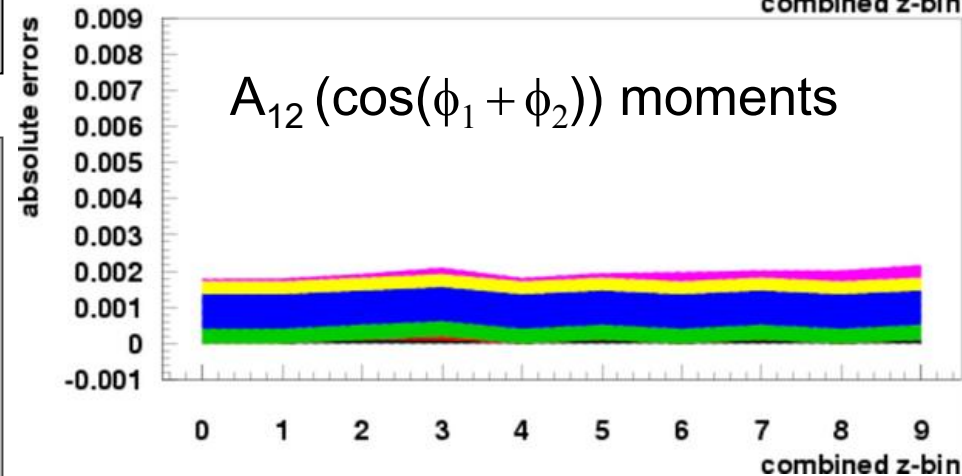
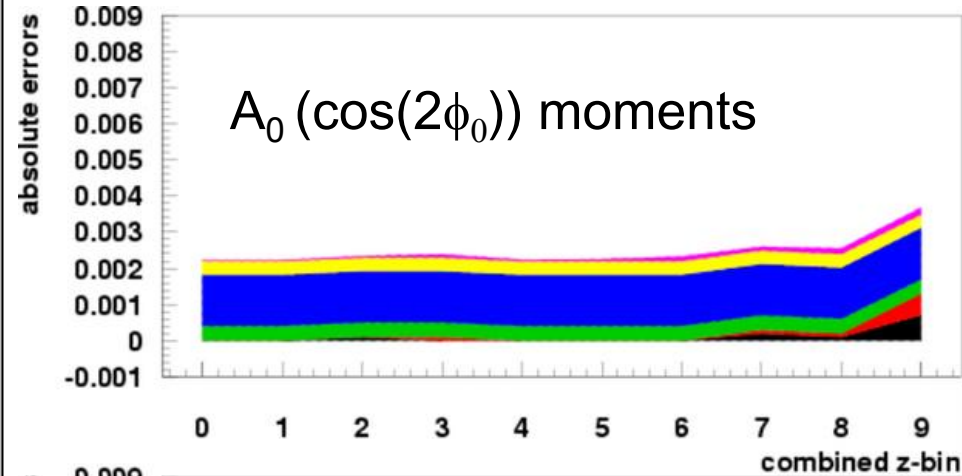
→underestimation of $\cos(\phi_1+\phi_2)$
asymmetries →rescaled by 1.21

Correlation studies:

→statistical errors rescaled by 1.02 (UL)
and 0.55 (UC)

Beam polarization studies

→consistent with zero



QCD analysis:

- (I) Efremov, Goeke, Schweitzer (Phys.Rev.D73:094025,2006): consistency between Belle, HERMES and COMPASS asymmetries.
- (II) Anselmino, Boglione, D'Alesio, Kotzinian, Murgia, Prokudin and Tuerk (hep-ph/0701006) extract transversity distributions and the Collins FF (see tomorrow).
- (III) UIUC fit to Belle data (work in progress):

$$H^{fav}(z) = a^{fav} \cdot z \cdot D^{fav}(z)$$

$$H^{dis}(z) = a^{dis} \cdot z \cdot D^{dis}(z)$$

Kretzer FFs (also KKP)

$$D^{fav}(z) = \frac{1}{4} \left(D_{\bar{d}}^{\pi^+} + D_u^{\pi^+} + D_{\bar{d}}^{\pi^-} + D_{\bar{u}}^{\pi^-} \right)$$

$$D^{dis}(z) = \frac{1}{4} \left(D_{\bar{d}}^{\pi^+} + D_{\bar{u}}^{\pi^+} + D_{\bar{d}}^{\pi^-} + D_u^{\pi^-} \right)$$

Experimental double ratio:

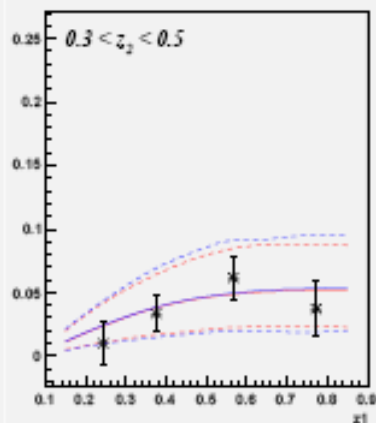
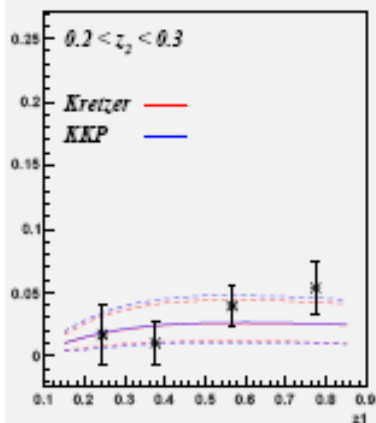
$$A_{12}^{UL/L}(z_1, z_2) = \frac{\sin^2 \theta}{1 + \cos^2 \theta} \left(\frac{H_1^{fav} H_2^{fav} + H_1^{dis} H_2^{dis}}{D_1^{fav} D_2^{fav} + D_1^{dis} D_2^{dis}} - \frac{H_1^{fav} H_2^{dis} + H_1^{dis} H_2^{fav}}{D_1^{fav} D_2^{dis} + D_1^{dis} D_2^{fav}} \right)$$



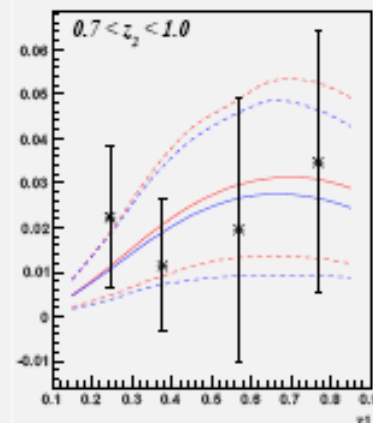
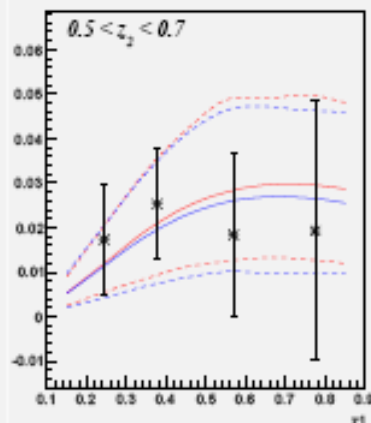
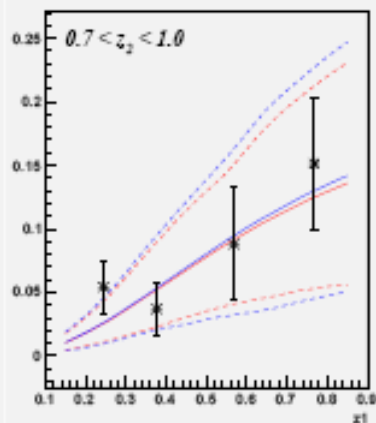
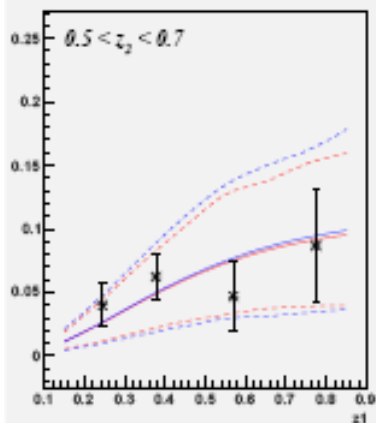
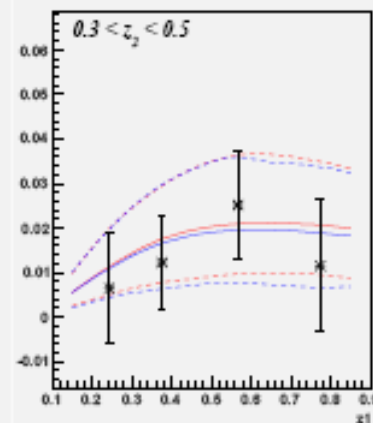
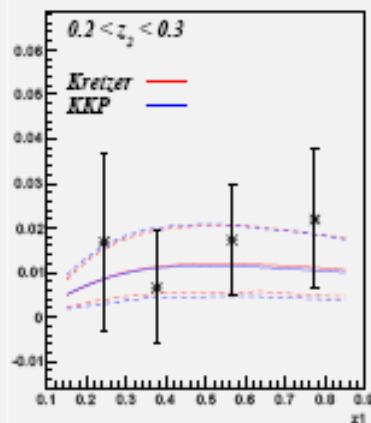
Fits of the Belle Collins

Asymmetries A_0 with $\int L dt = 29 \text{ fb}^{-1}$

$A_0^{UL/L}$, KKP and Kretzer Fits



$A_0^{UL/C}$, KKP and Kretzer Fits

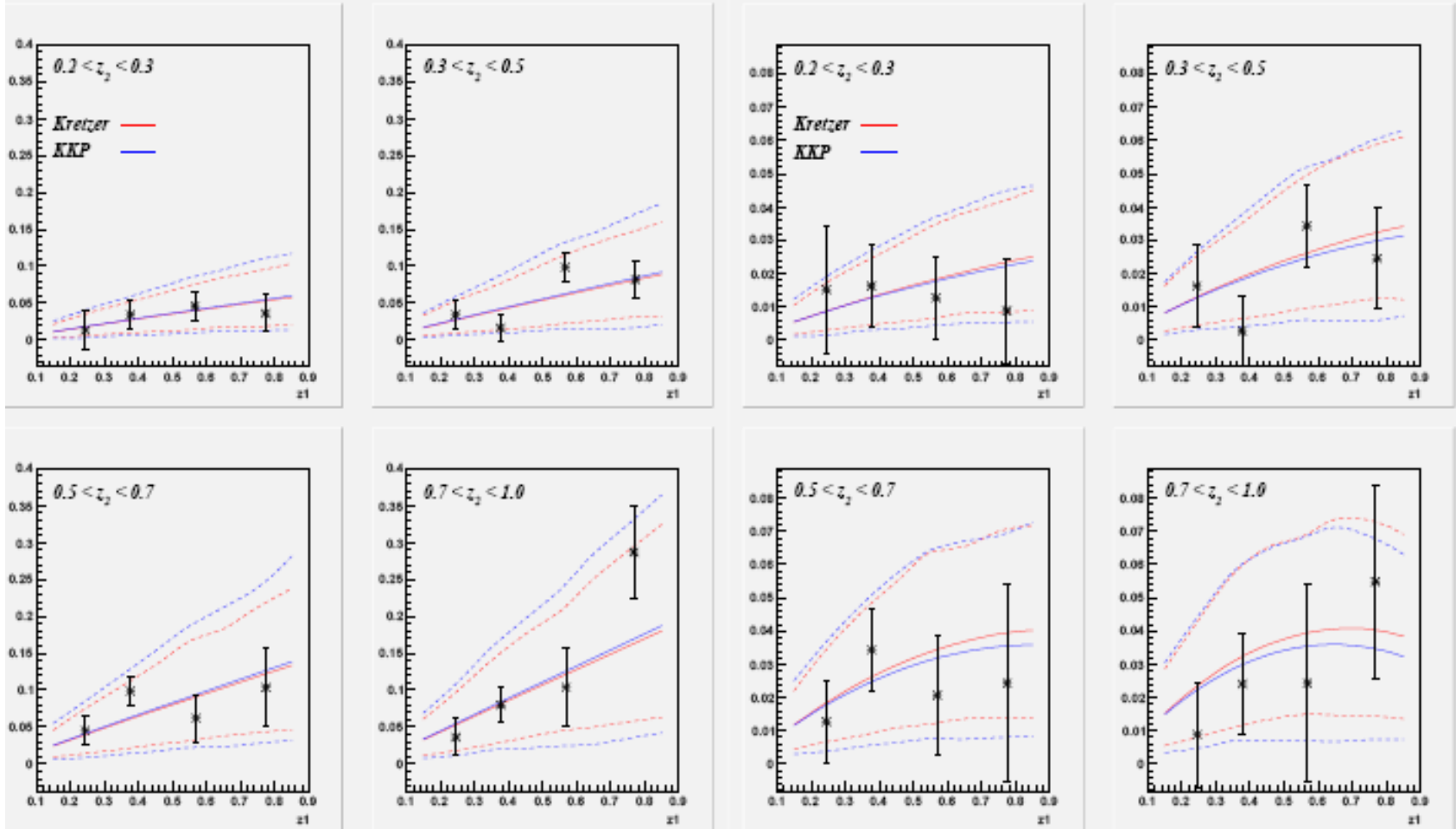


Fits of the Belle Collins

Asymmetries A_{12} with $\int L dt = 29 \text{ fb}^{-1}$

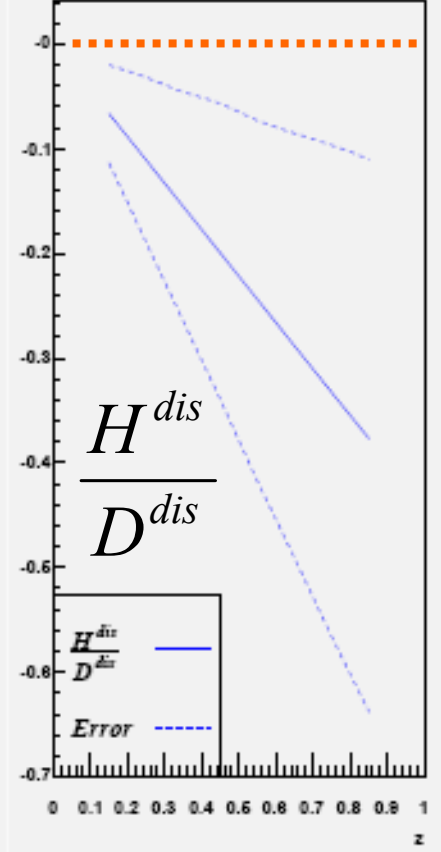
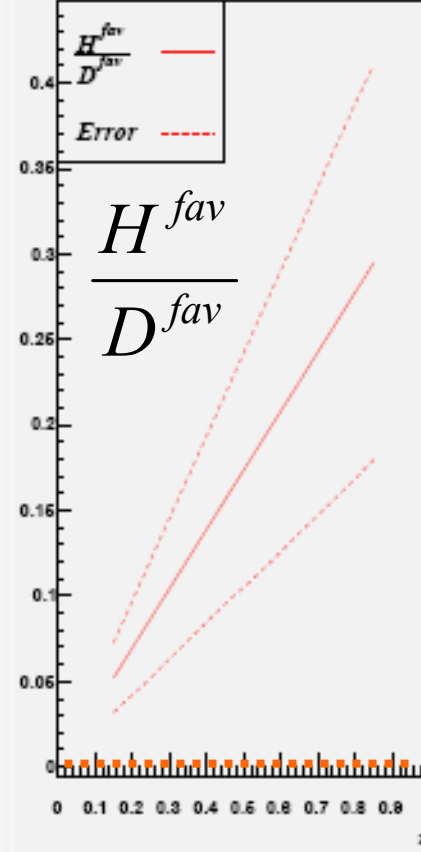
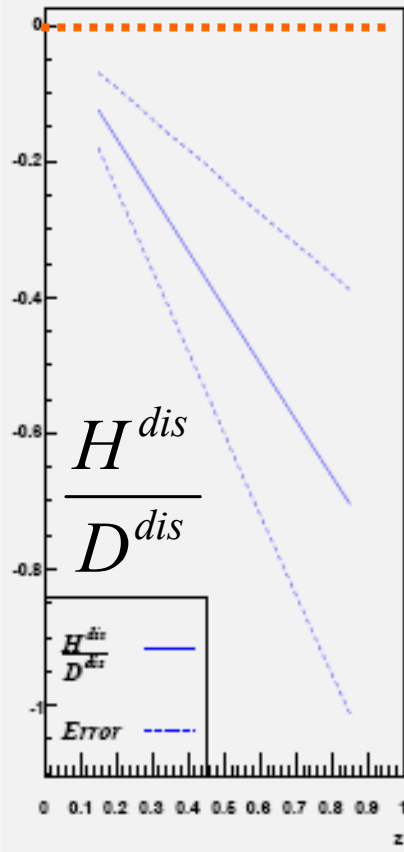
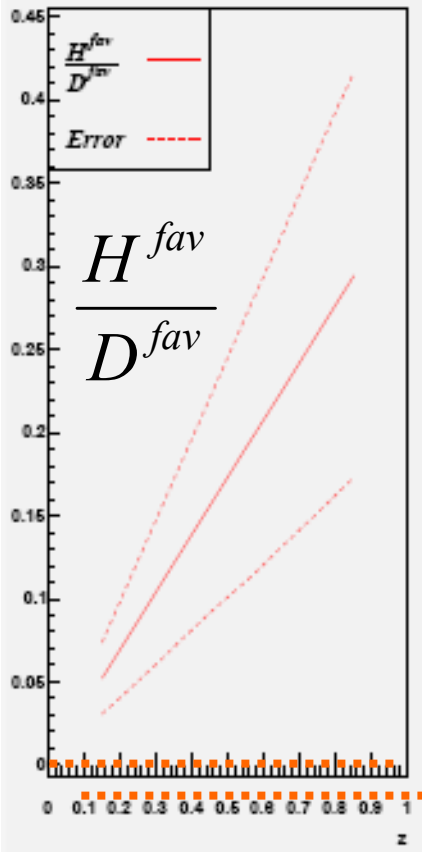
$A_{12}^{UL/L}$, KKP and Kretzer Fits

$A_{12}^{UL/C}$, KKP and Kretzer Fits



A_0

A_{12}



← $0 < z < 1$ →