

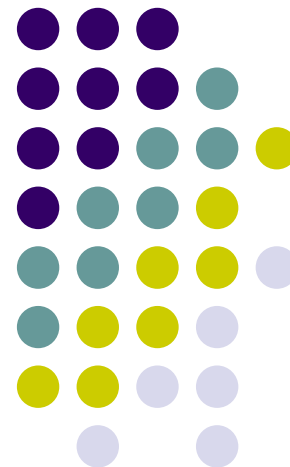
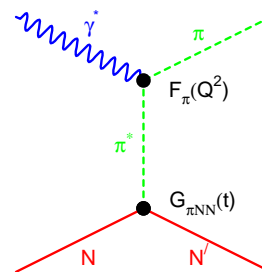
Meson Form Factors in the Space-Like Region

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Exclusive Reactions at High
Momentum Transfer

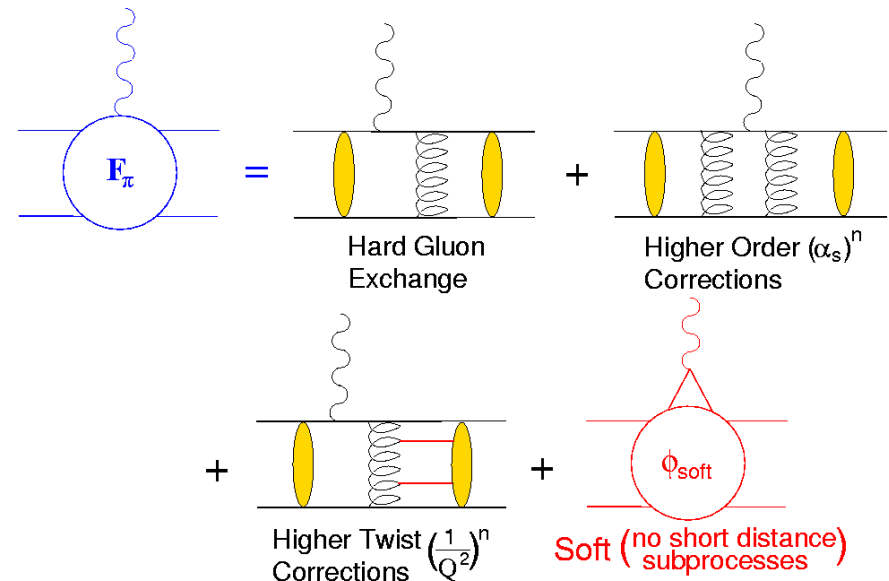
May 23, 2007



Meson Form Factors and QCD



- The simple $q\bar{q}$ valence quark structure of mesons presents the ideal laboratory for testing our understanding of bound quark systems
- Asymptotic form factors can be calculated in pQCD – we know where we need to end up
- Excellent opportunity for studying the **transition** from effective degrees of freedom to quarks and gluons, i.e., from the soft to hard regime



QCD Hard Scattering Picture



Example: π^+ form factor

At large Q^2 , perturbative QCD (pQCD) can be used

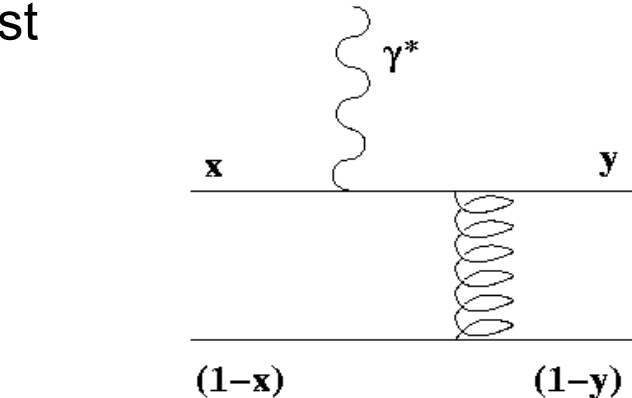
$$F_\pi(Q^2) = \frac{4\pi C_F \alpha_s(Q^2)}{Q^2} \left| \sum_{n=0}^{\infty} a_n \left(\log \left(\frac{Q^2}{\Lambda^2} \right) \right)^{-\gamma_n} \right|^2 \left[1 + O \left(\alpha_s(Q^2), \frac{m}{Q} \right) \right]$$

at asymptotically high Q^2 , only the hardest portion of the wave function remains

$$\phi_\pi(x) \xrightarrow{Q^2 \rightarrow \infty} \frac{3f_\pi}{\sqrt{n_c}} x(1-x)$$

and F_π takes the very simple form

$$F_\pi(Q^2) \xrightarrow{Q^2 \rightarrow \infty} \frac{16\pi\alpha_s(Q^2)f_\pi^2}{Q^2}$$



where $f_\pi^2 = 93 \text{ MeV}$ is the $\pi^+ \rightarrow \mu^+ \nu$ decay constant.

Meson Form Factor Experiments



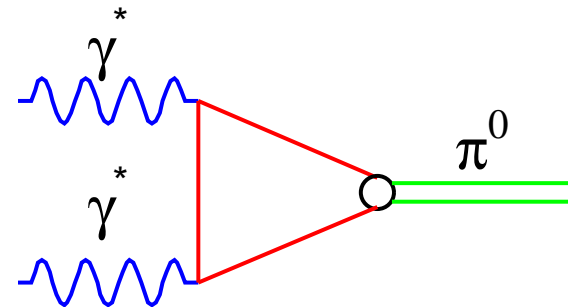
- Theoretically, meson form factors present clean testing ground for our understanding of bound quark systems
- Due to lack of “meson targets”, more challenging experimentally than hadron form factors
- Experiments to date have measured:
 - π^0 form factor - measured via $e^+e^- \rightarrow e^+e^-\pi^0$ up to $Q^2=8 \text{ GeV}^2$
 - π^+ form factor – measured via $\pi^+e^- \rightarrow \pi^+e^-$ and $p(e,e'\pi^+)n$ to $Q^2=2.5 \text{ GeV}^2$
 - K^+ form factor – measured via $K^+e^- \rightarrow K^+e^-$ up to $Q^2=0.1 \text{ GeV}^2$

$\gamma^* \gamma \rightarrow \pi^0$ Form Factor Measurement



- At lowest order in hard scattering, $\gamma^* \gamma \rightarrow \pi^0$ is a **pure QED process**

- Good test of pion distribution amplitude



- Measured via $e^+ e^- \rightarrow e^+ e^- \gamma^* \gamma$ (pure QED) \longrightarrow $\gamma^* \gamma \rightarrow \pi^0$ (Form Factor)

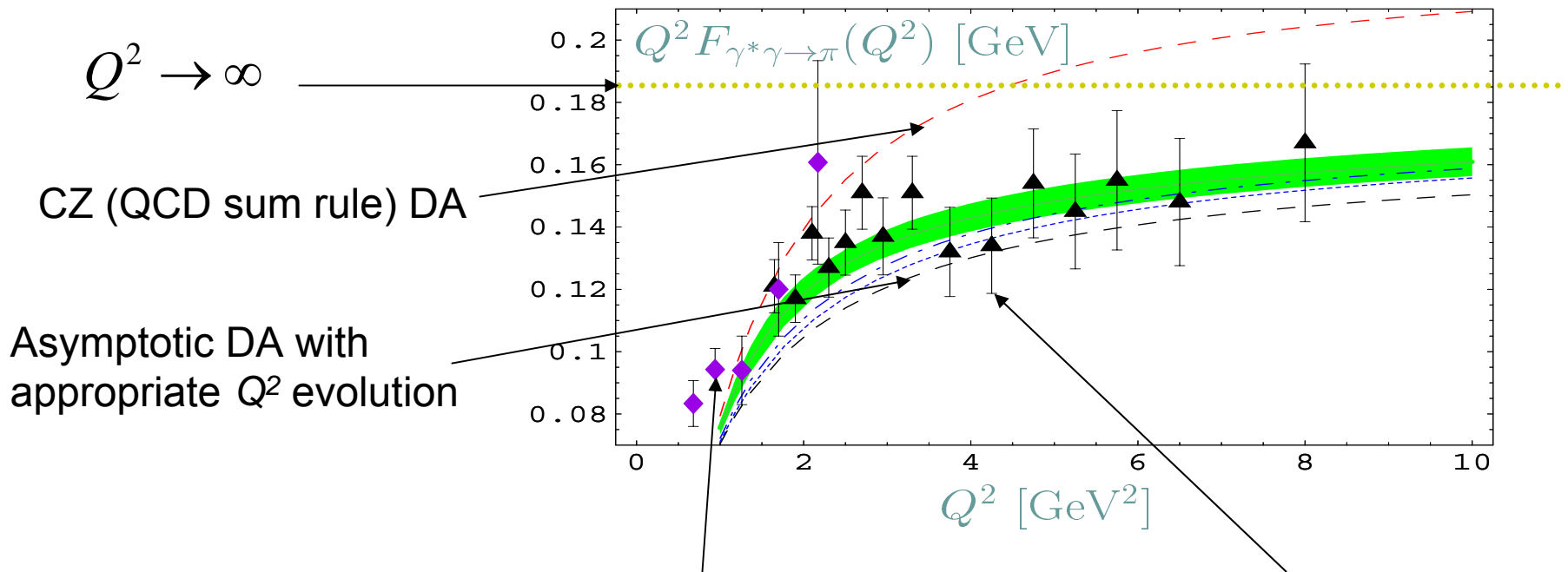
- One electron scattered at large angle (detected) yielding virtual photon with large Q^2
- Second electron (undetected) scattered at small angle yielding “nearly real” photon

$F_{\gamma^* \gamma \pi^0}(Q^2)$ Results



1. Asymptotic pion distribution amplitude (DA)
 2. Lowest order α_s
- $$\left. \vphantom{\begin{matrix} 1. \\ 2. \end{matrix}} \right\} F_{\gamma^* \gamma \pi^0}(Q^2) \xrightarrow{Q^2 \rightarrow \infty} \frac{2f_\pi}{Q^2}$$

Form factor approaches leading order pQCD results at $Q^2=8 \text{ GeV}^2$



CELLO [Behrend et al, Z.Phys. **C49**, 401(1991)]

CLEO [Phys. Rev. **D57**, 33(1998)]

Pion Distribution Amplitude



- $F_{\gamma^* \gamma \pi^0}(Q^2)$ results taken as evidence that asymptotic pion DA appropriate as low as $Q^2=1 \text{ GeV}^2$
- However, as will be seen, charged pion FF case is more complicated
- Interesting side note – modified QCD sum rule DA describes $F_{\gamma^* \gamma \pi^0}(Q^2)$ results well

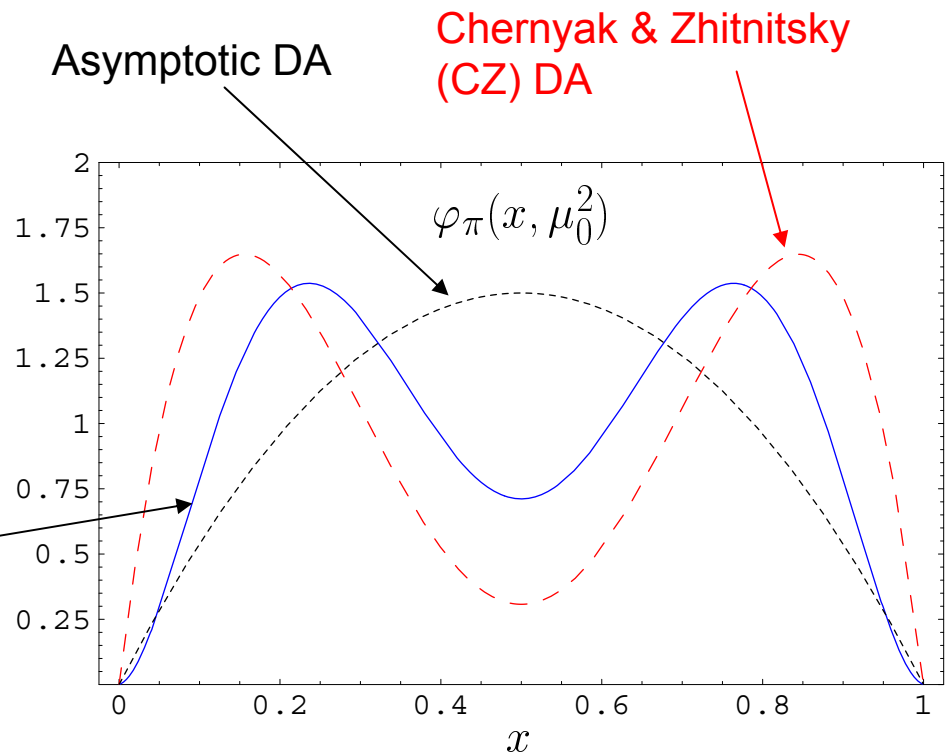


Figure from Bakulev et al, Phys. Rev. D70,033014

Measurement of π^+ Form Factor



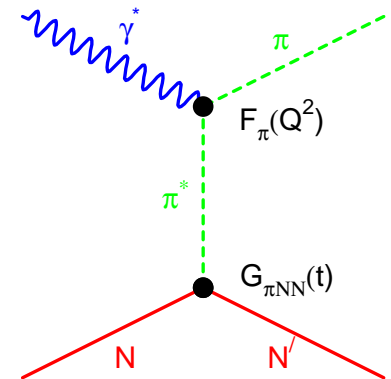
- **At low Q^2** , F_{π^+} can be measured directly via high energy elastic π^+ scattering from atomic electrons
 - CERN SPS used 300 GeV pions to measure form factor up to $Q^2 = 0.25 \text{ GeV}^2$ [*Amendolia et al, NPB277, 168 (1986)*]
 - These data used to constrain the pion charge radius

$$r_{\pi} = 0.657 \pm 0.012 \text{ fm}$$

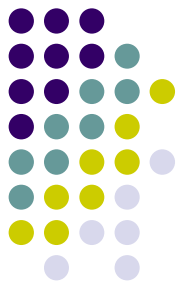
- **At larger Q^2** , F_{π} must be measured indirectly using the “pion cloud” of the proton via $p(e, e' \pi^+) n$

- At small $-t$, the pion pole process dominates σ_L
- F_{π}^2 in Born term model

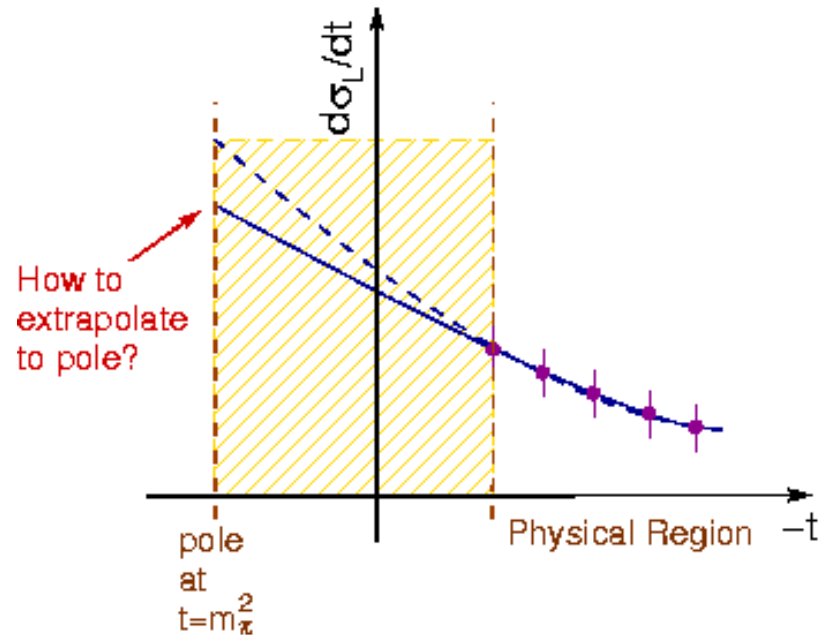
$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_{\pi}^2)} g_{\pi NN}^2(t) F_{\pi}^2(Q^2, t)$$



Extraction of π^+ Form Factor in $p(e, e' \pi^+) n$



- π^+ electroproduction can only access $t < 0$ (away from pole)
- Early experiments used “Chew-Low” technique
 - measured $-t$ dependence
 - Extrapolate to physical pole
- This method is unreliable – different fit forms consistent with data yet yield very different FF



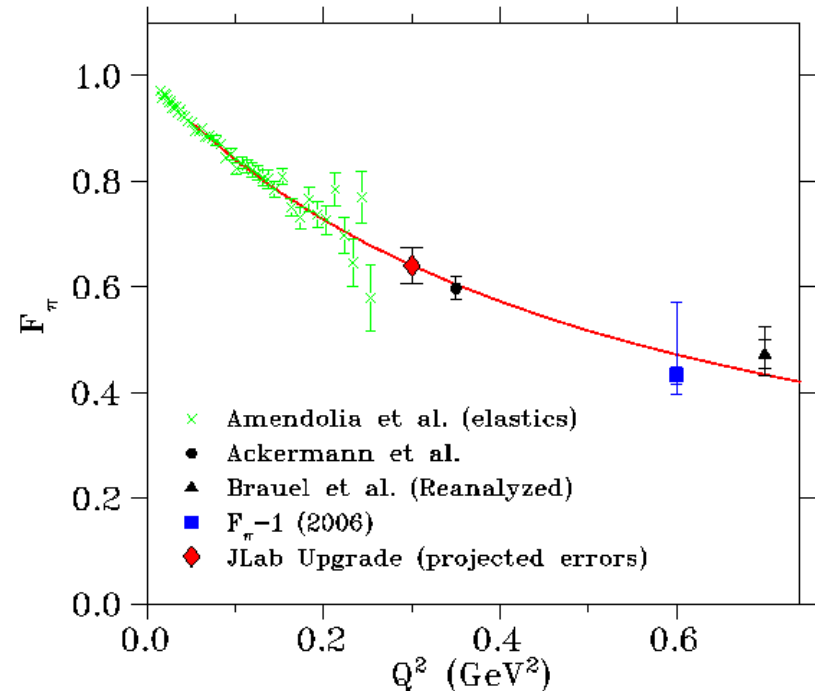
- Cross section model incorporating FF is required!

→ t -pole “extrapolation” is implicit, but one is only fitting data in physical region

Check of Pion Electroproduction Technique



- Does electroproduction really measure the physical form-factor since we are starting with an off-shell pion?
- This can be tested making $p(e, e' \pi^+)$ measurements at same kinematics as $\pi^+ e$ elastics
- Looks good so far
- Ackermann electroproduction data at $Q^2 = 0.35 \text{ GeV}^2$ consistent with extrapolation of SPS elastic data



An improved test will be carried out after the JLAB 12 GeV upgrade

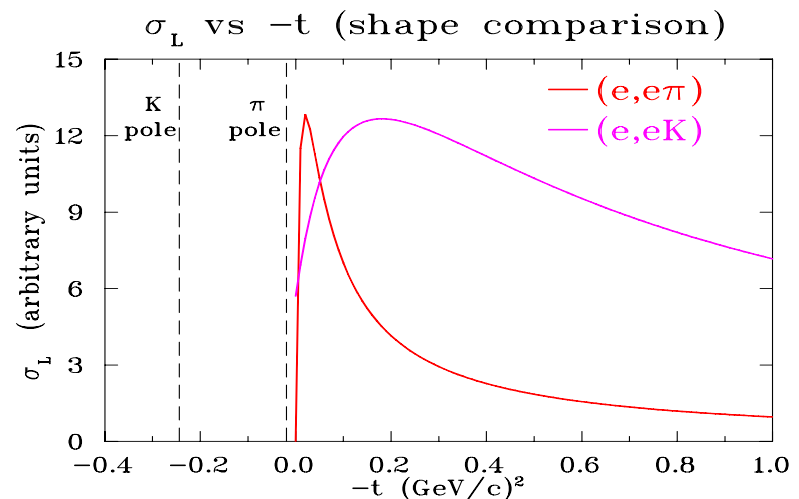
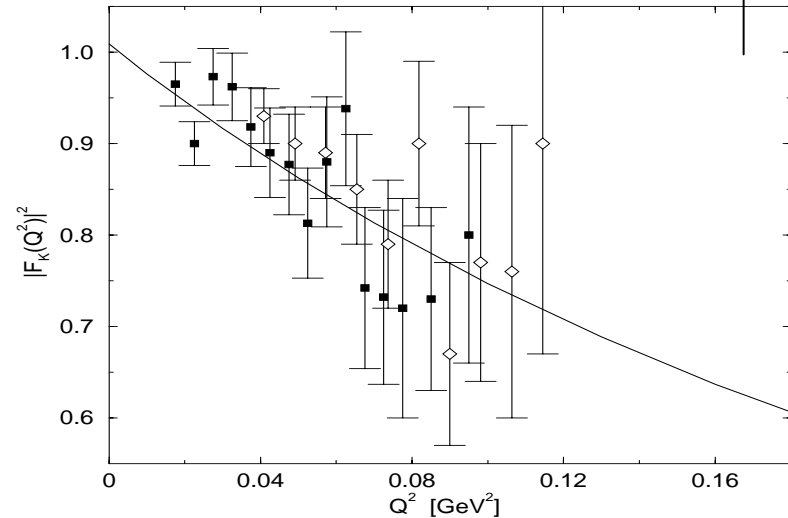
→ smaller Q^2 ($=0.30 \text{ GeV}^2$)

→ $-t$ closer to pole ($=0.005 \text{ GeV}^2$)

Measurement of K^+ Form Factor



- Similar to π^+ form factor, elastic K^+ scattering from electrons used to measure charged kaon form factor at low Q^2 [Amendolia et al, PLB 178, 435 (1986)]
- Can “kaon cloud” of the proton be used in the same way as the pion to extract kaon form factor via $p(e, e'K^+)\Lambda$?
- Kaon pole further from kinematically allowed region
- Can we demonstrate that the “pole” term dominates the reaction mechanism?



Kaon Form Factor at Large Q^2



- JLAB experiment E93-018 extracted $-t$ dependence of K^+ longitudinal cross section near $Q^2=1 \text{ GeV}^2$
- A trial Kaon FF extraction was attempted using a simple Chew-Low extrapolation technique

$$\sigma_L \approx \frac{-2tQ^2}{(t - m_K^2)^2} k (eg_{K\Lambda N})^2 F_K^2(Q^2)$$

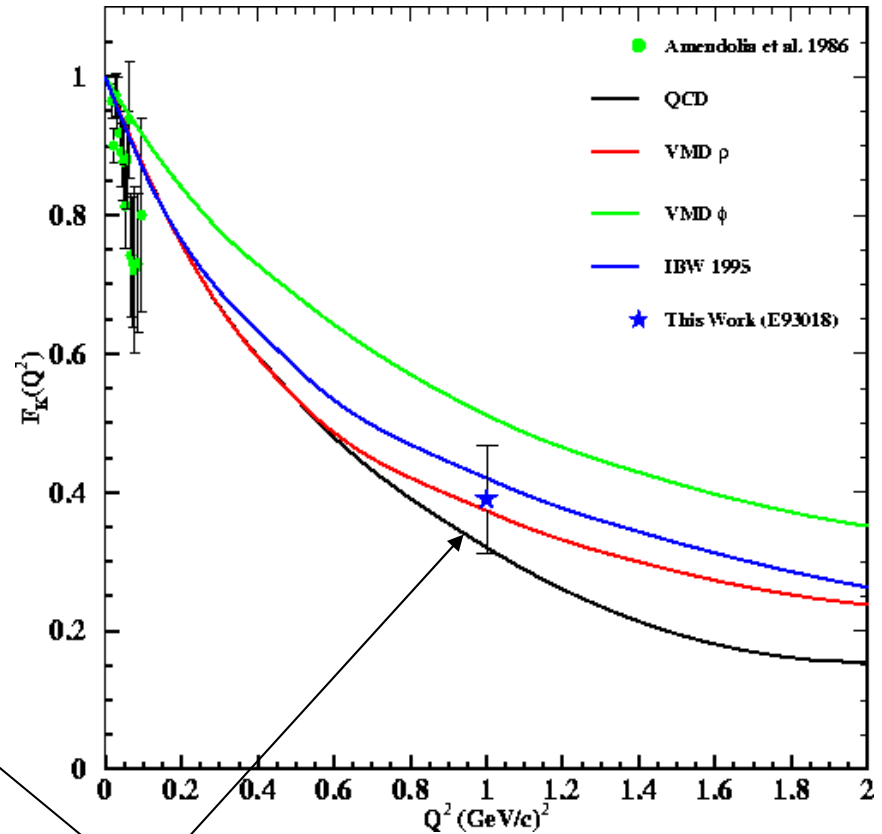
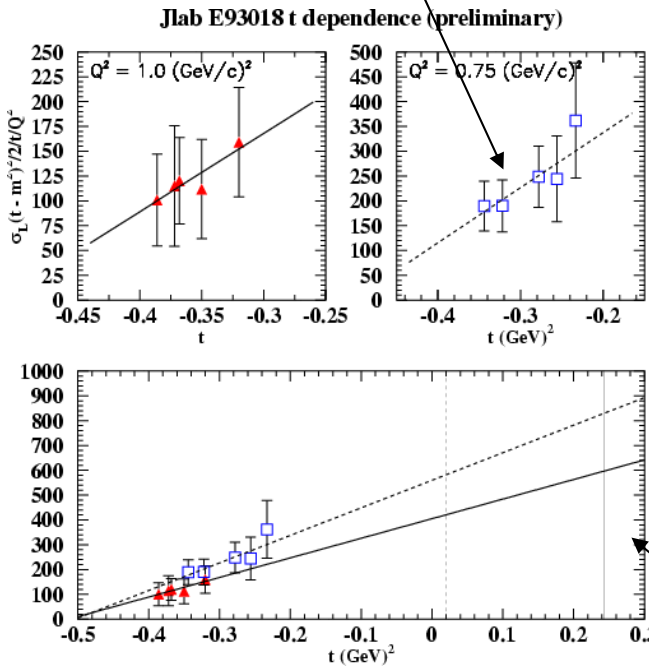
- $g_{K\Lambda N}$ poorly known
 - Assume form factor follows monopole form
 - Used measurements at $Q^2=0.75$ and 1 GeV^2 to constrain $g_{K\Lambda N}$ and F_K simultaneously
- Improved extraction possible using VGL model?

Test Extraction of K^+ Form Factor



- t dependence shows some “pole-like” behavior

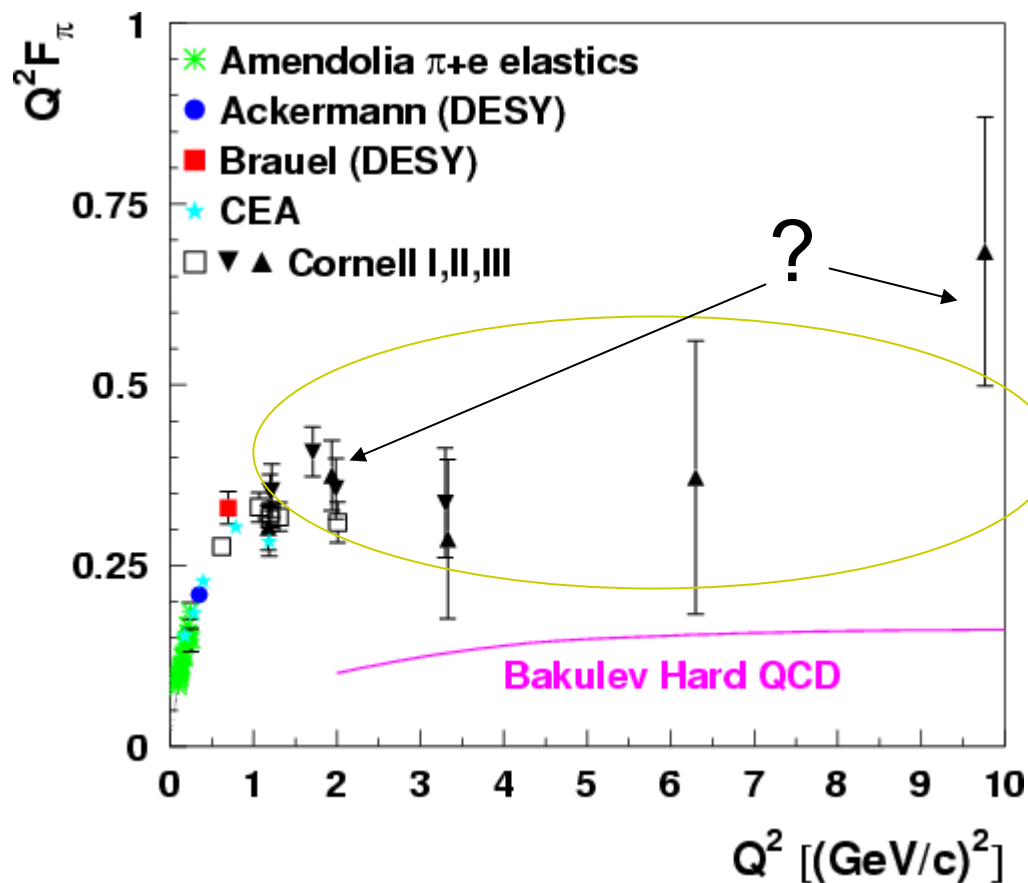
G. Niculescu, PhD. Thesis, Hampton U.



Extraction shows power of the data, but should not be interpreted (yet?) as real extraction of kaon FF!

“Chew-Low” type extraction

$F_{\pi^+}(Q^2)$ Measurements before 1997



- Older data at large Q^2 ($> 1 \text{ GeV}^2$) extracted F_{π} from unseparated cross sections

- Used extrapolation of σ_T fit at low Q^2 to isolate σ_L

- Largest Q^2 points also taken at large $-t_{min}$

- Carlson and Milana [*PRL* 65, 1717(1990)] predict $M_{p\text{QCD}}/M_{\text{pole}}$ grows dramatically for $-t_{min} > 0.2 \text{ GeV}^2$

• Pole term may not dominate!

F_π Backgrounds



- Carlson and Milana prediction only real guidance as to size of non-pole backgrounds
- $-t_{min} < 0.2 \text{ GeV}^2$ constraint limits Q^2 reach of F_π measurements (for older data, 6 GeV JLab data, and future 12 GeV JLab measurements)
- Measurement of π^0 longitudinal cross section could help constrain pQCD backgrounds
- Example: in a GPD framework, π^+ and π^0 cross sections involve different combinations of same GPDs – **but π^0 has no pole contribution**

π^0

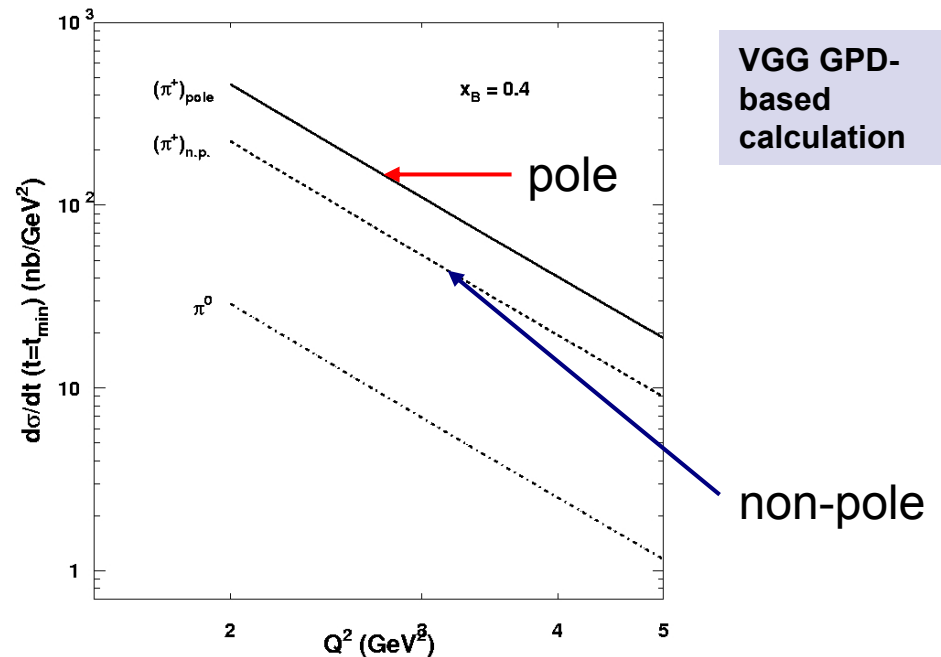
$$A_{p\pi^0} \sim (e_u \tilde{H}^u - e_d \tilde{H}^d)$$

$$B_{p\pi^0} \sim (e_u \tilde{E}^u - e_d \tilde{E}^d)$$

π^+

$$A_{p\pi^+} \sim (\tilde{H}^u - \tilde{H}^d)(e_u + e_d)$$

$$B_{p\pi^+} \sim (\tilde{E}^u - \tilde{E}^d)(e_u + e_d)$$



F_{π} Program at JLab



• 2 F_{π} experiments have been carried out at JLab (*spokespersons* H.Blok, G. Huber, D.Mack)

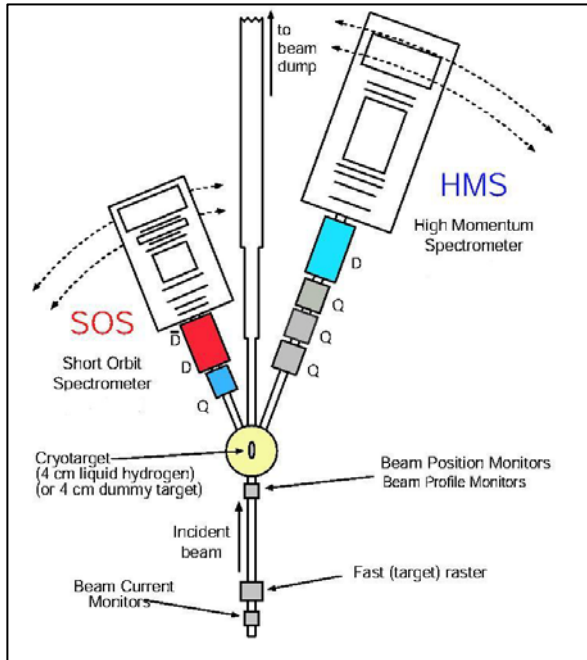
- $F_{\pi-1}$: $Q^2=0.6-1.6 \text{ GeV}^2$
- $F_{\pi-2}$: $Q^2=1.6, 2.45 \text{ GeV}^2$

• Second experiment took advantage of higher beam energy to access larger W , smaller $-t$

Expt	Q^2 (GeV^2)	W (GeV)	$ t_{\min} $ (GeV^2)	E_e (GeV)
$F_{\pi-1}$	0.6-1.6	1.95	0.03-0.150	2.445-4.045
$F_{\pi-2}$	1.6,2.45	2.22	0.093,0.189	3.779-5.246

- Full deconvolution of $L/T/TT/LT$ terms in cross section
- Ancillary measurement of π^-/π^+ (separated) ratios to test reaction mechanism
- Both experiments ran in experimental Hall C: $F_{\pi-1}$ in 1997 and $F_{\pi-2}$ in 2003

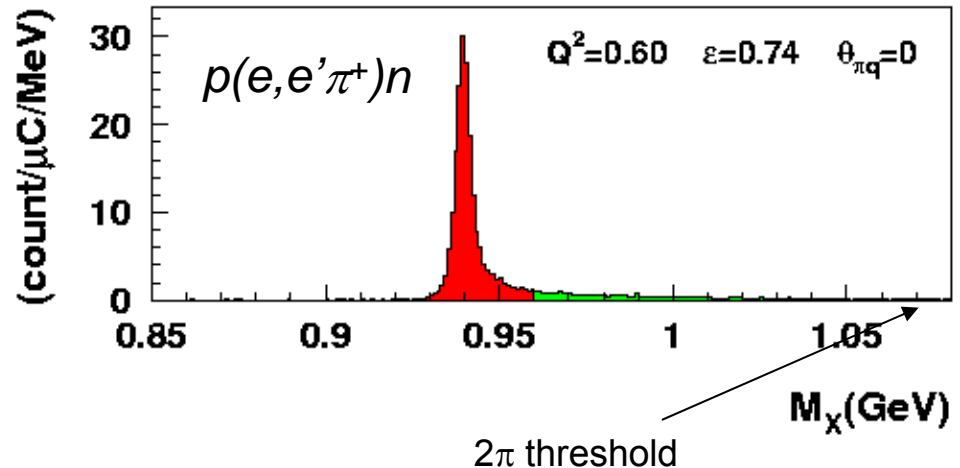
JLab F_{π} Experiment Details



- Short Orbit Spectrometer = e^-
- High Momentum Spectrometer = π^+
 - Relatively small acceptance – easily understood
 - “Pointing”, kinematics well constrained
- Cryogenic targets, high currents yield relatively fast measurement

- Easy to isolate exclusive channel
 - Excellent particle identification
 - CW beam minimizes “accidental” coincidences
 - Missing mass resolution easily excludes 2-pion contributions

$F_{\pi-1}$ missing mass distribution

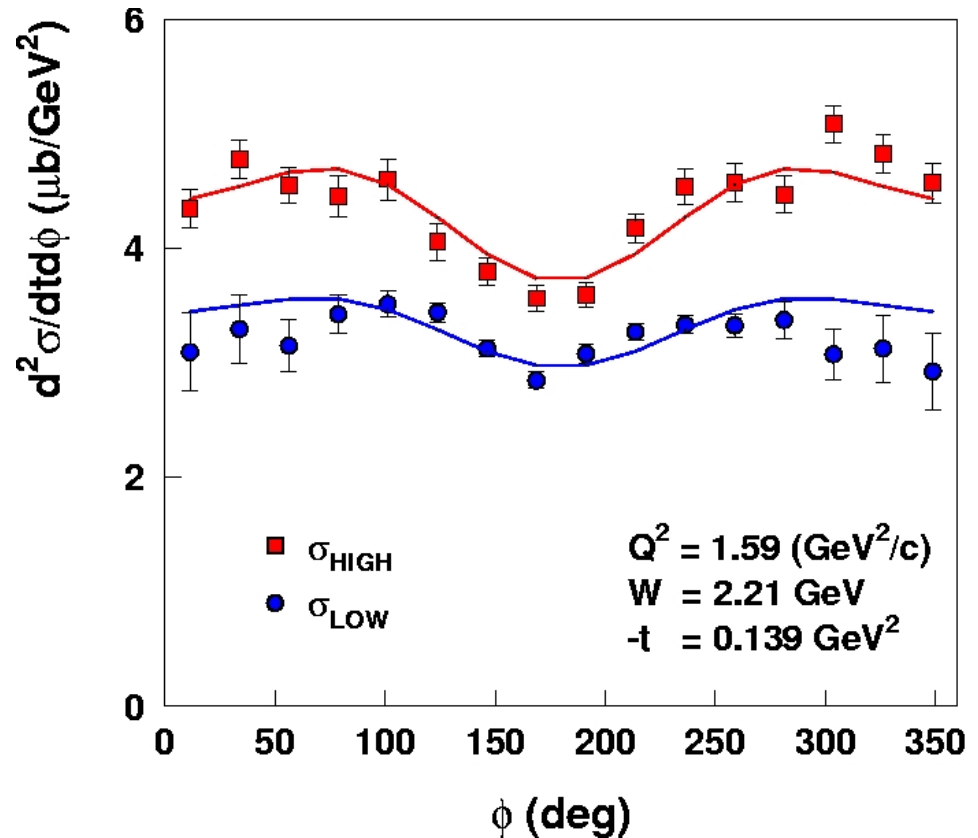


Measuring σ_L



$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

- Rosenbluth separation required to isolate σ_L
 - Measure cross section at fixed $(W, Q^2, -t)$ at 2 beam energies
 - Simultaneous fit at 2 ε values to determine σ_L , σ_T , and interference terms
- Control of point-to-point systematic uncertainties crucial due to $1/\varepsilon$ error amplification in σ_L
- Careful attention must be paid to spectrometer acceptance, kinematics, efficiencies, ...



F_π Extraction from JLab data



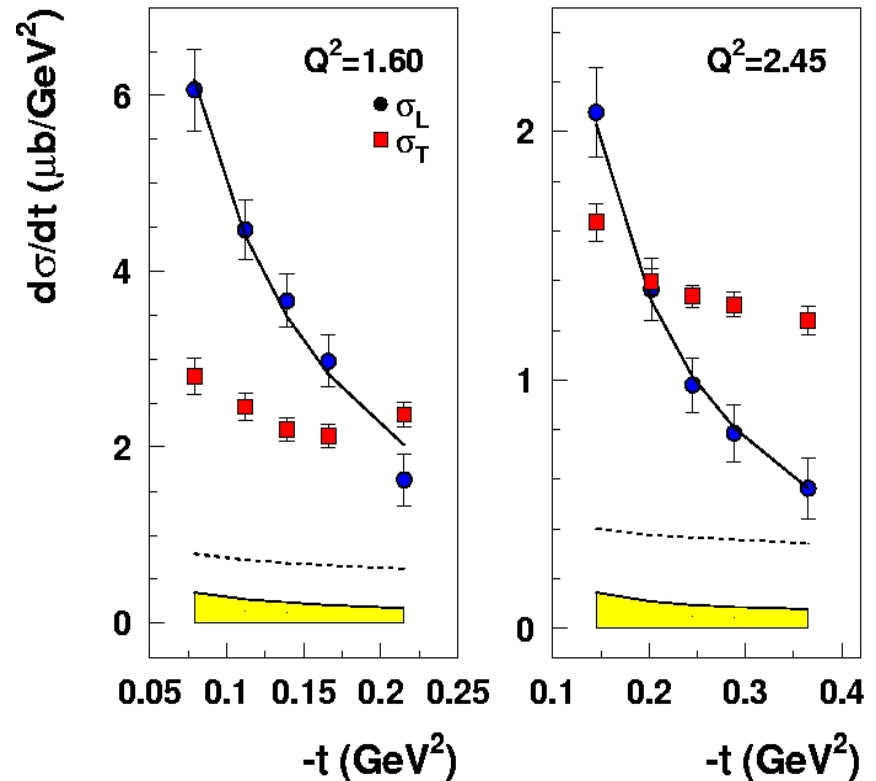
- Model is required to extract F_π from σ_L

Horn et al, PRL97, 192001,2006

- JLab F_π experiments used the VGL Regge model

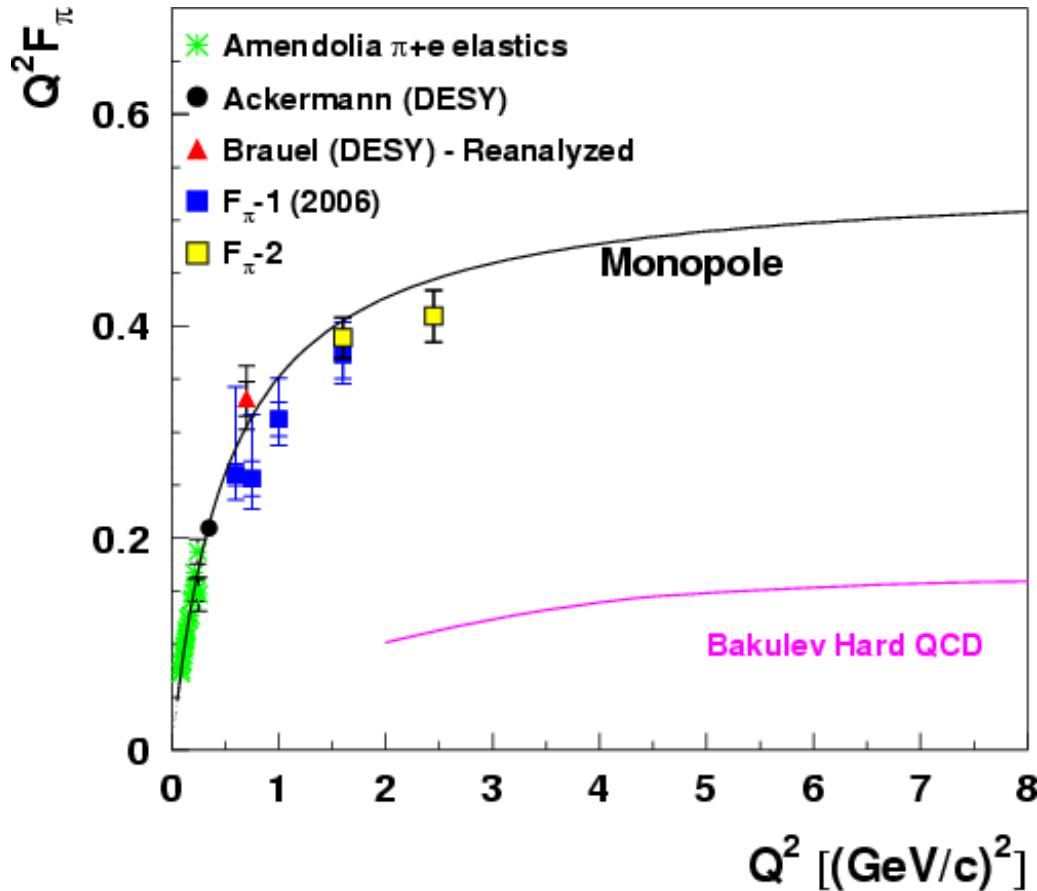
[Vanderhaeghen, Guidal, Laget, PRC 57, 1454 (1998)]

- Propagator replaced by π and ρ Regge trajectories
- Most parameters fixed by photoproduction data
- 2 free parameters: Λ_π , Λ_ρ
- At small $-t$, σ_L only sensitive to Λ_π



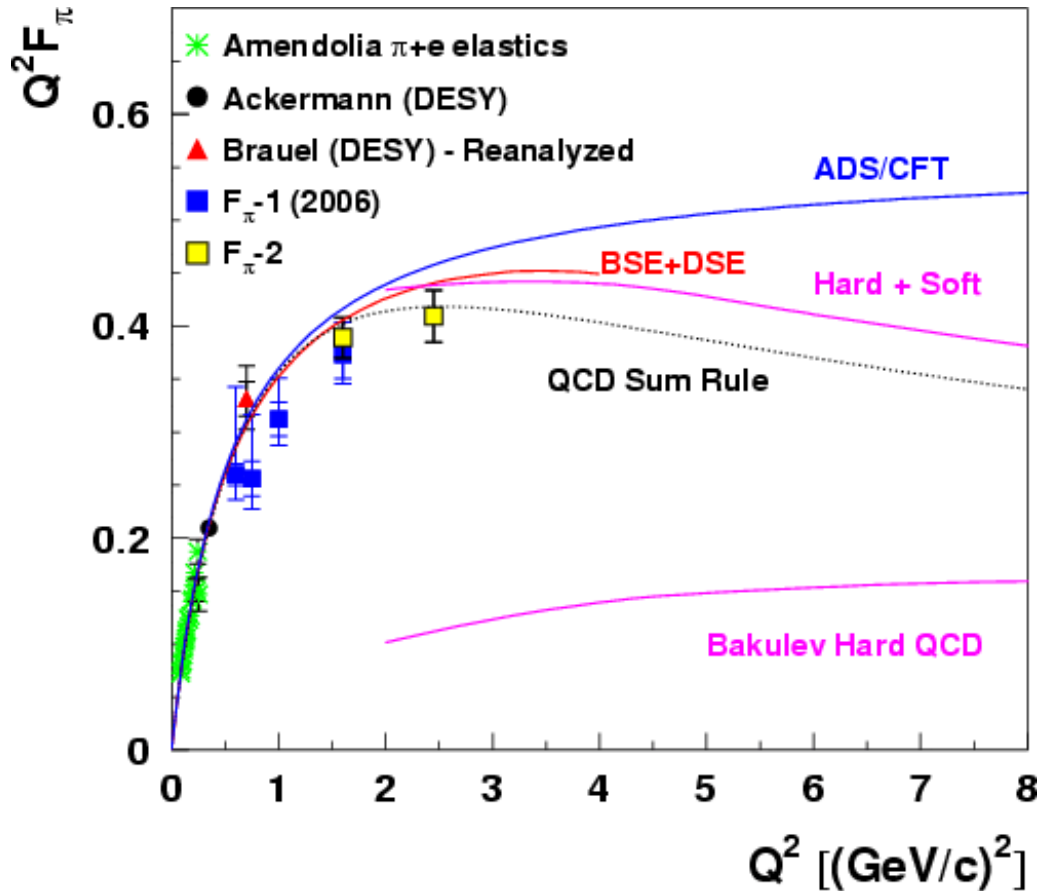
$$F_\pi(Q^2) = \frac{1}{1 + Q^2 / \Lambda_\pi^2}$$

$F_{\pi^+}(Q^2)$ in 2007



- Only true L-T separated data shown
- Trend suggested by extractions from unseparated cross sections still holds
 - Far from asymptotic limit
 - Inclusion of k_T effects has little impact
- Several effective models do a good job describing the data (QCD sum rules, constituent quark models, etc.)

$F_{\pi^+}(Q^2)$ in 2007



Brodsky and de Teramond, hep-th/0702205
 → Anti-de Sitter/Conformal Field Theory approach

Maris and Tandy, Phys. Rev. C62, 055204 (2000)

→ relativistic treatment of bound quarks (Bethe-Salpeter equation + Dyson-Schwinger expansion)

Nesterenko and Radyushkin, Phys. Lett. B115, 410(1982)

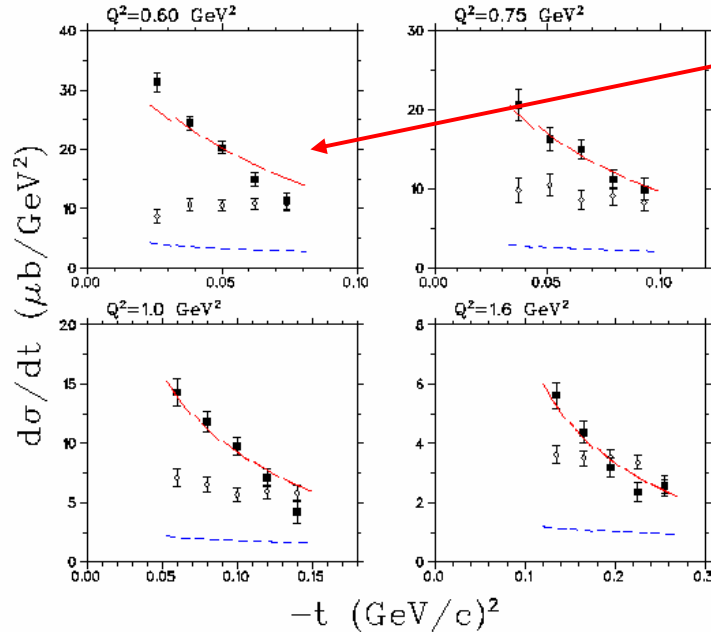
→ Green's function analyticity used to extract form factor

A.P. Bakulev et al, Phys. Rev. D70 (2004)

→ Hard contribution to NLO with improved pion DA

→ Soft contribution from local duality

Model/Interpretation Issues



- VGL Regge model does not describe $-t$ dependence of $F_{\pi-1}^{-1} \sigma_L$ at lowest Q^2

- Leads to large systematic errors for F_{π}

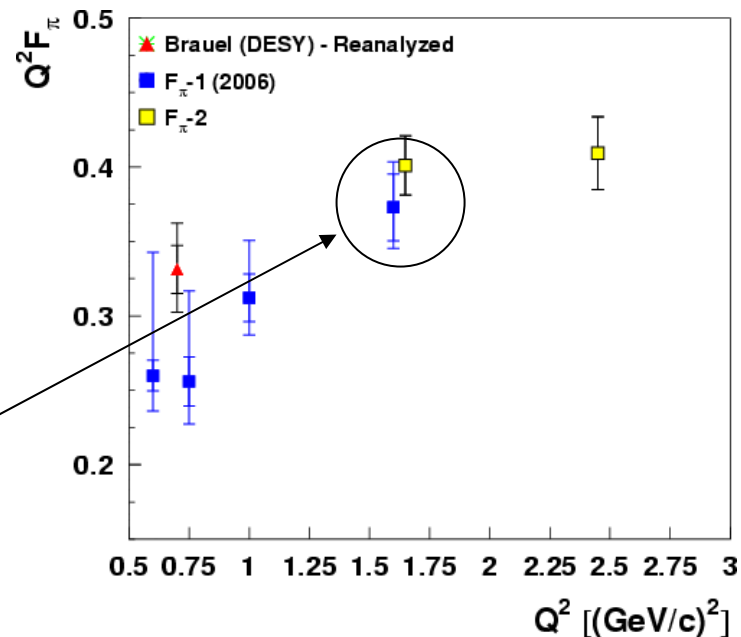
- Underscores the need for additional models

- Even if model describes data, does it give the “physical” form factor?

- Test by extracting FF at different distances from $-t$ pole

- Ex: $F_{\pi-2}$, $-t_{min}=0.093 \text{ GeV}^2$

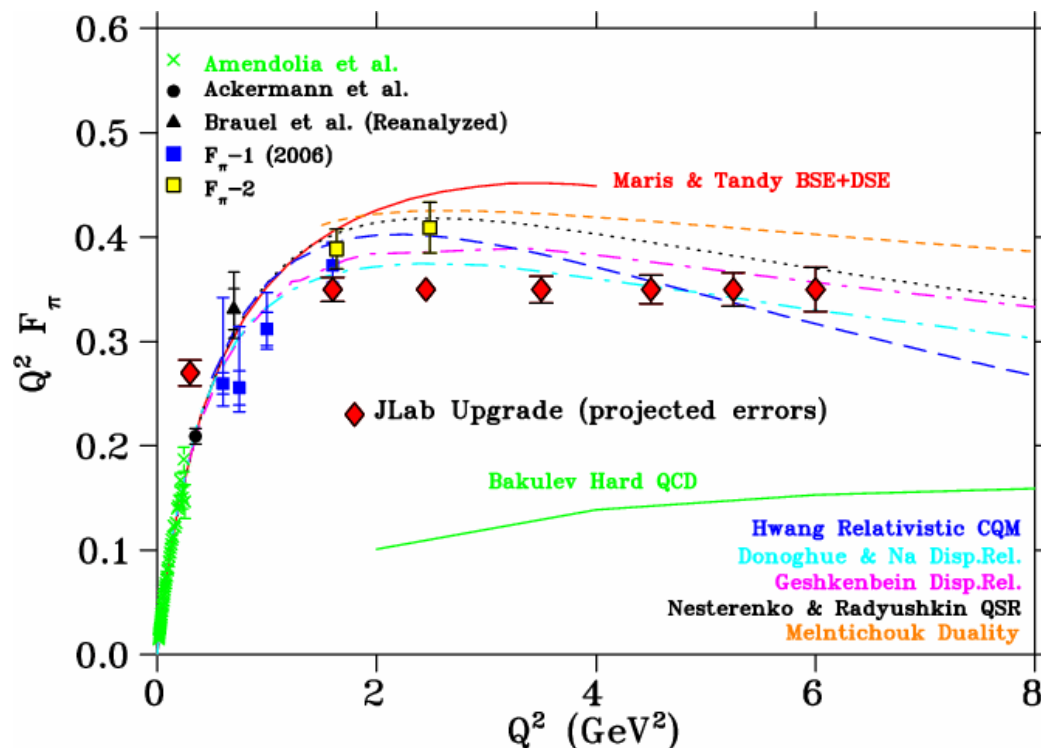
- $F_{\pi-1}$, $-t_{min}=0.15 \text{ GeV}^2$



$F_{\pi^+}(Q^2)$ after JLAB 12 GeV Upgrade



- JLab 12 GeV upgrade will allow measurement of F_{π} up to 6 GeV^2
 - Will we see the beginning of the transition to the perturbative regime?
- Additional point at $Q^2=1.6 \text{ GeV}^2$ will be closer to pole: will provide another constraint on $-t_{min}$ dependence
- $Q^2=0.3 \text{ GeV}^2$ point will be best direct test of agreement with elastic $\pi+e$ data



Summary



- Access to meson form factors in space-like region experimentally difficult
 - π^0 measurements most direct
 - π^+ (K^+ ?) require model or extrapolation to extract FF at physical meson mass
- $F_{\gamma^*\gamma\pi^0} / \text{GeV}^2(Q^2)$ results suggest perturbative behavior at Q^2 as low as 1
- F_{π^+} results more complicated – at $Q^2=2.5 \text{ GeV}^2$, data are still far from simple asymptotic picture
 - Soft processes seem to play a more important role for π^+
- Large Q^2 K^+ form factor measurements even more difficult
 - Large kaon mass means pole further from physically accessible region – interpretation less straightforward
 - F_{K^+} accessible with refined models? With what uncertainty?
- JLab 12 GeV upgrade will dramatically improve π^+ data set
 - Will we begin to see the transition to perturbative regime?