#### Nuclear electroweak processes from ChEFT

#### Luca Girlanda

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#### Credits:

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#### Refs:

Phys.Rev.C78 (2008) 064002, Phys.Rev.C80 (2009) 034004, Phys.Rev.Lett.105 (2010) 232502, Phys.Rev.C81 (2010) 034005, Phys.Rev.C84 (2011) 024001, Phys.Rev.C87 (2013) 014006, Phys.Rev.C89 (2014) 064004, Phys.Rev.C93 (2016) 015501, arXiv:1605.01620

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- after Weinberg's formulation of nuclear ChEFT, nuclear four-current operators were computed in heavy-baryon ChPT at 1-loop [Park-Min-Rho 1993, 1996]

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- after Weinberg's formulation of nuclear ChEFT, nuclear four-current operators were computed in heavy-baryon ChPT at 1-loop [Park-Min-Rho 1993, 1996]
- nuclear electromagnetic operators were reconsidered in "recoil corrected" TOPT [Pastore et al 2009, Piarulli et al. 2011] and with the "unitary transformation method" [Koelling-Epelbaum-Krebs-Meissner 2009, 2011]
- differences were found with the heavy-baryon derivation due to the treatment of "reducible diagrams"

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▶ generic constraints (Poincaré, Parity, Time reversal, ...)

 $\langle N(p')|\bar{\psi}\gamma_{\mu}\psi(x)|N(p)\rangle = e^{-iqx}\bar{u}(p')\left[\gamma_{\mu}F_{1}(q^{2}) + i\frac{\sigma^{\mu\nu}q_{\nu}}{2m}F_{2}(q^{2})\right]u(p)$ 

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► QCD specific constraints  $\rightarrow$  chiral symmetry and SB $\chi$ S ( $\Leftarrow$  color confinement)

Consequences:

 conserved Noether currents, vector and axial quark currents more generally: chiral Ward identities

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Chiral symmetry is not exact, but this can be easily incorporated in the chiral Ward identities

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#### Phenomenological relevance

Noether currents correspond to *physical currents*, coupled to weakly interacting particles their matrix elements enter in processes involving these particles (electron scattering, weak captures, β decays, ...)

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- SBχS ⇒ systematic calculational scheme for low-energy observables indeed pions (as Goldstone bosons)
  - are light,  $m_\pi \ll \Lambda_{
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  - interact weakly at low energies (soft pion theorems)

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however, there is no warranty about the convergence ... expect slower convergence if the mass scales are not well separated

### The effective theory

QFT of interacting pions and nucleons

$$Z[\mathbf{v}_{\mu}, \mathbf{a}_{\mu}, \mathbf{s}, \mathbf{p}, \eta, \bar{\eta}] = \int \mathcal{D}[\mathbf{N}, \bar{\mathbf{N}}, \pi] \mathrm{e}^{i \int d\mathsf{x} \mathcal{L}_{\mathrm{eff}}(\mathbf{N}, \bar{\mathbf{N}}, \pi, \mathbf{v}_{\mu}, \mathbf{a}_{\mu}, \mathbf{s}, \mathbf{p}, \eta, \bar{\eta})}$$

•  $\mathcal{L}_{\text{eff}}$  shares the QCD  $\chi S \implies$  chiral Ward identities are satisfied (besides general principles: analiticity, unitarity, crossing symmetry, clustering ...)

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- symmetry restricts the form of L<sub>eff</sub>, yet there are infinite structures increasingly suppressed by powers of small momenta or quark masses
- dynamical fields are integrated upon
   physical scattering amplitudes do not depend on the choice of pions and nucleons interpolating fields
- this gives useful checks for the calculation, and allows to use field equations of motion iteratively

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#### Low-energy expansion

the steps to be taken

- ▶ derive  $H = H_0 + H_1$  from  $\mathcal{L}_{\text{eff}}$  in the canonical formalism  $(\mathcal{H}_1 \neq -\mathcal{L}_1)$
- higher derivative theory! ⇒ eliminate higher time derivatives using iteratively fields' equations of motion
- compute in TOPT

$$\langle f|T|i\rangle = \langle f|H_l \sum_n \left(\frac{1}{E_i - H_0 + i\epsilon}H_l\right)^{n-1}|i\rangle$$

order by counting small momenta
 N vertices, N<sub>K</sub> purely nucleonic intermediate states, L loops:

$$\left[\prod_{i=1}^{N} p^{\nu_i}\right] \left(\frac{1}{p}\right)^{(N-N_K-1)} \left(\frac{1}{p^2}\right)^{N_K} \left(p^3\right)^L$$

Also expand recoil corrections

$$\frac{1}{E_i - E_l - \omega_{\pi}} \sim -\frac{1}{\omega_{\pi}} \left[ 1 + \frac{E_i - E_l}{\omega_{\pi}} + \dots \right]$$

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#### Renormalization

ultraviolet divergences are handled in dimensional regularization, and renormalized in the standard way

$$\pi = \sqrt{Z_{\pi}}\pi^{r}, \quad N = \sqrt{Z_{N}}N^{r}, \quad m_{\pi}^{r\,2} = m_{\pi}^{2} + \delta m_{\pi}^{2}, \quad m^{r} = m + \delta m$$

imposing that the nucleon and pion propagators behave as they should inside general time-ordered diagrams

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#### pion decay constant and nucleon axial charge are also renormalized



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finite scheme dependence may arise, but divergencies are dictated by general properties

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#### Irreducible kernels

as a result we have a well defined low-energy expansion, e.g. for the  $N\!N$  amplitude,

 $T = T^{(0)} + T^{(1)} + T^{(2)} + ..., \quad T^{(n)} \sim O(p^n)$ 

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- ▶ an infinite resummation is needed to account for nuclear bound states.
- we define an irreducible kernel  $v = v^{(0)} + v^{(1)} + ...$  that, when iterated in the LS equation, generates the on-shell T

 $T = v + vG_0v + vG_0vG_0v + \dots$ 

order by order in the chiral expansion

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Solving for  $v^{(n)}$  we have

where  $G_0 \sim p^{-2} d^3 p \sim O(p)$ 

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Solving for  $v^{(n)}$  we have

$$\begin{aligned} \mathbf{v}^{(0)} &= \mathbf{T}^{(0)} , \\ \mathbf{v}^{(1)} &= \mathbf{T}^{(1)} - \left[ \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \right] , \\ \mathbf{v}^{(2)} &= \mathbf{T}^{(2)} - \left[ \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \right] \\ &- \left[ \mathbf{v}^{(1)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} + \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(1)} \right] , \\ \mathbf{v}^{(3)} &= \mathbf{T}^{(3)} - \left[ \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \right] \\ &- \left[ \mathbf{v}^{(1)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} + \text{permutations} \right] \\ &- \left[ \mathbf{v}^{(2)} \, \mathbf{G}_0 \, \mathbf{v}^{(0)} + \mathbf{v}^{(0)} \, \mathbf{G}_0 \, \mathbf{v}^{(2)} \right] - \left[ \mathbf{v}^{(1)} \, \mathbf{G}_0 \, \mathbf{v}^{(1)} \right] . \end{aligned}$$

where  $G_0 \sim p^{-2} d^3 p \sim O(p)$ 

- this procedure allows to systematically subtract the terms due to the iteration of the dynamical equation
- nevertheless it is ambiguous, because we need the  $v^{(n)}$  off shell

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There exist a whole class of 2nd order recoil corrections to OPE which are equivalent on shell, parametrized by a parameter  $\nu$  (Friar 1980)

$$v_{RC}^{(2)}(\nu = 0) = v_{\pi}^{(0)}(\mathbf{k}) \frac{(E_1' - E_1)^2 + (E_2' - E_2)^2}{2\omega_k^2}$$
$$v_{RC}^{(2)}(\nu = 1) = -v_{\pi}^{(0)}(\mathbf{k}) \frac{(E_1' - E_1)(E_2' - E_2)}{2\omega_k^2}$$

$$v_{RC}^{(2)}(
u = 1) = -v_{\pi}^{(0)}(\mathbf{k}) rac{(E_1' - E_1)(E_2' - E_2)}{\omega_k^2}$$

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The off-shell ambiguities will affect successive terms  $v^{(n)}$ : for each  $v^{(2)}(\nu)$  there is a corresponding  $v^{(3)}$ 

However, the different choices are related by a unitary transformation,

$$H(\nu) = e^{-iU(\nu)}H(\nu = 0)e^{iU(\nu)}$$

with  $U = U^{(0)} + U^{(1)} + ...$  explicitly

$$i U^{(0)}(\nu) = -\nu \frac{v_{\pi}^{(0)}(\mathbf{p}'-\mathbf{p})}{(\mathbf{p}'-\mathbf{p})^2 + m_{\pi}^2} \frac{p'^2 - p^2}{2 m_N}, \quad i U^{(1)}(\nu) = -\frac{\nu}{2} \int_{\mathbf{s}} \frac{v_{\pi}^{(0)}(\mathbf{p}'-\mathbf{s})v_{\pi}^{(0)}(\mathbf{s}-\mathbf{p})}{(\mathbf{p}'-\mathbf{s})^2 + m_{\pi}^2}$$

thus extending the unitary equivalence to the TPEP

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Analogously for the axial transition operator  $v_5 = A^0 \rho_5 - \mathbf{A} \cdot \mathbf{j}_5$  we start by expanding the amplitude  $T_5 = T_5^{(-3)} + T_5^{(-2)} + \dots$  and then match order by order to the iteration of  $v + v_5$ 

$$\begin{split} v_5^{(-3)} &= T_5^{(-3)} \\ v_5^{(-2)} &= T_5^{(-2)} - \left[ v_5^{(-3)} \, G_0 \, v^{(0)} + v^{(0)} \, G_0 \, v_5^{(-3)} \right] \,, \\ v_5^{(-1)} &= T_5^{(-1)} - \left[ v_5^{(-3)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] - \left[ v_5^{(-2)} \, G_0 \, v^{(0)} + v^{(0)} \, G_0 \, v_5^{(-2)} \right] \,, \\ v_5^{(0)} &= T_5^{(0)} - \left[ v_5^{(-3)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] - \left[ v_5^{(-2)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] \\ &- \left[ v_5^{(-1)} \, G_0 \, v^{(0)} + v^{(0)} \, G_0 \, v_5^{(-1)} \right] - \left[ v_5^{(-3)} \, G_0 \, v^{(2)} + v^{(2)} \, G_0 \, v_5^{(-3)} \right] \\ v_5^{(1)} &= T_5^{(1)} - \left[ v_5^{(-3)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] \\ &- \left[ v_5^{(-2)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] - \left[ v_5^{(-1)} \, G_0 \, v^{(0)} \, G_0 \, v^{(0)} + \ldots \right] \\ &- \left[ v_5^{(0)} \, G_0 \, v^{(0)} + v^{(0)} \, G_0 \, v_5^{(0)} \right] - \left[ v_5^{(-3)} \, G_0 \, v^{(0)} + \ldots \right] \\ &- \left[ v_5^{(-3)} \, G_0 \, v^{(3)} + v^{(3)} \, G_0 \, v_5^{(-3)} \right] \,, \end{split}$$

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at this order, the offshell ambiguity in v only affects j<sub>5</sub>

we expect unitary equivalence of different choices

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# Axial charge diagrams



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- checks of calculation
  - independence of the pion field choice
  - after renormalization, results are finite, with the known anomalous dimensions of LECs
  - current conservation in the chiral limit is satisfied order by order in the power counting

$$\mathbf{q} \cdot \mathbf{j}_5 = [H, \rho_5], \quad H = T^{(-1)} + v^{(0)} + v^{(2)} + \dots$$

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axial current depends only on 1 LEC, z<sub>0</sub>, related to c<sub>D</sub> entering TNI Gardestig-Phillips 2006 PRL]

$$c_D = 2\Lambda f_\pi^2 z_0$$

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 Image: Constraint of the con

$$c_D = 2\Lambda f_\pi^2 z_0$$

axial charge depends on 3 independent short-distance LECs z<sub>1,2,3</sub>, yet to be determined
 a further combination is a 1/m correction induced by z<sub>0</sub>

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# Fitting of $z_0$ from <sup>3</sup>H $\beta$ -decay

- we evaluate the individual orders contribution to the Gamow-Teller matrix element with Montecarlo techniques
- ► accurate trinucleon wavefunction from HH method AV18/UIX and chiral N3LO/N2LO ( $\Lambda = 500, 600 \text{ MeV}$ )
- GT matrix element extracted from

$$(1+\delta_R)tf_V = rac{K/G_V^2}{\langle \mathbf{F} \rangle^2 + f_A/f_V g_A^2 \langle \mathbf{GT} \rangle^2}, \quad GT_{\mathrm{EXP}} = 0.9511 \pm 0.0013$$

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▶ also 3-body currents enter at the same order  $O(p^4)$ 

[Park et al. 2003 PRC]

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#### Convergence study cumulative contributions



AV18/UIX

# Fitting with the chiral TNI $\Lambda = 500 \text{ MeV}_{\Lambda_{\chi}=1 \text{ GeV}}$ $0.2 \begin{bmatrix} - & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & &$



#### Fitting with the chiral TNI $\Lambda = 600 \operatorname{MeV}_{\Lambda_{\gamma}=1 \text{ GeV}} V$ -0.6 c<sub>p</sub>=-0.443 (N3LO) -0.8 c<sub>D</sub>=-2.030 (N4LO) -1.2 പ്പ -1.4 • $B(^{3}H)$ •--• $B(^{3}He)$ -1.6 - B(A=3)-average and -1.8

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c<sub>D</sub>

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# Concluding remarks

- nuclear axial operators derived in TOPT open the way to fully consistent calculation of electroweak observables of few-nucleon systems in ChEFT
- our formalism allows to control the off-shell ambiguities by addressing simultaneously the transition operator and the interaction potential
- finiteness upon renormalization, current conservation in the chiral limit, independence on the pion field choice, give us confidence on the formalism
- convergence looks problematic for hybrid calculations
- strict consistency not achieved yet in the chiral calculations need to include the N3LO TNI and to match different off-shell behaviours
- ▶ open issues: are contact interaction to be "promoted"? will the inclusion of ∆ improve convergence?

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