

Cascades on the Lattice

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LHP Collaboration

LHPC collaborators

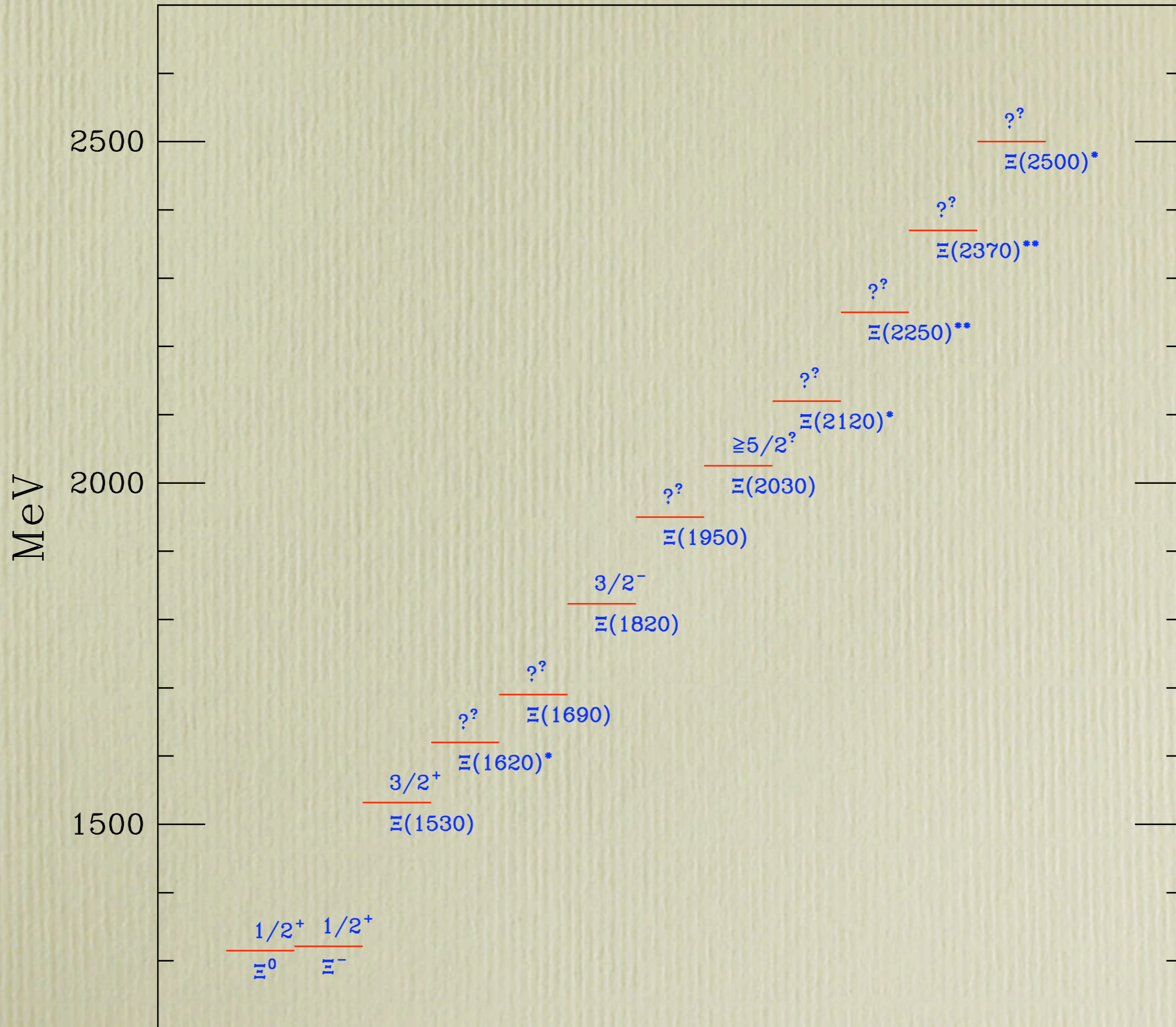
- R. Edwards (Jlab)
- G. Fleming (Yale)
- P. Hagler (Vrije Universiteit)
- C. Morningstar (CMU)
- J. Negele (MIT)
- A. Pochinsky (MIT)
- D. Renner (UofA)
- D. Richards (Jlab)
- W. Schroers (DESY)

Summary

- What can the Lattice do for you?
- How will we make it happen?
- What has been done?
- Some **very preliminary** results from **LHPC**

Thanks to [D. Richards](#)

Particle Data Group



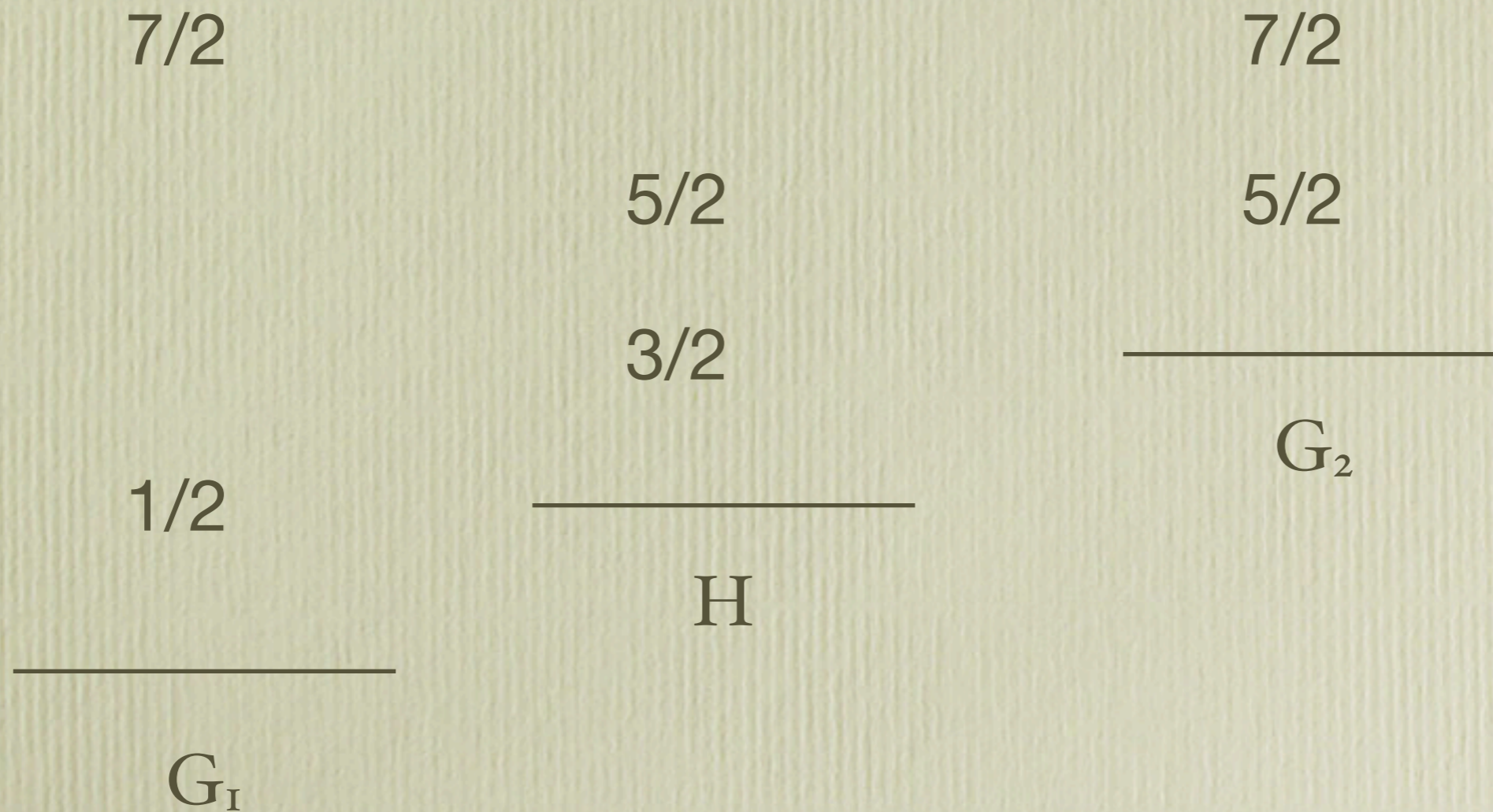
Lattice QCD

- Spectrum calculation: **simplest thing to do**
- Strange quarks don't decay
 - stable cascades
- Better signal than protons (strange quark is heavy)
- Can vary quark masses
- Quantum numbers easy to identify

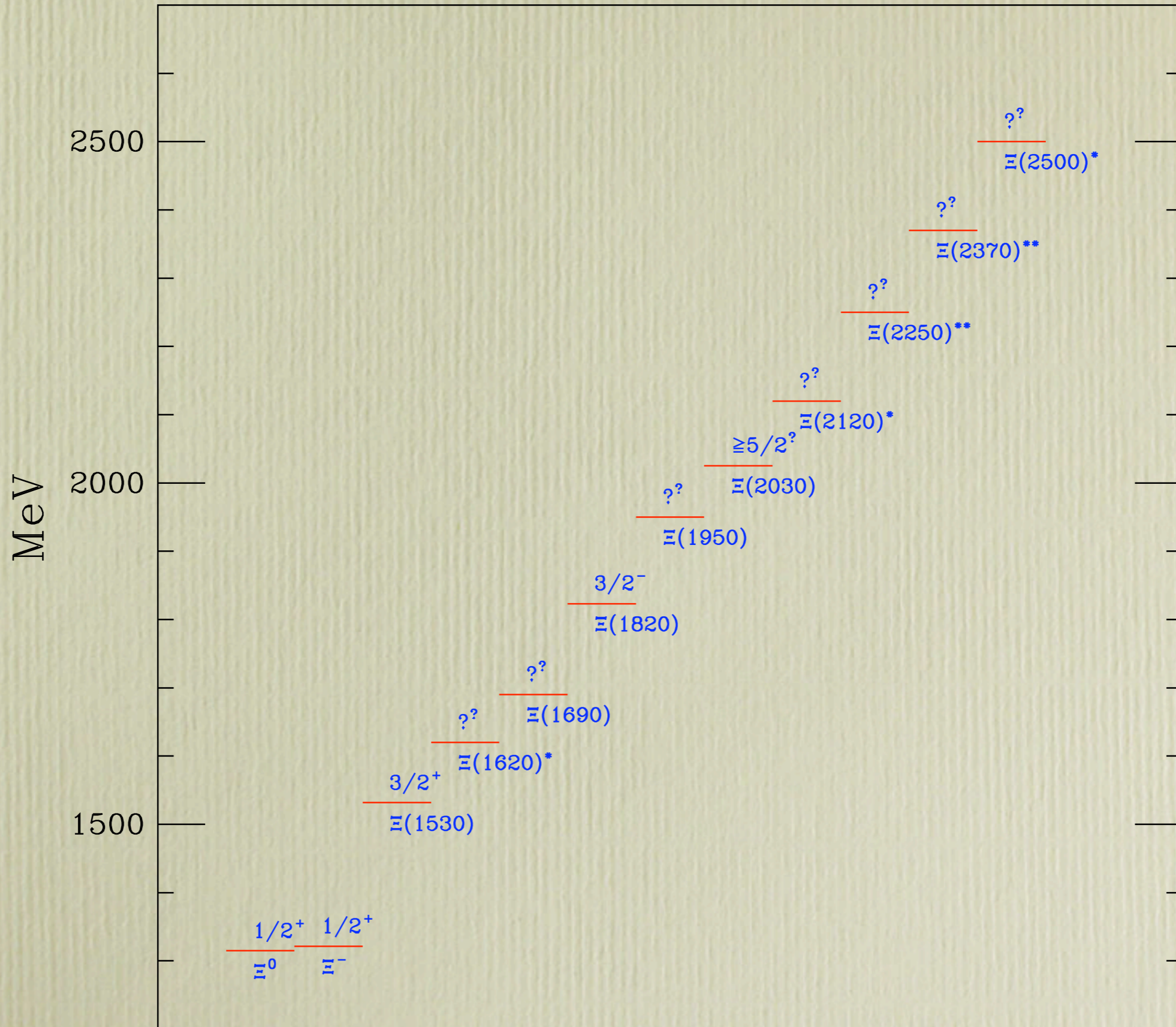
Difficulties

- Strong decays: Unstable particles
 - Finite volume techniques
 - Heavy quark masses: above threshold
- Broken rotational symmetry
 - Angular momentum not a good quantum number
- Vacuum polarization effects
 - Inefficient algorithms
 - mass of up and down quarks too light!
- Chiral symmetry and lattice fermions

Lattice Operators



Particle Data Group



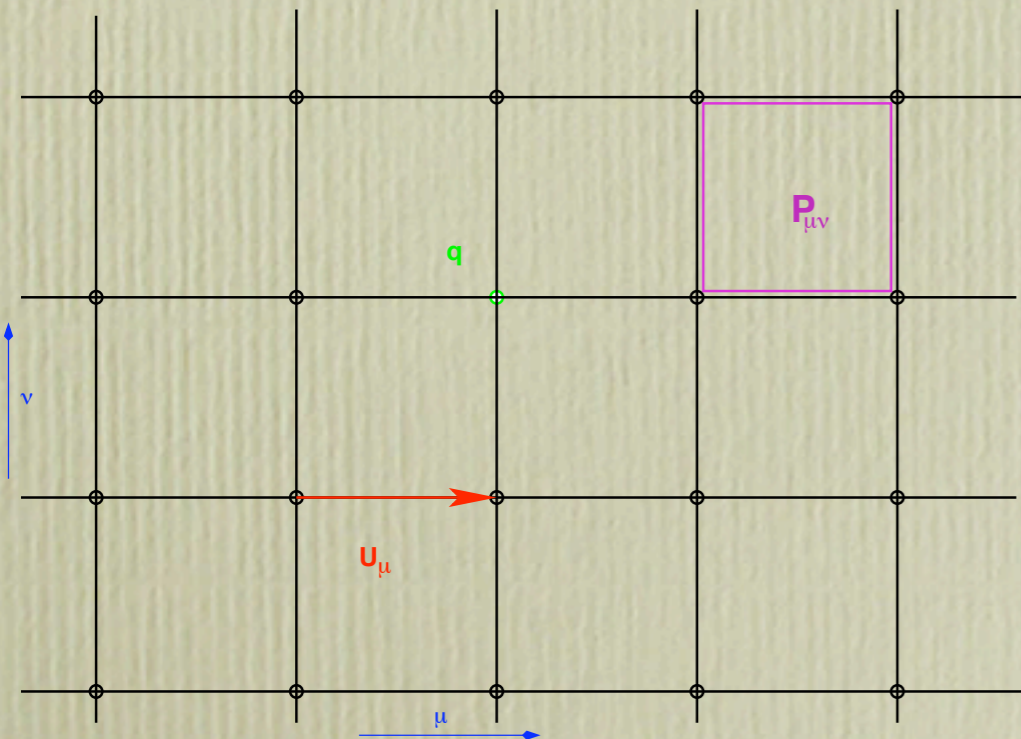
Lattice QCD

In continuous Euclidian space:

$$\mathcal{Z} = \int \mathcal{D}q \mathcal{D}\bar{q} \mathcal{D}A_\mu e^{-S[\bar{q}, q, A_\mu]}$$

$$\langle \mathcal{O} \rangle = \frac{1}{\mathcal{Z}} \int \mathcal{D}q \mathcal{D}\bar{q} \mathcal{D}A_\mu \mathcal{O}(\bar{q}, q, A_\mu) e^{-S[\bar{q}, q, A_\mu]}$$

Lattice regulator:



Gauge sector:

$$U_\mu(x) = e^{-iaA_\mu(x + \frac{\hat{\mu}}{2})}$$

Fermion sector:

$$\mathcal{Z} = \int dU \det(\Delta)^{n_f} e^{-\sum \frac{\beta}{N_c} \text{ReTr}[1 - P_{\mu,\nu}(x)]}$$

Fermion doubling

Chiral symmetry breaking

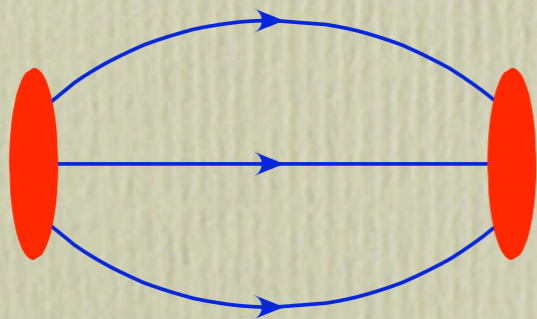
Spectrum

- Correlation functions

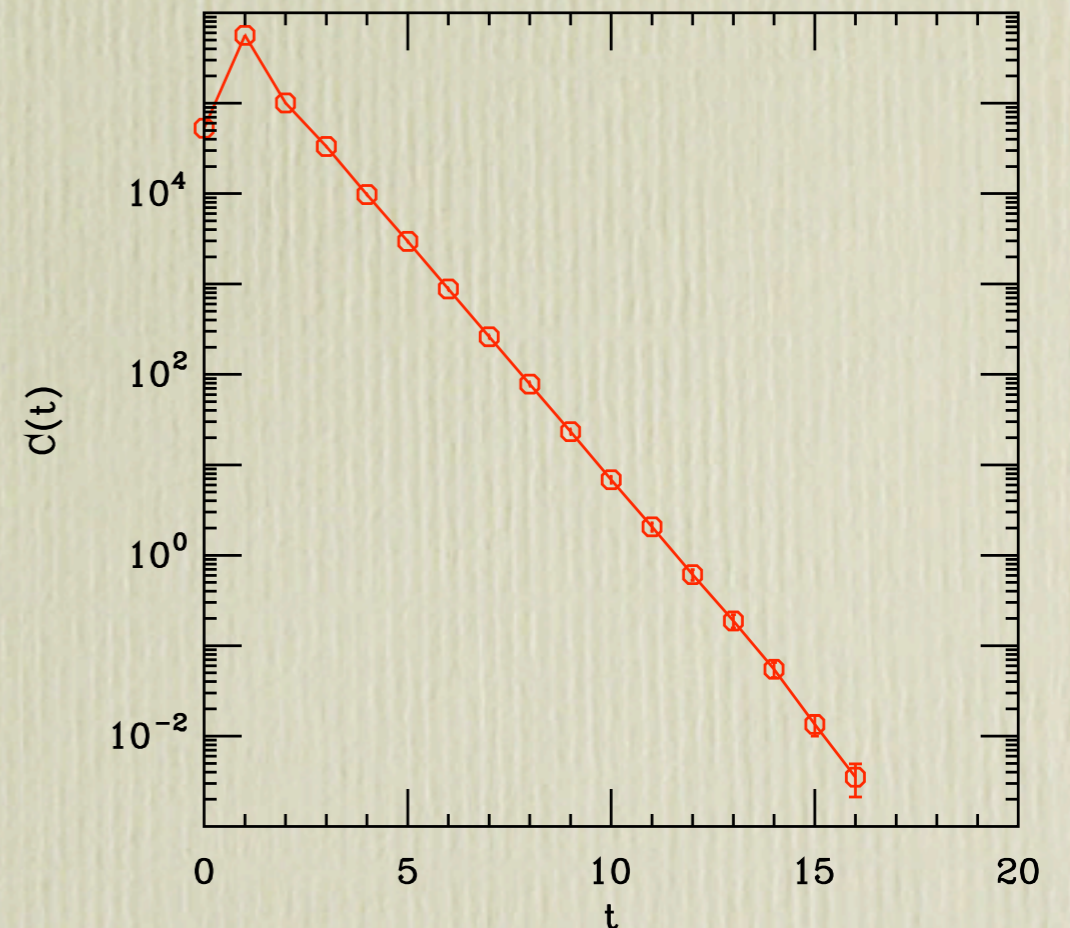
$$C(t) = \langle J(t) \bar{J}(0) \rangle$$

- J an interpolating field for some state

Proton



$$C(t) = Z_0 e^{-M_0 t} + \dots$$



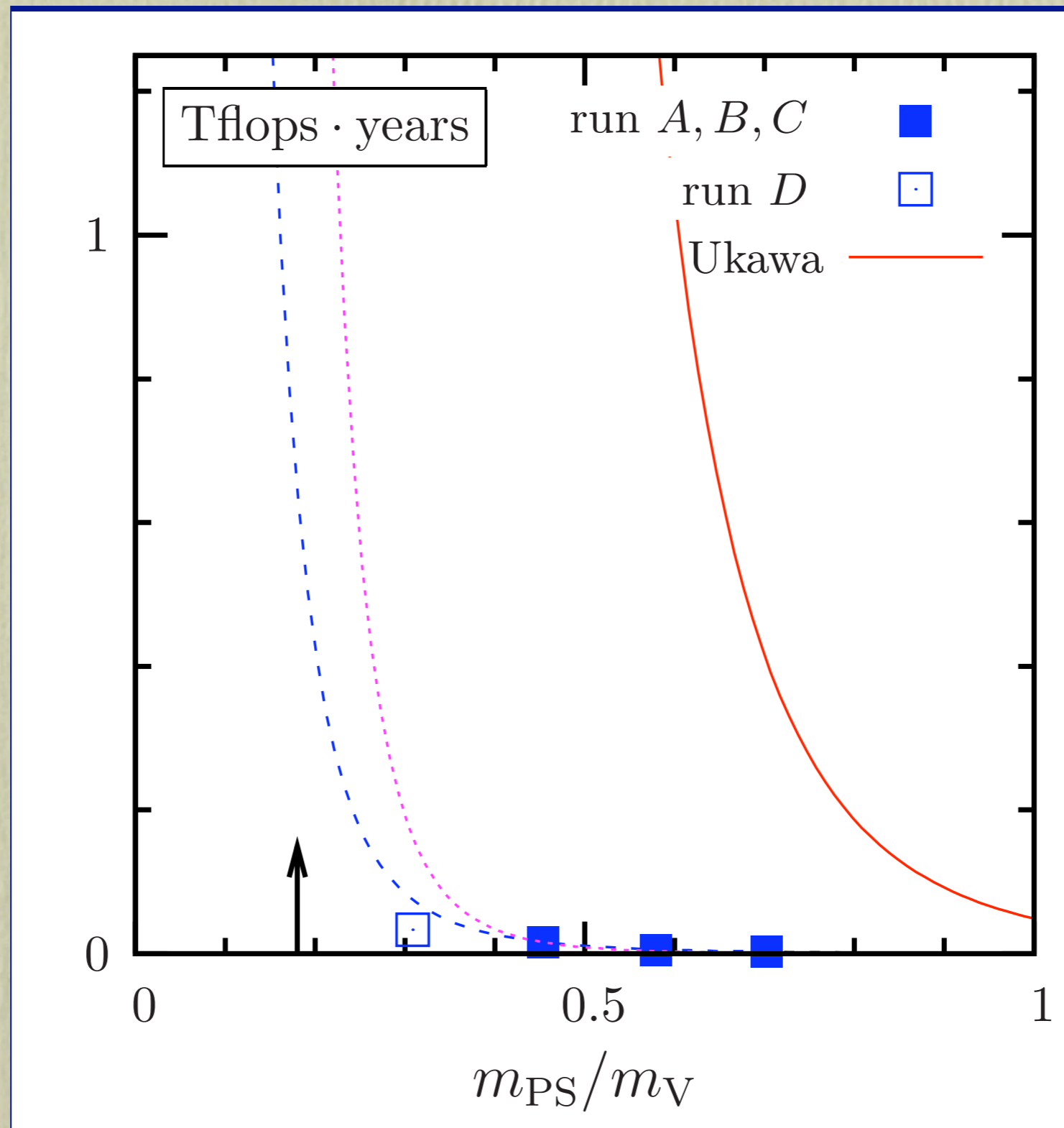
Need to do

- Continuum extrapolation
- Chiral extrapolation
- Infinite volume extrapolation
- In all cases use Effective field theory
- Scale setting
 - Heavy quark potential (Sommer scale)
 - Rho mass (bad choice)
 - Heavy quarkonia

What does it take

- 2+1 Dynamical flavors
 - 2 light (up down) 1 heavy (strange)
 - charm bottom top (treated in HQET as external)
- Light quark masses $m_{\pi} < 400\text{MeV}$
 - Chiral extrapolations
 - Finite volume corrections
 - Numerical algorithm slows down (algorithm scaling $\sim \frac{1}{m_q^{2.5}}$)
- Continuum extrapolations
 - compute at several lattice spacings (algorithm scaling $\sim \frac{1}{a^7}$)

The Berlin Wall

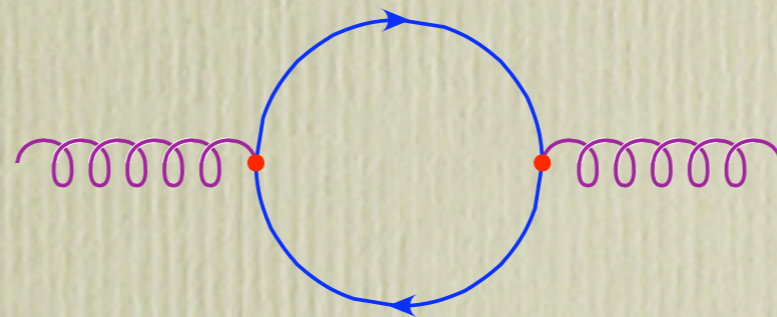


Urbach (ILFTN 3)

Queching

$$\mathcal{Z} = \int dU \det(\Delta)^{n_f} e^{-\sum \frac{\beta}{N_c} \text{ReTr}[1 - P_{\mu,\nu}(x)]}$$

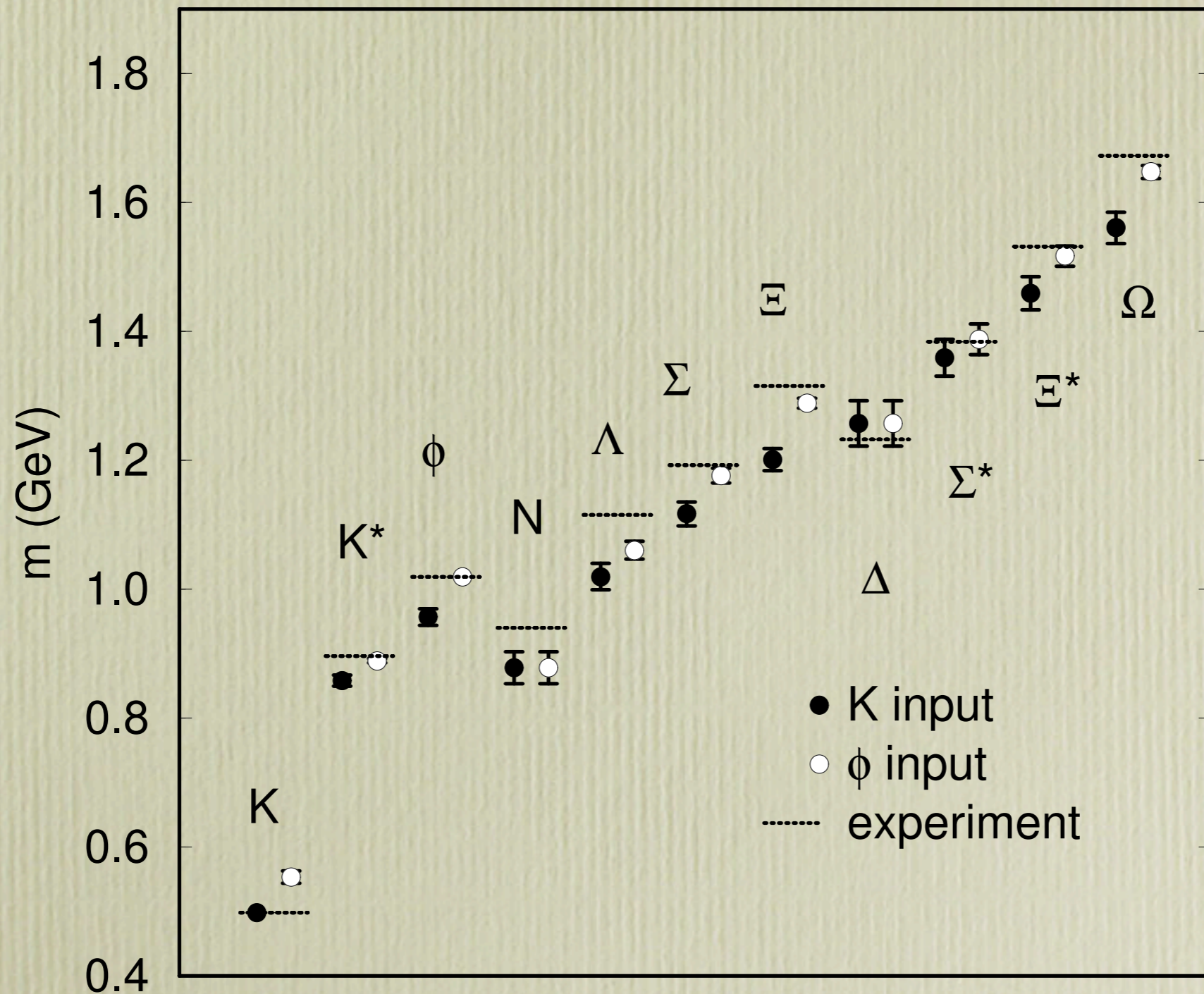
The computation simplifies if we ignore the fermion loops



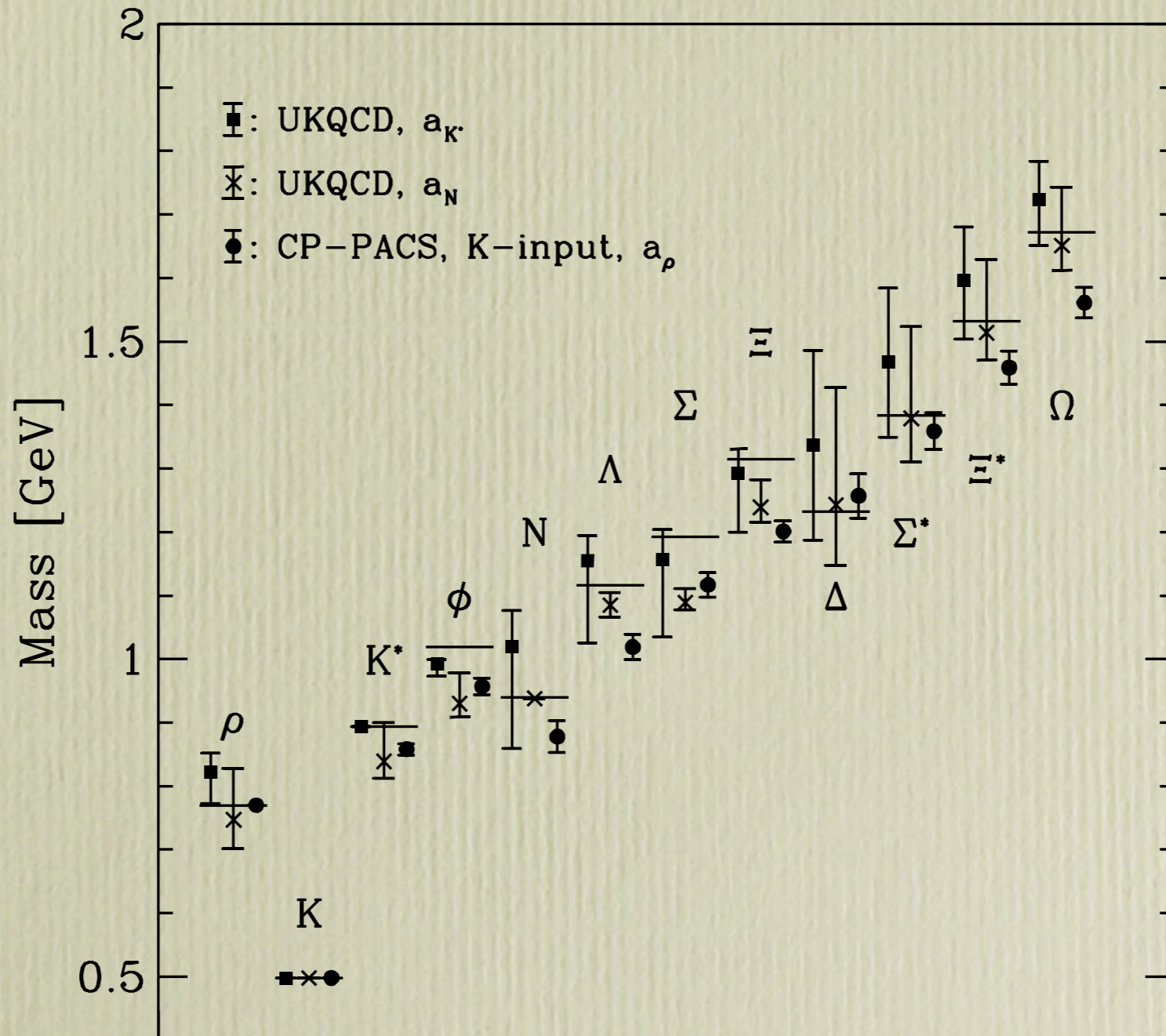
$$\det(\Delta) = 1$$

Uncontrolled “approximation”

Quenched spectrum



Quenched Spectrum

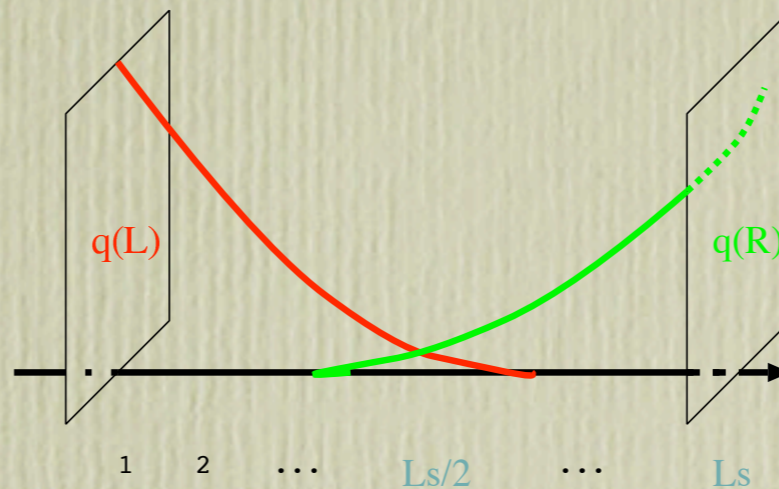


Recent Developments

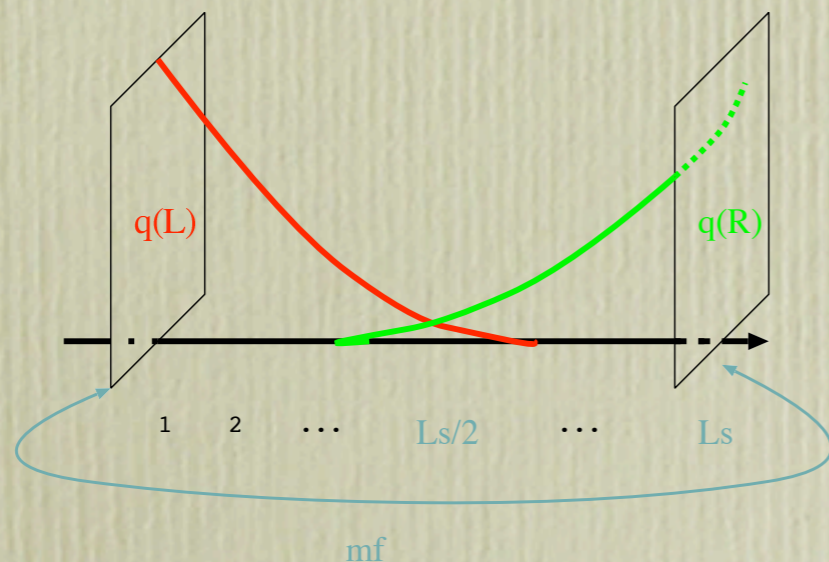
- Cheap dynamical fermions (Kogut-Susskind)
 - “Taste” breaking
 - Improved KS action (Asqtad $O(a^4, g^2 a^2)$) [KO, Sugar, Toussaint ‘99]
 - MILC has generated lattices: Ready to milk the MILC
- Chiral symmetry on the lattice ($O(a^2)$ errors)
 - Domain wall fermions [Kaplan -- Shamir]
 - Overlap fermions [Neuberger, Narayanan]
 - Costly for dynamical: RBC now starting
 - Improvements:
 - Improved gauge actions [KO with RBC ‘02]
 - Mobius fermions [Brower, Neff, KO ‘04]
- Big Computers!

Domain Wall Fermions for QCD

Formulate the 5D Wilson fermions with mass $M \neq 0$ in $s \in [1, L_s]$



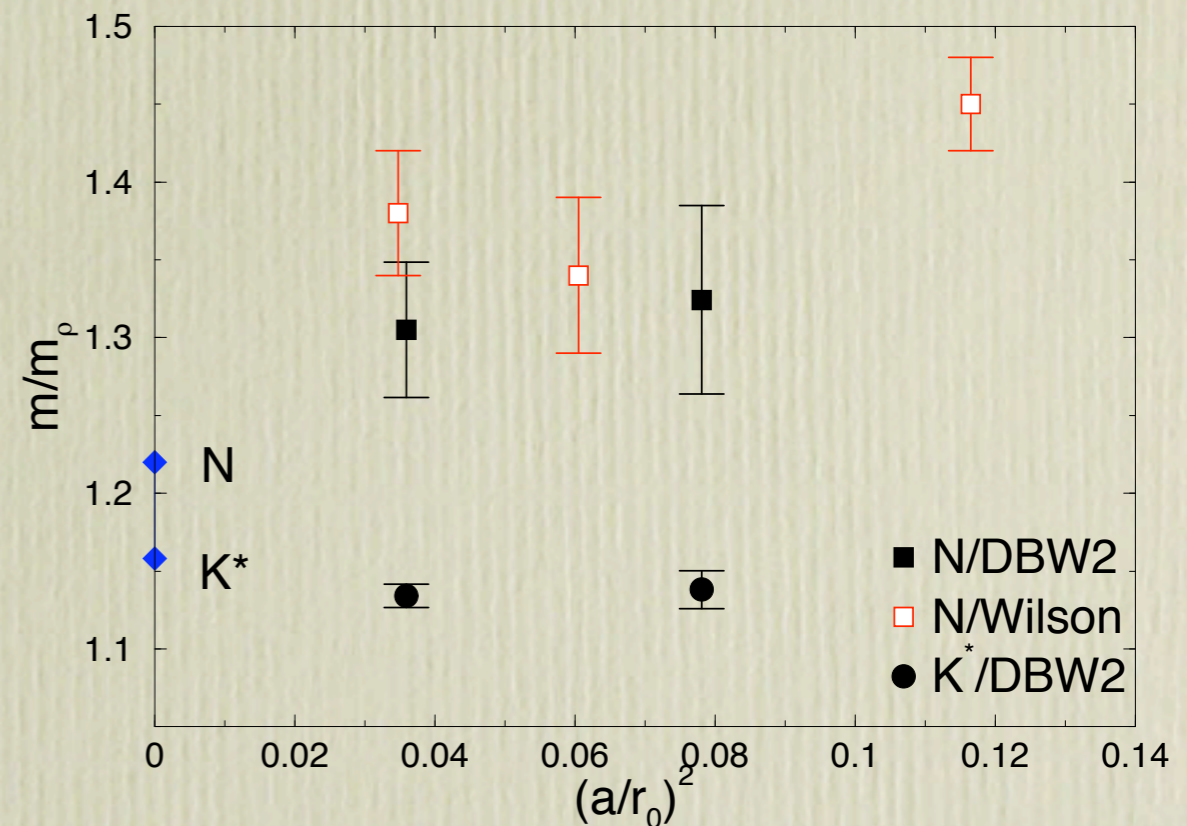
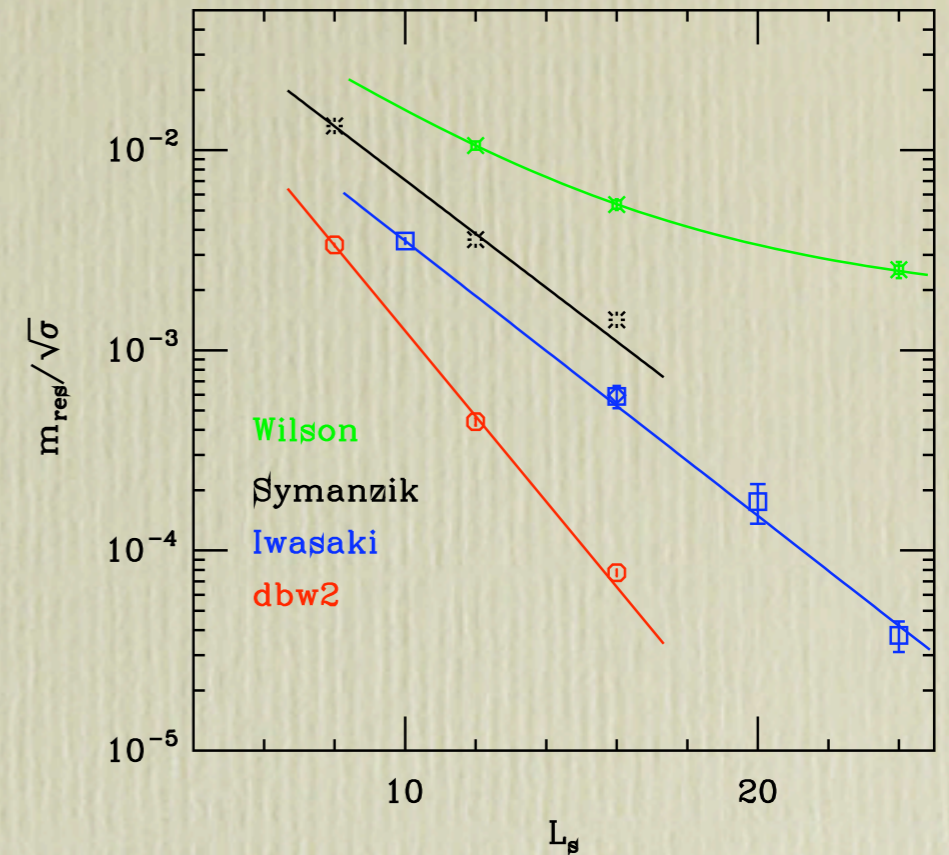
For $-2 < M < 0$, light chiral modes are bound on the walls.
Only one Dirac fermion without doublers remains.



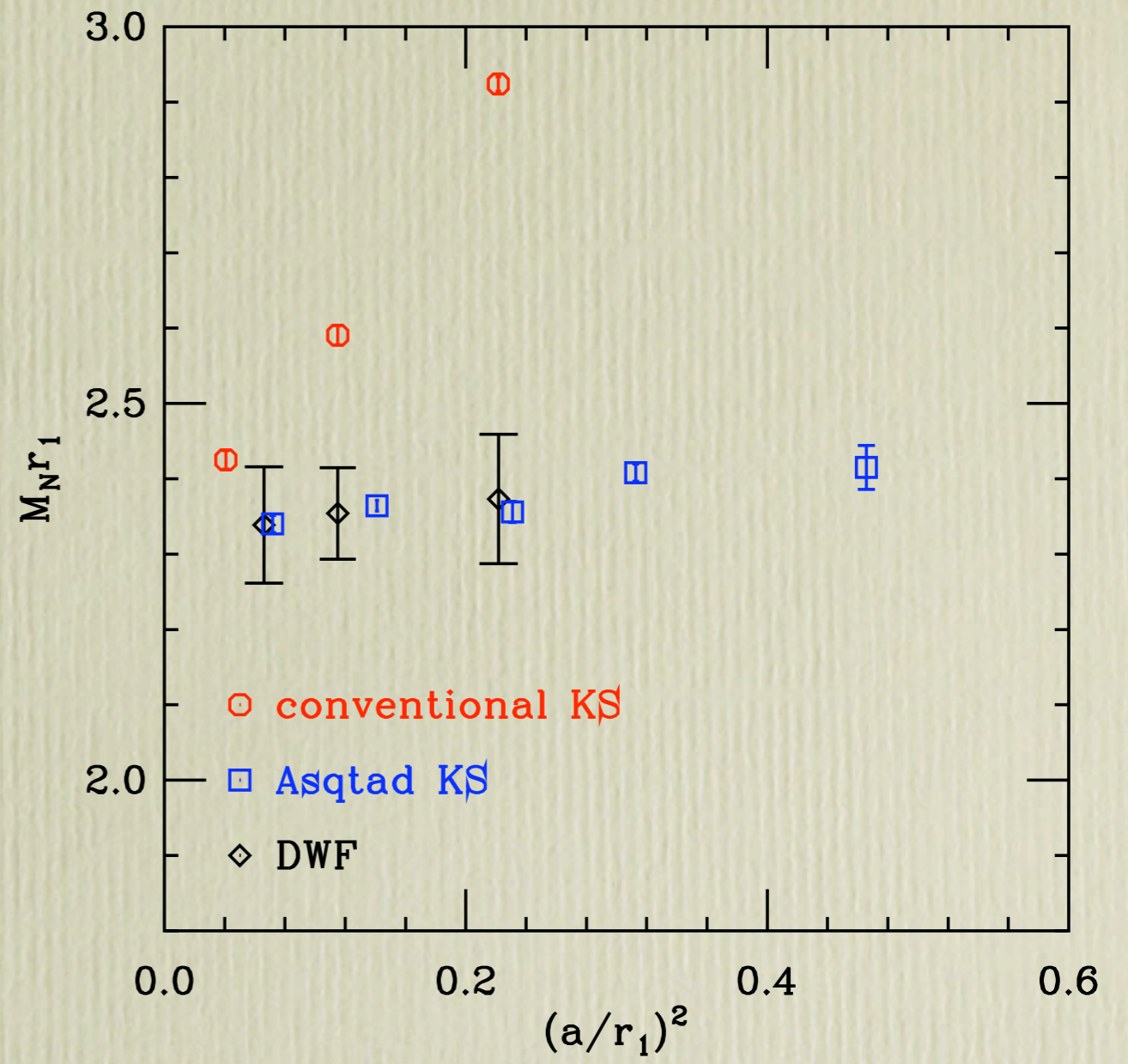
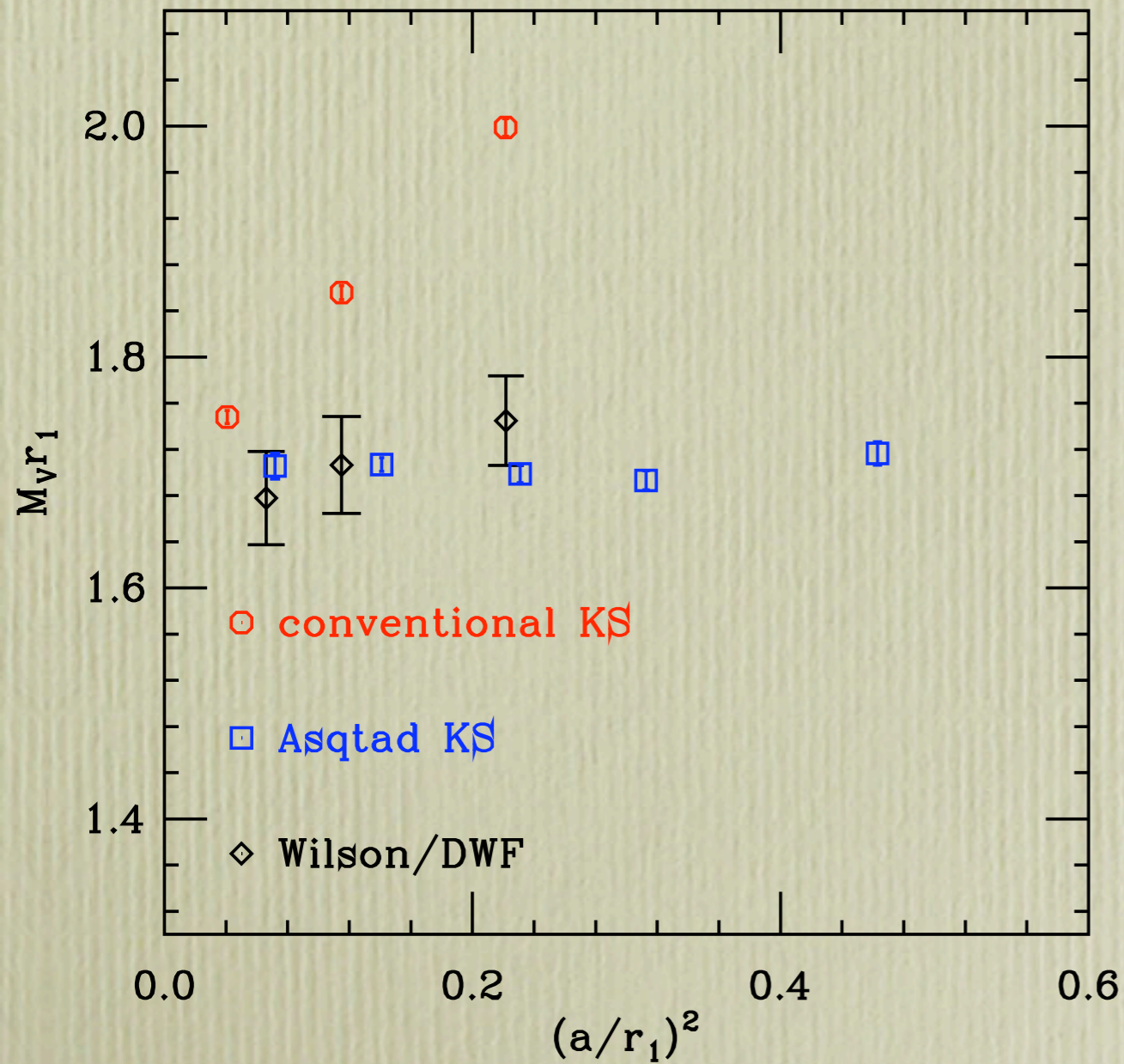
Fermion mass is introduced by explicitly coupling m_f of the walls.
[Shamir, Furman & Shamir]

Why Domain Wall Fermions

- Excellent chiral properties at finite lattice spacing:
 - $L_s \rightarrow \infty$ Exact chiral symmetry
 - L_s finite: Exponentially small chiral symmetry breaking
 - Gauge action affects chiral symmetry [KO with RBC hep-lat/0211023]
 - Chiral extrapolations
- Simpler renormalization due to symmetry
- Can work close to the chiral limit
- Have $O(a^2)$ errors
- Excellent scaling properties

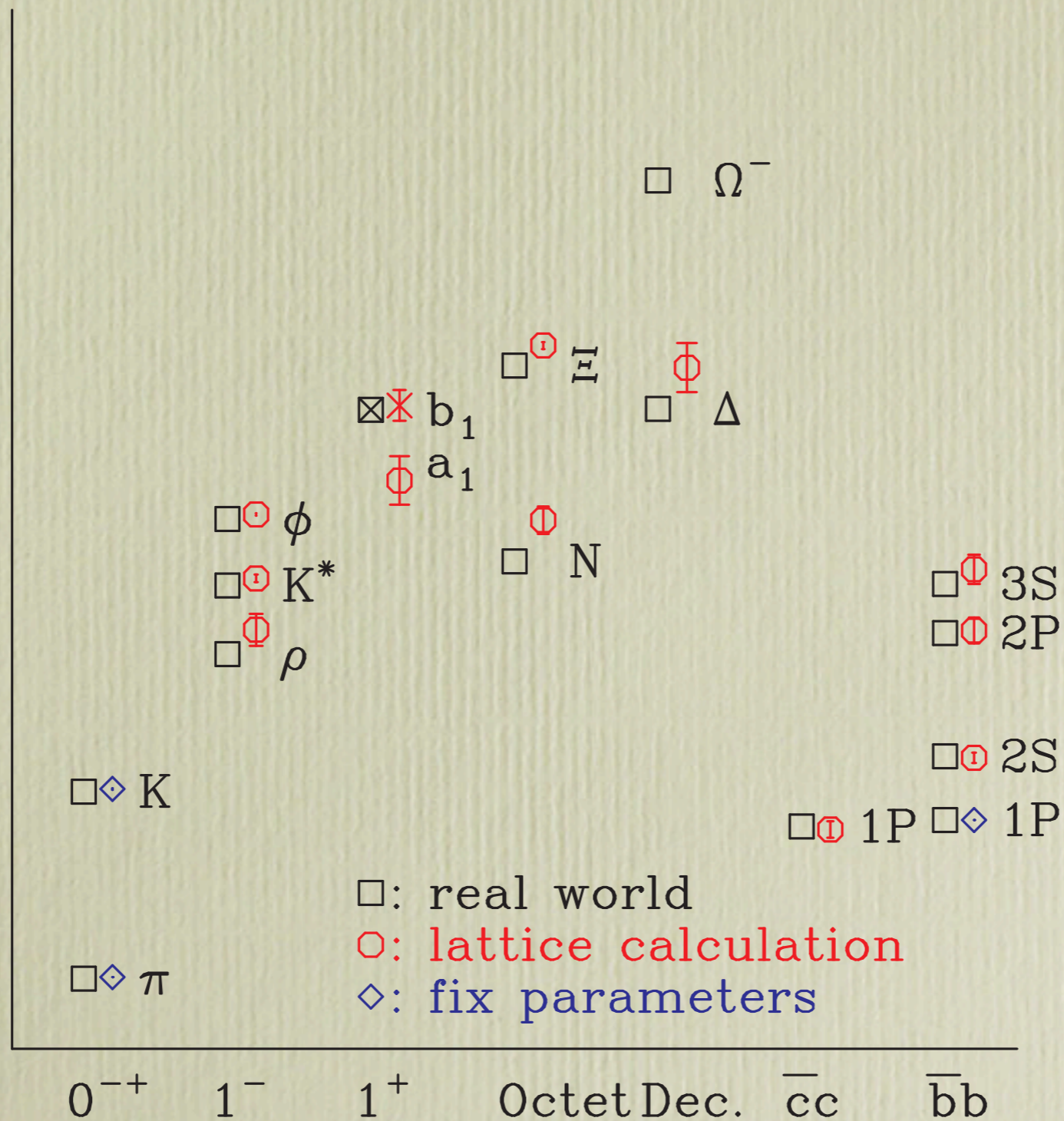


Scaling

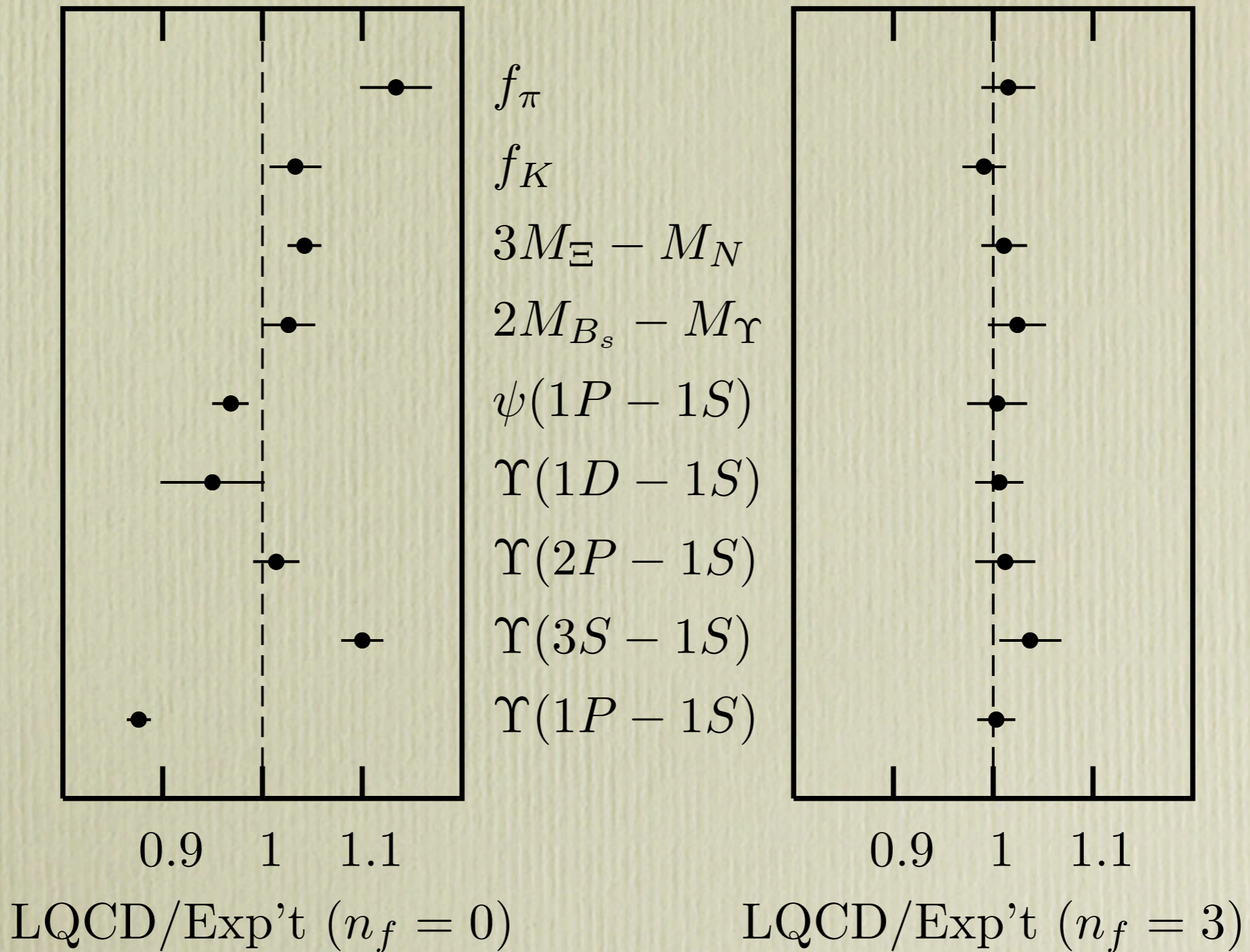


MILC and RBC data

Dynamical 2+1 flavors



Quenched vs Dynamical



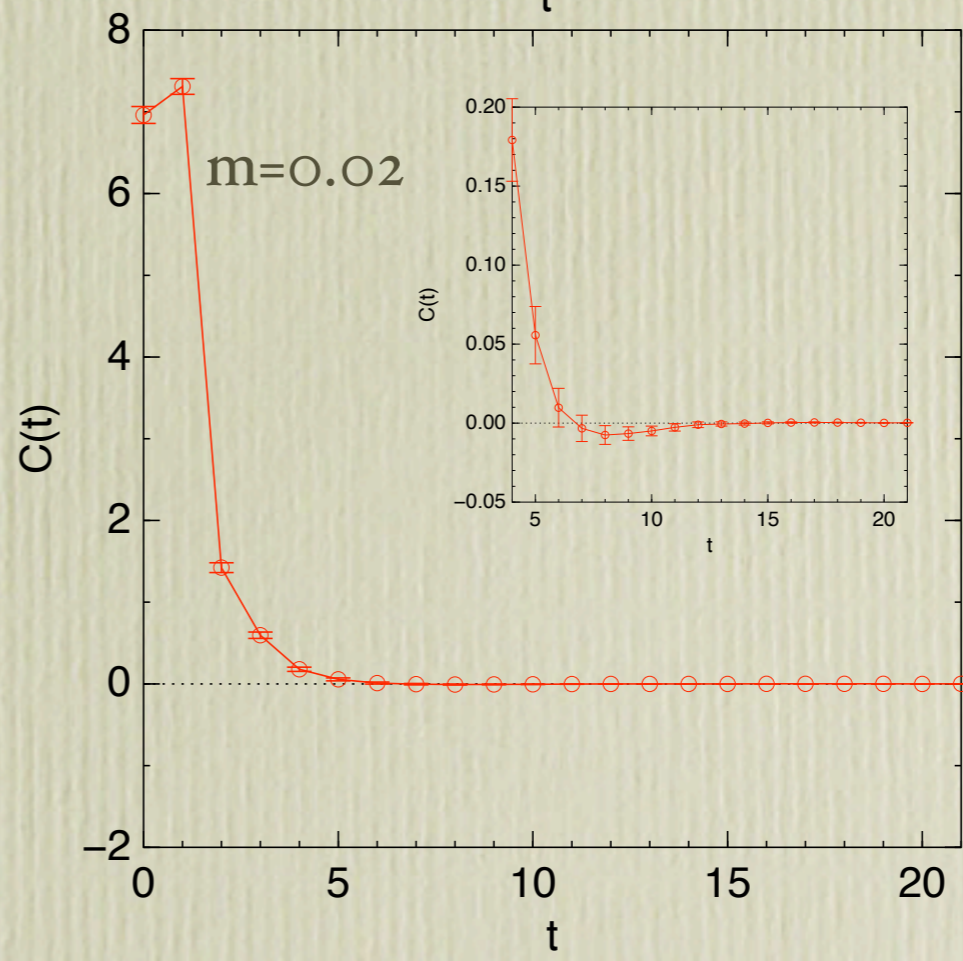
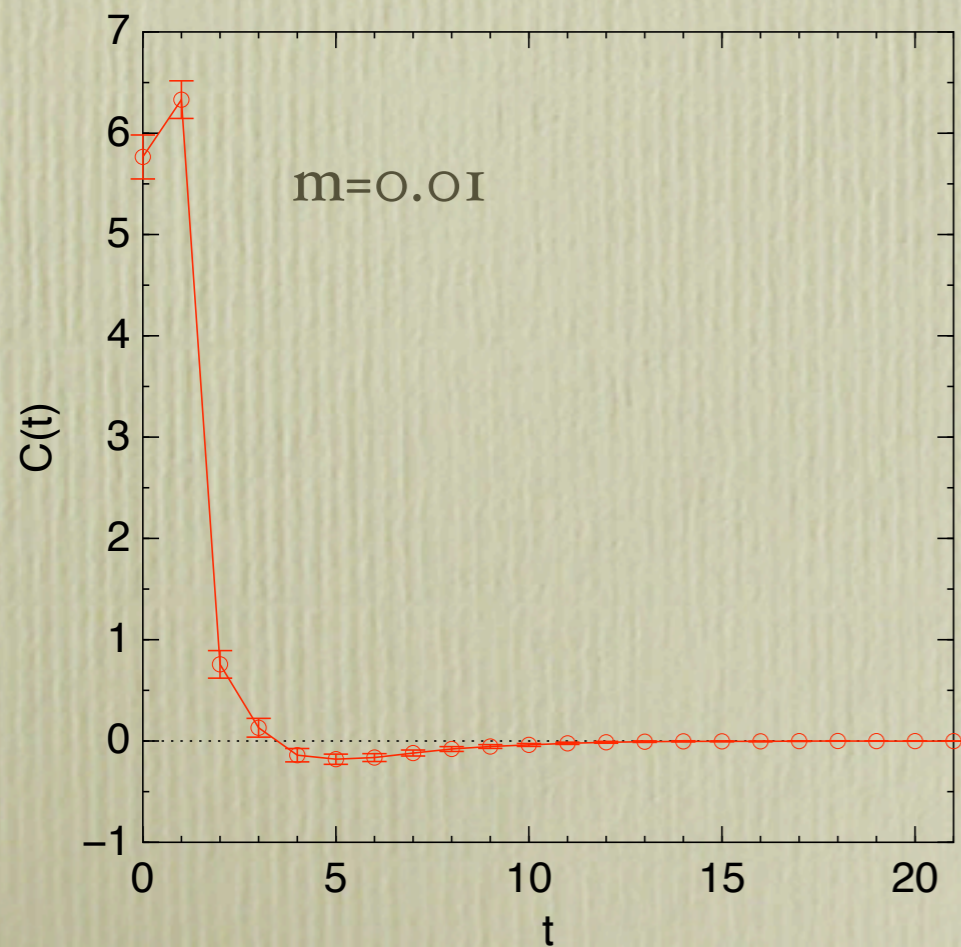
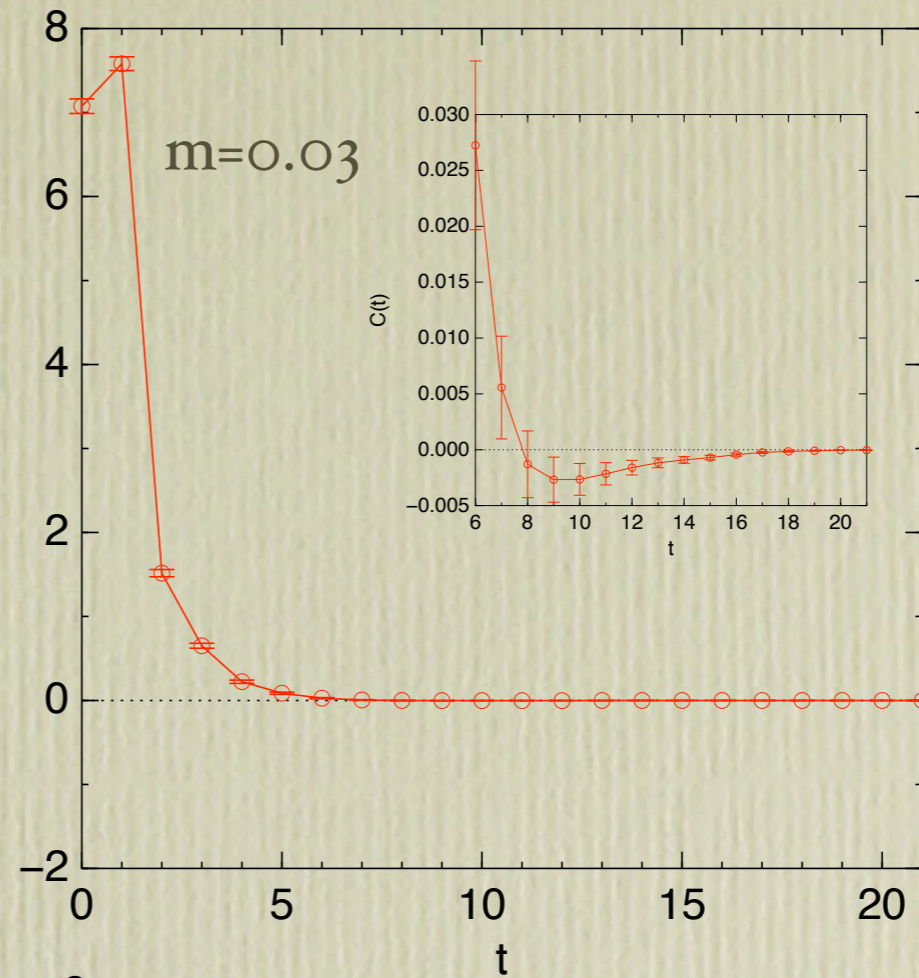
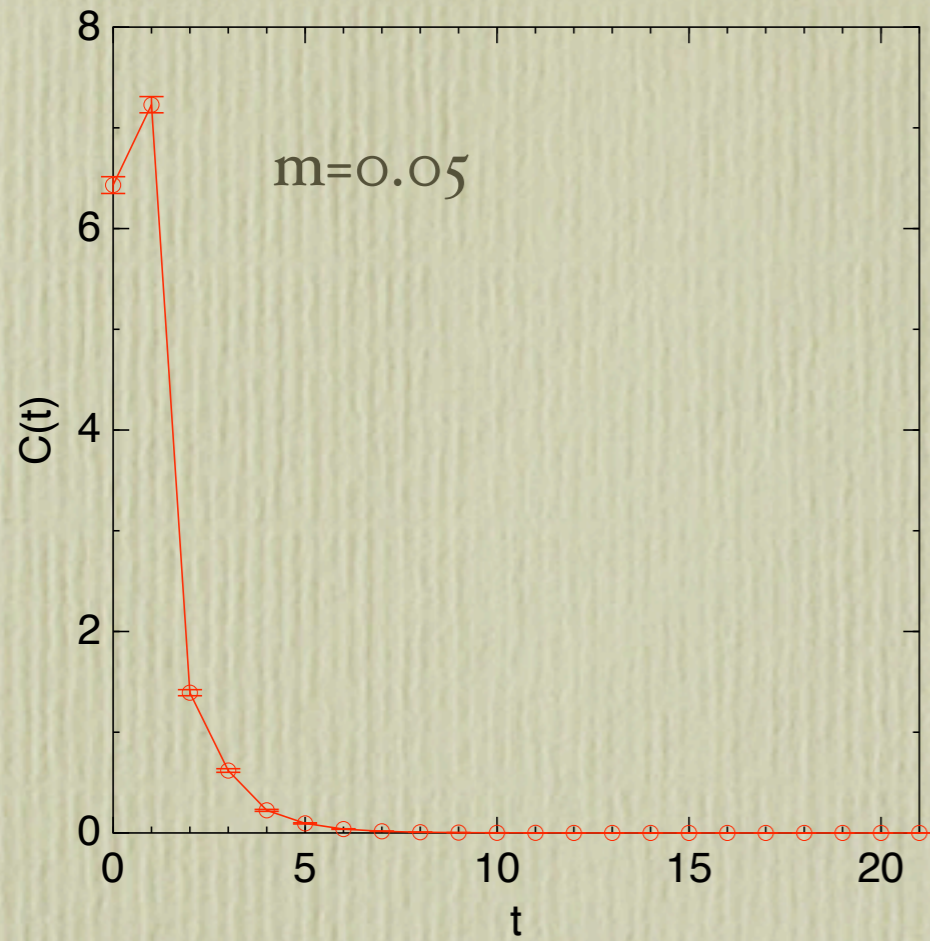
The LHPC program

- Domain wall fermions for valence (with hyp smeared links)
 - Chiral symmetry
 - Ward Identities
- Kogut-Susskind 2+1 Dynamical flavors
 - Improved KS action (Asqtad: $O(a^4, g^2 a^2)$) [KO, Sugar, Toussaint '99]
 - MILC has generated lattices: Ready to milk the MILC
- Light quark masses: Lightest pion $m_\pi \sim 250\text{MeV}$
- Volumes: 2.6 to 3.2 fm
- Future: Continuum extrapolation
 - MILC lattice spacings: $a=0.125\text{fm}$, 0.09fm
 - $a=0.06\text{fm}$ in 1 - 2 years

The DWF quark masses

- Domain wall fermions for valence (hyp smeared links)
 - We tune the DWF quark mass to the staggered Goldstone pion
- Unitarity violation
- Baer et.al.: tune to the taste singlet for m_π
- Not clear it helps for other quantities (ex. f_π)
- Unitarity is restored in the continuum in any case

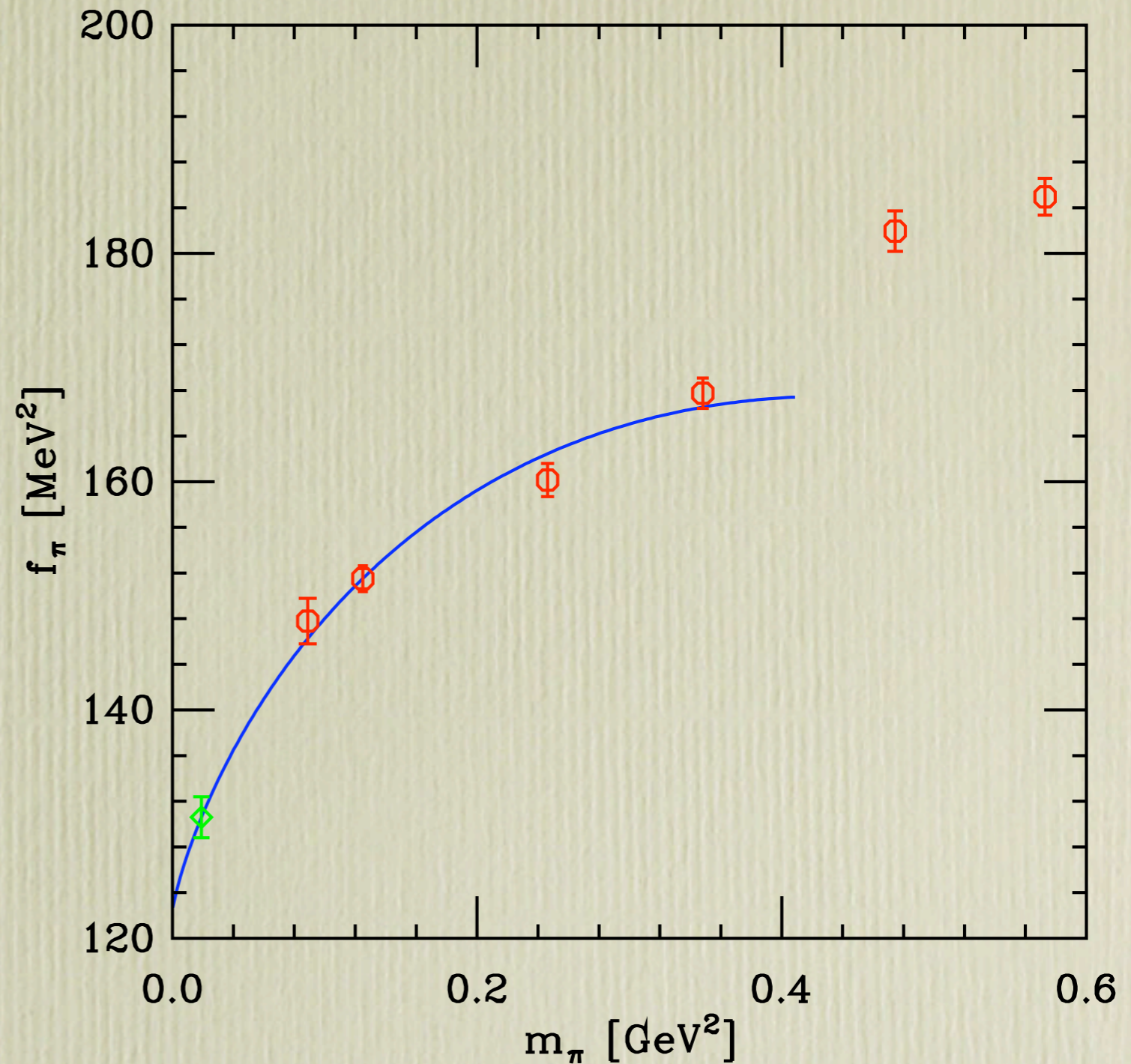
IsoVector scalar correlator



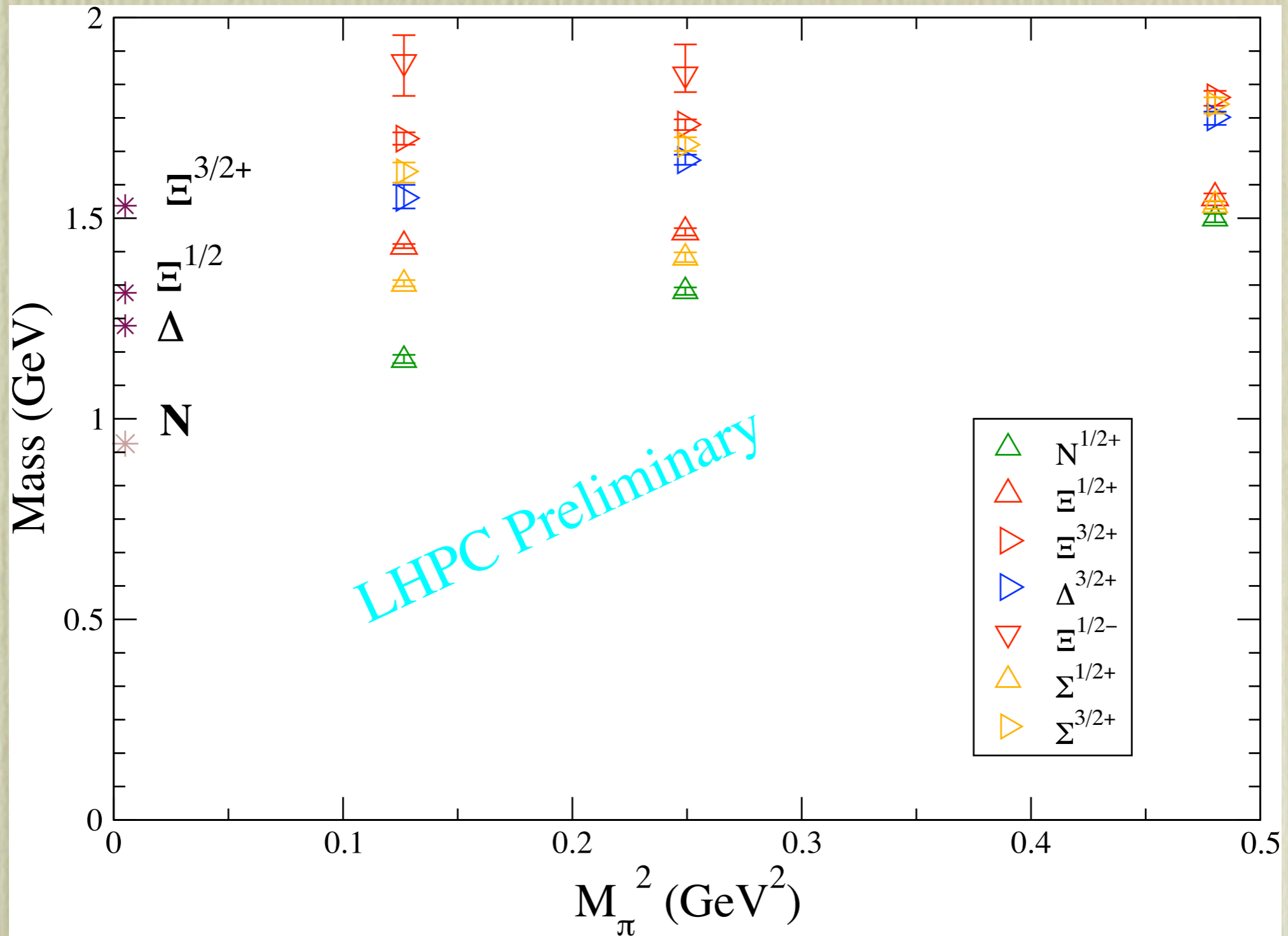
χ PT
calculation:
Prelovsek
LAT 05

Pion decay constant

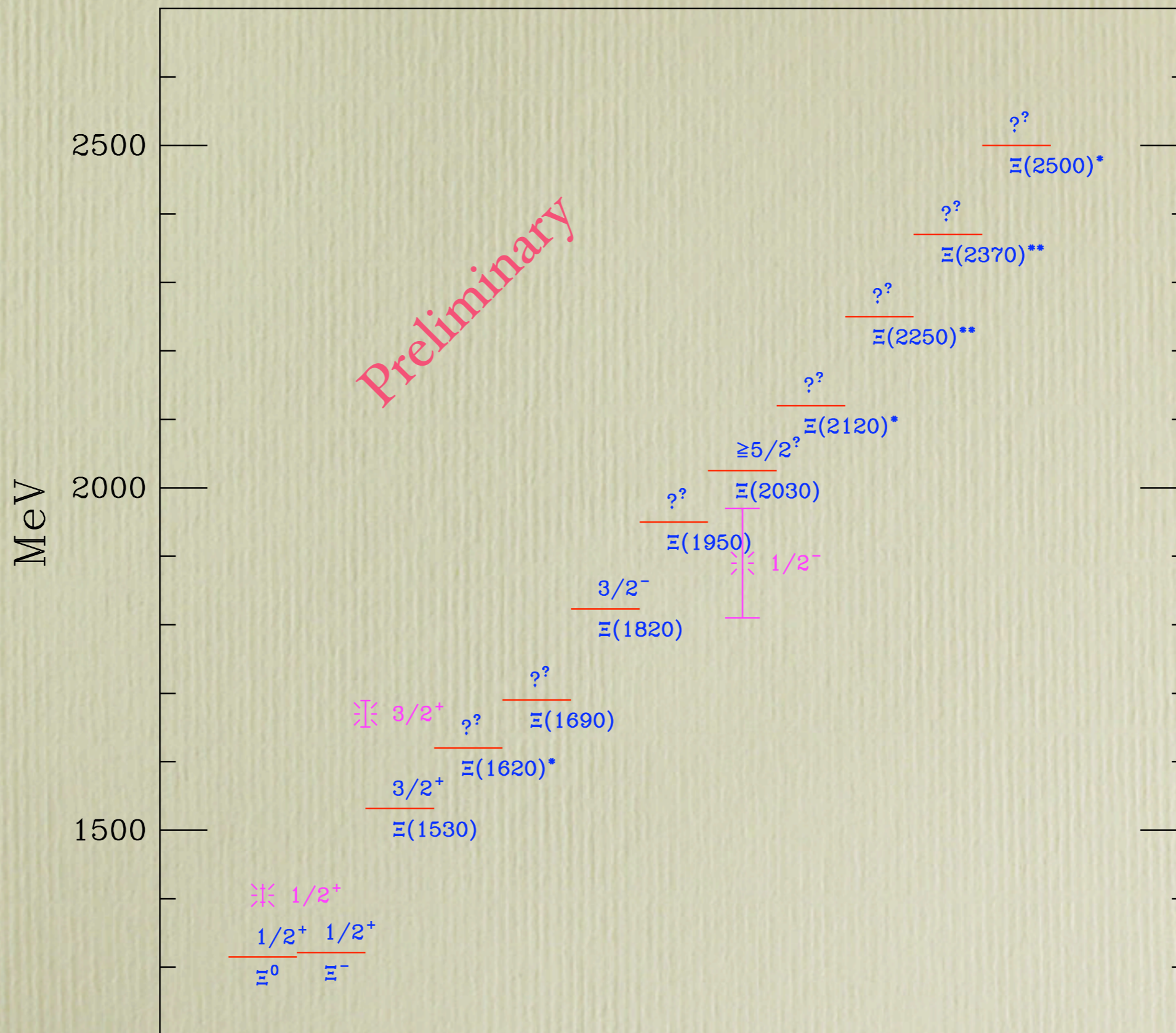
- Fit the lower 4 points
- Scale used $a = 0.125$ fm
- One loop χ PT extrapolation:
 $130.6(1.8)\text{MeV}$
- Systematic error:
 - chiral extr. 3 MeV
 - 2% from scale setting
- $\chi^2/\text{d.o.f.} \sim 2$
- Need mixed χ PT of Baer et.al.



LHPC dwf on MILC

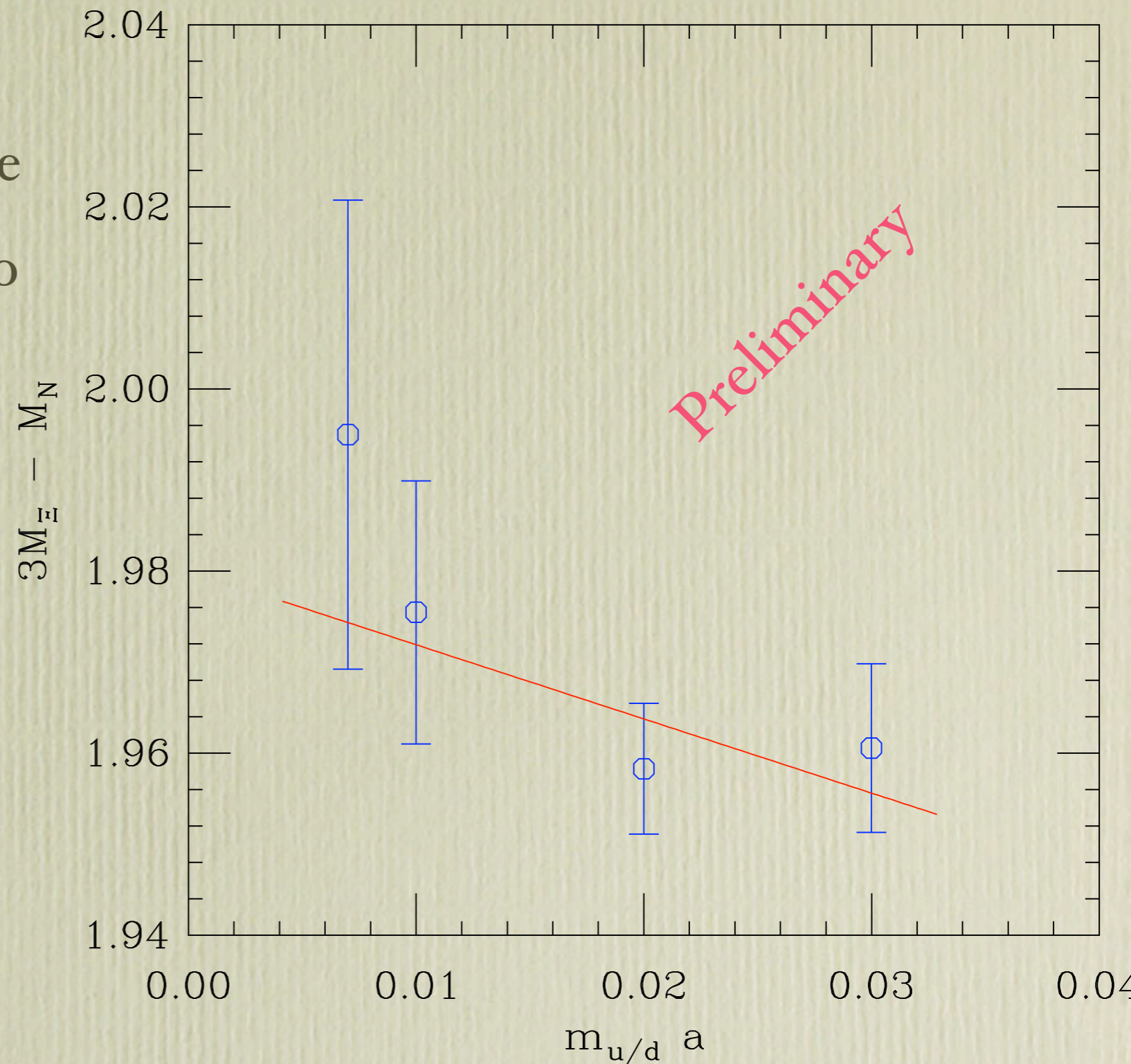


LHPC data vs Experiment

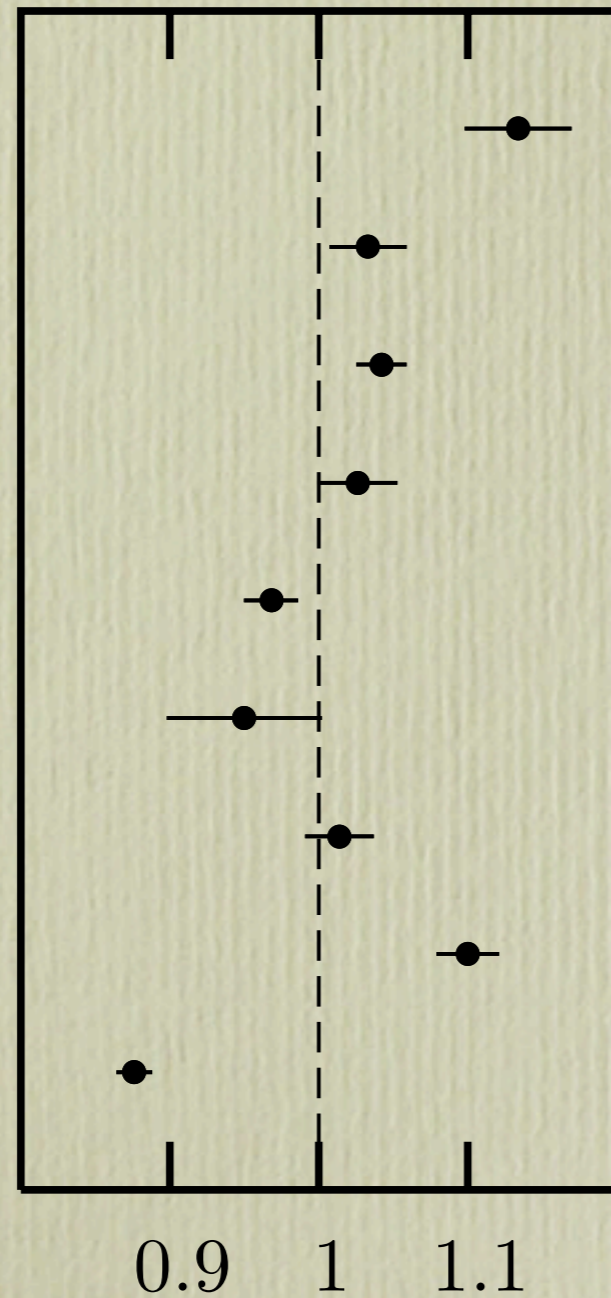


Cascade - Nucleon mass splitting

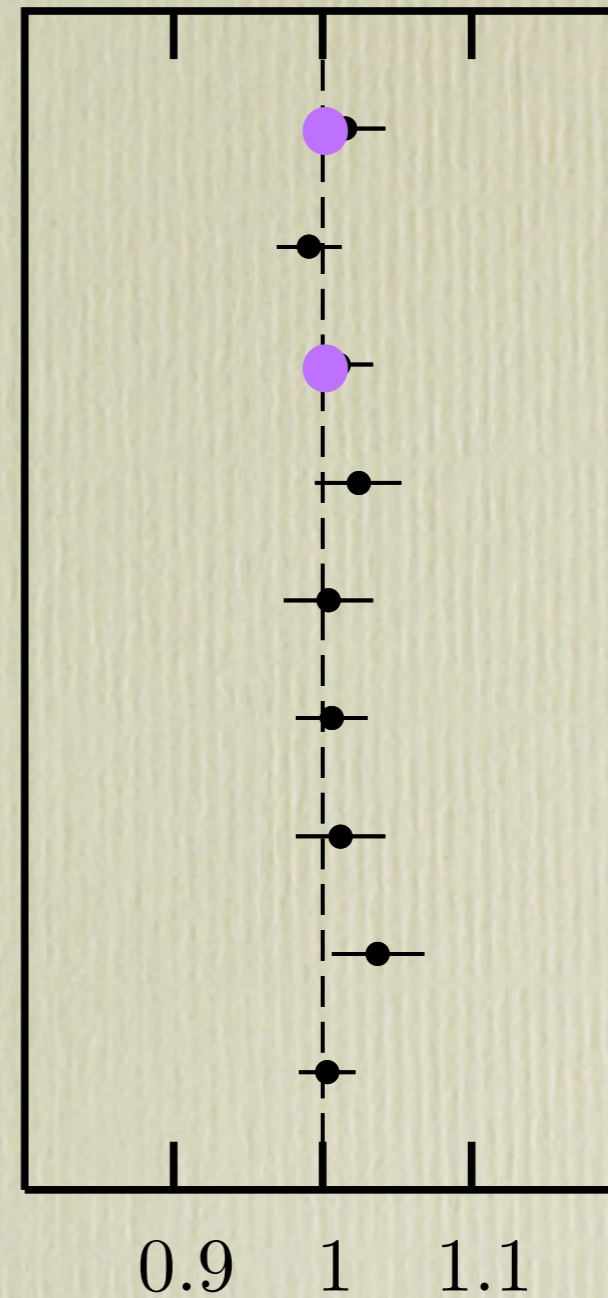
- Mild quark mass dependence
- Small systematic error due to chiral extrapolation
- Other systematic errors cancel
- Scale used $a = 1588 \text{ MeV}$
- Latt./Exp. = $1.006(8)$



Quenched vs Dynamical



LQCD/Exp't ($n_f = 0$)



LQCD/Exp't ($n_f = 3$)

Conclusions

- Lattice QCD can be very helpful in studying the cascade spectrum
- Not much has been done up to now
- The “gold plated” observable $3M_{\Xi} - M_{\Lambda}$ is well reproduced (MILC and LHPC).
- LHPC: Need to work on statistics and extrapolations
- Finer lattice spacing is on the way