

# Small- $x$ Evolution of Unintegrated Gluon Distributions

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## Two Different Distributions

- Weizsäcker-Williams distribution
  - Explicitly counts number of gluons in a physical gauge
- Fourier transform of dipole cross section
  - Widely used in  $k_T$ -factorized formulas for inclusive processes

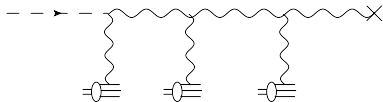
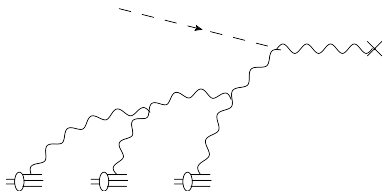
# Dipole Distribution

- Inclusive gluon production
- Also appears in less inclusive measurements like  $\gamma + \text{Jet}$  in  $pA$  collisions
- Evolution given by BK equation

# Weizsäcker-Williams Distribution

Can be calculated in specific models

- McLerran-Venugopalan
- Kovchegov-Mueller

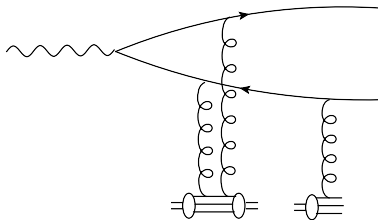


## Weizsäcker-Williams Distribution From DIS

- No such colorless current available in the lab
- Consider two-jet events in DIS
- Make separation between quark and antiquark by taking correlation limit
- Singlet pair looks like a colorless object
- Octet pair looks like a gluon

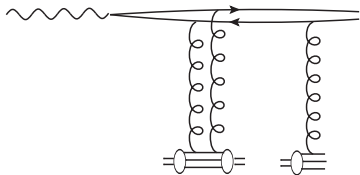
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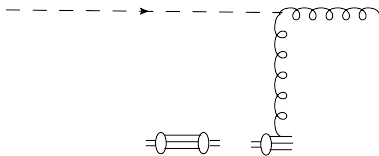
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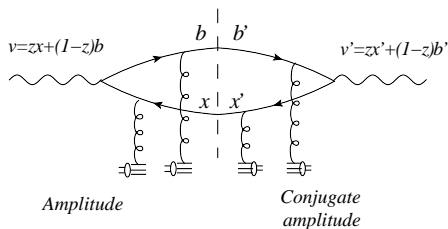
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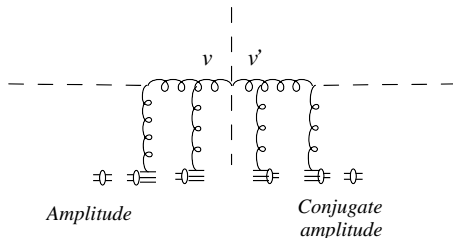


## Dijet in DIS



$$\begin{aligned}
 \frac{d\sigma_{\gamma_T^* A \rightarrow q\bar{q}X}}{d^3k_1 d^3k_2} &= N_c \alpha_{em} e_q^2 \delta(p^+ - k_1^+ - k_2^+) \int \frac{d^2x}{(2\pi)^2} \frac{d^2x'}{(2\pi)^2} \frac{d^2b}{(2\pi)^2} \frac{d^2b'}{(2\pi)^2} \\
 &\times e^{-ik_{1\perp} \cdot (x-x')} e^{-ik_{2\perp} \cdot (b-b')} \sum \psi_T^*(x-b) \psi_T(x'-b') \\
 &\times \left[ 1 + Q_{x_g}(x, b; b', x') - S_{x_g}^{(2)}(x, b) - S_{x_g}^{(2)}(b', x') \right]
 \end{aligned}$$

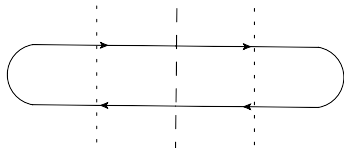
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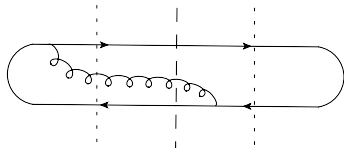
$$\frac{d\sigma^{\gamma_T^* A \rightarrow q\bar{q}+X}}{dy_1 dy_2 d^2 P_\perp d^2 q_\perp} = \delta(x_{\gamma^*} - 1) x_g G^{(1)}(x_g, q_\perp) H_{\gamma_T^* g \rightarrow q\bar{q}}$$

$$x_g G^{(1)}(x_g, q_\perp) = -\frac{2}{\alpha_S} \int \frac{d^2 v}{(2\pi)^2} \frac{d^2 v'}{(2\pi)^2} e^{-iq_\perp \cdot (v-v')} \times \left\langle \text{Tr} [\partial_i U(v)] U^\dagger(v') [\partial_i U(v')] U^\dagger(v) \right\rangle_{x_g}$$

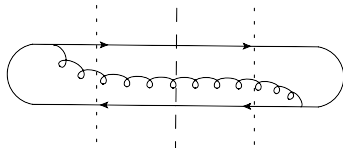
# Quadrupole Evolution



- Soft gluon can create a new dipole

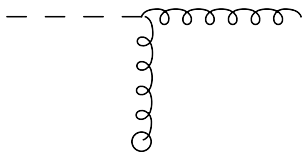


- Soft gluon can split quadrupole into two dipoles

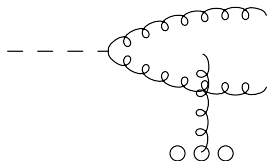


# Weizsäcker-Williams Evolution

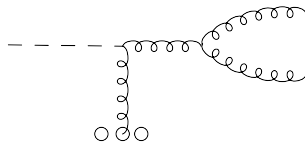
Effective vertex



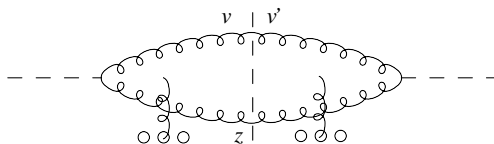
• Early emission



• Late emission

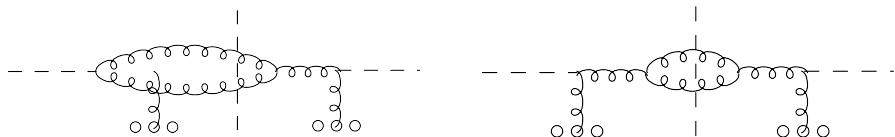


# Early Emissions Only



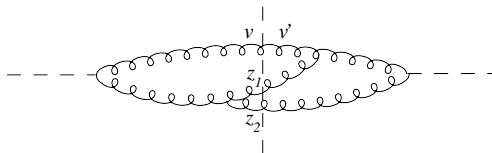
- Can be written in terms of dipole scattering only
- At the quadrupole level this corresponds to picking only the terms where the quadrupole splits into two dipoles

## Late Emissions - First Step



- Virtual corrections have to be included too
- Complete cancelation at leading twist
- Lots of cancelations in different momentum regions. Not when softer gluon has a transverse momentum close to saturation scale

# Quadrupole Comes Back



- For large  $N_c$  we get a quadrupole and two dipoles
- Large growth of the wavefunction
- Not clear it should give a small contribution

## Conclusion

- Further insight into quadrupole evolution is needed
- Asymptotic limits seem to be dominated by dipole evolution