Introduction to Parity Violation

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Introduction to Parity Violation

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Discovery of Parity Violation (late 1950s)





Discovery of Parity Violation (late 1950s)



Weak decay of ⁶⁰Co Nucleus



matter particles have spin = 1/2

$$h = \frac{\vec{s} \bullet \vec{p}}{|\vec{s}\|\vec{p}|} = \pm 1$$

handedness or *helicity/chirality*



Discovery of Parity Violation (late 1950s)



handedness or helicity/chirality



Outline

Weak Interactions without Neutrinos

- Earliest Speculations & Measurements
- Parity-Violating Electron Scattering
- Experiments that Established the Electroweak Theory
- Weak Probes of Hadrons
- Outlook Disclaimer

I have developed a roughly chronological narrative. My goal here is to set the context that has made PREX feasible. I have neither attempted to be comprehensive nor taken the care to give credit to all major advances

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A Classic Paper

LETTERS TO THE EDITOR

PARITY NONCONSERVATION IN THE FIRST ORDER IN THE WEAK-INTER-ACTION CONSTANT IN ELECTRON SCATTERING AND OTHER EFFECTS

Ya. B. ZEL' DOVICH

Submitted to JETP editor December 25, 1958

J. Exptl. Theoret. Phys. (U.S.S.R.) 36, 964-966 (March, 1959)

Parity Violation in Electron Scattering?

WE assume that besides the weak interaction that causes beta decay,

$$g(\overline{PON})(\overline{e}^{-}Ov) + \text{Herm. conj.},$$
 (1)

there exists an interaction

$$g(\overline{P}OP)(\overline{e}^{-}Oe^{-})$$
(2)

with $g \approx 10^{-49}$ and the operator $O = \gamma_{\mu} (1 + i\gamma_5)$ characteristic¹ of processes in which parity is not conserved.*

Then in the scattering of electrons by protons the interaction (2) will interfere with the Coulomb scattering, and the nonconservation of parity will appear in terms of the first order in the small quantity g. Owing to this it becomes possible to test the hypothesis used here experimentally and to determine the sign of g.

In the scattering of fast (~10⁹ ev) longitudinally polarized electrons through large angles by unpolarized target nuclei it can be expected that the cross-sections for right-hand and left-hand electrons (i.e., for electrons with $\sigma \cdot p > 0$ and $\sigma \cdot p < 0$) can differ by 0.1 to 0.01 percent. Such

an effect is a specific test for an interaction not conserving parity.

Neutron β *Decay*

Electron-proton Weak Scattering





$$A_{\rm PV} = \frac{\sigma_{\uparrow} - \sigma_{\downarrow}}{\sigma_{\uparrow} + \sigma_{\downarrow}} = -A_{\rm LR}$$



4-momentum transfer $Q^2 = 4 EE' \sin^2 \frac{\theta}{2}$

Observable Parity-Violating Asymmetry



One of the incident beams longitudinally polarized
Change sign of longitudinal polarization
Measure fractional rate difference

The matrix element of the Coulomb scattering is of the order of magnitude e^2/k^2 , where k is the momentum transferred ($\hbar = c = 1$). Consequently, the ratio of the interference term to the Coulomb term is of the order of gk^2/e^2 . Substituting $g = 10^{-5}/M^2$, where M is the mass of the nucleon, we find that for $k \sim M$ the parity nonconservation effects can be of the order of 0.1 to 0.01 percent.

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$$A_{PV} = \frac{\sigma_{\uparrow} - \sigma_{\downarrow}}{\sigma_{\downarrow} + \sigma_{\downarrow}} \sim \frac{A_{\text{weak}}}{A_{EM}} \sim \frac{G_F Q^2}{4 \pi \alpha}$$
$$A_{PV} \sim 10^{-4} \cdot Q^2 (\text{GeV}^2)$$

Early Hadron-Hadron Measurements

• Longitudinal (or circular) polarization in initial or final state of one or the other particle

- Hadron-hadron interactions easier to access experimentally
- Find reactions where the denominator (electromagnetic amplitude) is small; enhancing the numerator (weak amplitude)
- In early measurements involving nuclei, connection to underlying fundamental dynamics rather tenuous

Low energy p-p elastic scattering $\vec{p} + p \rightarrow p + p$ Tanner (1957)

$$^{180}Hf^*(8^-) \rightarrow ^{180}Hf + \gamma \qquad A_{\gamma} = -(1.66 \pm 0.18) \times 10^{-2} \quad (1971)$$

$$\vec{n} + {}^{139}La \qquad A_z = (9.55 \pm 0.35) \times 10^{-2}$$
 (1991)

Neutral Weak Interaction Theory

A Model of Leptons Steve Weinberg - 1967

The Z boson incorporated



Yu

 \mathbf{Z}^{0}

electron-nucleon scattering

$\binom{\nu}{e}_l (e)_r$	-Weinberg model	
	Parity is violated	
or		
$\begin{pmatrix} \nu \\ e \end{pmatrix}_l \begin{pmatrix} E^\circ \\ e \end{pmatrix}_r$	Parity is conserved	

	Left-	Right-
γ Charge	$0,\pm 1,\pm \frac{1}{3},\pm \frac{2}{3}$	$0,\pm 1,\pm \frac{1}{3},\pm \frac{2}{3}$
W Charge	$T = \pm \frac{1}{2}$	zero
Z Charge	$T-q\sin^2\theta_W$	$-q\sin^2\theta_W$

The weak mixing angle introduced Gargamelle finds one $v_{\mu} e^{-}$ event in 1973! (two more by 1976)

Landmark experiment (late 1970s) at Stanford Linear Accelerator Center (SLAC)

E122 at SLAC demonstrated parity-violation in electronnucleon deep inelastic scattering

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PV Deep-Inelastic Scattering

The discovery of electron-nucleon deep inelastic scattering \sim 1966 gave rise to an opportunity: large cross-section at large Q^2

Instead of left- and right- $g_V = g_L + g_R$ handed couplings, use g_V and g_A : $g_A = g_L - g_R$

Vector and Axial-vector couplings





A_{PV} in Electron-Nucleon DIS:

$$A_{PV} = \frac{G_F Q^2}{\sqrt{2}\pi\alpha} \left[a(x) + f(y)b(x) \right]$$

x: struck quark's nucleon momentum fraction $f_i(x)$: probability distribution of i^{th} quark



For a ²H target, assuming charge symmetry, structure functions largely cancel in the ratio:

$$a(x) = \frac{3}{10} \Big[(2C_{1u} - C_{1d}) \Big] + \cdots \qquad b(x) = \frac{3}{10} \Big[(2C_{2u} - C_{2d}) \frac{u_v(x) + d_v(x)}{u(x) + d(x)} \Big] + \cdots$$

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Atomic Parity Violation

•6S → 7S transition in ¹³³Cs is forbidden within QED
•Parity Violation introduces small opposite parity admixtures
•Induce an E1 Stark transition, measure E1-PV interference
•5 sign reversals to isolate APV signal and suppress systematics
•Signal is ~ 6 ppm, measured to 40 ppb

Boulder Experiment



Partial Level Structure of Cesium

Elastic Electron-Nuclear Scattering *Elastic scattering from* $(J^{\pi}, T) = (0^+, 0)$ *nuclei Feinberg* (1975)

For a spinless, iso-scalar nucleus, A_{PV} in elastic scattering at forward angle insensitive to nuclear structure: clean measurement of $C_{1u} + C_{1d}$

¹²C at MIT-Bates: $A_{PV} = (1.69 \pm 0.39 \pm 0.06) \times 10^{-6}$ Souder (1990)

Quasi-elastic backward angle scattering from ⁹*Be Additional dependence on C*₂ *couplings*

⁹Be at Mainz: $A_{PV} = (-9.4 \pm 1.8 \pm 0.5) \times 10^{-6}$ Heil (1989)

First measurements of electron-nuclear weak interactions
Pushed experimental technology
Low energy tests of electroweak theory

Parity Violation at the Z Resonance

$$e^+e^- \rightarrow Z^0 \rightarrow l^+l^-, q\bar{q}$$

 $\xrightarrow{e^+} \xrightarrow{g_L} \xrightarrow{e^-} \xrightarrow{e^+} \xrightarrow{g_R} \underbrace{e^-} \xrightarrow{e^-}$

Polarize the electron beam and measure Z production

 $P_{b} = \frac{N_{+} - N_{-}}{N_{+} + N}$ Fraction of electron beam polarized along or against the momentum

$$A_{LR} = \frac{N_{Z-} - N_{Z+}}{N_{Z-} + N_{Z+}} = \frac{(1 - P_b)g_L^2 - (1 + P_b)g_R^2}{(1 - P_b)g_L^2 - (1 + P_b)g_R^2} = P_b P_e$$

All final states can be used!

$$P_e = \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} = 2(1 - 4\sin^2\theta_W) \approx 0.14$$

The SLD detector at SLAC measured P_e to 1% relative precision, which has yielded the single most precise value of the weak mixing angle to date

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Strange Quarks in the Nucleon

Quark Model (2) QCD

Strange quarks carry nucleon momentum: Other external properties affected?



⁴*He target: Unique* G_E sensitivity

²*H*: Enhanced G_A sensitivity

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World Program

SAMPLE

open geometry, integrating

G_Ms, **(G_A)** at Q² = 0.1 GeV²

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+ TOF for background rejection $G_{E}^{s} + \eta G_{M}^{s}$ over $Q^{2} = [0.12, 1.0] GeV^{2}$

 G_{M}^{s} , G_{A}^{e} at $Q^{2} = 0.23$, 0.62 GeV²

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A_{PV} off ¹H & ⁴He at Low Q² at JLab



HydrogenSystematic control ~ 10-8 $A_{PV} = -1.58 \pm 0.12$ (stat) ± 0.04 (syst) ppm $A(G^s=0) = -1.66$ ppm ± 0.05 ppm

Helium Normalization control ~ 2% A_{PV} = +6.40 ± 0.23 (stat) ± 0.12 (syst) ppm A(G^s=0) = +6.37 ppm

Corrected and Raw, Left arm alone, Superimposed!

Total correction for beam position asymmetry on Left, Right, or ALL detector: 10 ppb

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Current Status



At 95% C.L., strange quarks contribute:

< 5% of the magnetic moment, < 5% of the charge radius squared

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Axial Form Factor and the Anapole Moment

Axial-vector hadronic current has contributionsfrom parity-violating momentsZel'dovich (1957)



Haxton & Wieman (2001)

Wood et. al (1997)



In nuclei, such moments are large enough to be observed via atomic parity violation



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Such moments are generated by purely hadronic weak interactions, described by weak meson-nucleon couplings

Møller Scattering





Purely leptonic reaction

$$\mathbf{PV} = -\mathbf{mE} \frac{\mathbf{G}_{\mathbf{F}}}{\sqrt{2}\pi\alpha} \frac{\mathbf{16}\sin^2 \Theta}{(\mathbf{3} + \cos^2 \Theta)^2} \mathbf{Q}_{\mathbf{W}}^{\mathbf{e}}$$

$$A_{PV} \propto m_e E_{lab} (1 - 4 \sin^2 \vartheta_W)$$

Small, well-understood dilution

$$\frac{\delta(\sin^2\vartheta_W)}{\sin^2\vartheta_W} \cong 0.05 \frac{\delta(A_{PV})}{A_{PV}}$$



Figure of Merit rises linearly with E_{lab}

SLAC: Highest beam energy with moderate polarized luminosity JLab 11 GeV: Moderate beam energy with LARGE polarized luminosity

Comprehensive Search for New Neutral Current Interactions

Important component of indirect signatures of "new physics"

Consider
$$f_1 \bar{f}_1 \rightarrow f_2 \bar{f}_2$$
 or $f_1 f_2 \rightarrow f_1 f_2$
 $L_{f_1 f_2} = \sum_{i, j=L,R} \frac{4\pi}{\Lambda_{ij}^2} \eta_{ij} \bar{f}_{1i} \gamma_{\mu} f_{1i} \bar{f}_{2j} \gamma^{\mu} f_{2j}$

$$f_1 \rightarrow f_1 f_2 \rightarrow f_1 f_2 \qquad f_1 \rightarrow f_1 f_2 \qquad f_1 \rightarrow f_1 f_2 \qquad f_1 \rightarrow f_1 \qquad f_1 \rightarrow f_2 \qquad f_1 \rightarrow f_1 \qquad f_1 \rightarrow f_2 \qquad f_1 \rightarrow f_1 \qquad f_2 \rightarrow f_1 \qquad f_1 \rightarrow f_1 \qquad f_2 \rightarrow f_1 \qquad f_1 \rightarrow f_1 \rightarrow f_1 \qquad f_2 \rightarrow f_1 \qquad f_1 \rightarrow f_1 \rightarrow f_1 \qquad f_1 \rightarrow f_1 \rightarrow f_1 \qquad f_1 \rightarrow f_1 \rightarrow$$

Many new physics models give rise to non-zero Λ 's at the TeV scale: Heavy Z's, compositeness, extra dimensions...

One goal of neutral current measurements at low energy AND colliders: Access $\Lambda > 10$ TeV for as many f_1f_2 and L,R combinations as possible

LEPII, Tevatron access scales Λ 's ~ 10 TeV

e.g. Tevatron dilepton spectra, fermion pair production at LEPII

 - L,R combinations accessed are parity-conserving LEPI, SLC, LEPII & HERA accessed some parity-violating combinations but precision dominated by Z resonance measurements
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Colliders vs Low Q²



Window of opportunity for weak neutral current measurements at $Q^2 << M_Z^2$

Processes with potential sensitivity:

- neutrino-nucleon deep inelastic scattering
- Atomic parity violation
- parity-violating electron scattering





g-2 spin precession half-wave circularly plate 45 GeV: 14.0 revs polarized **R** 48 GeV: 14.5 revs

Phys. Rev. Lett. **95** 081601 (2005)

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light



Physics Implications





Lepton-Quark Couplings

Atomic Parity Violation

•¹³³Cs 6s to 7s transition

•Future: isotope measurements•Neutrino DIS: NuTeV

- ·3 σ deviation
- Many hadronic physics issues
- •Look at other I-q couplings?



$$\begin{split} & \overbrace{Q}^{e} - \overbrace{[Q}^{e} - \overbrace{[I]_{I}^{e} - I_{I}^{e} - \overbrace{[I]_{I}$$

 $A_{PV} \text{ in elastic e-p scattering: Qweak at JLab}$ $A(Q^{2} \rightarrow 0) = -\frac{G_{F}}{4\pi\alpha\sqrt{2}} \left[Q^{2} Q_{weak}^{p} + Q^{4}B(Q^{2}) \right]$ $Q_{weak}^{p} = 2C_{1u} + C_{1d} \propto 1 - 4\sin^{2}\vartheta_{W} \text{ Data ~ 2010}$

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Lepton-Quark Couplings

Atomic Parity Violation

·¹³³Cs 6s to 7s transition

•Future: isotope measurements•Neutrino DIS: NuTeV

·3 σ deviation

SLAC: D DIS

-0.7

-0.6

 $C_{1u} - C_{1d}$

-0.5

-0.4

- Many hadronic physics issues
- •Look at other I-q couplings?



-0.7 -0.6 -0.5

 $C_{1u} - C_{1d}$

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Bates: C

-0.8

0.18

0.16

 $C_{1 n+C_{1 d}}^{n+C_{1 d}}$

0.12

0.1

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-0.8

-0.9

-0.4

-0.3

Advances in Experimental Techniques

Four electron scattering laboratories: SLAC, MIT-Bates, Mainz & JLab



Steady progress in technology
part per billion systematic control
1% normalization control
1% normalization control
Intensive R&D on:

Photocathodes
Photocathodes
Polarimetry
High Luminosity cryotargets
Nanometer beam stability
Precision Beam Diagnostics
Counting Electronics
Radiation hard detectors

Parity-violating electron scattering has become a precision tool

Physics over a range of energy scales:

- •Nucleon structure: strangeness contribution to form factors
- •Search for new TeV physics: Precision electroweak parameters
- Many-body nuclear physics: Neutron skin of 208Pb
- Valence quark structure: Deep inelastic scattering at high-x

Technical Achievements at Jefferson Laboratory

HAPPEX-II set a new benchmark precision for e⁻-nuclear scattering

- ~100 parts per billion (best in nuclear scattering)
- ~4% relative precision (⁴He)
- statistics dominated
- \cdot ~1 nm average difference in beam position
- ~1% low-energy e⁻ polarimetry

Future Program (2009-2011): 5 ppb, 3%

Future Program (12GeV): 0.5 ppb, 0.5%

PREX



The proton distribution of heavy nucleus: mapped via electron scattering
The neutron distribution:

probed with hadrons
opportunity to measure with EW probe

Neutron density a fundamental observable:

•Impacts a variety of physics

 $Q^{p}_{EM} \sim 1 \qquad Q^{n}_{EM} \sim 0$

$$Q^n_W \sim 1$$
 $Q^p_W \sim 1 - 4 \sin^2 \theta_W$

 Donnelly et al, 1988
 R. Michaels et al, 2001

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$$\delta(A_{PV}) \sim 3\% \implies \delta(R_p - R_n) \sim 0.05$$

Q² ~ 0.01 GeV² _____ A_{PV} ~ 0.5 ppm

A technically demanding measurement:

•Rate ~ 2 GHz

Acceptance cut off at E-E'<2.5 MeV
Stat. Error ~ 15 ppb, Syst. Error < 2 %
Test run: Jan 2008 Physics: Early 2010

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Future 12 GeV Projects

- Parity-Violating Deep Inelastic Scattering
 - C_{2i} couplings: complementary
 - partonic charge symmetry violation
 - d(x)/u(x) as $x \rightarrow 1$
- Parity-Violating Møller Scattering
 - Precision measurement of the weak mixing angle
 - Multi-TeV sensitivity complementary to LHC

Summary

- Parity Violation is a critical tool to study fundamental interactions
 - Underlying weak interaction dynamics
 - Novel aspects of strong interactions
- Advances over several decades have made the PREX measurement feasible
 - Theoretical understanding of strong and weak dynamics
 - Increasingly sensitive experimental techniques
- I look forward to learning more about the impact of PREX in the larger physics community