

# Measuring the Neutron Star Mass-Radius Relationship with X-ray Spectroscopy

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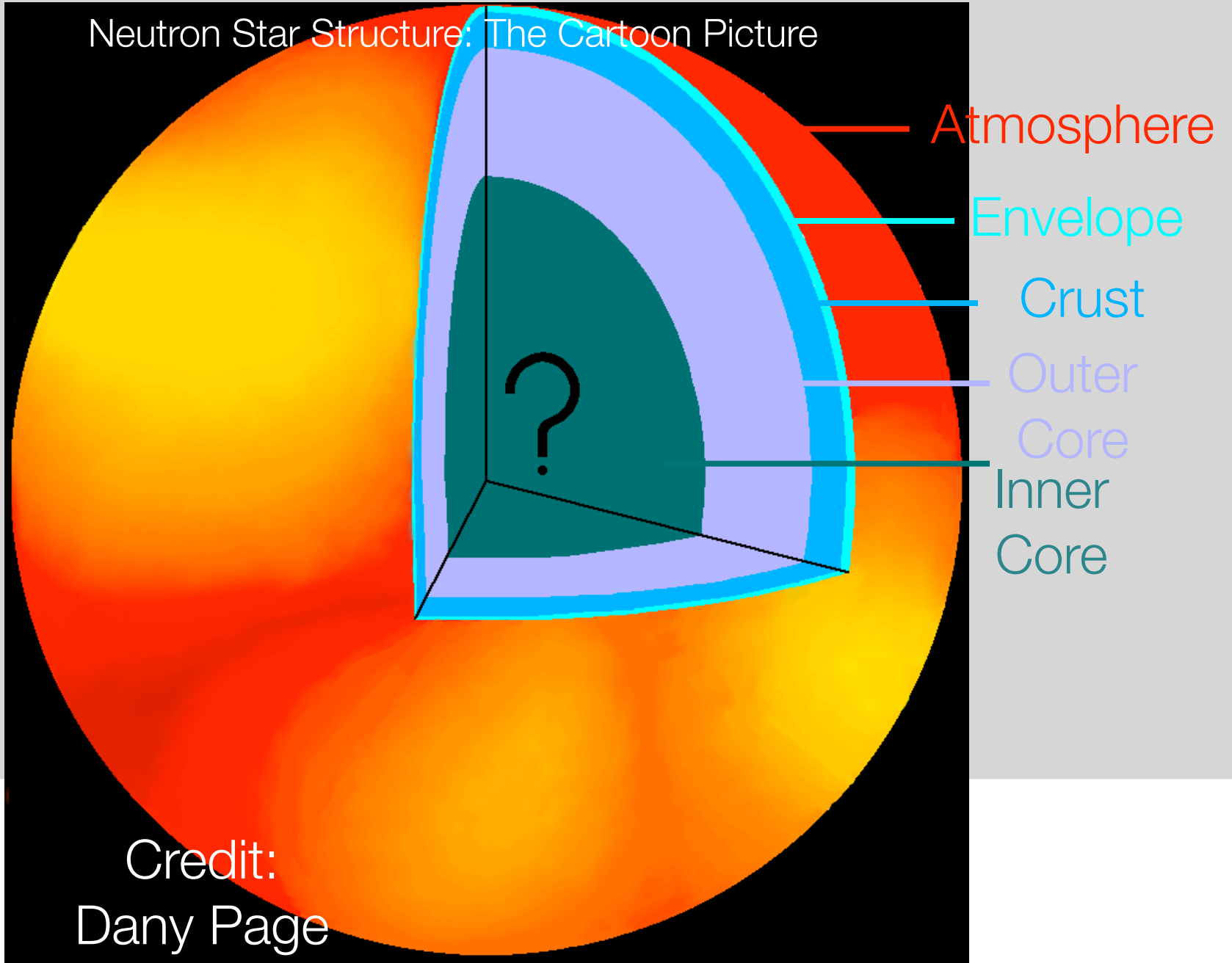
Greg Ushomirsky (Lincoln Lab.)

# Summary

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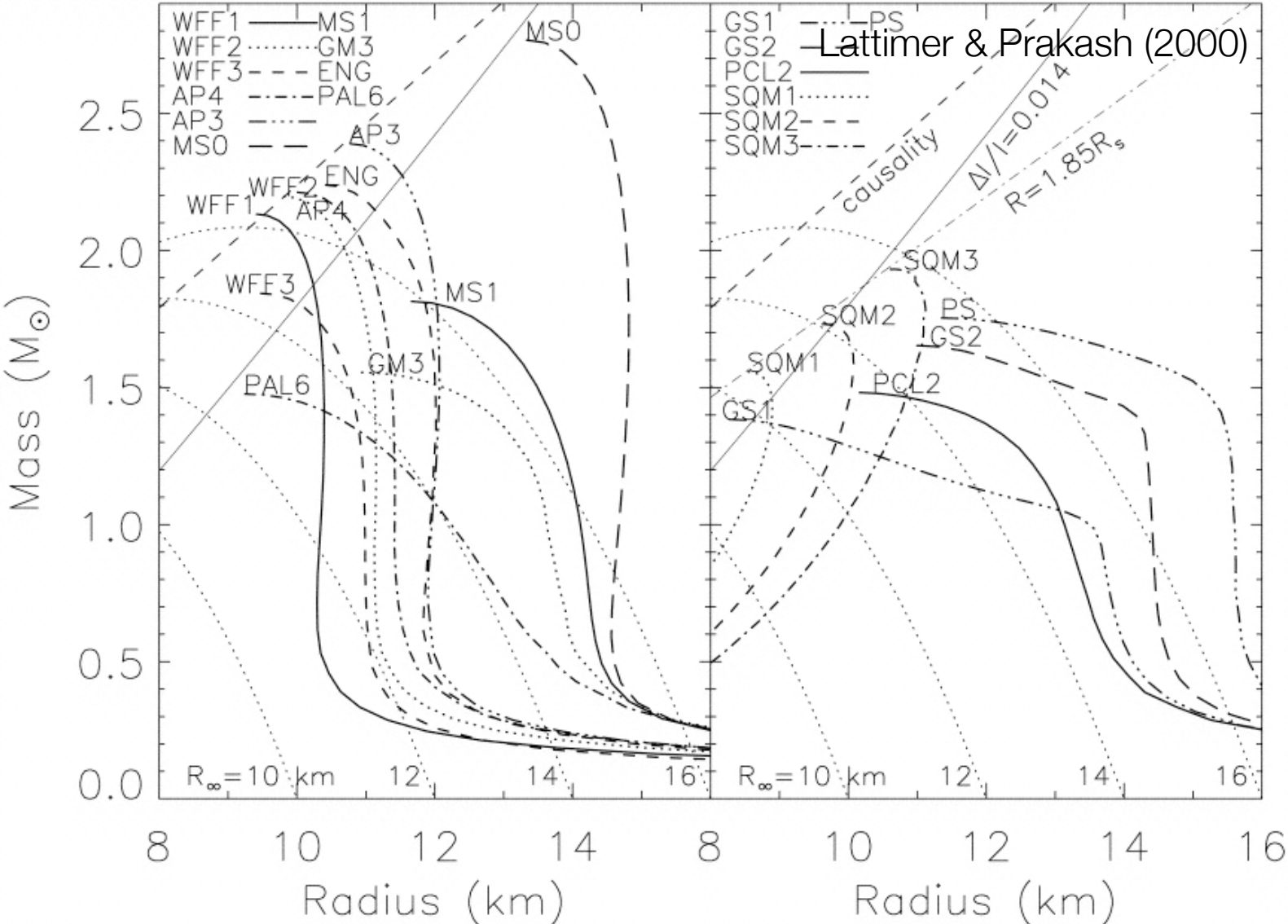
- Neutron Star Masses and Radii can be measured - independently, simultaneously - from Hydrogen atmosphere neutron stars, to  $< \text{few}\%$  accuracy, each.
- Signal to noise required is out of reach of existing X-ray observatories, but can be done with proposed missions (Constellation-X/International X-ray Observatory).

# Neutron Star Structure: The Cartoon Picture



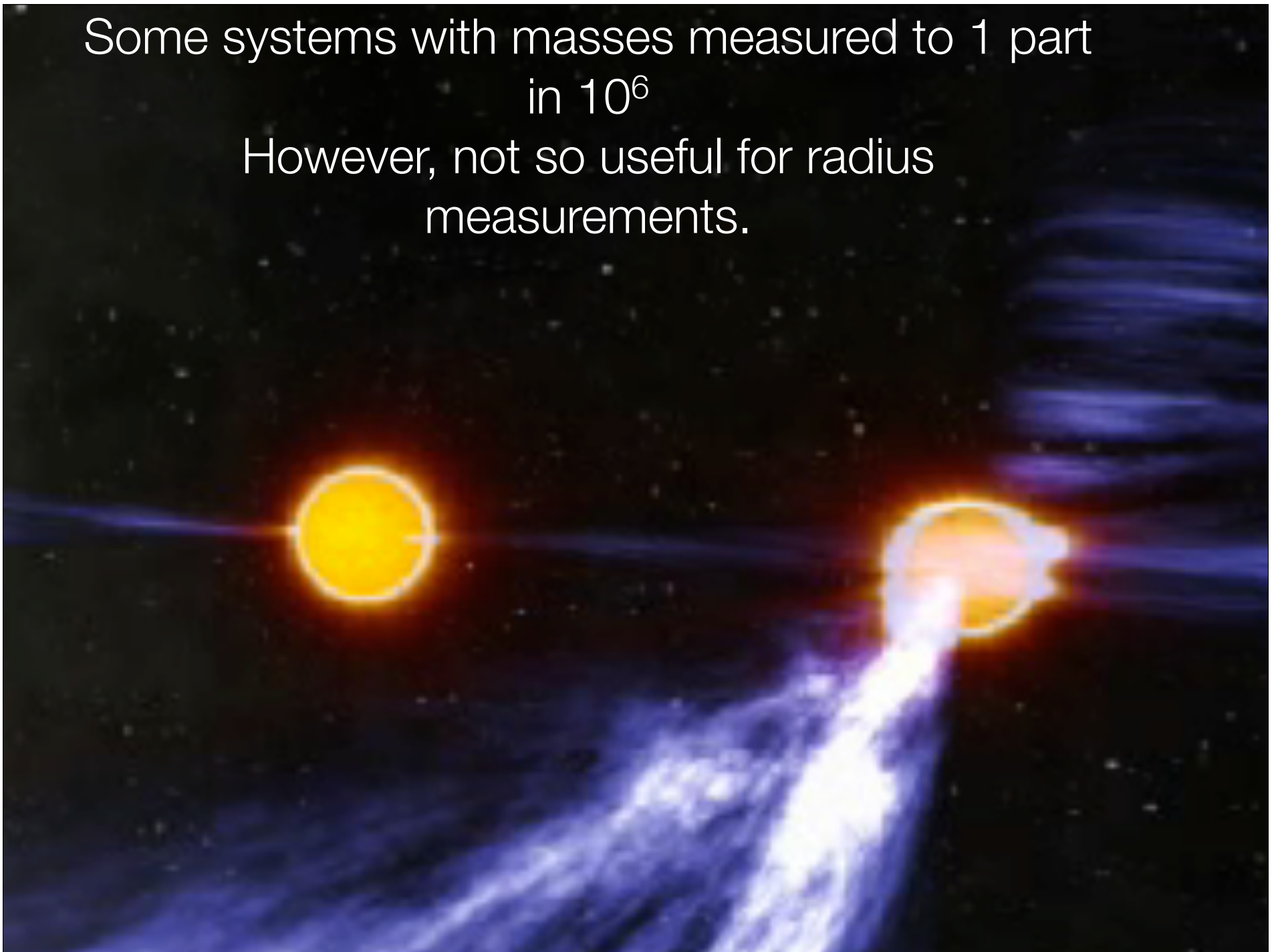
Credit:  
Dany Page

# Mass-Radius Relation from the Equation of State

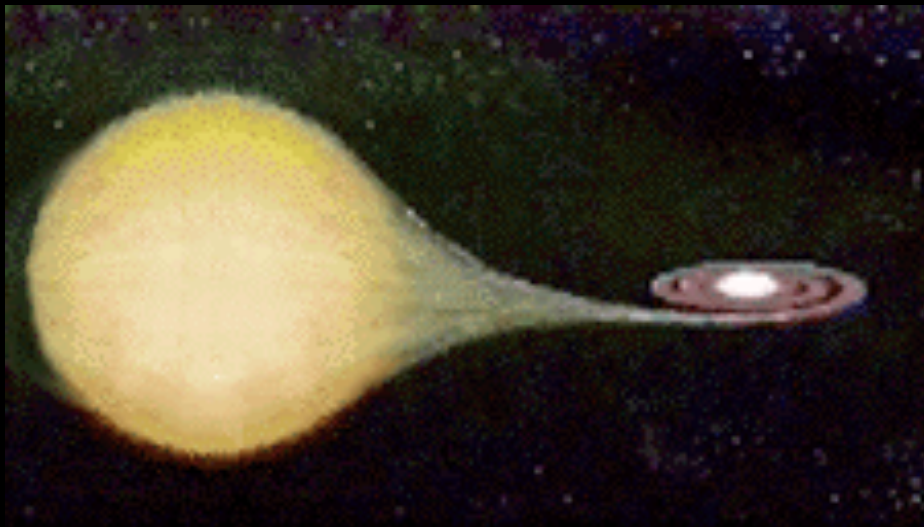


Some systems with masses measured to 1 part  
in  $10^6$

However, not so useful for radius  
measurements.



## Quiescent Low Mass X-ray Binaries



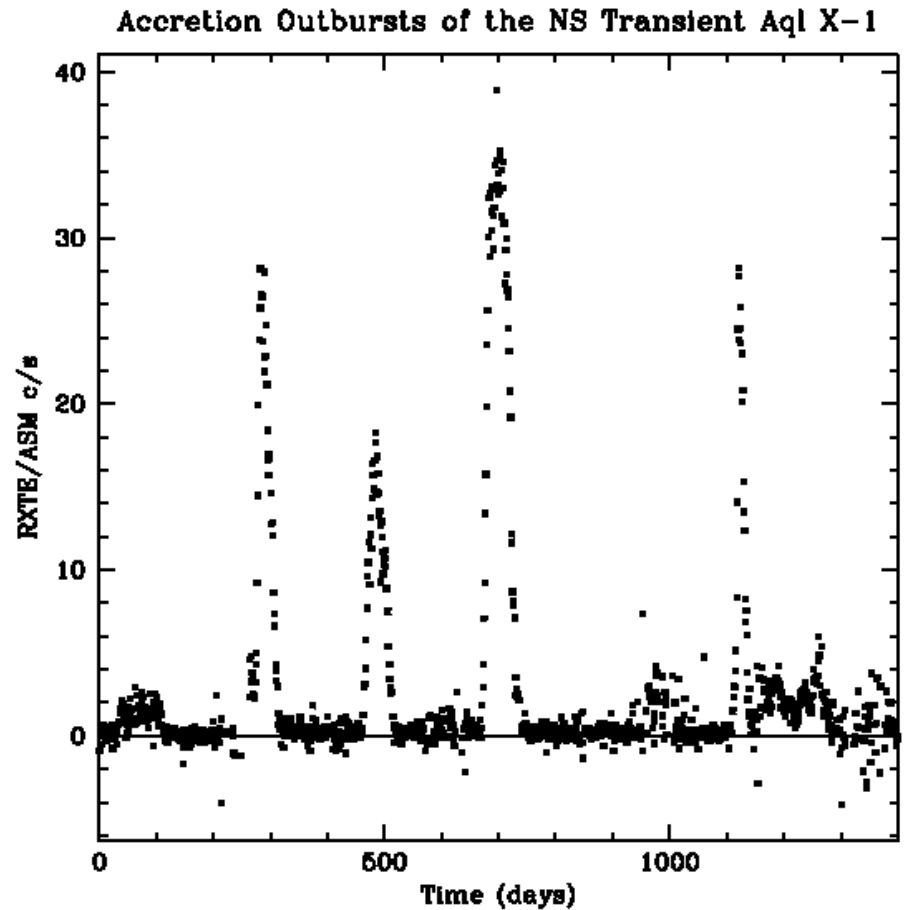
- When accreting (pictured) we mostly observe X-rays from the disk.
- In some sources (“transients”) accretion can stop -- and then we see only the neutron star.

System Names: LMXBs, Soft X-ray Transients,  
Neutron-Star Binaries.

# Soft X-ray Transients

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- Outbursts are due to disk instability; peak luminosities are  $10^{36}$ - $10^{38}$  ergs  $s^{-1}$ .
- Outbursts last  $\sim 30$  days (or as long as years).
- Exhibit type-I X-ray bursts (thermonuclear flashes).
- After outburst, X-ray sources return to quiescence ( $10^{31}$ - $10^{33}$  ergs  $s^{-1}$ )

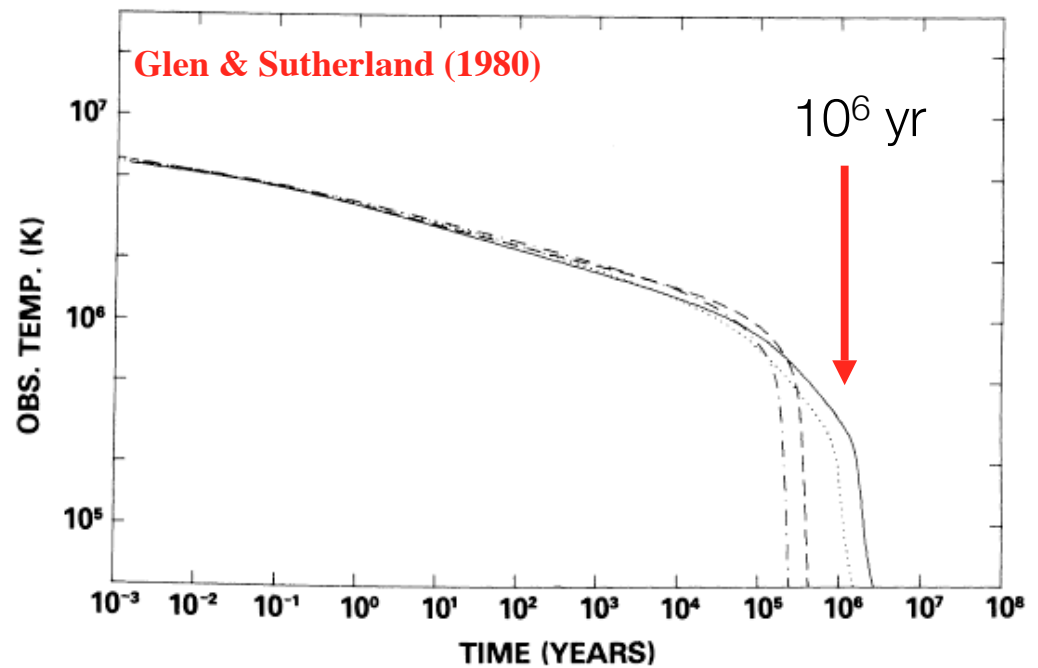


# Why are qLMXBs promising for measuring NS radii?

Brown, Bildsten & RR (1998)

First detection: transient neutron star was discovered in quiescence (Cen X-4;  $L_x \sim 10^{33} \text{ erg s}^{-1}$ . Van Paradijs et al 1984), resulted in two problems :

1. The neutron stars should be cold. Luminosity provided by accretion? (van Paradijs et al 1984)



**Alternative:**  
**Deep Crustal Heating**



# Deep Crustal Heating (Haensel & Zdunik 1990, 2003)

Non-Equilibrium Processes in the Outer Crust			
Beginning with $^{56}\text{Fe}$			
$\rho$ (g cm $^{-3}$ )	Reaction	$\Delta\rho/\rho$	Q (Mev/np)
$1.5 \cdot 10^9$	$^{56}\text{Fe} \Rightarrow ^{56}\text{Cr} - 2e^- + 2\nu_e$	0.08	0.01
$1.1 \cdot 10^{10}$	$^{56}\text{Cr} \Rightarrow ^{56}\text{Ti} - 2e^- + 2\nu_e$	0.09	0.01
$7.8 \cdot 10^{10}$	$^{56}\text{Ti} \Rightarrow ^{56}\text{Ca} - 2e^- + 2\nu_e$	0.10	0.01
$2.5 \cdot 10^{10}$	$^{56}\text{Ca} \Rightarrow ^{56}\text{Ar} - 2e^- + 2\nu_e$	0.11	0.01
$6.1 \cdot 10^{10}$	$^{56}\text{Ar} \Rightarrow ^{52}\text{S} + 4n - 2e^- + 2\nu_e$	0.12	0.01

Series of reactions  
deposit  $Q=1.45$  MeV/np  
within the crust

Non-Equilibrium Processes in the Inner Crust			
$\rho$ (g cm $^{-3}$ )	Reaction	$X_n$	Q (Mev/np)
$9.1 \cdot 10^{11}$	$^{52}\text{S} \Rightarrow ^{46}\text{Si} + 6n - 2e^- + 2\nu_e$	0.07	0.09
$1.1 \cdot 10^{12}$	$^{46}\text{Si} \Rightarrow ^{40}\text{Mg} + 6n - 2e^- + 2\nu_e$	0.07	0.09
$1.5 \cdot 10^{12}$	$^{40}\text{Mg} \Rightarrow ^{34}\text{Ne} + 6n - 2e^- + 2\nu_e$		
	$^{34}\text{Ne} + ^{34}\text{Ne} \Rightarrow ^{68}\text{Ca}$	0.29	0.47
$1.8 \cdot 10^{12}$	$^{68}\text{Ca} \Rightarrow ^{62}\text{Ar} + 6n - 2e^- + 2\nu_e$	0.39	0.05
$2.1 \cdot 10^{12}$	$^{62}\text{Ar} \Rightarrow ^{56}\text{S} + 6n - 2e^- + 2\nu_e$	0.45	0.05
$2.6 \cdot 10^{12}$	$^{56}\text{S} \Rightarrow ^{50}\text{Si} + 6n - 2e^- + 2\nu_e$	0.50	0.06
$3.3 \cdot 10^{12}$	$^{50}\text{Si} \Rightarrow ^{44}\text{Mg} + 6n - 2e^- + 2\nu_e$	0.55	0.07
$4.4 \cdot 10^{12}$	$^{44}\text{Mg} \Rightarrow ^{36}\text{Ne} + 6n - 2e^- + 2\nu_e$		
	$^{36}\text{Ne} + ^{36}\text{Ne} \Rightarrow ^{72}\text{Ca}$		
	$^{68}\text{Ca} \Rightarrow ^{62}\text{Ar} + 6n - 2e^- + 2\nu_e$	0.61	0.28
$5.8 \cdot 10^{12}$	$^{62}\text{Ar} \Rightarrow ^{60}\text{S} + 6n - 2e^- + 2\nu_e$	0.70	0.02
$7.0 \cdot 10^{12}$	$^{60}\text{S} \Rightarrow ^{54}\text{Si} + 6n - 2e^- + 2\nu_e$	0.73	0.02
$9.0 \cdot 10^{12}$	$^{54}\text{Si} \Rightarrow ^{48}\text{Mg} + 6n - 2e^- + 2\nu_e$	0.76	0.03
$1.1 \cdot 10^{13}$	$^{48}\text{Mg} + ^{48}\text{Mg} \Rightarrow ^{96}\text{Cr}$	0.79	0.11

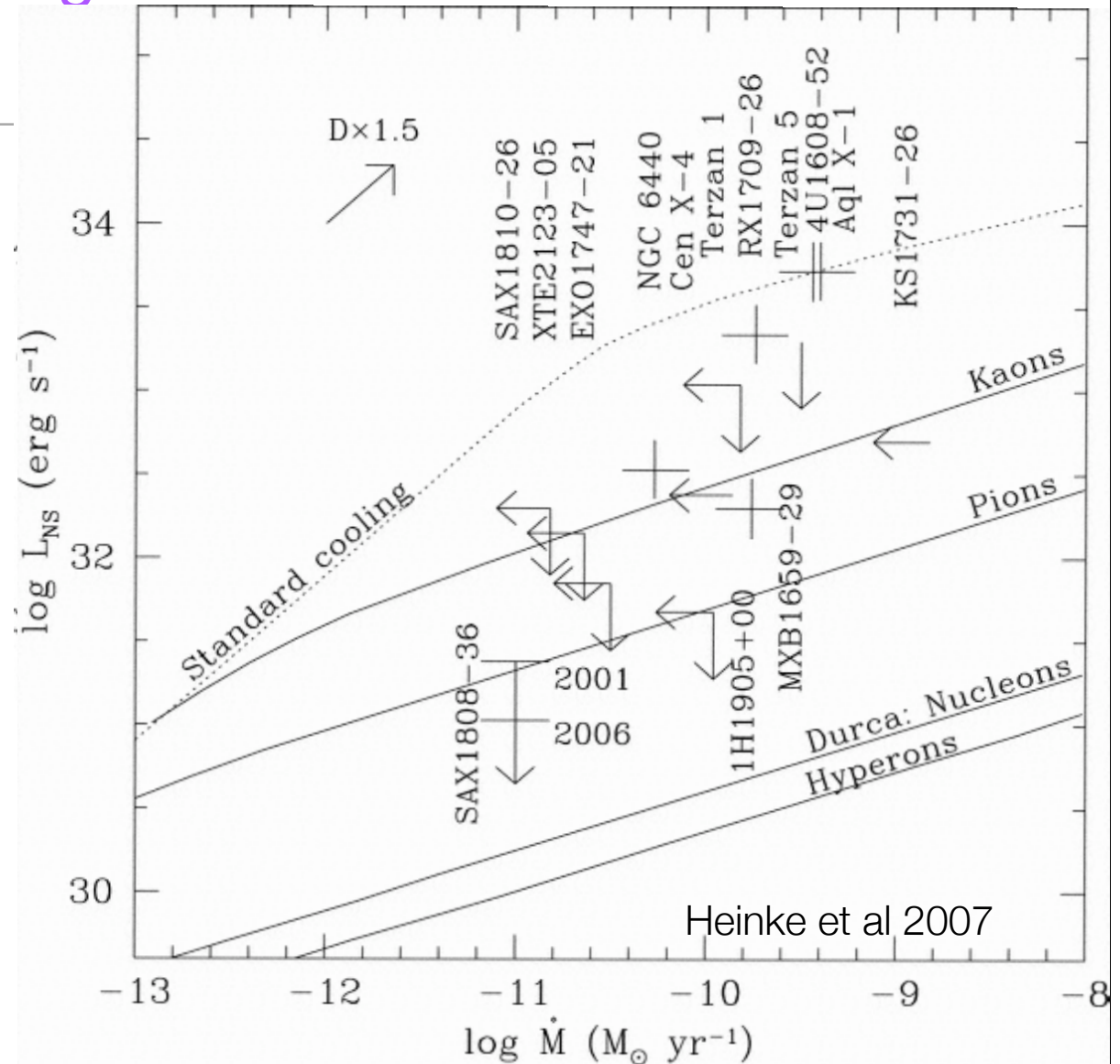
1.45 Mev per np

# Deep Crustal Heating

Reactions in the crust provide  $\sim 1$  MeV/np. Because the crust is in close thermal contact with the NS core, this will heat a cold core until a steady-state is reached ( $10^4$  yr; cf. Colpi 1999) in which the energy emitted between outbursts (the quiescent luminosity) is equal to the energy deposited in the crust during outbursts.

$$L_q \approx 6 \times 10^{33} \frac{\langle \dot{M} \rangle}{10^{-10} M_{sun} \text{ yr}^{-1}} \frac{Q}{1 \text{ MeV}} \text{ erg s}^{-1}$$

$$F_q \approx \frac{\langle F \rangle}{200 \text{ 1MeV}} \frac{Q}{1 \text{ MeV}}$$



Brown, Bildsten & RR (1998)

## Why are qNSs promising for measuring NS radii?

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2. Spectral fits using blackbody spectra produced too small of radii for a neutron star (<1 km vs. ~10-20 km, with  $kT_{\text{eff}} \sim 100$  eV).

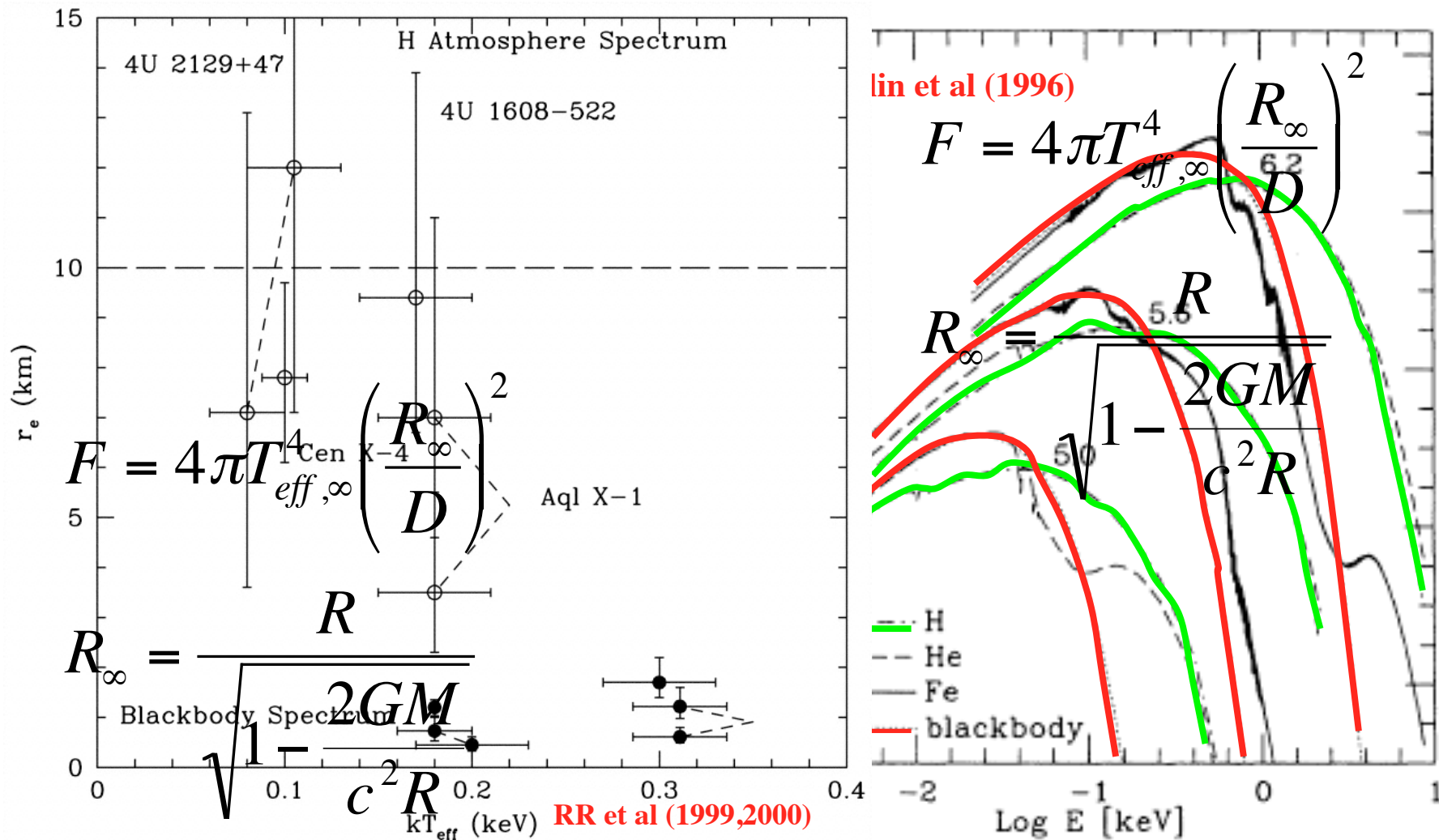
Solution: qNSs are not blackbodies.

When the accretion rate onto the NS drops below a certain rate ( $\sim 10^{34}$  erg s<sup>-1</sup>) metals settle out of the photosphere on a timescale of 10-100 sec (Bildsten et al 1992). This leaves a photosphere of pure Hydrogen. The dominant opacity of a ~100 eV H photosphere is free-free processes, which is strongly energy dependent.

$$\kappa_{\frac{ff}{E}} \approx 114 \left( \frac{kT}{50 \text{ eV}} \right)^{-3/2} \left( \frac{E}{1 \text{ keV}} \right)^{-3} \text{ cm}^2 \text{ g}^{-1}$$

Brown, Bildsten & RR (1998)

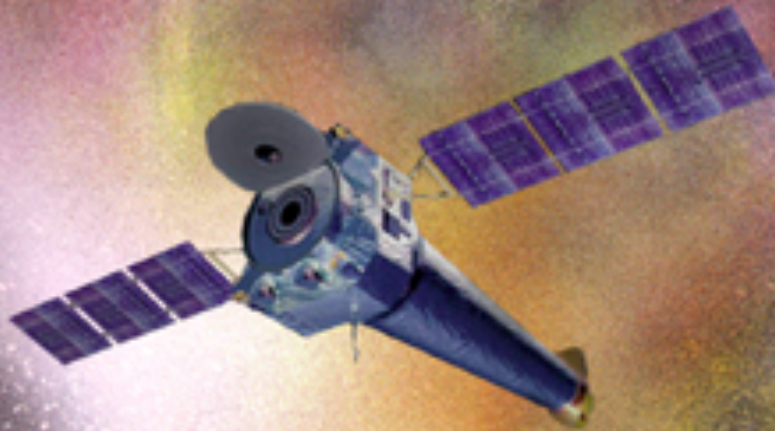
# Emergent Spectra from Neutron Star Hydrogen Atmosphere





## Chandra X-ray Observatory

- Launched 1999 (NASA)
- 1" resolution

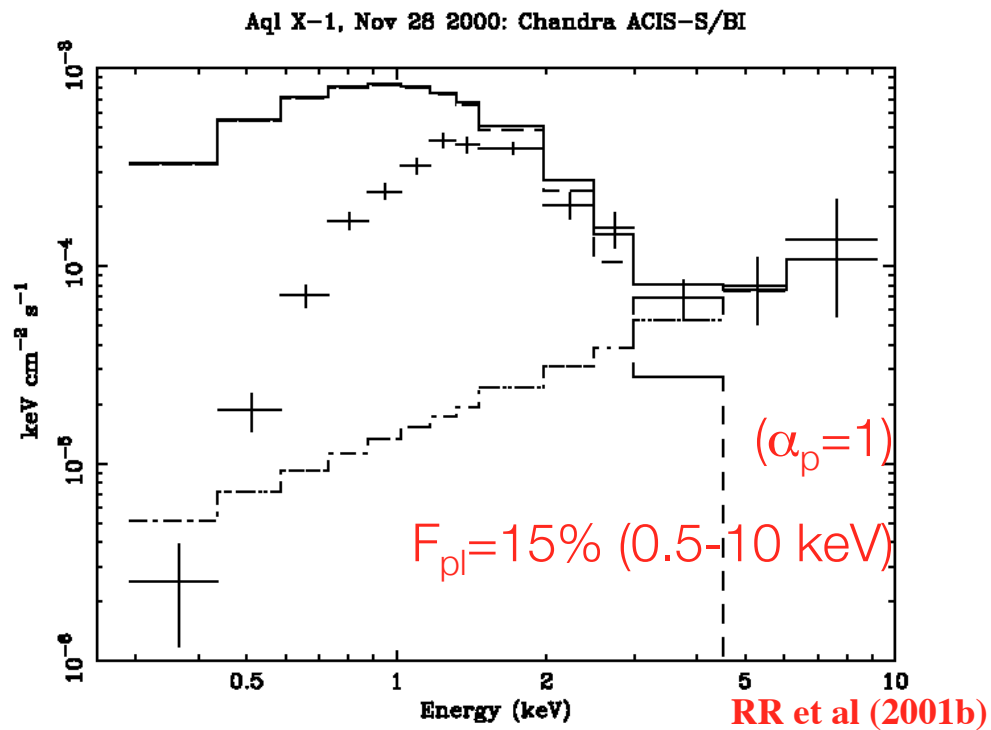


## XMM/Newton

- Launched 1999 (ESA)
- 6" resolution
- ~4x area of Chandra.



# Aql X-1 with Chandra -- Field Source

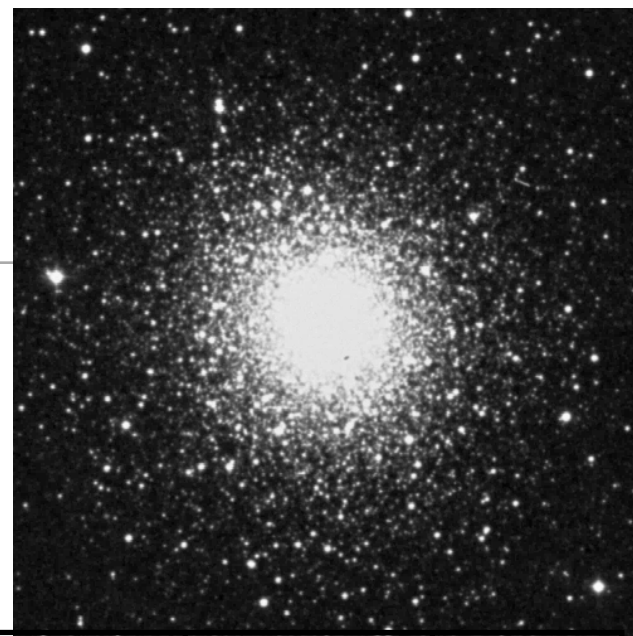


$R_\infty$ (d/5 kpc)	$kT_{\text{eff},\infty}$	$N_H$ ( $1e20 \text{ cm}^{-2}$ )
$13_{-4}^{+5} \text{ km}$	$135_{-12}^{+18} \text{ eV}$	$35_{-7}^{+8}$

## The LMXB Factories: Globular Clusters

- GCs : overproduce LMXBs by 1000x vs. field stars -- contain 10% of the known LMXBs vs. 0.01% of the stars in the galaxy.
- Accurate distances are important for a number of studies (Stellar evolution, WD cooling).

**qNSs can be identified by their soft X-ray spectra, and confirmed with optical counterparts.**



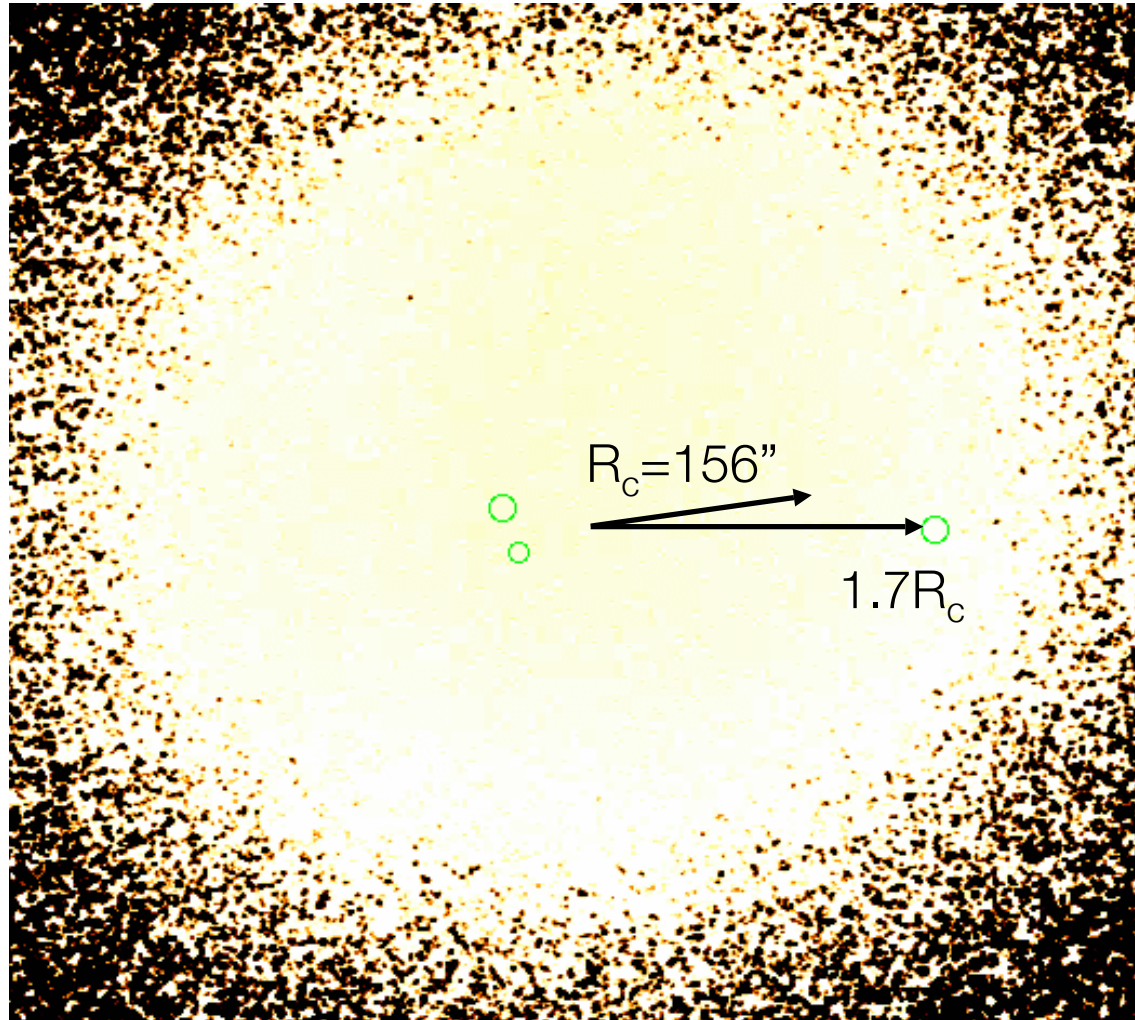
NGC	D (kpc)	+/- (%)
104	5.13	4
288	9.77	3
362	10.0	3
4590	11.22	3
5904	8.28	3
7099	9.46	2
6025	7.73	2
6341	8.79	3
6752	4.61	2

Carretta et al (2000)



# NGC 5139 (Omega Cen)

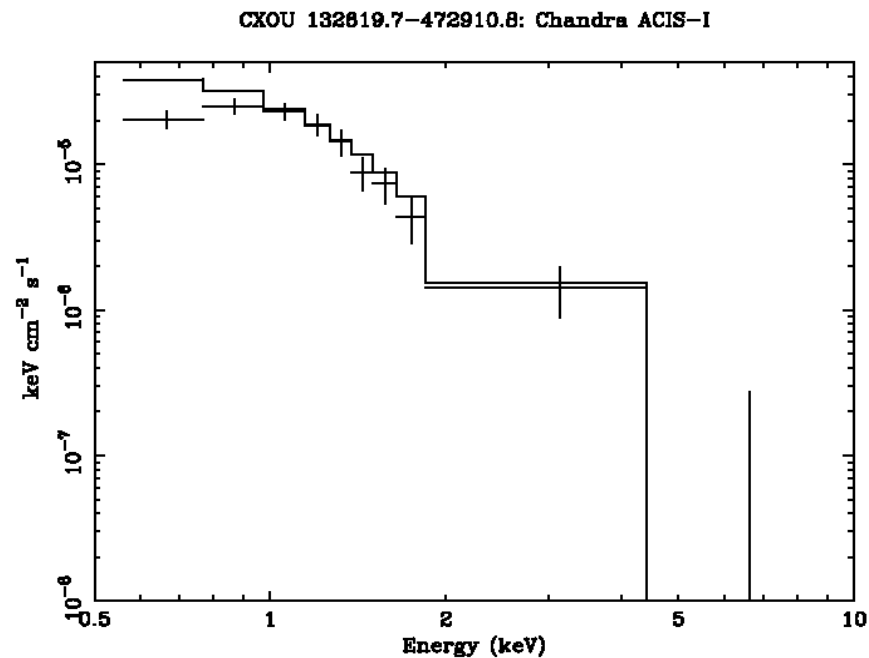
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The optical counterpart has been identified!  
(second one)



# NGC 5139 (Omega Cen)



$R_\infty$ (d/5 kpc)	$kT_{\text{eff},\infty}$	$N_H$ ( $1e20 \text{ cm}^{-2}$ )
$14.3 \pm 2.1 \text{ km}$	$66_{-5}^{+4} \text{ eV}$	(9)

**RR et al (2002)**

# The Best Measured Neutron Star Radii

Name	$R_\infty$ (km/D)	D (kpc)	$kT_{\text{eff},\infty}$ (eV)	$N_{\text{H}}$ ( $10^{20} \text{ cm}^{-2}$ )	Ref.
<b>omega Cen</b> (Chandra)	$13.5 \pm 2.1$	<b>5.36</b> $\pm 6\%$	$66^{+4}_{-5}$	(9)	Rutledge et al (2002)
<b>omega Cen**</b> (XMM)	$13.6 \pm 0.3$	<b>5.36</b> $\pm 6\%$	$67 \pm 2$	$9 \pm 2.5$	Gendre et al (2002)
<b>M13**</b> (XMM)	$12.6 \pm 0.4$	<b>7.80</b> $\pm 2\%$	$76 \pm 3$	(1.1)	Gendre et al (2002)
<b>47 Tuc X7</b> (Chandra)	$34_{-13}^{+22}$	<b>5.13</b> $\pm 4\%$	$84^{+13}_{-12}$	$0.13^{+0.06}_{-0.04}$	Heinke et al (2006)
<b>M28**</b> (Chandra)	$14.5_{-3.8}^{+6.9}$	<b>5.5</b> $\pm 10\%$	$90_{-10}^{+30}$	$26 \pm 4$	Becker et al (2003)
<b>NGC 7099</b> (Chandra)	$16.9_{-4.3}^{+5.4}$	--	$94_{-12}^{+17}$	$2.9^{+1.7}_{-1.2}$	Lugger et al (2006)
<b>NGC 2808</b> (XMM)	??	<b>9.6 (?)</b>	$103_{-33}^{+18}$	$18^{+11}_{-7}$	Webb et al (2007)

Caveats:

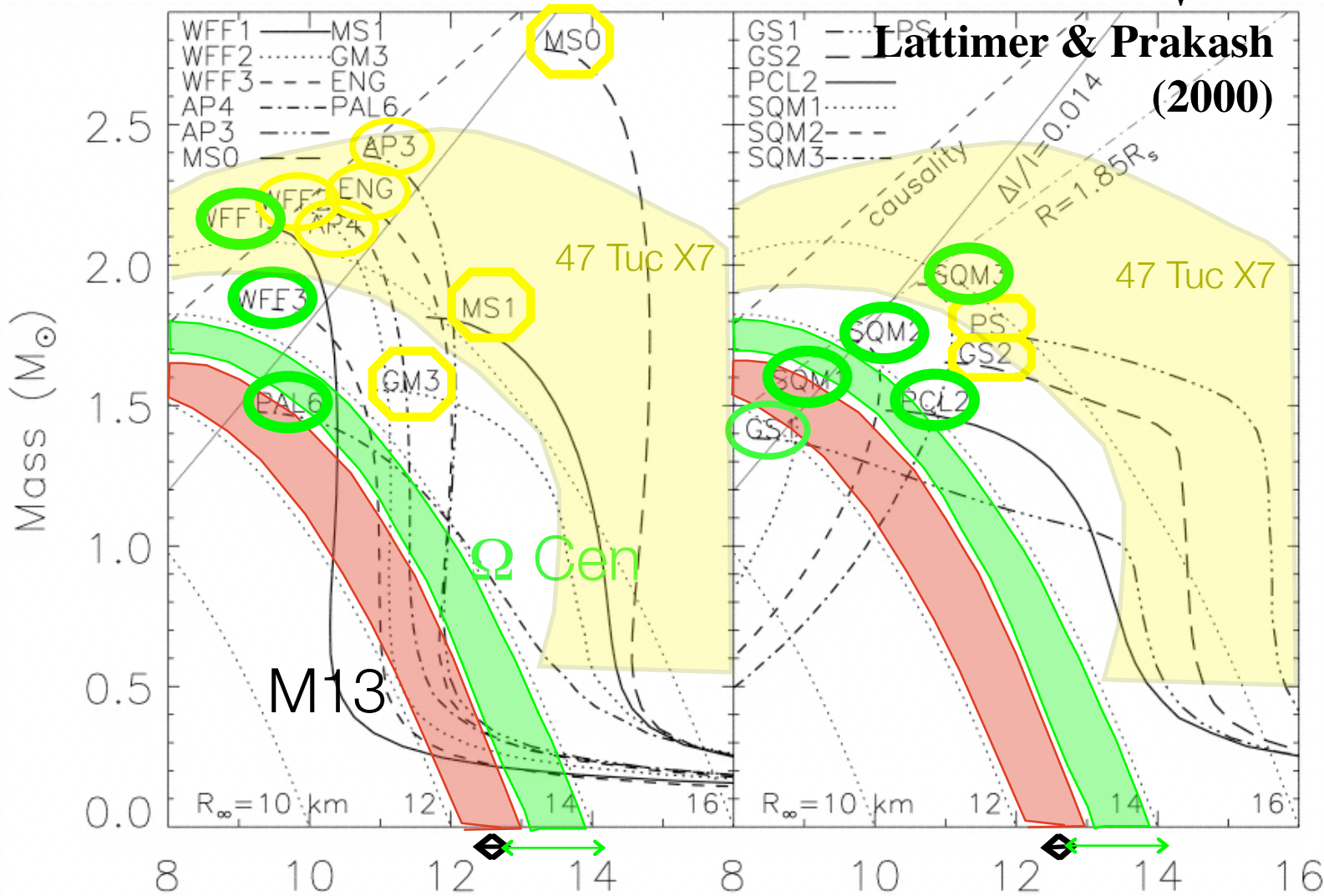
- All IDd by X-ray spectrum (47 Tuc, Omega Cen now have optical counterparts)
- calibration uncertainties

Distances:

**Carretta et al (2000),  
Thompson et al (2001)**

# Best Mass-Radius Constraints on the Equation of State

$$R_\infty = \frac{R_{NS}}{\sqrt{1 - \frac{2GM_{NS}}{c^2 R_{NS}}}}$$



47 Tuc X7 - Heinke et al (2006)  
 M13 - Gendre et al (2002a)  
 Omega Cen - Gendre et al (2002b)

**Observed****Observed with insufficient time****Not Observed**

NGC	Rcore (")	D (kpc)	log NH	Obs. Time	qNS detect	qNSs?
104	22.5	4.6	20.3	74 I/ 299 S	33	2
5904	24.2	7.6	20.2	45	87	
3201	86.3	5.0	21.1	(XMM: 70)	56	1?
4372	104.2	5.2	21.4	(XMM)	89	
4833	60.2	5.8	21.3	0	91	
5139	156.3	4.9	20.9	70 S	48	1
6121	50.3	2.0	21.4	25	12	
6205	52.0	7.2	20.0	60 ksec 11/05	76	1/XMM
6218	39.4	5.6	21.0	30	66	
6254	51.3	4.3	21.2	0	47	
6352	49.9	6.1	21.0	0	80	
6366	110.1	4.0	21.6	XMM 70; 24	68	
6397	3.0	2.2	21.0	109	10	1
6496	62.8	5.7	21.0	0	66	
6539	4.0	32.5	21.7	(scheduled)	92	
6541	17.9	6.6	20.9	46 S	83	
6544	2.9	2.5	21.6	17	29	
6553	33.1	3.5	21.7	XMM 21	73	
6656	84.3	3.0	21.3	XMM 470	26	
6752	10.5	4.2	20.3	30 S	28	
6809	170.6	4.8	20.8	XMM 27	43	
6838	38.2	3.9	21.2	55	39	
7099	3.4	7.4	20.5	50 S	88	

- 23 GCs for which one could easily detect  $10^{32}$  erg/s qNS in <100 ksec w/ Chandra

- 12 have sufficient time, in which 5 (6?) qNSs detected.

- 5 observed with insufficient time.

6 not observed.

# Mass Measurements with Continuum Spectra

$$R_\infty \rightarrow$$

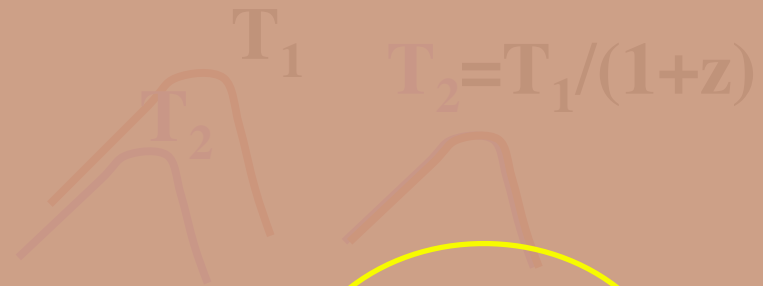
Normalization

$$T_\infty \rightarrow$$

Peak of the spectrum

$$z = \frac{GM_{NS}}{c^2 R_{NS}} \rightarrow \text{Second Derivative at the Peak of the Spectrum}$$

$$I(E_\gamma) \propto \left(\frac{E_\gamma}{kT}\right)^3 \frac{1}{e^{\frac{E_\gamma}{kT}} - 1}$$

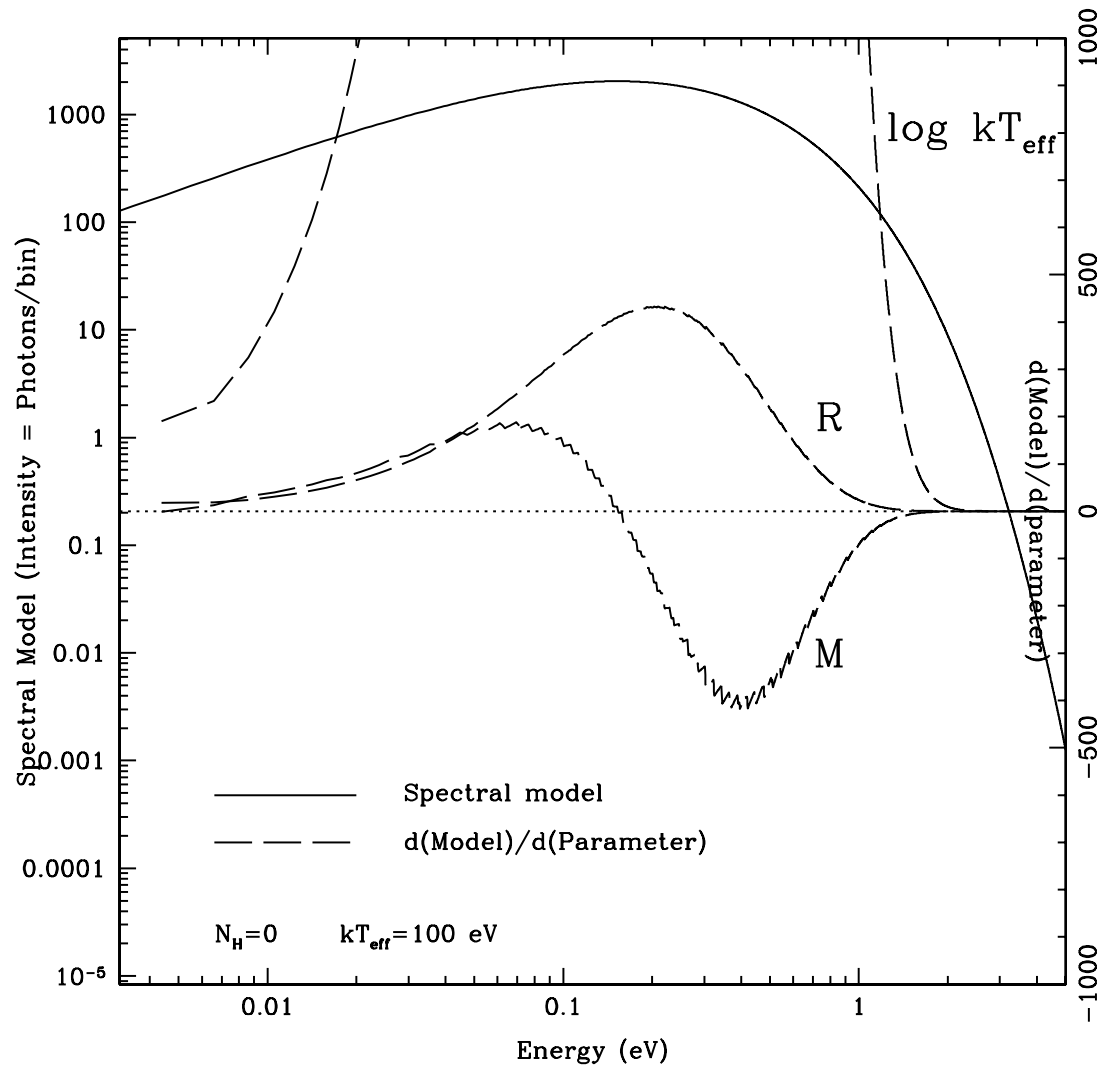


- But the free-free opacity breaks this degeneracy. This spectrum, redshifted, permits (in principle) determination of the redshift.

$$I(E_\gamma) \propto \left(\frac{E_\gamma}{kT}\right)^3 \frac{1}{e^{\frac{E_\gamma}{kT}} - 1} K_{ff,o} \left(\frac{E_o}{E_\gamma}\right)^3$$



# Neutron Star Mass and Radius Measurement with Broad-Band X-ray Spectroscopy: Fisher Analysis



$$M_j = \sum_i F(E_i) A_{i,j}$$

$$C_{\alpha,\beta} = \sum_i \frac{1}{M_i} \frac{dM_i}{dP_\alpha} \frac{dM_i}{dP_\beta}$$

$$\sigma_{\alpha,\beta}^2 = (C^{-1})_{\alpha,\beta}$$

# X-ray Observatories -- Beyond 2010

## Constellation X / (International X-ray Observatory)?

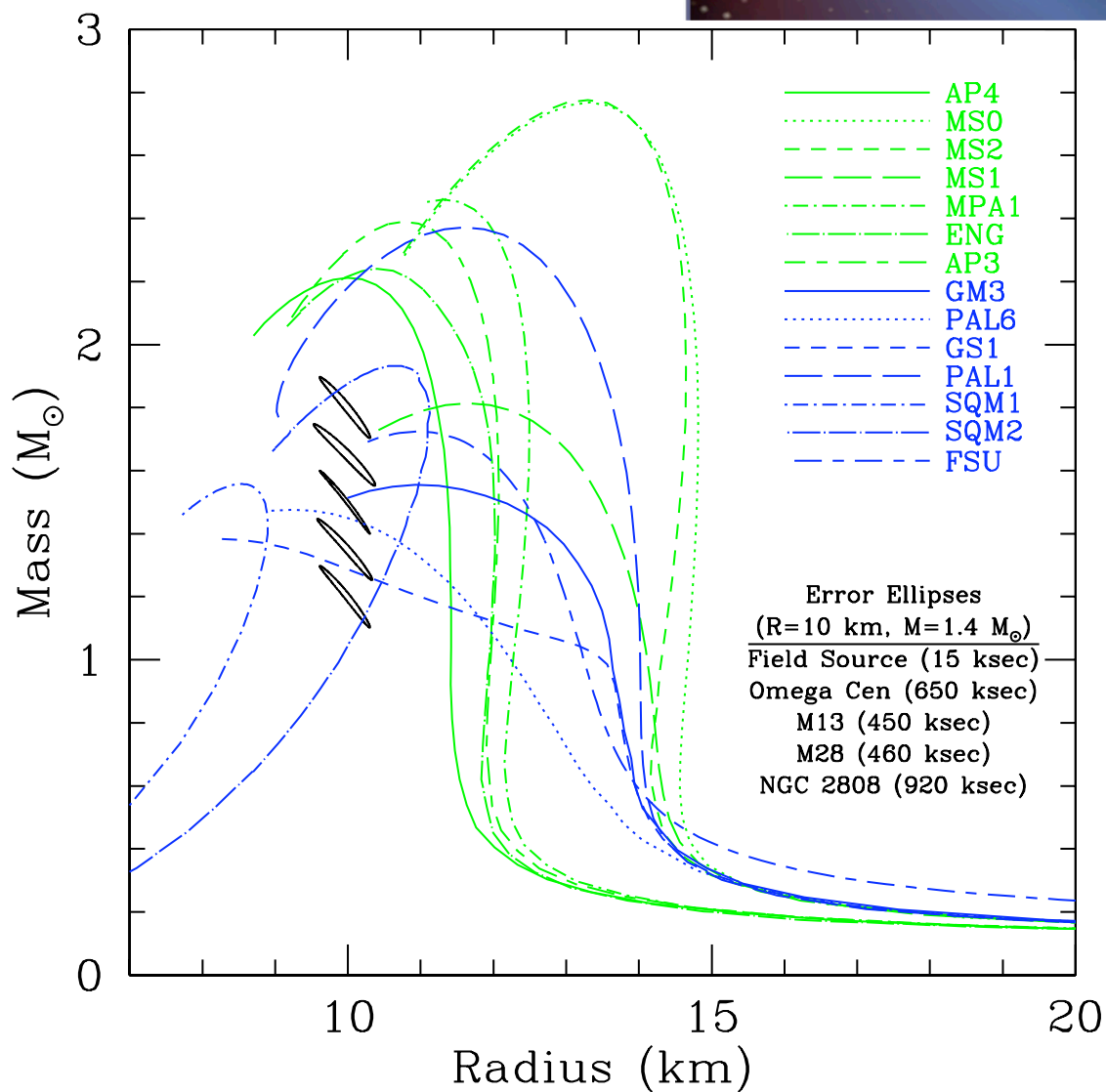
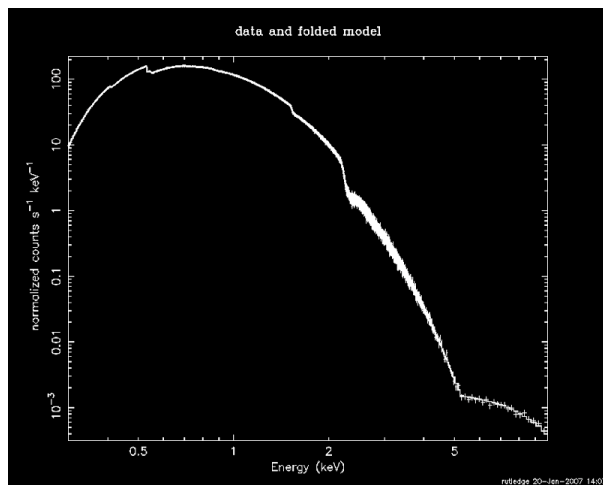
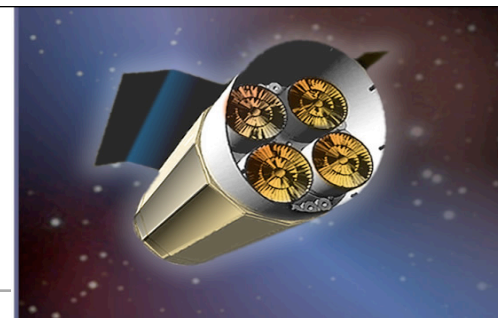
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- Collecting area 50-100x present missions. High S/N X-ray spectroscopy will make possible precise ( $\sim 5\%$  accurate) simultaneous Mass and Radius measurements of neutron stars.
- Status: Under Review to determine priority under the Einstein program (Behind JDEM). Earliest launch: 2016.
- NASA Recently signed MOU with ESA & JAXA to explore an International X-ray Observatory.
- 15" sized PSF excludes all but  $\sim 3$  of the known Globular Cluster sources for detailed study (OCen, M13, M28)
- A return to the field sources is required for progress. This will also require a high-precision (10  $\mu$ arcsec) parallax mission, to obtain  $\sim 2\%$  distances to field sources.



# Constellation X

## Simultaneous Mass and Radius Measurement



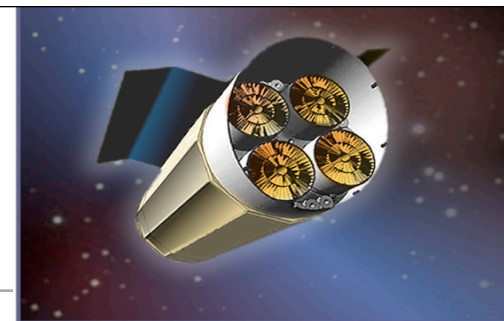


# Observationally important qLMXBs in Globular Clusters

qLMXB	kT_eff(infty) (ev)	NH	Fx ( $10^{-13}$ cgsflux)	Band (keV)	Ref.	
47 Tuc X7	105(5)	0.04(2)	5.3	0.5-10	Heinke et al (2006)	<: 5"
47 Tuc X5	100(20)	0.09(7)	4.3	0.5-10	Heinke et al (2003)	< 5"
M28	90(+30-10)	0.26(4)	3.4	0.5-8	Becker et al (2003)	
NGC 6304 X4	120(50)	[0.266]	2.3	0.5-10	Guillot et al (2008)	
oCen	67(2)	0.09(3)	1.7	0.1-5	Rutledge et al (2002), Gendre et al (2003)	
NGC 6304 X9	100(20)	[0.266]	1.5	0.5-10	Guillot et al (2008)	
NGC 6397	74(18)	0.1-0.26	1.06	0.5-2.5	Grindlay et al (2001)	< 15"
M13	76(3)	[0.011]	1.03	0.1-5	Gendre et al (2003)	
M30 A-1	94(15)	0.03(1)	0.73	0.5-10	Lugger (2007)	
NGC 6304 X5	70(25)	[0.266]	0.59	0.5-10	Guillot et al (2008)	
M80 CX2	82(2)	0.09(2)	0.23	0.5-6	Heinke et al (2003)	<5"
M80 CX6	76(6)	0.22(7)	0.07	0.5-6	Heinke et al (2003)	<15"
NGC 2808 C2	--	0.86	0.02	--	Servillat et al (2008)	<15"

# Constellation X/IXO

## Simultaneous Mass and Radius Measurement



- Neutron Star Masses and Radii can be measured from Hydrogen atmosphere neutron stars with ~few% accuracy with coming generation X-ray telescope.
- Field sources are the most promising targets, due to their brightness.
- Parallax mission will also be required to obtain accurate (1%) distances.

