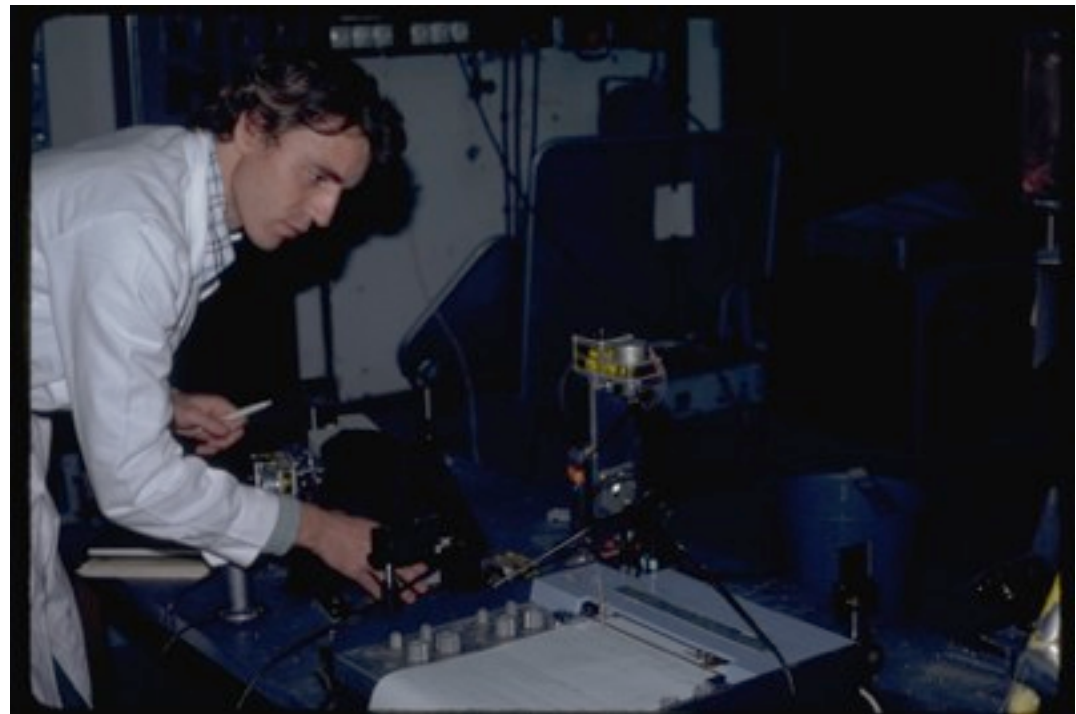


Some recent Insertion Device innovations on operating third and fourth generation light sources

M. E. Couprie,

C. Benabderrahmane, F. Briquez, O. Marcouillé, F. Marteau, M. Valleau, P. Berteaud, L. Chapuis, M. Massal, J. Vétérán, H. Abualrob, P. Brunelle, L. Nadolski, R. Nagaoka, A. Nadji (Synchrotron SOLEIL), O. Chubar, C. Kitegi (BNL), J. M. Filhol (Fusion to Energy)



**Talk dedicated to P. Elleaume
(† 2011, March 19)**

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

1- In vacuum undulators and wigglers

issues (transitions, direct in vacuum measurements..)

quest for short period high field, cryogenic systems

in vacuum wigglers as an alternative to superconducting wigglers

2- EPU and fast polarization switching

electromagnetic system

Permanent magnet approach

Combined electromagnetic- permanent magnet approach : EMPHU

3- Effect of IDs on the light source operation

strategies to compensate unwanted effects

desired effects : A Robinson wiggler as an alternative to the damping wiggler

canted undulators



Accelerator type issues for insertion devices

	storage ring	linac / ERL	LWFFA
Emittance	E^2	I/E	
Beamsize (μm)	100 (H)-10 (V)	50-10	10-3
vacuum chamber H /V aperture	flat min gap: 5 mm	round (ex : bore 5 mm), min gap : 3 mm	round
charge	high	1 nC	10 pC
Pulse duration	10 ps	100 fs	10 fs
impedance	very critical	critical	critical
field integrals	very critical	very critical	very critical
double field integrals	very critical	very critical	very critical
phase error	very critical for high harmonics operation	critical	critical
multipoles	for beam lifetime and injection efficiency	less critical	not critical

In vacuum undulators

Motivation : reach a higher field by placing directly the magnets inside the vacuum chamber

$\text{Sm}_2\text{Co}_{17}$: $B_r \leq 1.05\text{T}$; $\mu\text{Hc}_j = 2.8\text{T}$; $\text{Nd}_2\text{Fe}_{14}\text{B}$: $B_r \leq 1.4\text{T}$ (1.26T); $\mu_0\text{Hc} = 1.4\text{-}1.6$ (resp. 2.4T)

Coercivity to avoid demagnetisation when baking and to resist against irradiation (GeV electrons, high energy photons and gamma-rays, neutrons) => $B_r < 1.26\text{T}$

Machine protection for the IVU to avoid magnet degradation, cases ESRF,APS

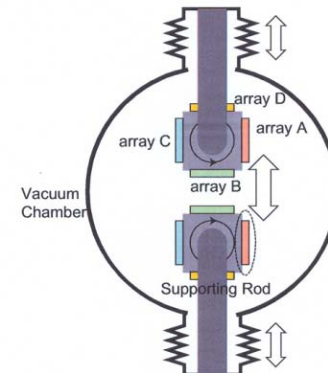
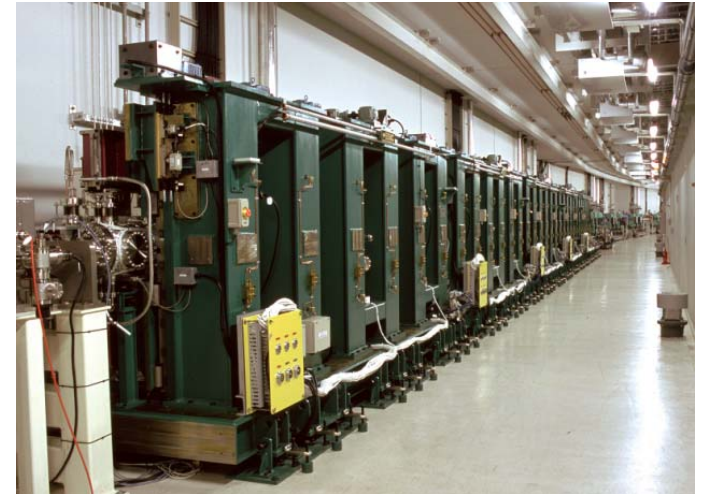
Historical steps :

- First prototype at BESSY
W. Gudat et al. NIMA 246, 1986 50

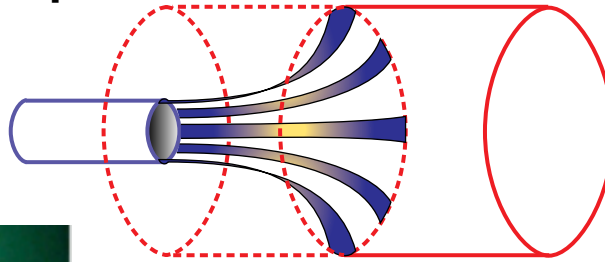
- **First In vac. undulator Installed on TRISTAN AR**, Period : 40 mmX90, NdFeB ($B_r=1.2\text{T}$, $i\text{Hc}=21\text{kOe}$), min gap 10 mm, $B=0.82\text{-}0.36\text{T}$, NEG and sputter ion pumps, magnet stabilization at 125°C and vacuum commissioning at 115°C , *S. Yamamoto et al. Rev. Sci. Instr 63, 400 (1992)*

- **30 m long in-vacuum undulator at SPring-8 (SLUS-I)** :
32 mm x 780, min gap = 12 mm ($\beta\text{V} = 15\text{ m}$) $B=0.59\text{T}$
5 segments without gaps, very fine adjustments of the gap segments for phase error ($11^\circ \Rightarrow 3.6^\circ$)
H. Kitamura et al., NIMA 467 (2001) 110; T.Tanaka et al. NIMA 467, (2001) 149

- **Revolver in-vacuum undulator (INVRUM)** :
6 mm x 133, 10 mmx100, 15 mmX66, 20mmx50; min gap = 3.2 mm, $B=0.74, 1.07, 1.32, 1.44\text{T}$
T. Bizen et al. AIP 705, (2004), 175, 18th International Conference on Synchrotron Radiation Instrumentation, San Francisco, 2003 417, H.S. Kang et al., EPAC 2006, 2771

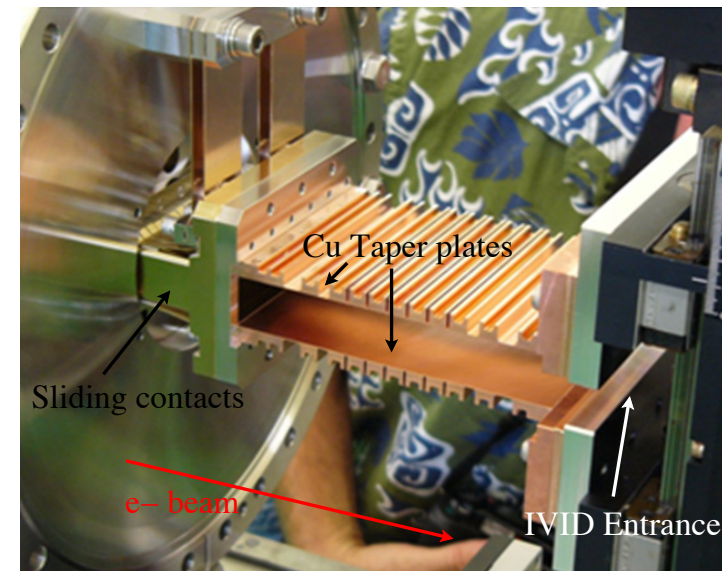
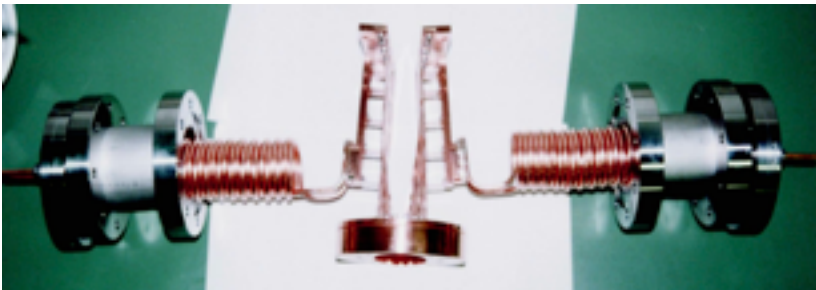


Impedance issues : RF transitions



ALS design

A. Madur et al., PAC 2009; 333



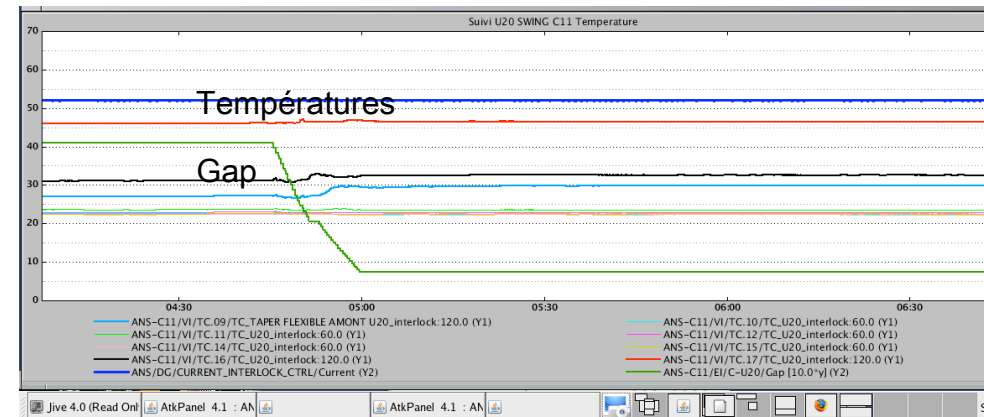
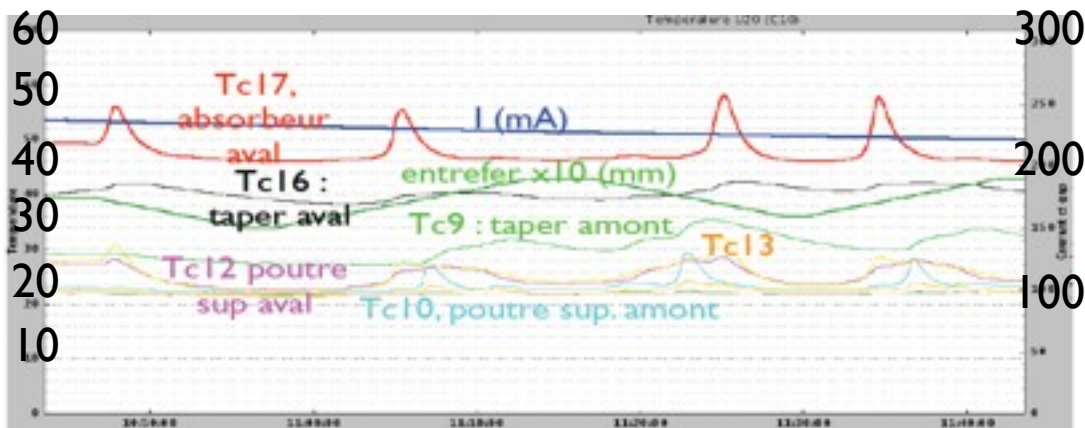
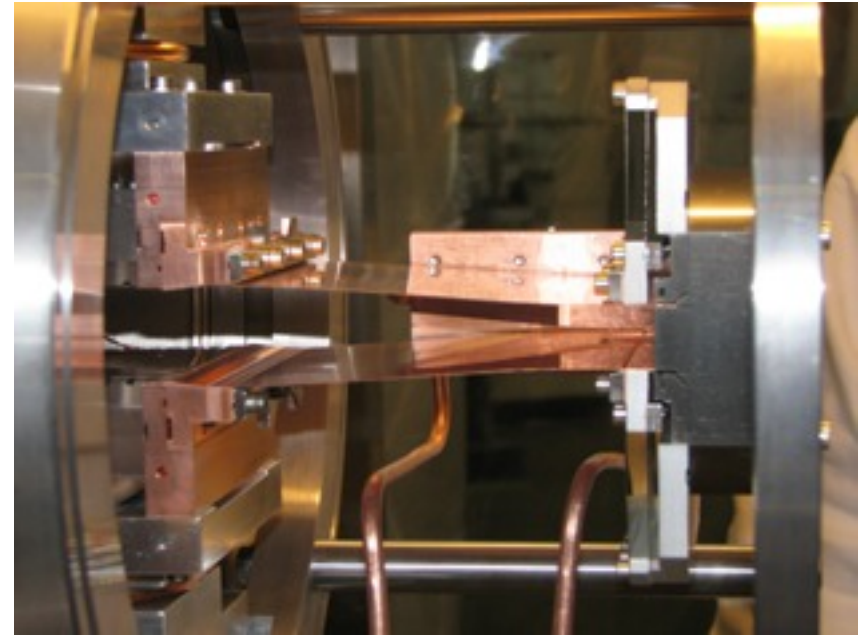
Spring-8 design, first adopted by SLS
(images : courtesy T. Hara)

T. Nakamura et al. PAC 2001, 1969

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Impedance issues : RF transitions

Change of the design at SOLEIL : for SOLEIL storage ring operation at 500 mA

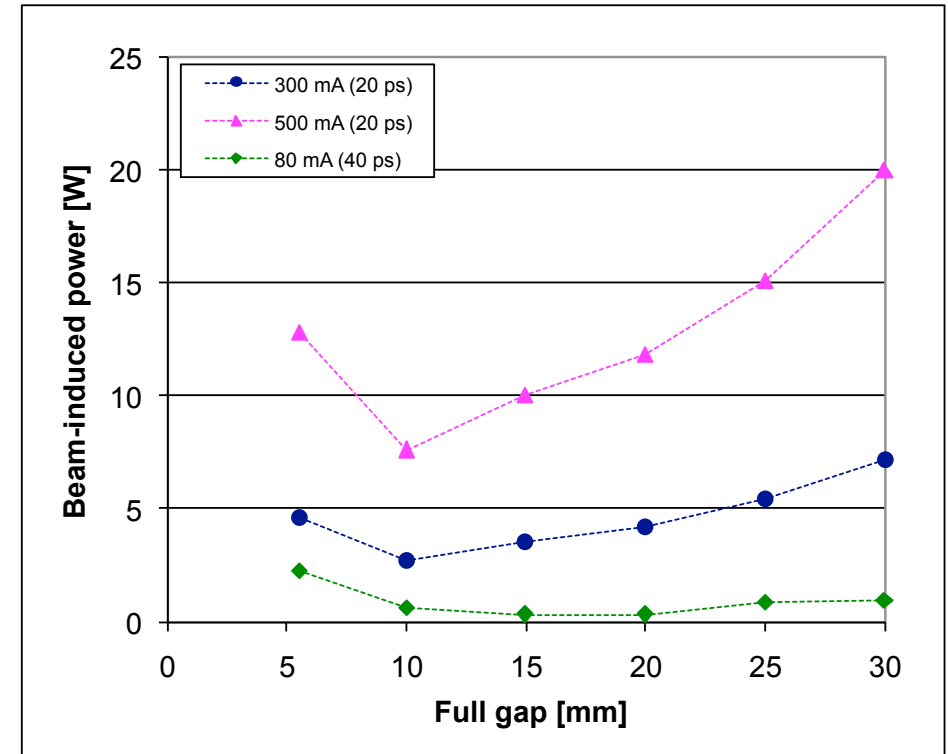
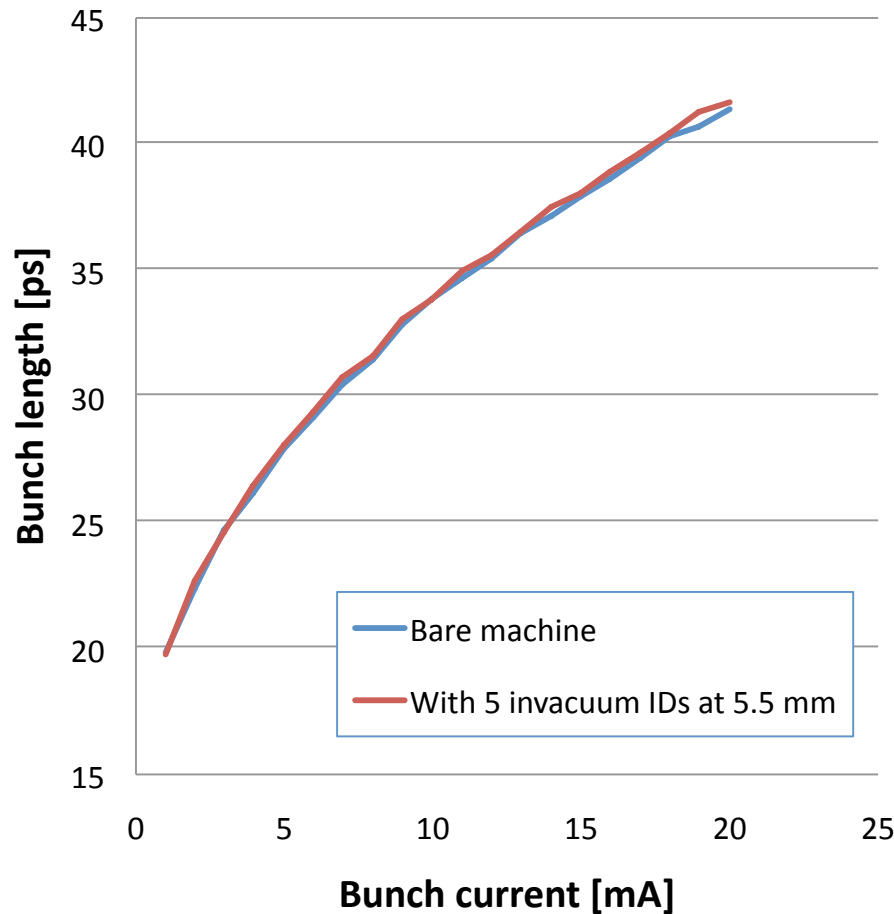


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Impedance issues : RF transitions

R. Nagaoka, SOLEIL case (GdfidL)

sbtrack calc: $V_{rf} = 2.8 \text{ MV}$



$|Z/n|_{\text{eff}} = 0.45 \Omega$, 5 in vacuum ID
contribution : 11.6 m Ω

10 taper of middle SS contribution : 9.3 m Ω

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Impedance issues : liner

Liner : Conductive foil

image current, heat load due to wakefields or upstream synchrotron radiation

Some observations of liner degradation

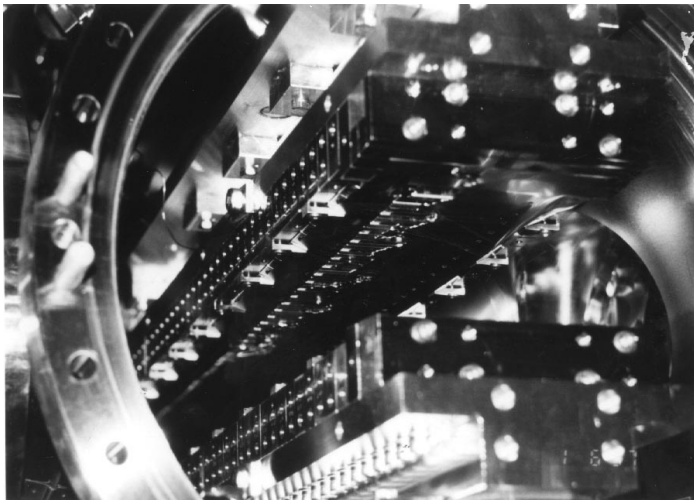
beam measurements

- obstacles with bumps
 - outgassing
 - partial loss

ESRF/SPring-8 : burned 50 μm stainless steel foil

=> demagnetisation of 0.5 % between poles 70-120

=> Cu(10 μm)-Ni(50 μm) foil with better thermal and electric conductivity



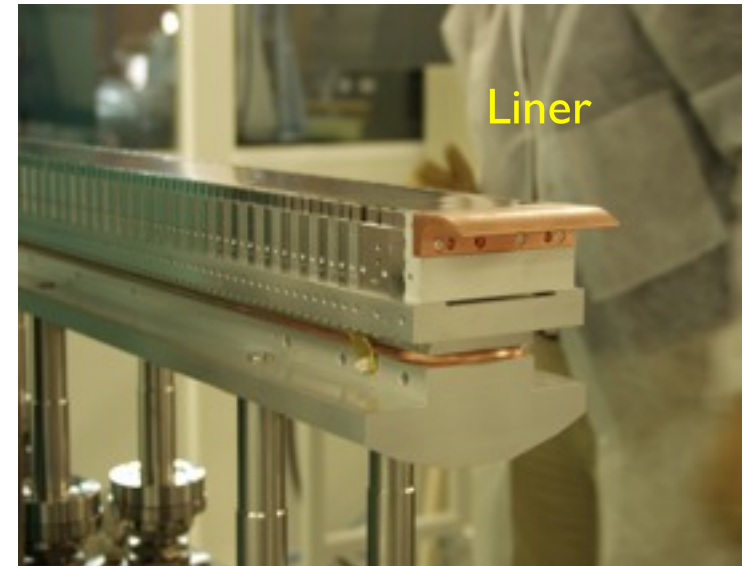
T. Hara et al., SPring-8 in-vacuum undulator beam test at the ESRF, *J. Synchrotron Rad.* (1998), 5, 406-408

Table 2

Power of the resistive wall heating calculated for the 1.5 m in-vacuum undulator at ESRF.

	Beam mode	Average current (mA)	Bunch length, σ_t (ps)	Material	Power (W m^{-1})
Magnet sheet gap 5 mm	1/3 filling (300 bunches)	140	15	SUS	28
	16 bunches	90	35	Ni + Cu	4.4
RF finger gap 5 mm	1/3 filling (300 bunches)	140	15	SUS	61
	16 bunches	90	35	Ni + Cu	9.6
				BeCu	2.2
				BeCu	4.8

Liner : conductive Ni-Cu foil



Impedance issues : Liner

0.7mm off axis, 0.4 mm excitation

Some observations of liner degradation

ALS



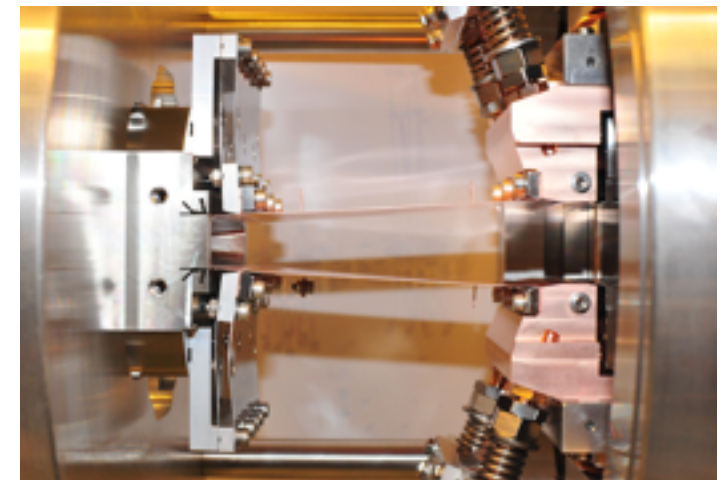
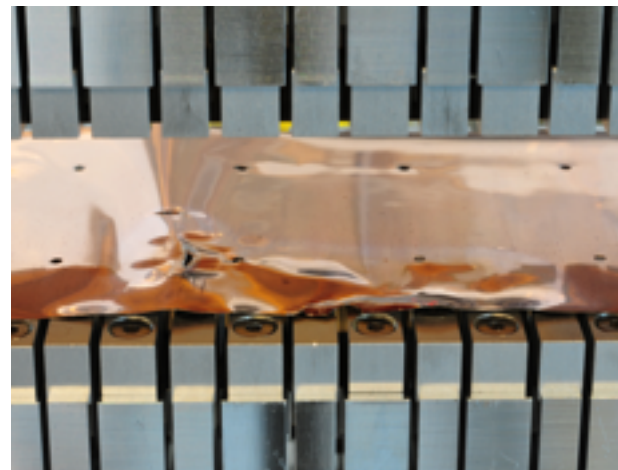
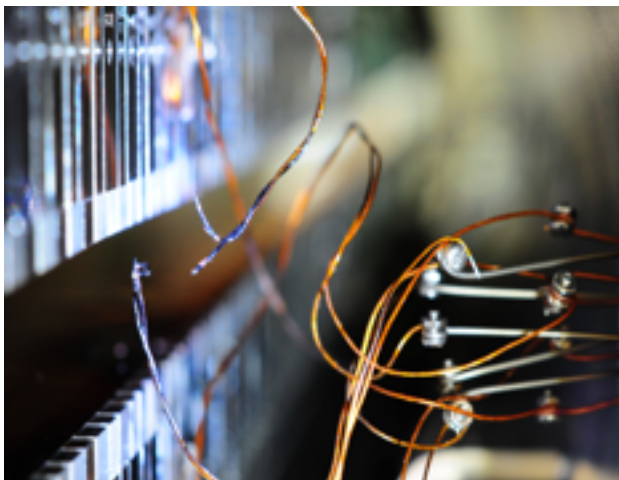
A. Madur et al., PAC 2009; 333

Section	SDC					SDM				
	T		L		Pt	T		L		Pt
Type	RS	CS	RS	CS		RS	CS	RS	CS	
4 /4	1.2	9.8	3	13.1	27.1	2.4	9.8	3.4	13.1	28.7
3 /4	1.2	13.2	3	17.5	34.8	2.4	13.2	3.4	17.5	36.5
hybrid	1.2	13.3	3	18	35.5	2.4	13.3	3.4	18	37.1
8 b 120	0.3	2.6	0.7	21.4	25	0.6	2.6	0.8	21.4	25.4
8 b 80	0.2	2.3	0.5	9.5	12.5	0.4	2.3	0.5	9.5	12.7
1 bunch	0.05	2.57	0.1	4.7	7.4	0.09	2.57	0.14	4.7	7.5

Section	SDL9					SDL13				
	T		L		Pt	T		L		Pt
Type	RS	CS	RS	CS		RS	CS	RS	CS	
4/4	6.4	9.8	3.4	13.1	32.7	17.6	9.8	1	13.1	41.5
3 /4	6.4	13.2	3.4	17.7	40.5	17.6	13.2	1	17.5	49.3
hybrid	6.4	13.3	3.4	18	41.1	17.6	13.3	1	18	49.9
8 b 120	1.5	2.6	0.8	21.4	26.3	4.2	2.6	0.24	21.4	28.5
8 b 80	1	2.3	0.5	9.5	13.3	2.8	2.3	0.16	9.5	14.8
1 bunch	0.26	2.57	0.14	4.7	7.7	0.7	2.57	0.04	4.7	8

SOLEIL : burned thermocouple (U20 n°4), beam heating (U20 n°5)

Solution : liner tensor

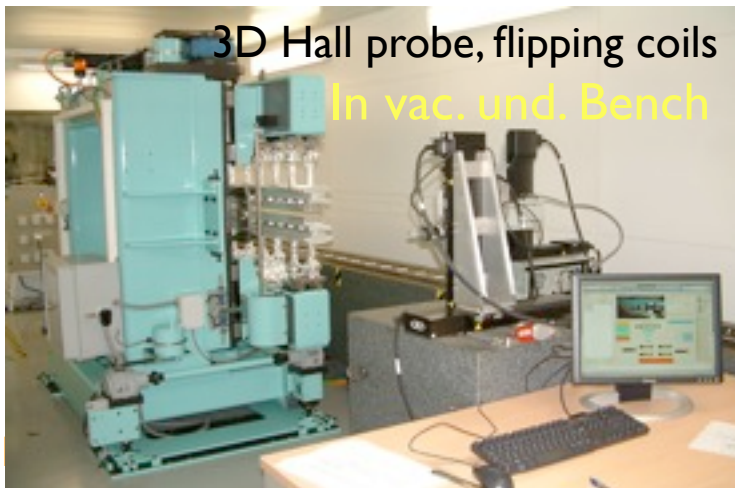
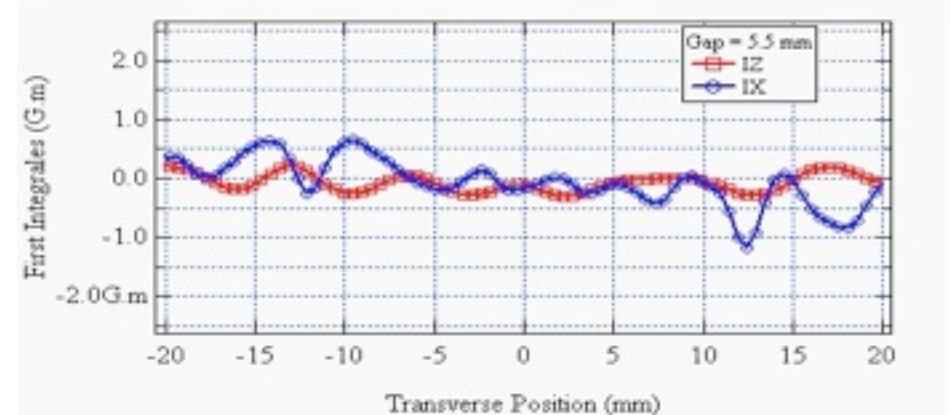
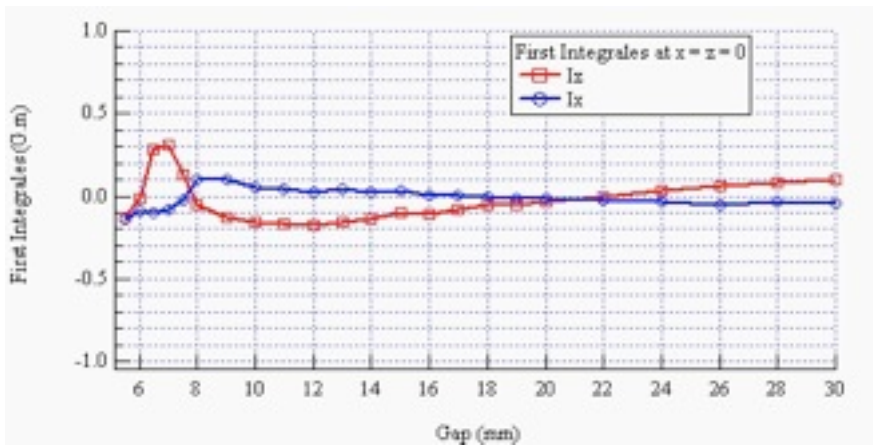
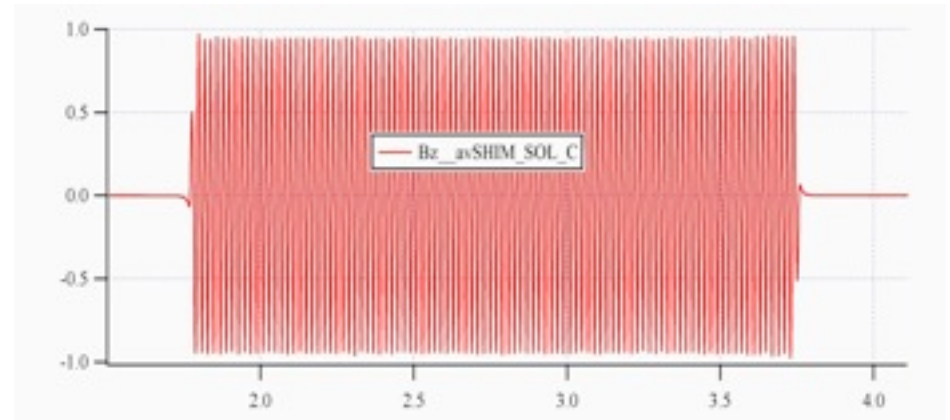


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Magnetic measurements

- without in situ magnetic measurements

- Use of a conventional bench based on the displacement of the magnetic sensor (Hall probe, flopping coil) by an actuation stage of high precision



M.

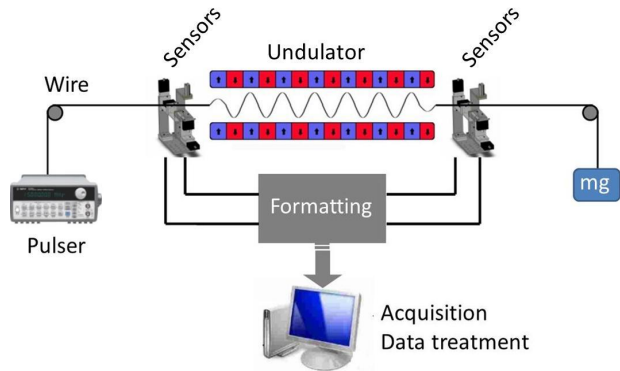
t Source, Thomas Jeffer

nvited

Magnetic measurements

- without in situ magnetic measurements, for no lateral access
- Use of the pulsed wire technique

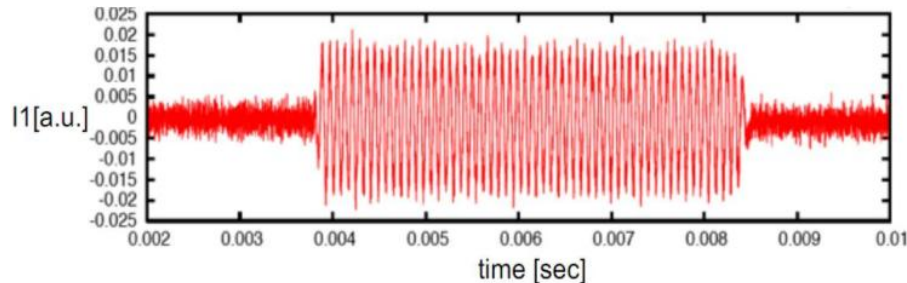
SOLEIL : 1 T, 18 mm period, 2 m long undulator



R.W.Warren, "Limitations on the use of the pulsed-wire field measuring technique", *Nucl. Instr. and Meth.*A272 (1988) 257

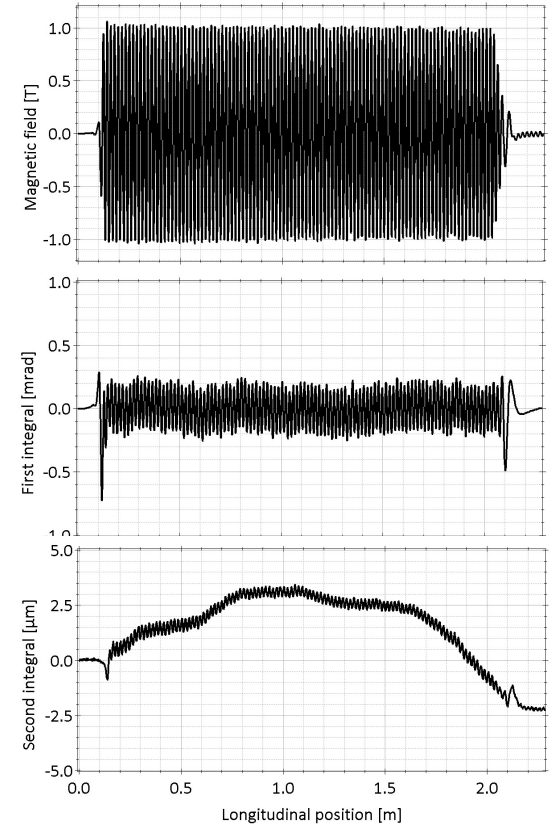
Swiss Light Source : 1 T, 19 mm period,
Signal/Noise = 26.02 dB

The Pulse wire magnetic measurement system, T. Schmidt,
International Magnetic Measurements Workshop 16, 2009



CuBe wire : 125 μm diameter, 10 N, sag : 65 μm
5 A 2 μs bipolar pulse generator developed in house
Photodiode for vibration detection

Pulse 4.5 A $\Delta t = 10 \mu\text{s}$, Signal/Noise : 26.02 dB



Measurements of SOLEIL Insertion Devices using Pulsed Wire Method , M.Valléau, C. Benabderrahmane, M.-E. Couprie, O. Marcouillé, F. Marteau, J.Vétérán , IPAC2011, San Sebastián, Spain, 3242-3244

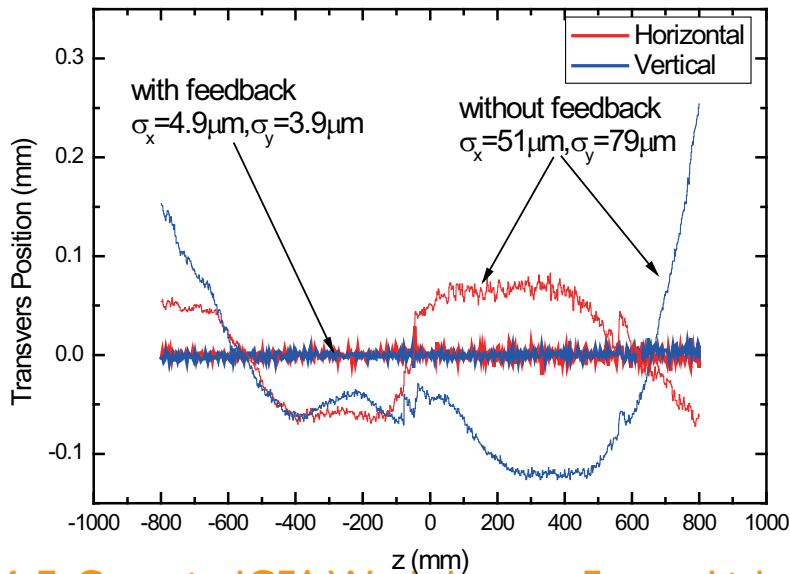
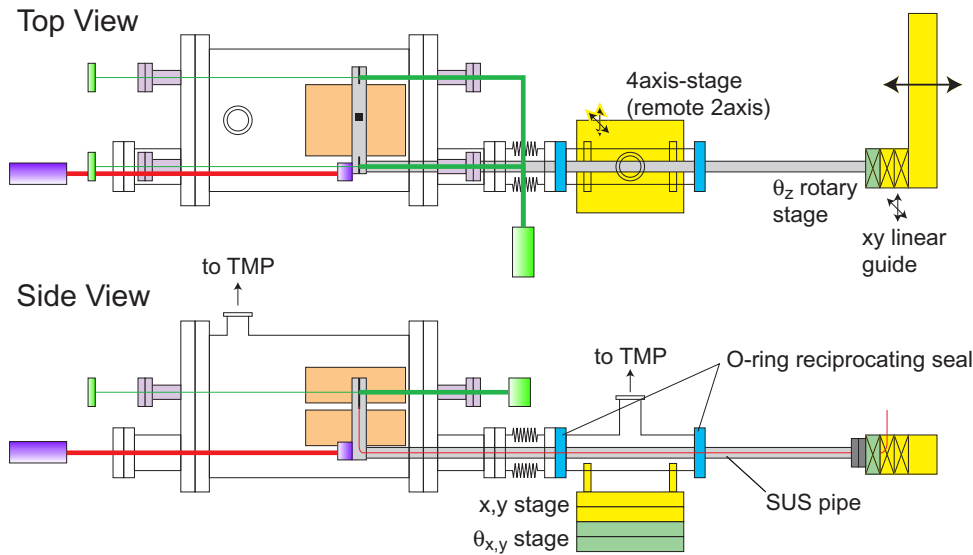


M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc.

Magnetic measurements

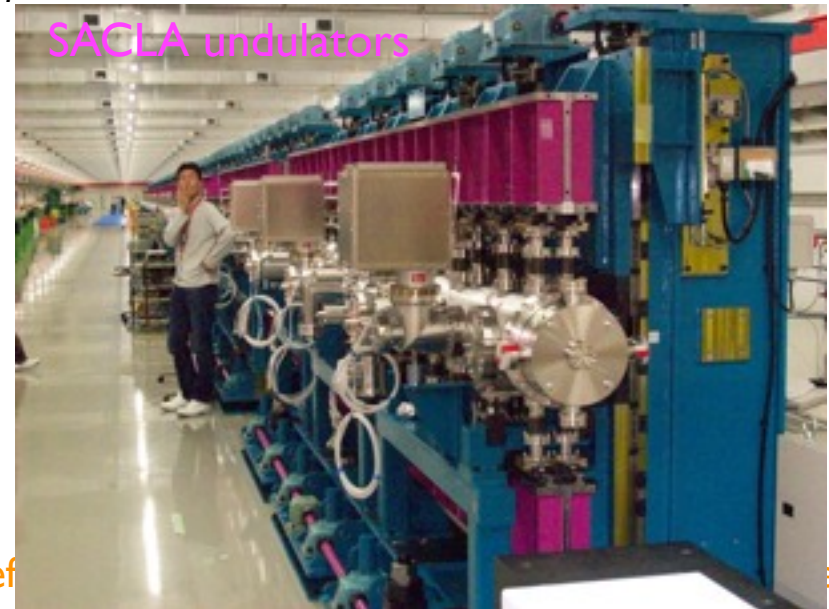
- in situ magnetic measurements

ex : SAFALI (Self aligned field analyzer with laser instrumentation)



T. Tanaka et al, FEL 2007, Novosibirsk, 468;
 T. Tanaka et al. FEL 2008, Gyeongju, 371;
 T. Tanaka, et al., Phys. Rev. Spec. Topics 12, 120702 (2009)

T. Tanabe, et al., Design concept for a modular in vacuum probe mapper for use with CPMU convertible in vacuum undulators of varying magnetic length, PAC 2011, 2534

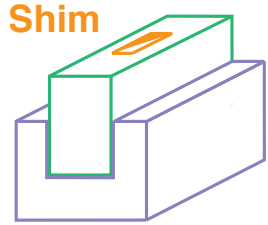


M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson

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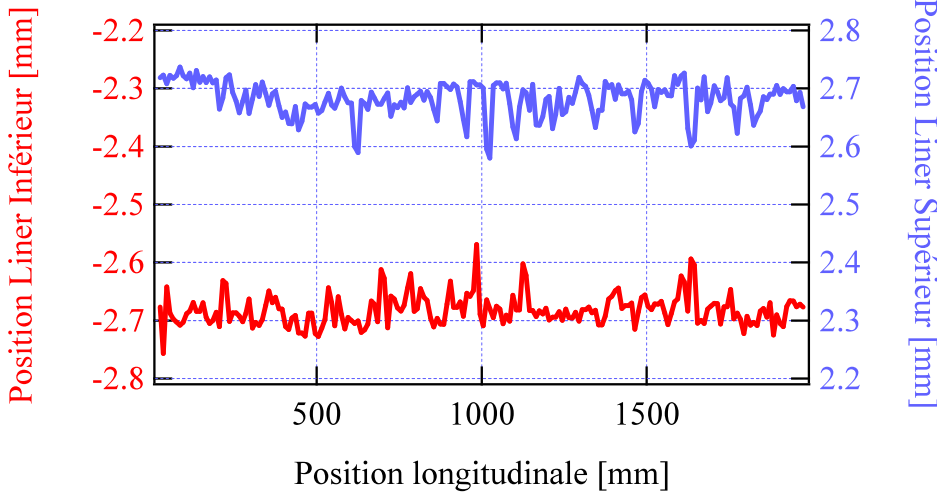
Magnetic corrections

Shimming



Change of the undulator inner gap

ex : 5.5 mm => 5.15 mm

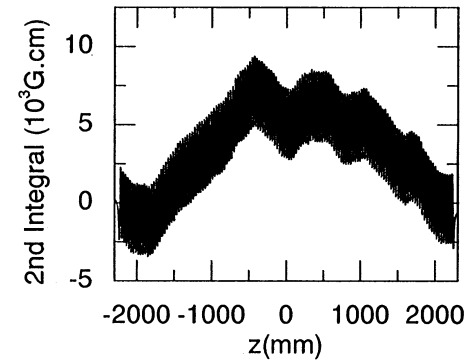
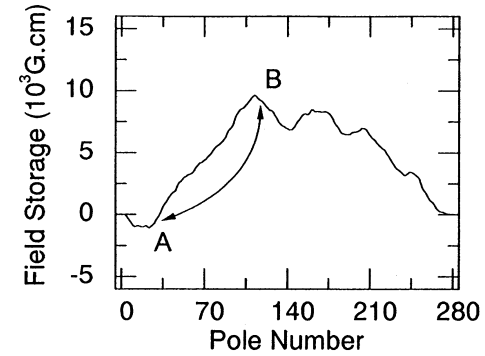
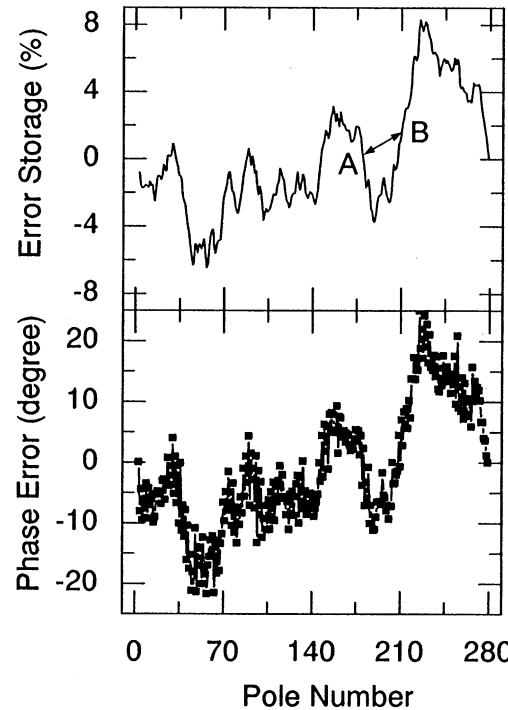


In Situ Sorting, Swapping

exchange (phase error), rotation (multiple components)

$$I_{1n} = \int_{z_n}^{z_{n+1}} B(z) dz, \quad ES_n = \sum_{m=1}^n i_m, \\ z_n = -L/2 + n\lambda_u/2, \quad i_n = \frac{|I_{1n}| - \langle I \rangle}{\langle I \rangle}$$

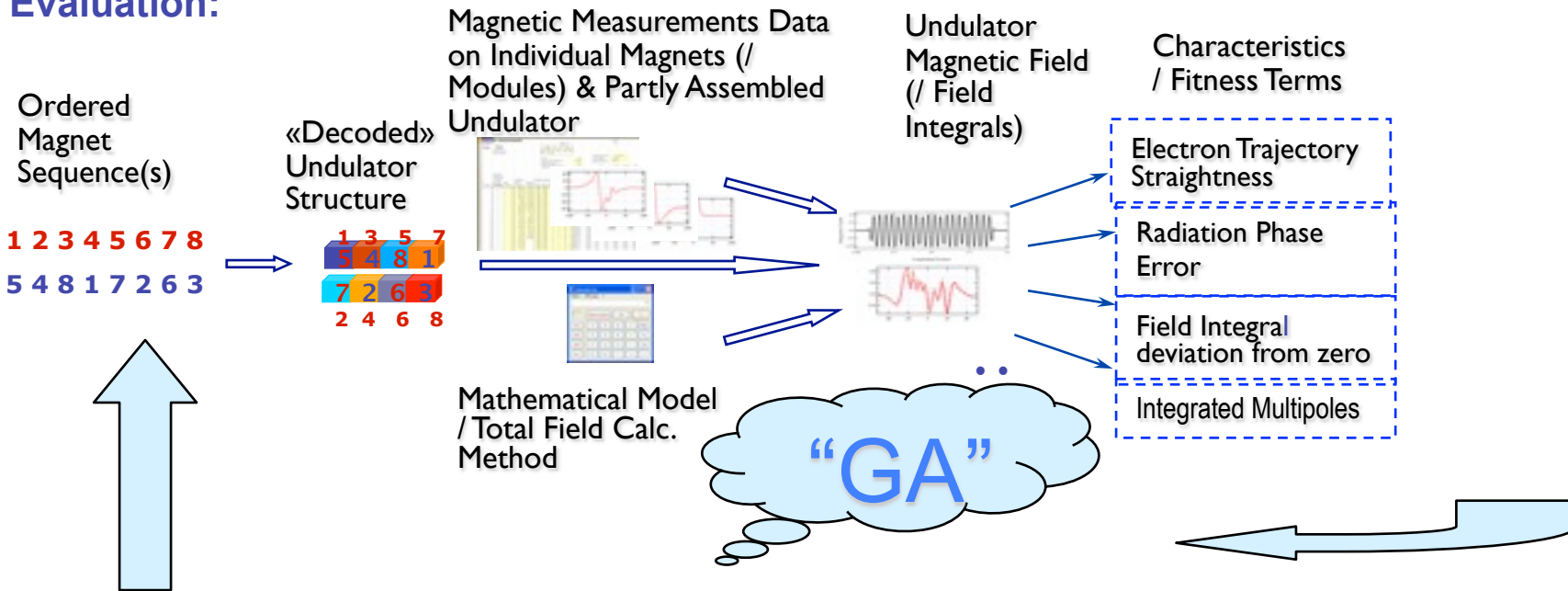
$$FS_n = \sum_{m=1}^n f_m, \quad f_n = I_{1n} - (-1)^n \langle I \rangle$$



T. Tanaka et al, Undulator field correction by in situ sorting, NIMA 465 (2001) 600
ex : phase error 16° to 2.2°

Genetic algorithm based ID Builder

Evaluation:



Variation Operators for Permutations:

Mutation : - e.g. swap items (magnets) at two randomly chosen positions - [5 4 8 1 7 2 6 3] \rightleftarrows

Crossover : - e.g. «order I» -
 [1 2 3 4 5 6 7 8]
 [3 5 6 8 1 2 7 4] \rightleftarrows [??? 4 5 6 7 ?] \rightleftarrows

Advantages : object function, arbitrary search space, search from ap population, mutation and cross-over => global optimum, multi-modal/multi-objet

Efficient Computation of Coherent Synchrotron Radiation taking into account 6D Phase space distribution of emitting electrons, O. Chubar, M. E. Couprie, International Conference on Synchrotron Radiation Instrumentation Daegu (KO) 28 May-2 June 2006, AIP Conference Proceedings 2007, 879, 259-362

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Towards short period high field in vacuum undulators

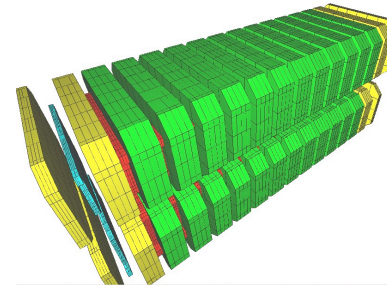
- **Configuration** : Pure Permanent magnet (magnet configuration) to Hybrid technology

K. Halbach, Jour. Physics, 44 (1983) 211

- **Magnet and poles choices**

SmCo magnets => NdFeB magnets

Vanadium Permendur poles => Dysprosium poles



Proposed alternative to superconducting undulators : cryogenic undulators

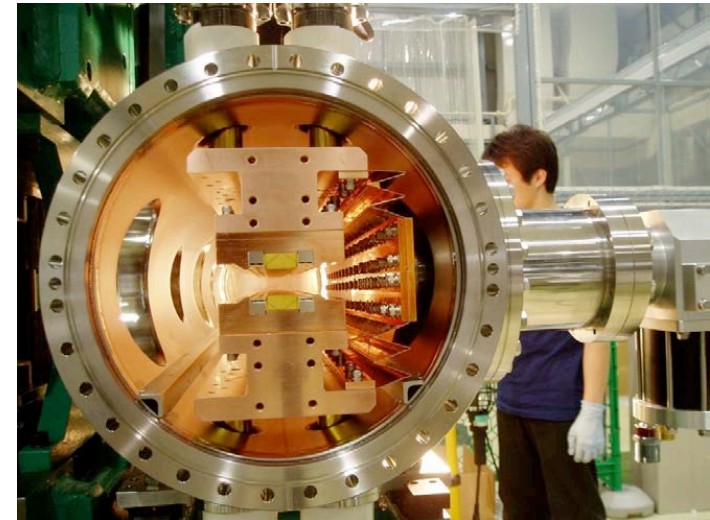
RADIA design

- increase of remanent field and coercivity at low temperature
- operation at liquid nitrogen temperature => manageable heat budget
- easy operation on synchrotron light sources

T. Hara, T. Tanaka, H. Kitamura, T. Bizen, X. Maréchal, T. Seike, T. Kohda, Y. Matsuura, Phys. Rev. Spc. Topics 7, 050702 (2004)

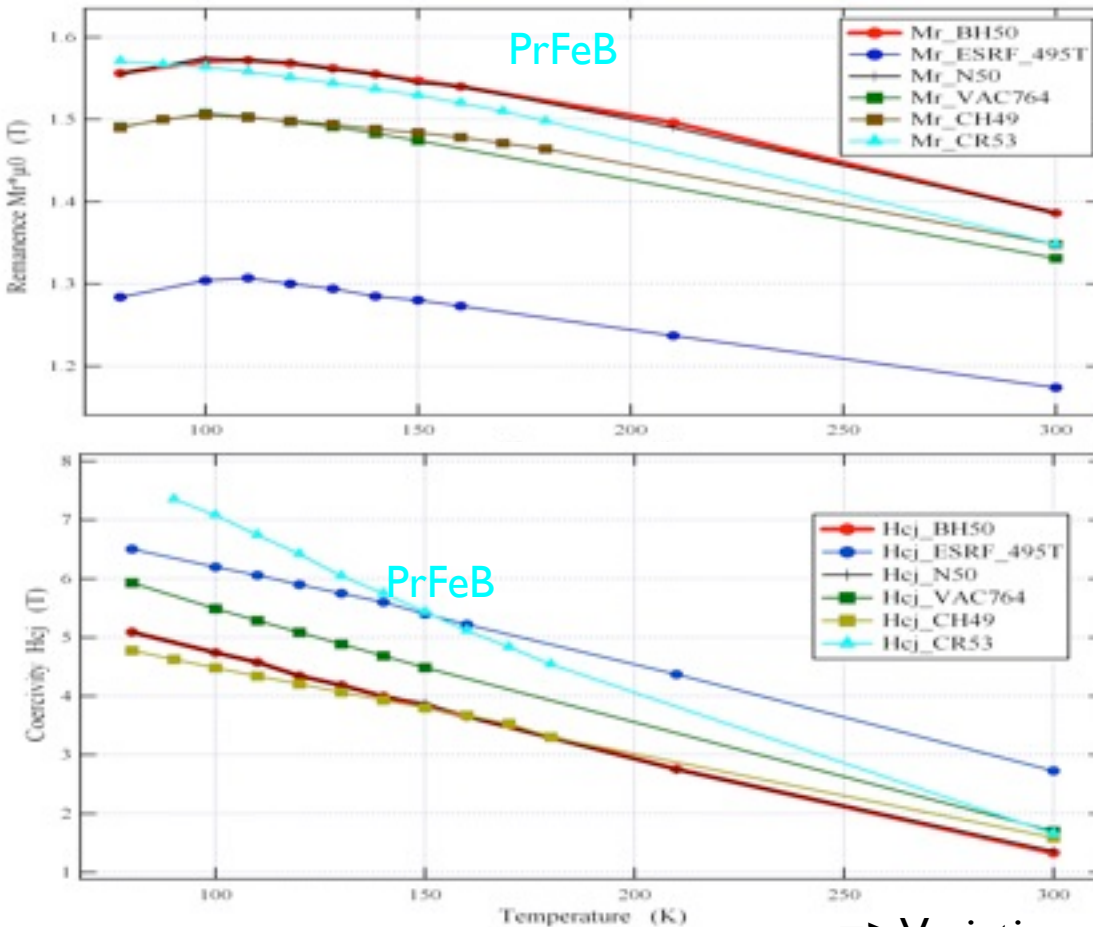
Cryogenic undulator with high Tc superconductors

T. Tanaka et al. PRSTAB 7, 090794 (2004)



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Magnetic characterisation on sample magnets



=> Variation of the susceptibility vs T

M. Sagawa et al. *J. Magn. Magn. Mater.* 70, 316 (1987)

T. Hara et al. *APAC2004*, Gyeongju, Korea, 216

C. Benabderrahmane et al. *NIMA* 669 (2012) 1-6

K. Uestuener et al., *Sintered (Pt,Nd)FeB permanent magnets with $(BH)_{max}$ of 520 kJ/m³ at 85 K for cryogenic applications*, 20th Workshop on Rare Earth Permanent Magnets 2008, Crete

Spin Transition Reorientation

NdFeB strong Magneto-Crystalline Anisotropy (MCA) => orientation along [001]

Magneto-crystalline orientation given by the energy : $E(T) = K_1 \sin^2(\theta) + K_2 \sin^4(\theta)$, θ angle between the magnetisation and [001]

at room temperature : magnetisation // c

Fe MCA independant of T, Nd : K_1 // [001]

dominant at room T and K_2 // [110] at low T

Characteristics of different magnet samples at 20 °C: B_r remanence, H_{cj} coercivity. VAC stands for Vacuumschmelze.

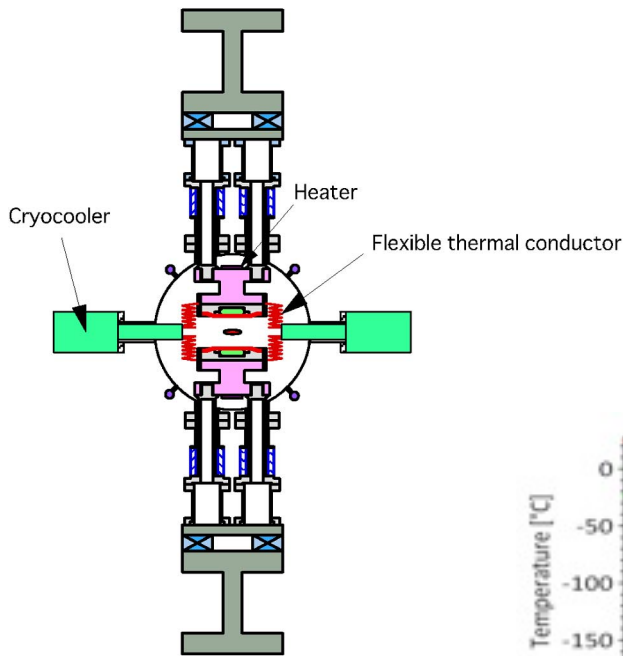
Characteristics	CR53	BH50	CH49	VAC764	495T	N50
Company	Hitach-Neomax			VAC	Neorem	Atlas-Yunshen
Type of magnet	Pr ₂ Fe ₁₄ B	Nd ₂ Fe ₁₄ B	Nd ₂ Fe ₁₄ B	Nd ₂ Fe ₁₄ B	Nd ₂ Fe ₁₄ B	Nd ₂ Fe ₁₄ B
Remanence B_r (T)	1.35	1.40	1.39	1.37	1.18	1.40
Coercivity H_{cj} (T)	1.65	1.39	1.63	1.63	2.81	1.38
Temp. Coef. ΔB_r (%/°C)	0.11	0.11	0.11	0.12	0.11	0.11
Temp. Coef. ΔH_{cj} (%/°C)	0.58	0.58	0.58	0.70	0.58	0.60
Dimensions (mm ³)	4 × 4 × 4	4 × 4 × 4	4 × 4 × 4	4 × 4 × 4	4 × 4 × 4	4 × 4 × 4

D. Givord et al. *Solid State Comm.* 51 (1984) 857

L. M. Garcia et al. *Phys. Rev. Lett.* 85 (2) 429

CPMU cooling strategy

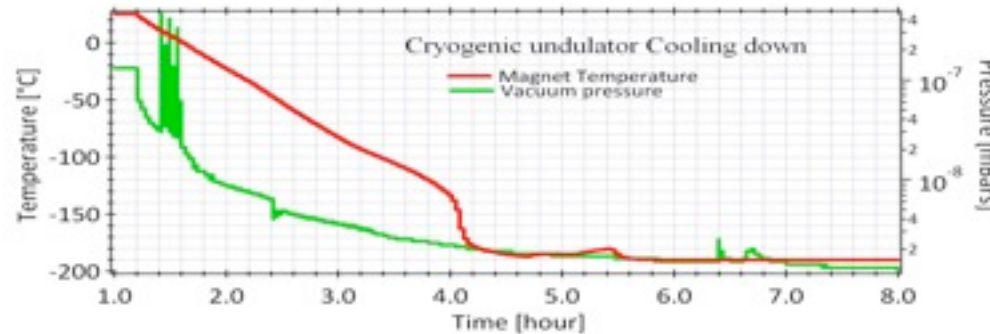
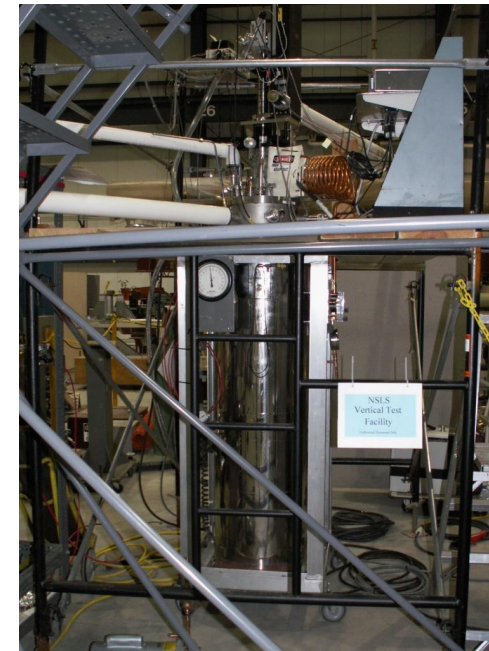
Cryocoolers



Cryo Cooler:
 Power 2000 W
 (<300 W), Liquid LN2, Pump : 30 to 90 Hz (40 Hz), Flow : 1 to 30 l/mn (5 l/mn)



Cooling to He temperature at BNL



SPring-8

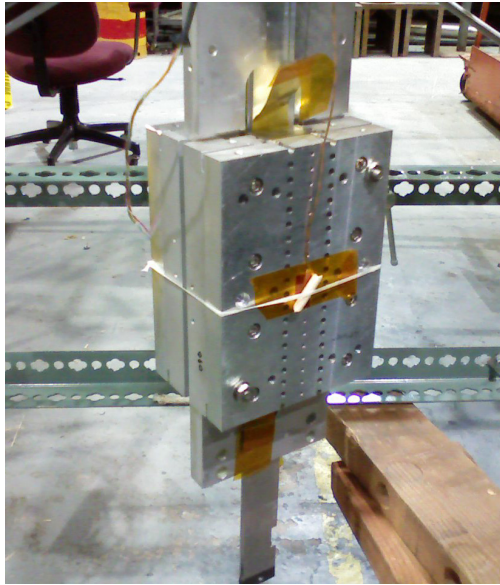
T. Hara et al. Phys. Rev. Spc. Topics 7, 050702 (2004)

SOLEIL

C. Benabderrahmane et al 7, 050702 (2004)

Mini Cryogenic undulators

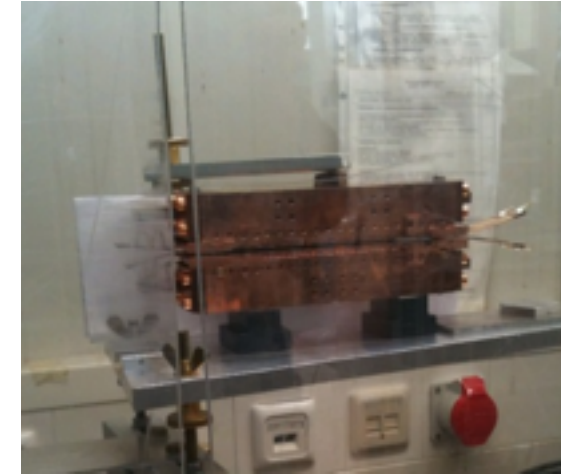
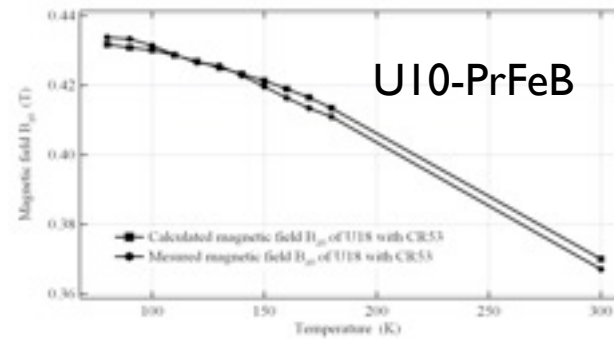
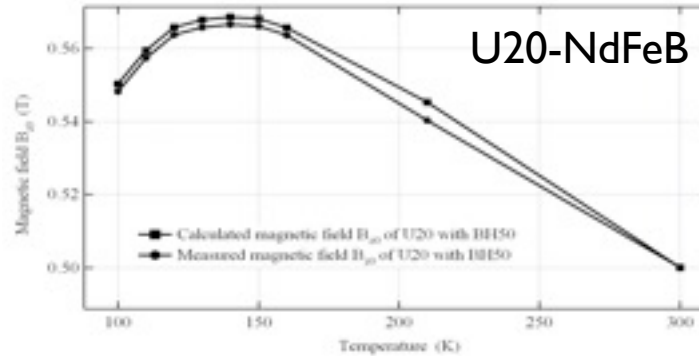
at NSLS-II



at SOLEIL

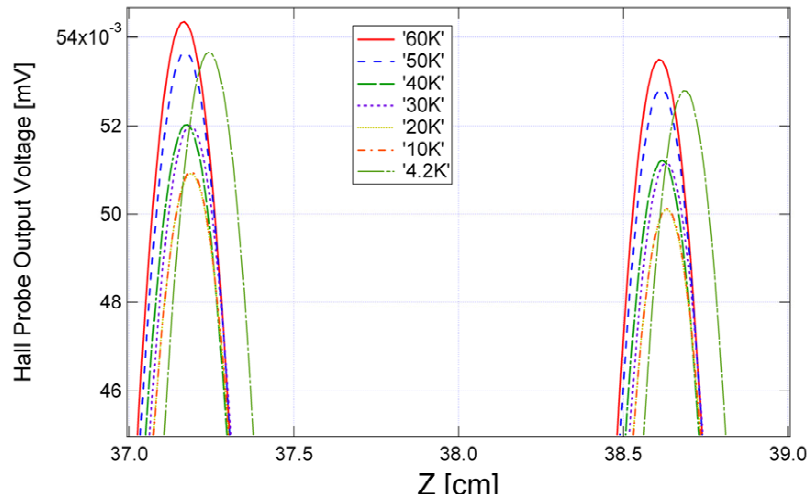
at BESSY

Validation of magnetic model at low temperature

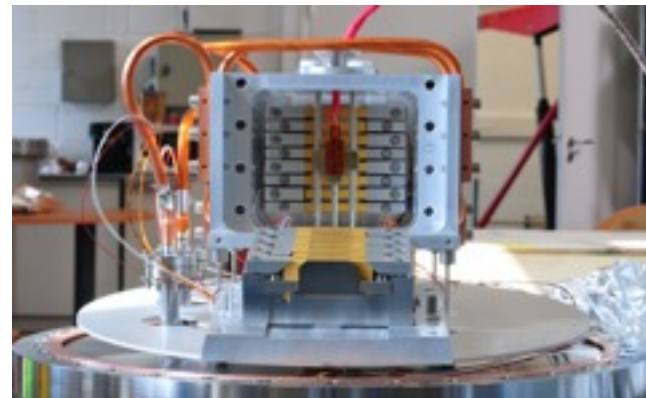


J. Bahrtdt et al. IPAC10, 3111

fixed gap=2.5 mm



T.Tanabe, et al., *AIP Conference Proceedings*, Vol. 1234, p.29 (2010). 4.85 mm gap



Nd₂Fe₁₄B and Pr₂Fe₁₄B magnets characterisation and modelling for cryogenic permanent magnet undulator applications, C. Benabderrahmane, P. Berteaud, M. Valléau, C. Kitegi, K. tavakoli, N. Béchu, A. Mary, J. M. Filhol, M. E. Couprie, *Nucl. Instrum. Methods A* 669 (2012) 1-6

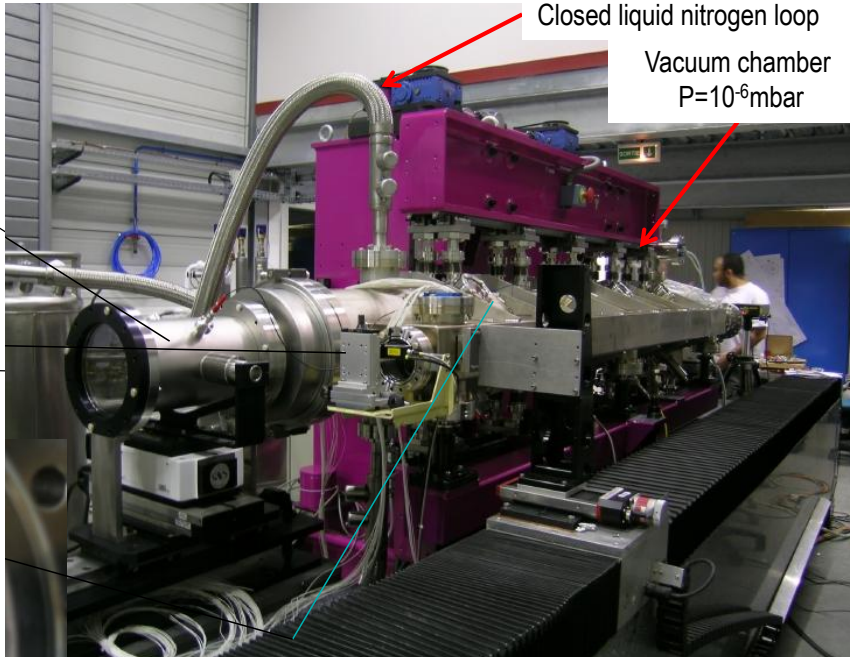
M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

In vacuum low temperature measurements

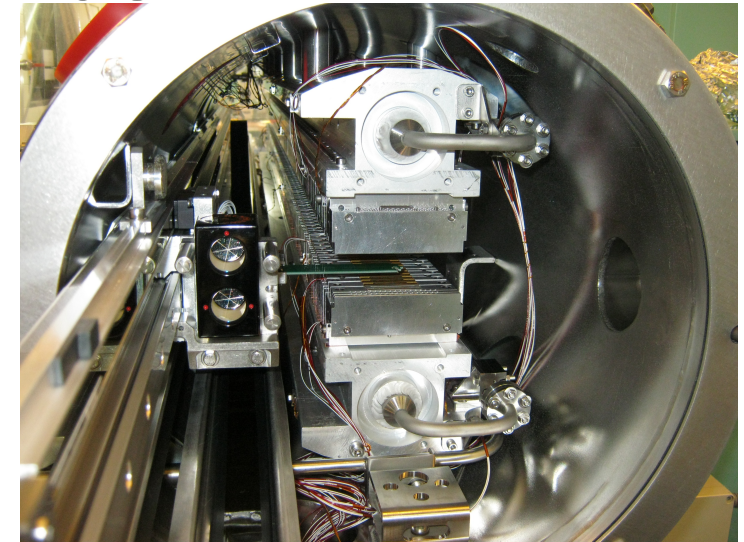
ESRF

Stretched wire
Field integral measurement

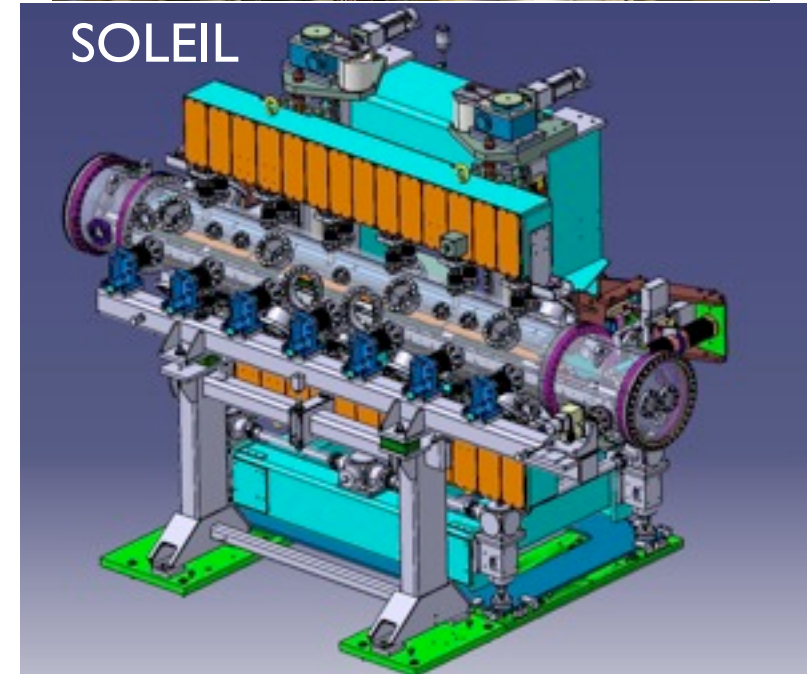
Laser



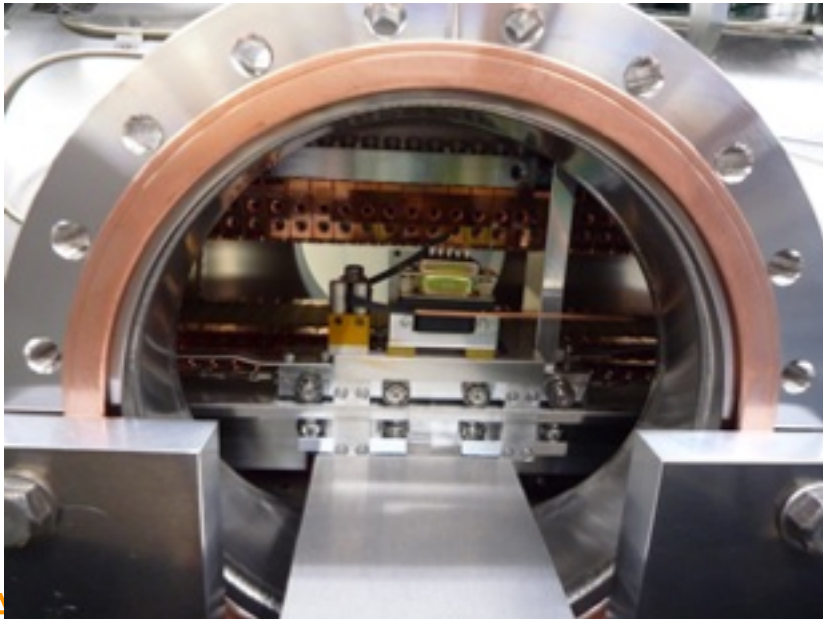
SOLEIL



SOLEIL



SPring-8



Mechanical changes at low temperature

- **Gap opening** due to thermal contraction of the supporting rods to be compensated

Measurement :

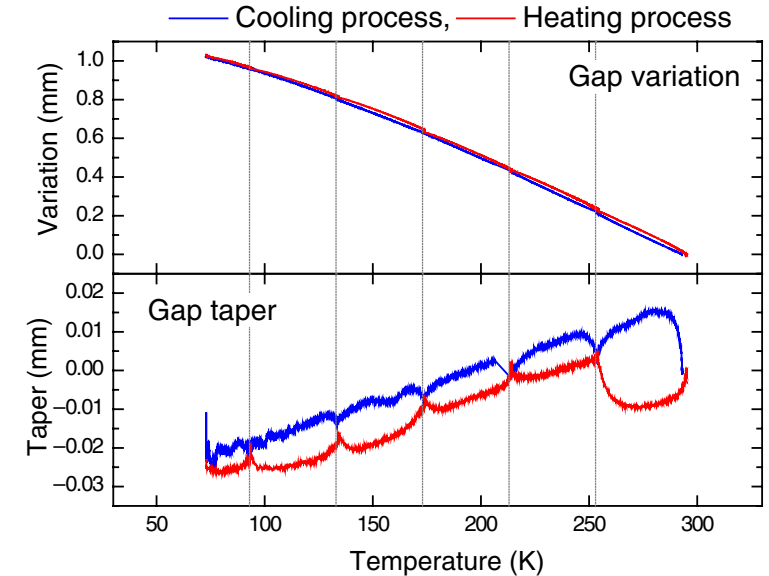
Capacitance type displacement monitors

(Nantex Corp.) SPring-8

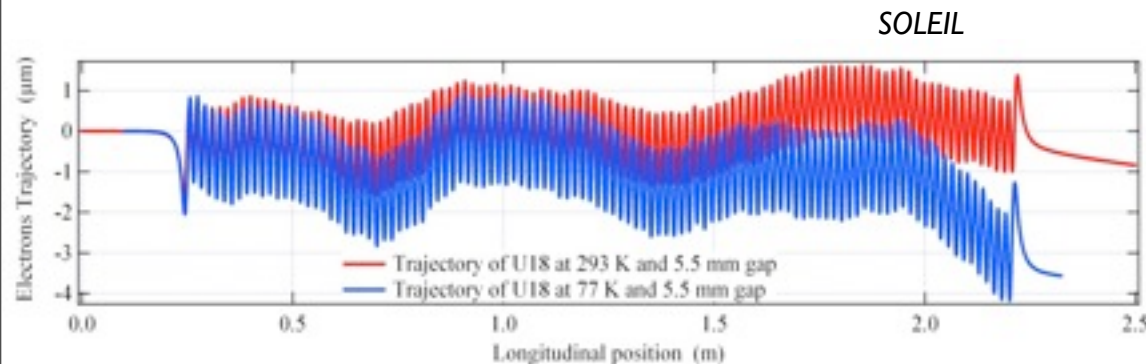
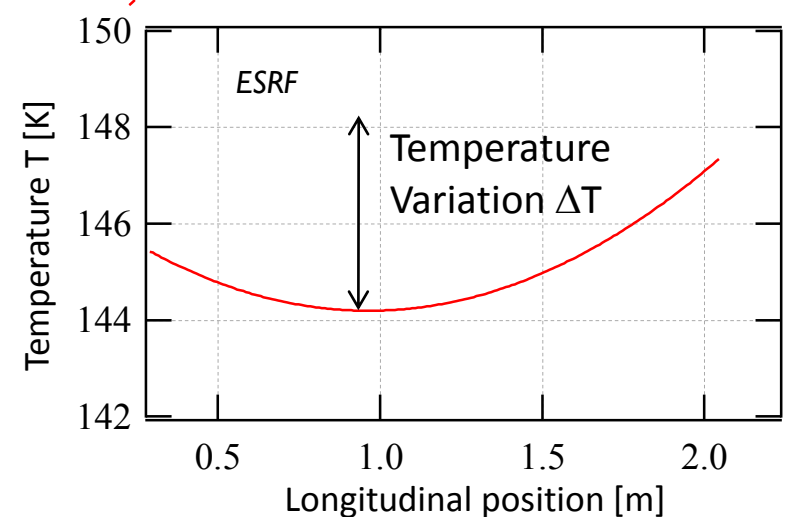
Wire resistivity : ESRF, SOLEIL

- **Period reduction** due to girder contraction, ex at SOLEIL 9 mm over 2 m, i.E. $38 \mu\text{m} / \text{period}$)

- **Phase error** correction via rod shimming

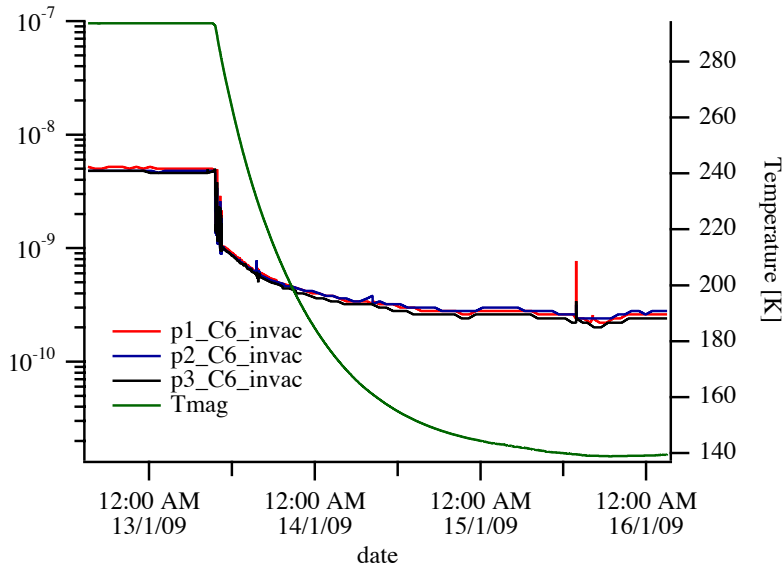
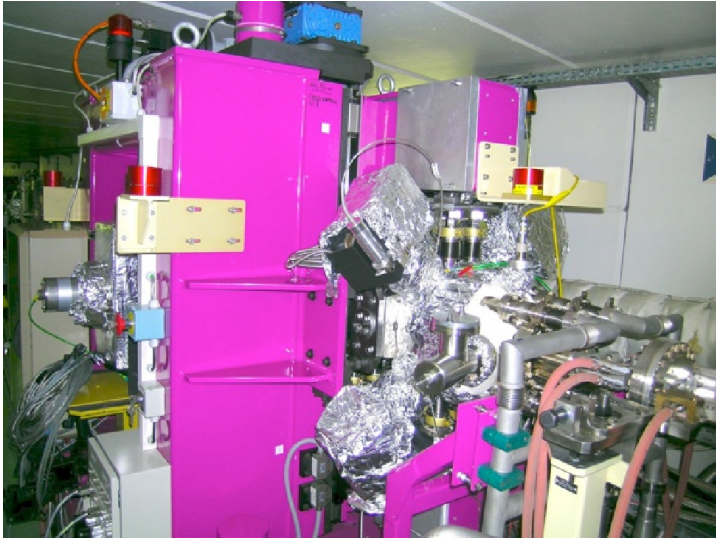


T.Tanaka et al., New Journal of Physics, Development of cryogenic permanent magnet undulators operating around liquid nitrogen temperature. New Jour. Physics 6. 2011. 287



Cryogenic undulators on operation

ESRF



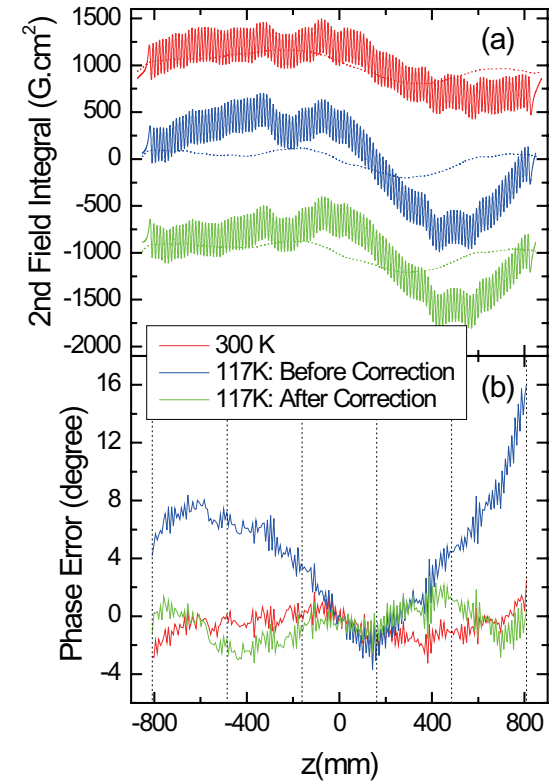
J. Chavanne et al., First operational experience with a cryogenic permanent magnet undulator at the ESRF, PAC09, 2414

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas

SLS

T. Tanaka et al., in situ magnetic correction for cryogenic undulators, IPAC 2010, 3147

Tanaka, et al., Phys. Rev. Spec. Topics 12, 120702 (2009)



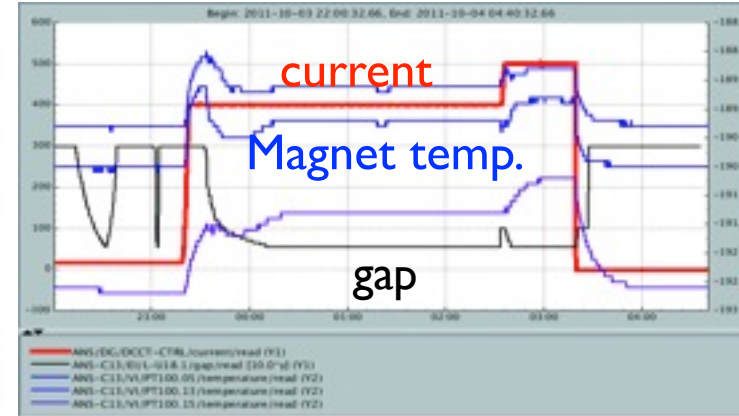
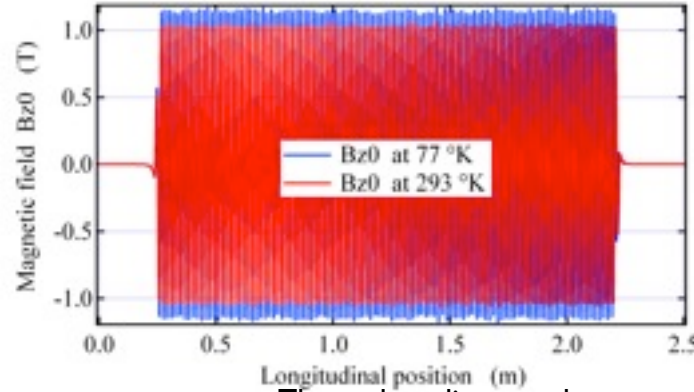
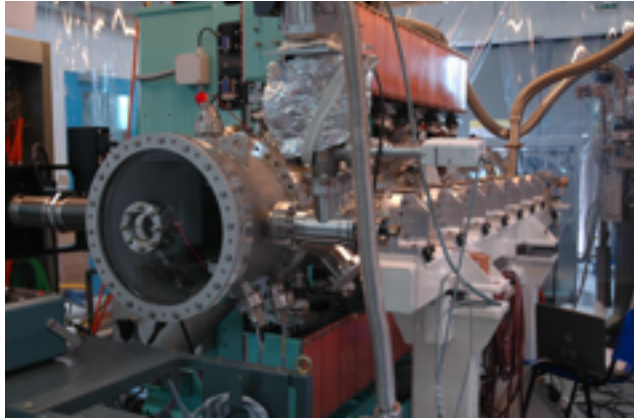
2012, Invited

Cryogenic undulators on operation

SOLEIL Cryo UI8 PrFeB

operation at 77 K, Non baked, $B = 1.16 \text{ T}$ @ 5.5 mm gap

C. Benabderrahmane et al. IPAC 2011



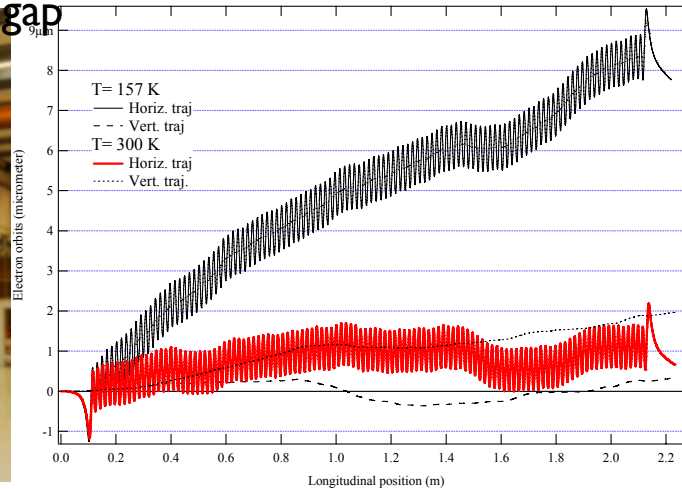
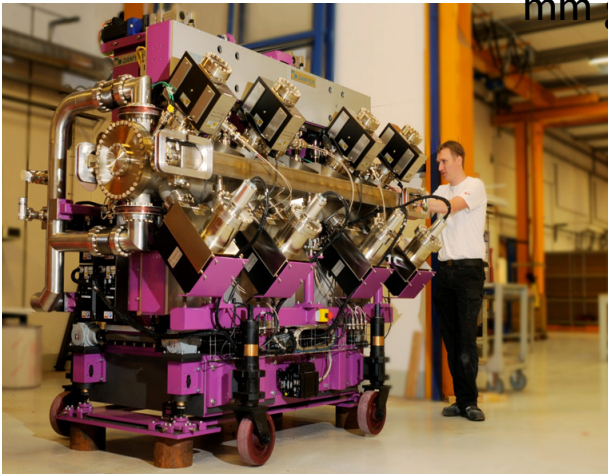
Thermal gradient on the magnetic system $< 1.2 \text{ K/m}$

Total temperature variation due to electron beam (500 mA) and gap variation $< 2.5 \text{ K}$

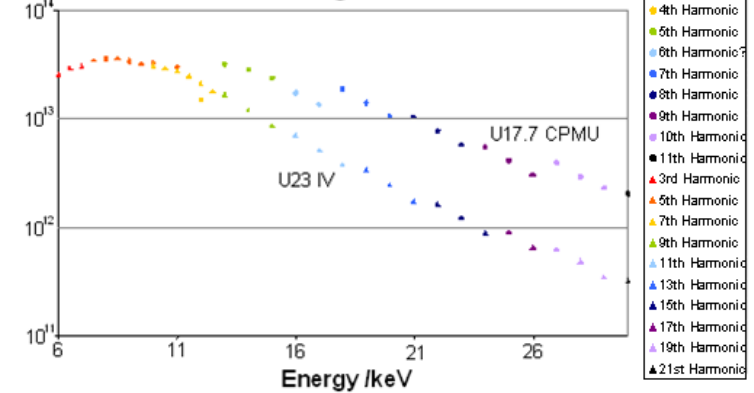
DIAMOND

NdFeB, operation at 157 K, Non baked, $B = 1.04 \text{ T}$ @ 4

mm gap



Flux /s/0.1% b/w @ 150mA Ring current



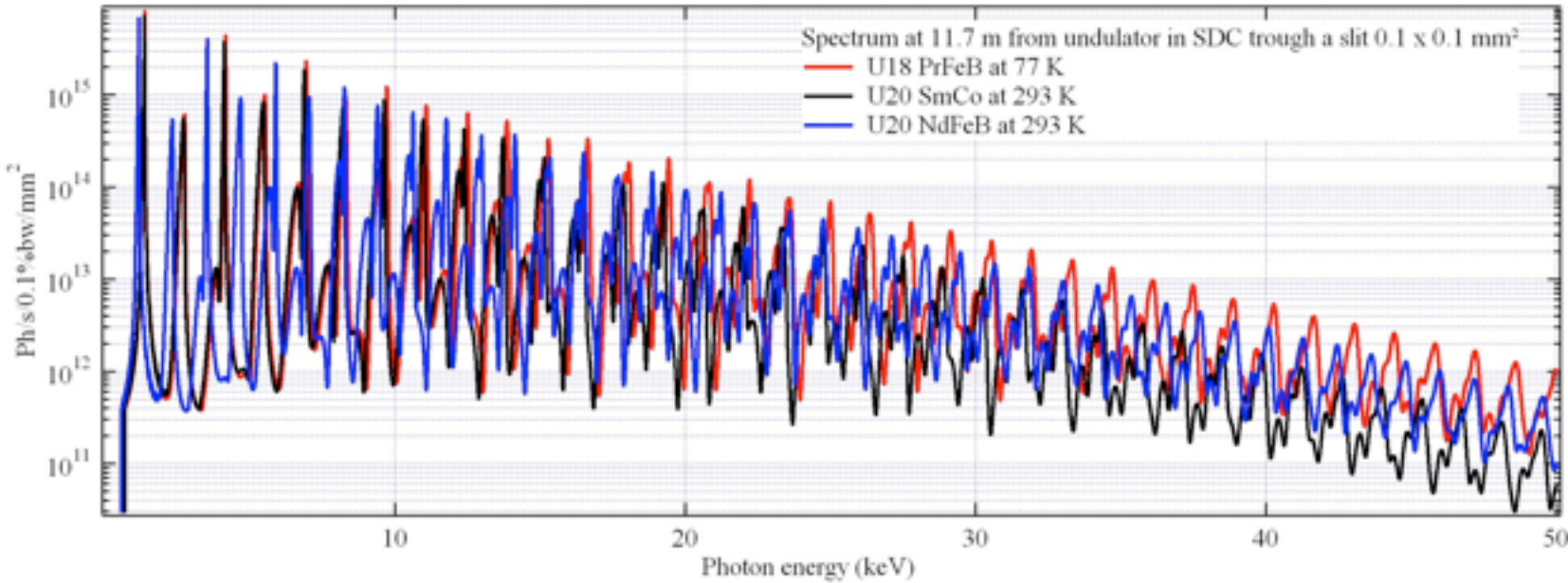
C.W. Ostefeld et al., Cryogenic in vacuum unduator at Danfysik, IPAC2010, 3093

J. Schouten et al, Electron beam heating and operation of the cryogenic undulator and superconducting wigglers at DIAMOND, IPAC 2011, 3323

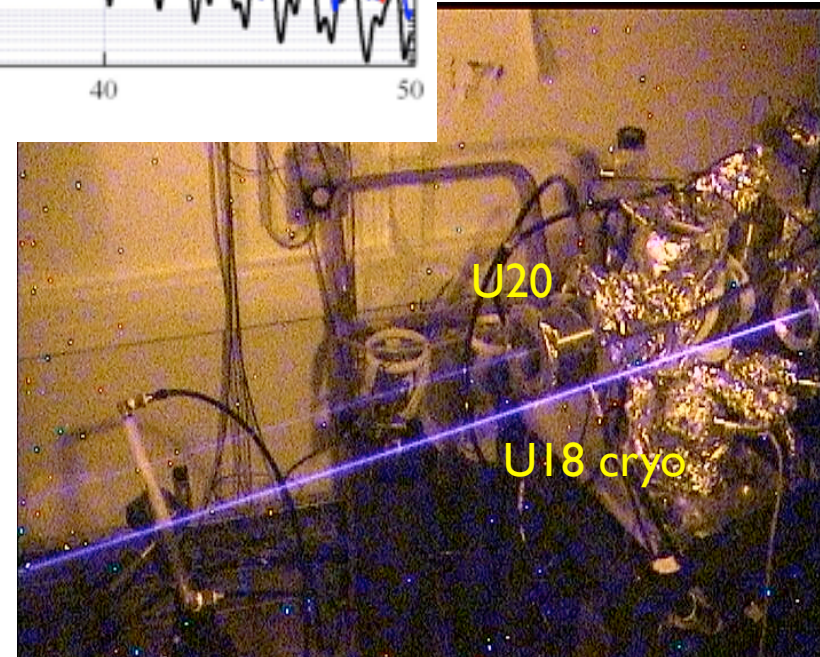
M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Cryogenic undulators radiation

SOLEIL



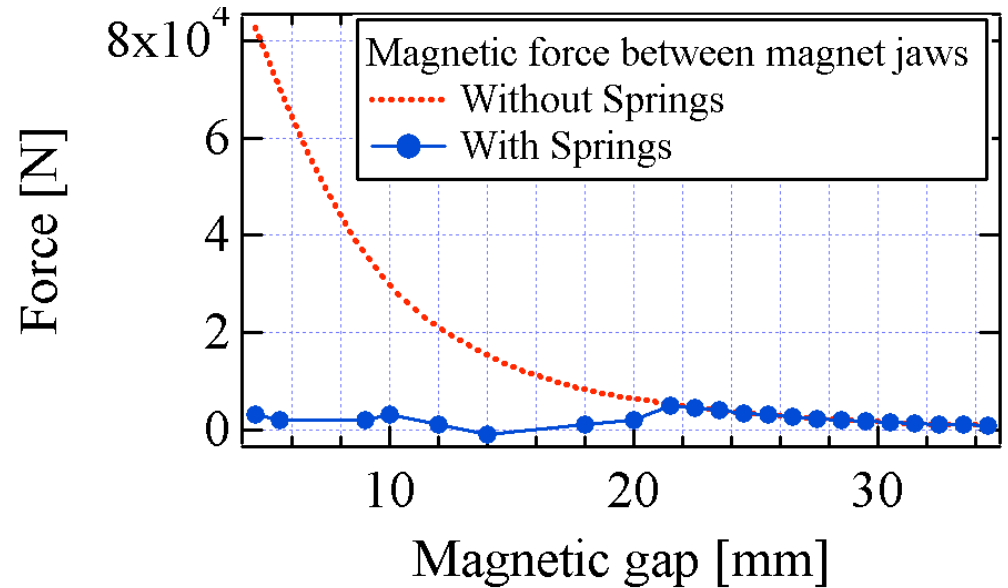
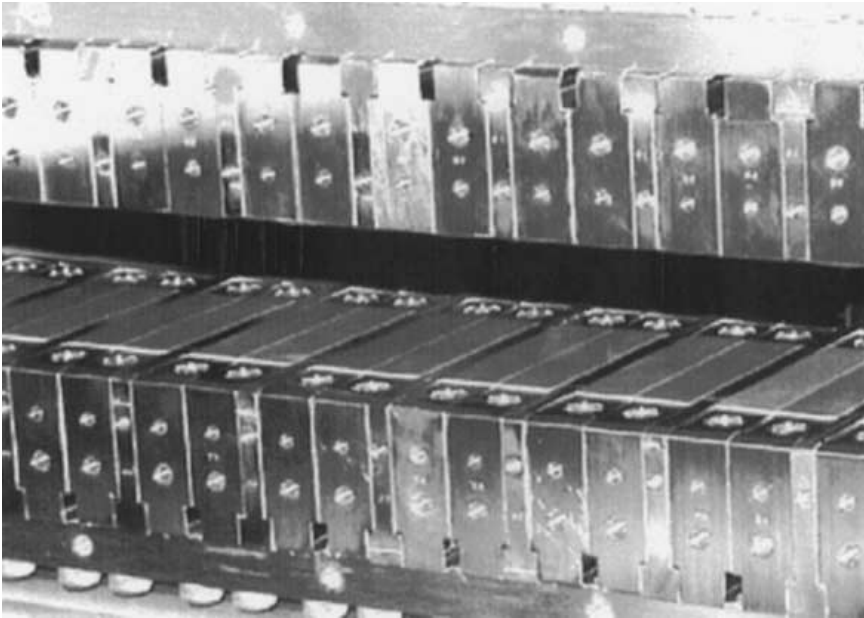
Test RP : 13 décembre 2011



M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

In vacuum wiggler

Choice of an in vacuum wiggler rather than a superconducting wiggler

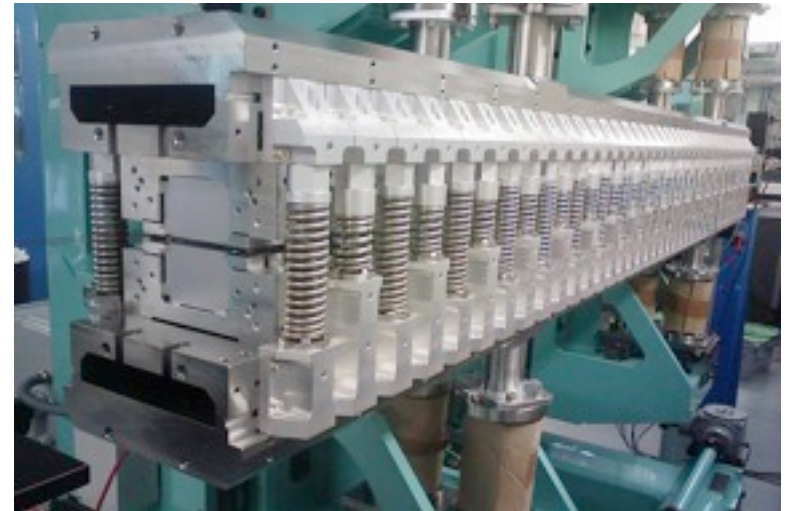


SPring-8 : 1.95T, gap=7 mm, 10x90 mm

X.M. Marechal et al, NIMA 4676-468 (2001) 138-140

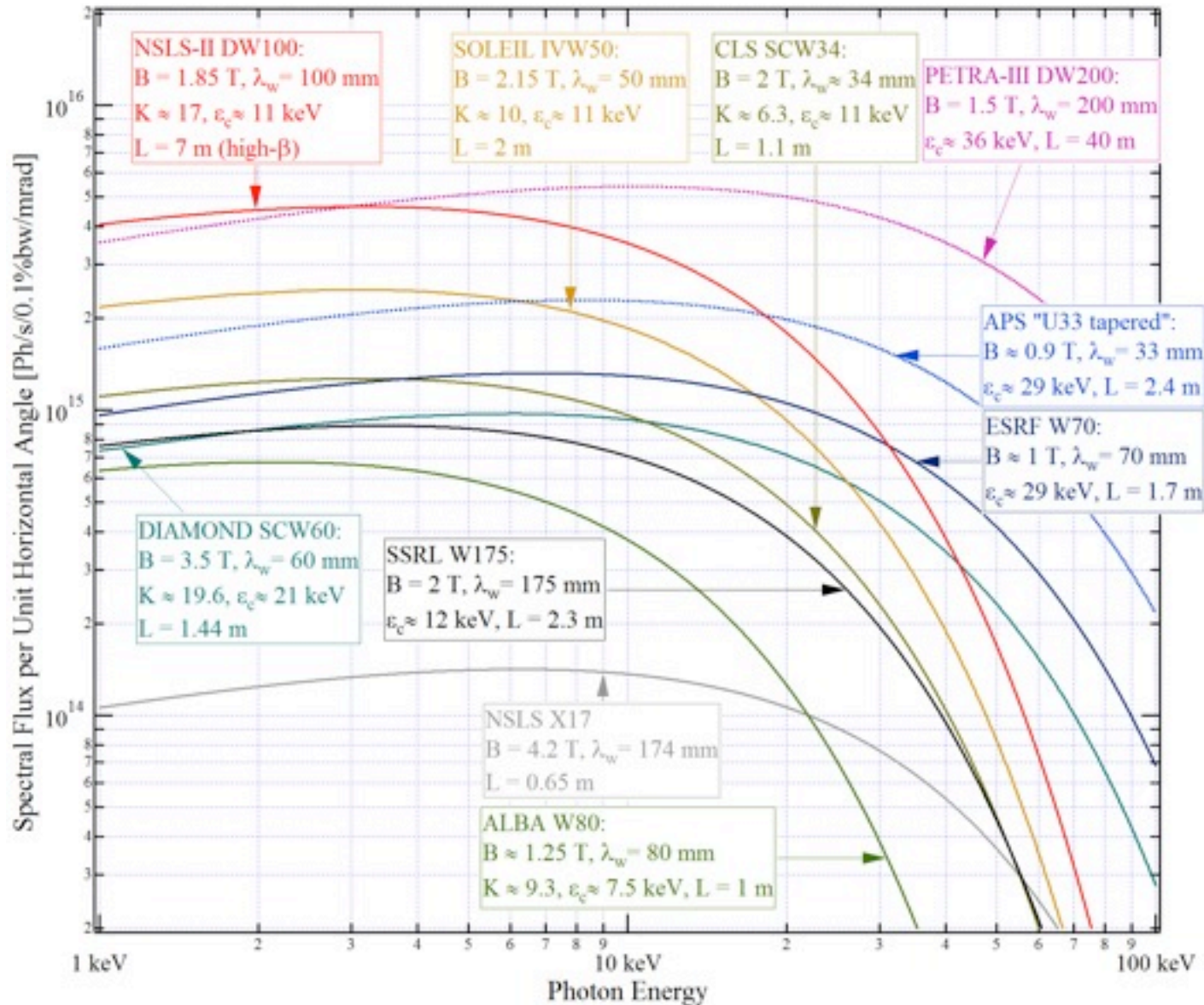
SOLEIL : 2.1T, gap=5.5 mm,
10x150 mm

O. Marcouillé et al., SRI 09



In vacuum wiggler

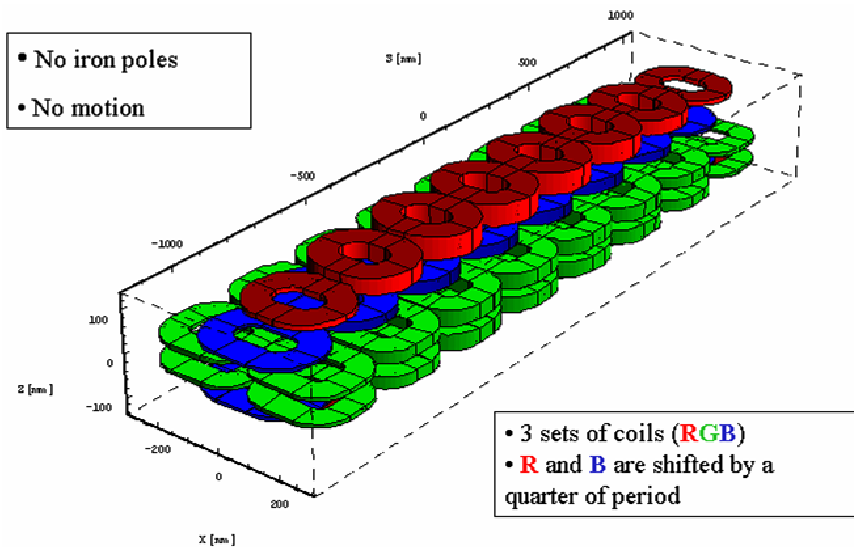
Spectral Flux per Unit Horizontal Angle (Far-Field Estimation)



O. Chubar

Electromagnetic undulators

Ex of the SOLEIL 10 m HU640



Radia code: <http://www.esrf.fr>

$$B_z(s) = B_B \cdot \cos[2\pi s / \lambda_0] + B_R \cdot \sin[2\pi s / \lambda_0] = B_{z0} \cdot \cos[2\pi s / \lambda_0 + f]$$

Fast switching : 1 Hz : 270 ms for switching ± 600 A on PSI, 300 ms flat top for data acquisition

SOLEIL conception- Realisation Danfysik, Magnetic measurements SOLEIL



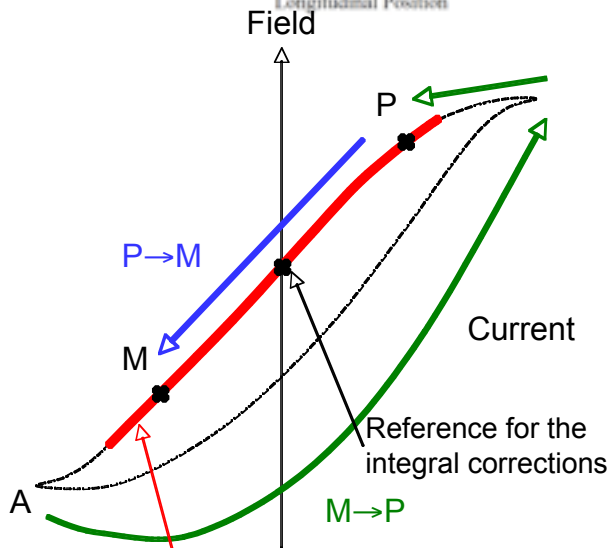
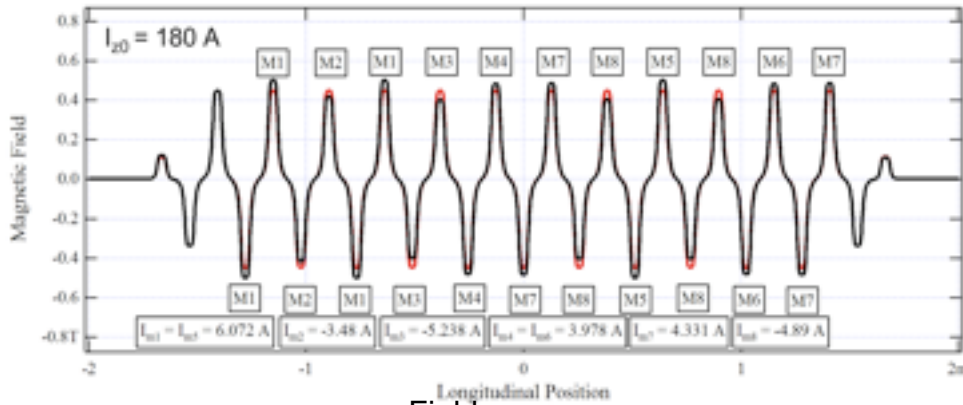
Design, Construction and Magnetic Measurements of the DESIRS Undulator at SOLEIL, O. Marcouillé et al., International Conference on Synchrotron Radiation Instrumentation Daegu (KO) 2006, AIP Conference Proceedings 2007, 879, 396-399

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility, March. 5-9, 2012, Invited

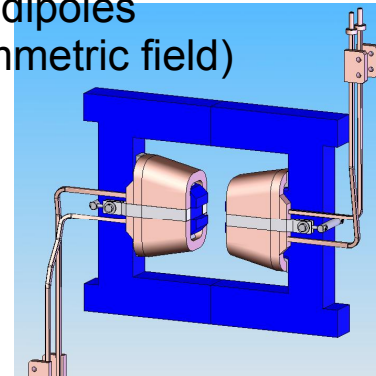
Electromagnetic undulators

Ex of the SOLEIL 526

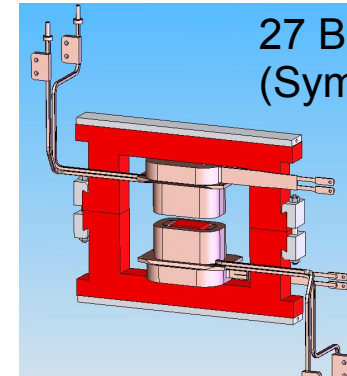
Linear H,V, + Quasi periodic,
Circular
Coll. BINP



28 Bx dipoles
(Asymmetric field)



27 Bz dipoles
(Symmetric field)



Magnetic design and manufacture of elliptical undulators HU256A. Batrakova, F. Briquez, O. Chubar, I. Churkin, M.-E. Couprie, A. Dael, I. Ilyin, Yu. Kolokolnikov, G. Roux, E. Rouvinski, E. Semenov, A. Steshova, M. Valleau, P. Vobly, Nuclear Instruments and Methods in Physics Research A 575 (2007) 29–32

M. E. Couprie, ICFP Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility, March. 5-9, 2012, Invited

Permanent magnets EPU: Crossed undulators

Onuki undulators

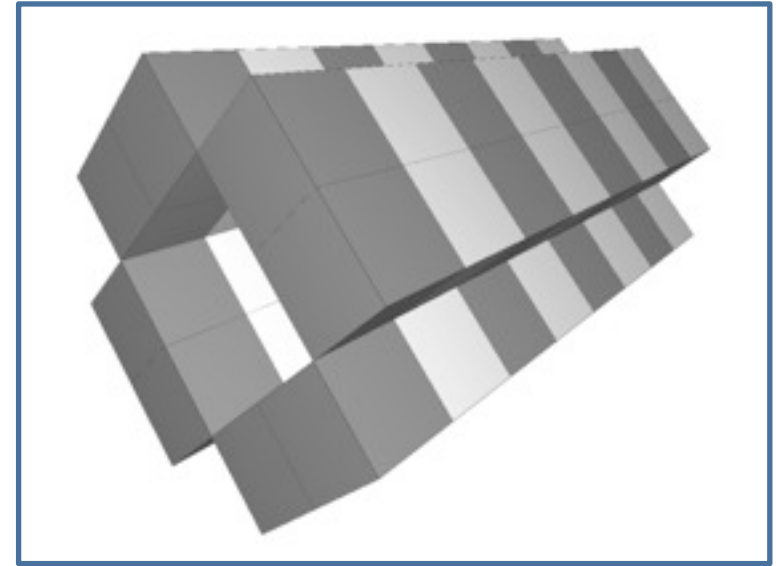
Modes	B_z [T]	B_x [T]
Linear H.	0,4	
Linear V.		0,4
Circular	0,28	

Undulator :

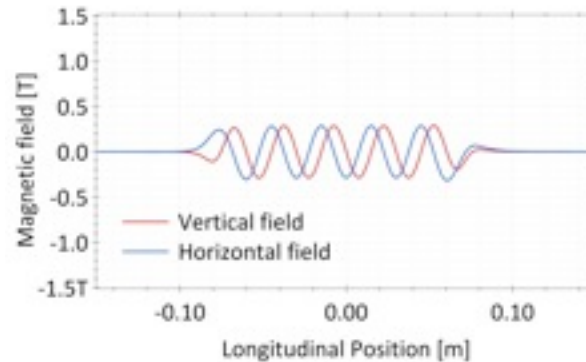
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

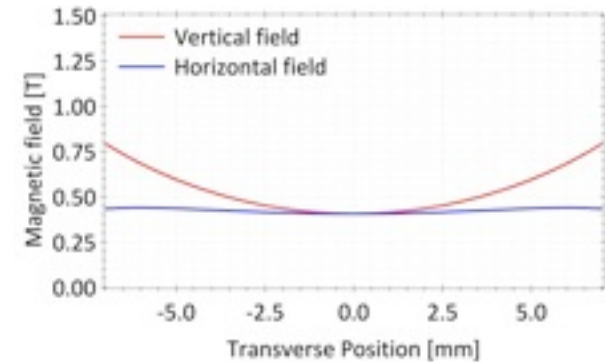
- NdFeB
- Size : 8 x 15,5 mm
- B_r : 1,26 T
- $\Theta_{mag} = 0^\circ$
- $X_{dist} = 1$ mm



- Crossed and overlapped type polarizing undulator



H. & V. field values in circular polarisation.



H. & V field roll-off at minimal gap

M. Moissev et al. *Sov. Phys. J.* 21, 332, 1978
K. J. Kim *NIMA* 219, 426 (1986)

H. Onuki, *Nucl. Instr. Meth.*, A246, 94, (1986)
H. Onuki et al, *Appl. Phys. Lett.*, 52, 173, (1988)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU: HELIOS

Helios undulators

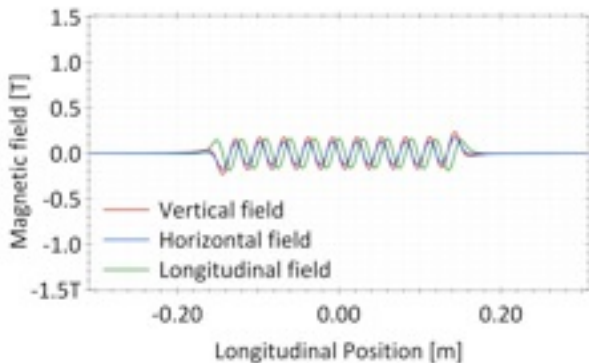
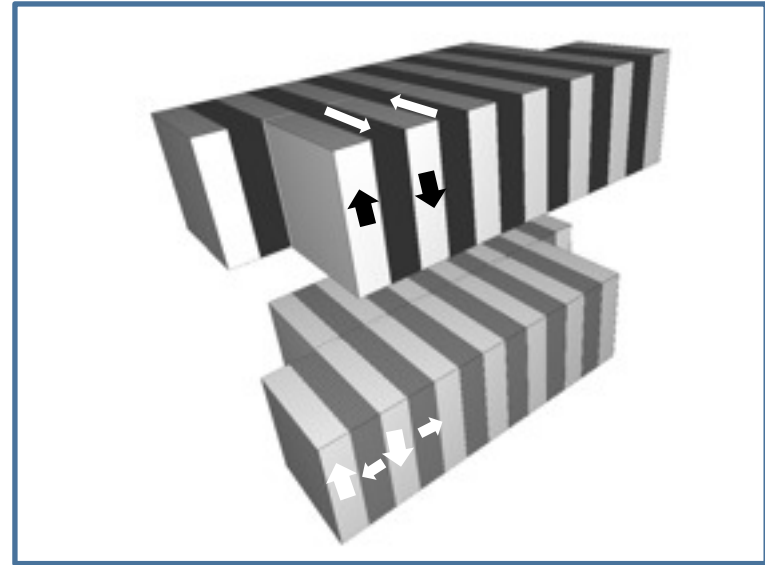
Modes	B_z [T]	B_x [T]
Linear H.	0,173	
Linear V.		0,125
Circular	0,1	

Undulator :

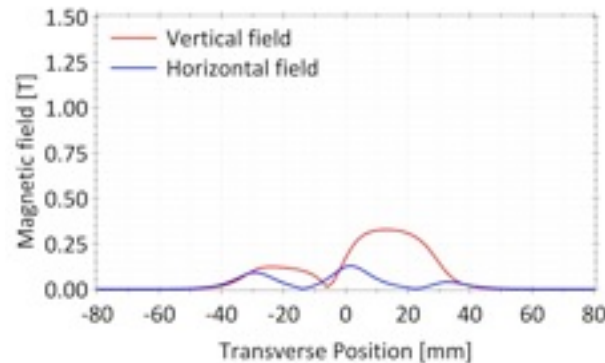
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

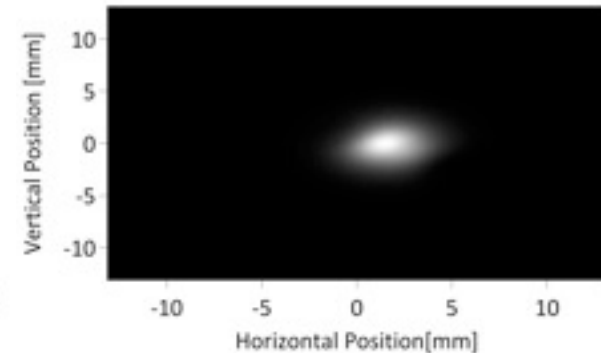
- NdFeB
- Size : 30 x 30 mm
- B_r : 1,26 T
- $\Theta_{mag} = 0^\circ$
- $X_{dist} = 1$ mm



H. & V. field values versus gap at 0 mm shift.



H. & V field roll-off at minimal gap,



P. Elleaume, A flexible planar / helical undulator design for synchrotron radiation sources, Nucl. Instr. Meth., A291, 371 (1990)
 P. Elleaume, J. Synch. Rad., 1, 19 (1994)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU: Diviacco/Walker

Diviacco/Walker undulators

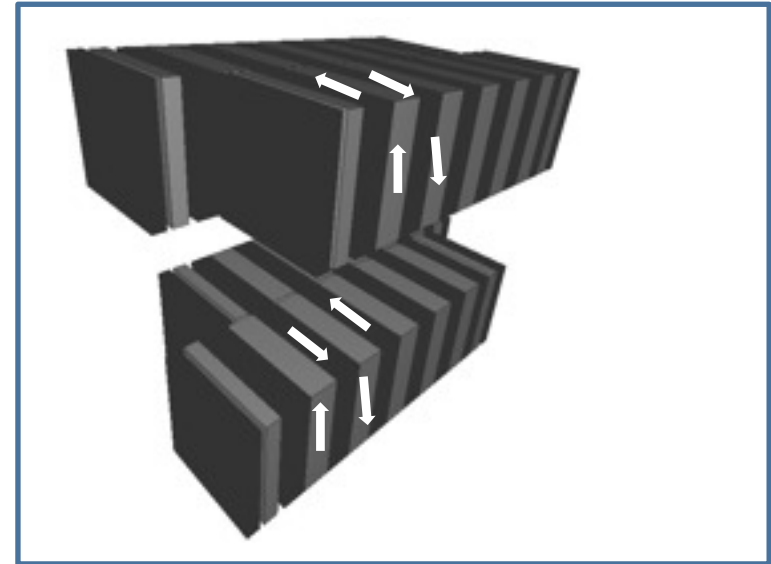
Modes	Bz [T]	Bx [T]
Linear H.	-	
Linear V.		-
Circular	0,13	

Undulator :

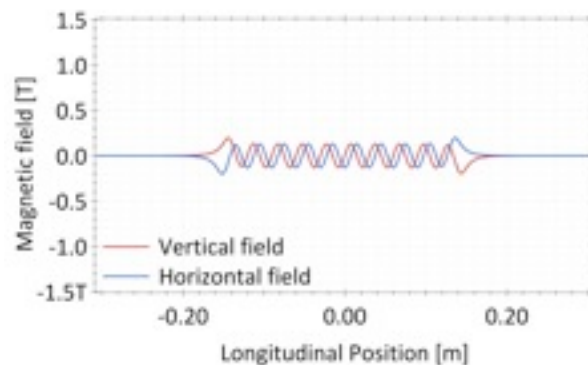
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

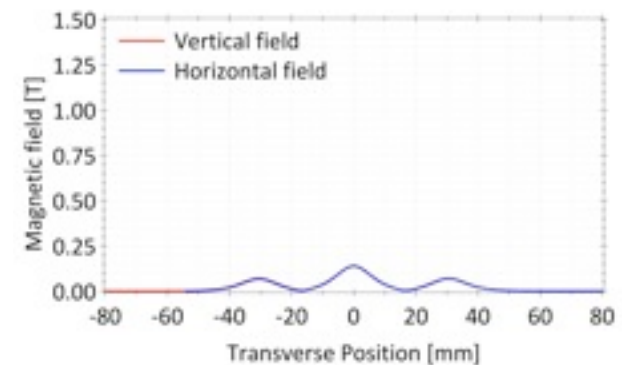
- NdFeB
- Size : 30 x 30 mm
- $B_r : 1,26 \text{ T}$
- $\Theta_{\text{mag}} = 0^\circ$
- $X_{\text{dist}} = 1 \text{ mm}$



- No phase shift
- No longitudinal component



H. & V. fields at minimal gap



H. & V. fields roll-off at minimal gap

B. Diviacco and R. P. Walker, Nucl. Instrum. Meth., A292, 517 (1990)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU : APPLE I

Apple I undulators

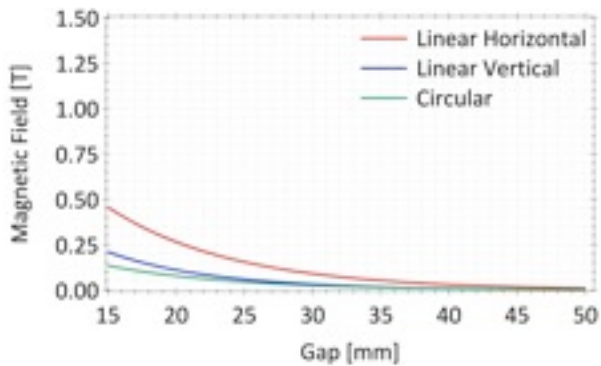
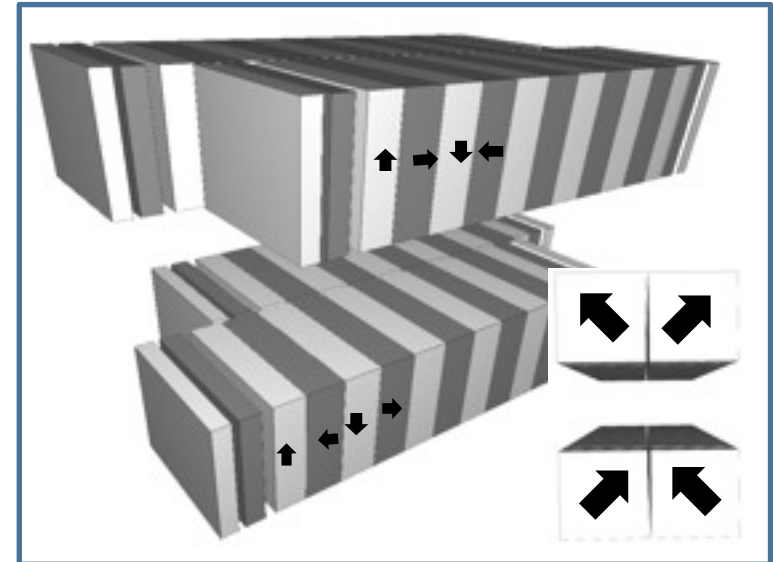
Modes	Bz [T]	Bx [T]
Linear H.	0,456	
Linear V.		0,21
Circular	0,135	

Undulator :

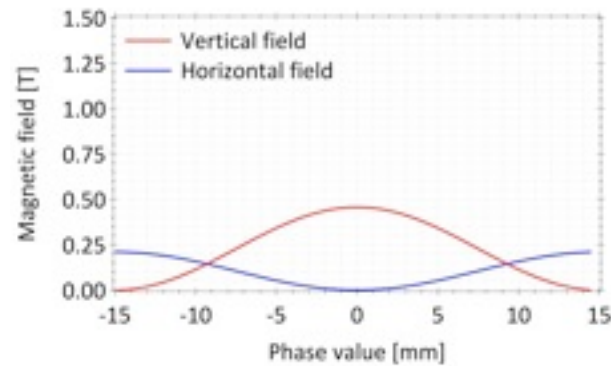
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

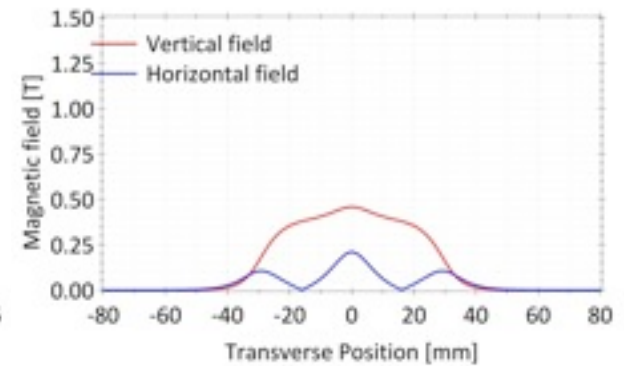
- NdFeB
- Size : 30 x 30 mm
- B_r : 1,26 T
- $\Theta_{mag} = 45^\circ$
- $X_{dist} = 1$ mm



H. & V. field values versus gap at 0 mm shift.



H. & V. field values versus shift at minimal gap



H. & V field roll-off at minimal gap,

S. Sasaki et al, A new undulator for generating variably polarized radiation, *Jpn. J. Appl. Phys.*, 31, L194 (1992)

S. Sasaki et al, *Nucl. Instr. Meth.*, A331, 763 (1993)

S. Sasaki et al, *Nucl. Instr. Meth.*, A347,87 (1994)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU : APPLE II

Apple II undulators

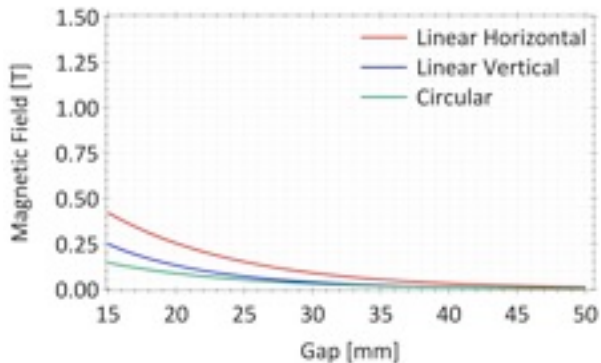
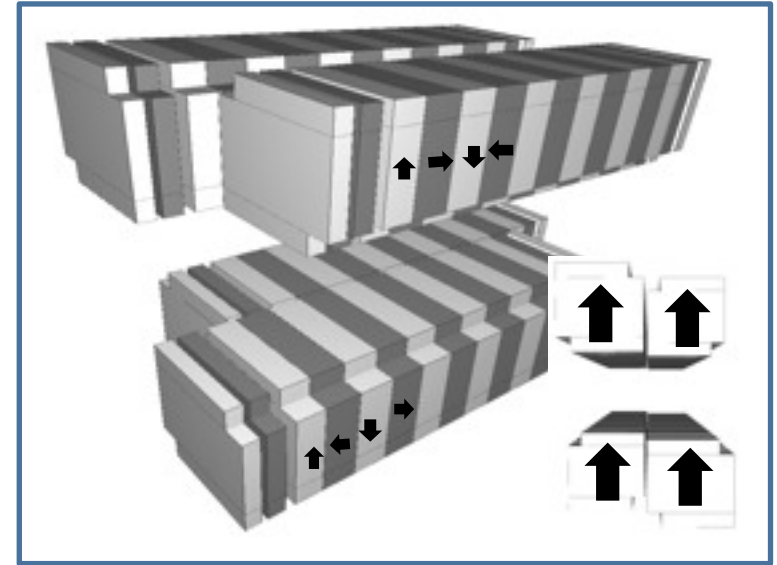
Modes	Bz [T]	Bx [T]
Linear H.	0,421	
Linear V.		0,247
Circular	0,145	

Undulator :

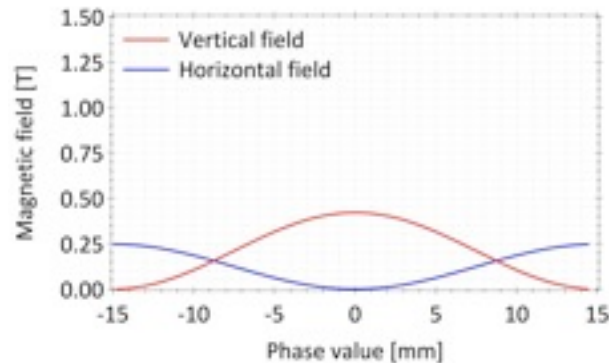
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

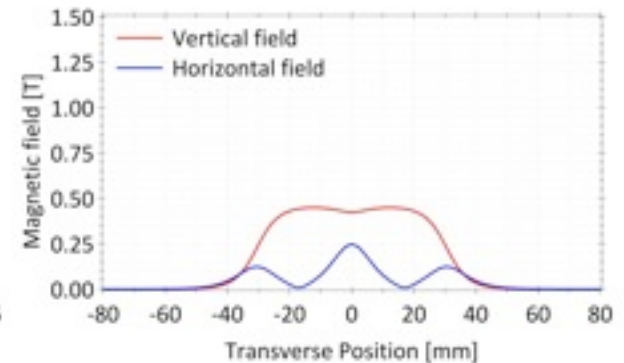
- NdFeB
- Size : 30 x 30 mm
- $B_r : 1,26 \text{ T}$
- $\Theta_{\text{mag}} = 0^\circ$
- $X_{\text{dist}} = 1 \text{ mm}$



H. & V. field values versus gap at 0 mm shift.



H. & V. field values versus shift at minimal gap



H. & V field roll-off at minimal gap,

- R. Carr , Nucl. Instr. Meth., A306, 391 (1991)
- R. Carr et al , Rev. Sci. Instrum., 63, 3564 (1992)
- R. Carr, Proceedings of 1992 EPAC, p489 (1992)

Permanent magnets EPU : APPLE III

Apple III undulators

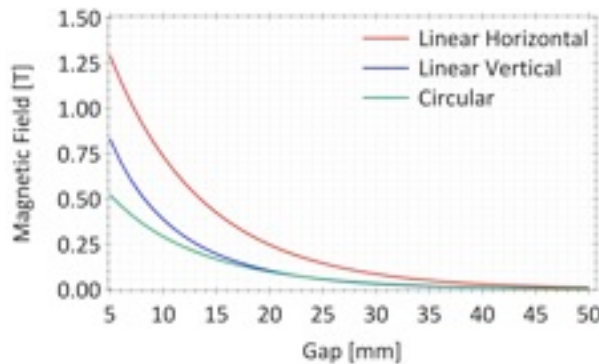
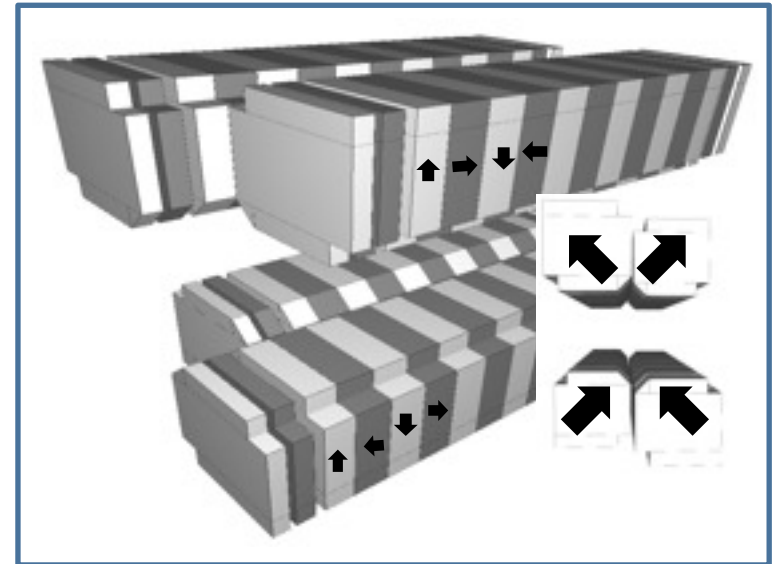
Modes	Bz [T]	Bx [T]
Linear H.	1,29	
Linear V.		0,83
Circular	0,52	

Undulator :

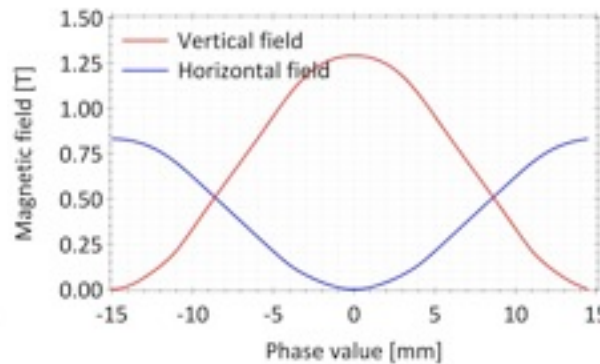
- Period : 30 mm
- Minimal gap : 5,4 mm

Magnets :

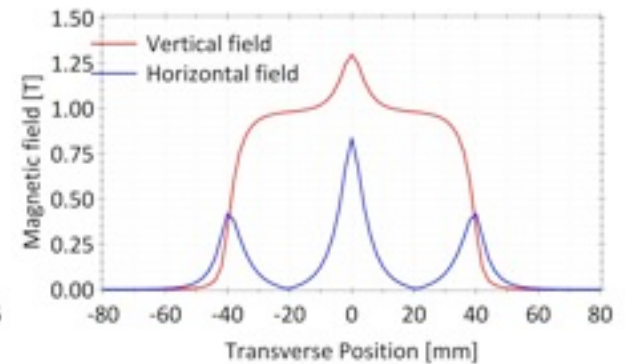
- NdFeB
- Size : 40 x 40 mm
- B_r : 1,13 T & 1,19 T
- $\Theta_{mag} = 45^\circ$
- $X_{dist} = 1$ mm



H. & V. field values versus gap at 0 mm shift.



H. & V. field values versus shift at minimal gap



H. & V field roll-off at minimal gap,

[1] J. Bahrtdt et al, Proceedings of the 2004 FEL Conference, Trieste, ITALY, p610 (2004)

Permanent magnets EPU : APPLE III

Apple III undulators (SOLEIL model)

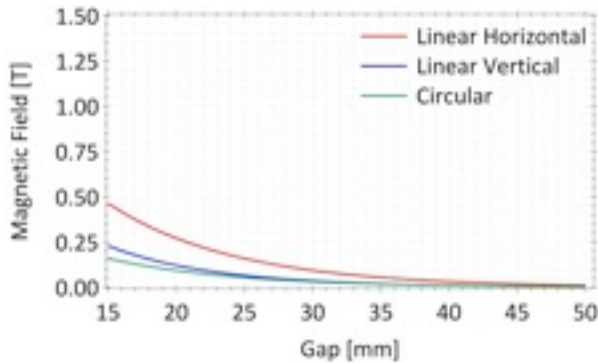
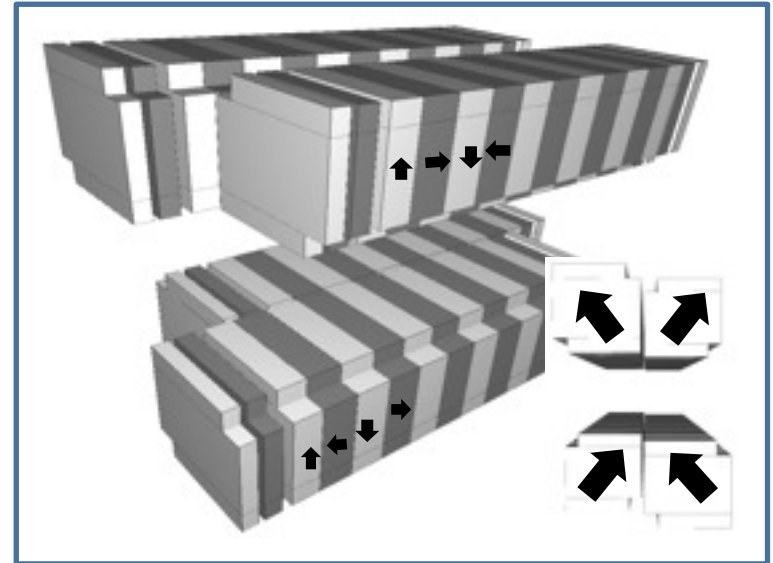
Modes	B_z [T]	B_x [T]
Linear H.	0,463	
Linear V.		0,23
Circular	0,16	

Undulator :

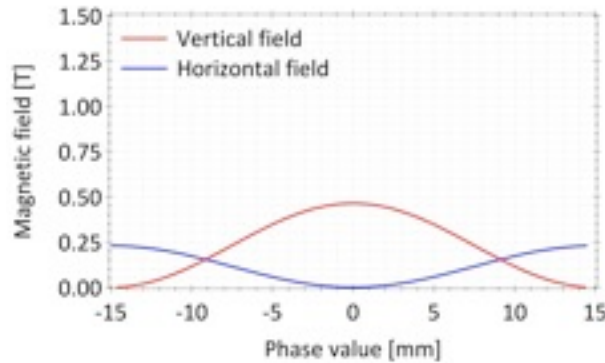
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

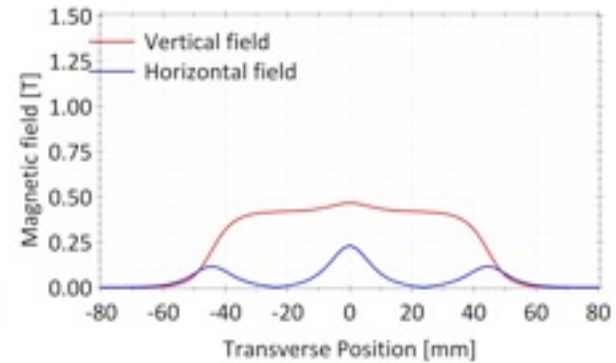
- NdFeB
- Size : 45 x 45 mm
- B_r : 1,26 T
- $\theta_{mag} = 33^\circ$
- $X_{dist} = 1$ mm



H. & V. field values versus gap at 0 mm shift.



H. & V. field values versus shift at minimal gap



H. & V field roll-off at minimal gap,

J. Bahrtdt et al, Proceedings of the 2004 FEL Conference, Trieste, ITALY, p610 (2004)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU : DELTA

Delta undulators

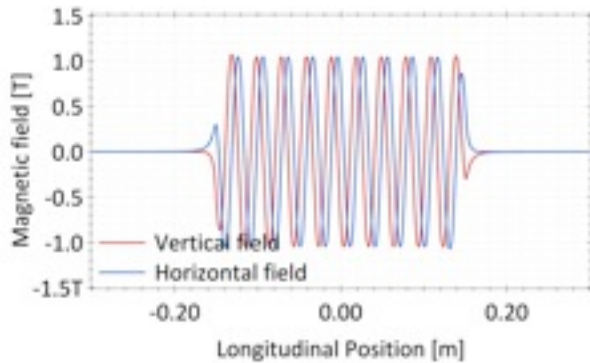
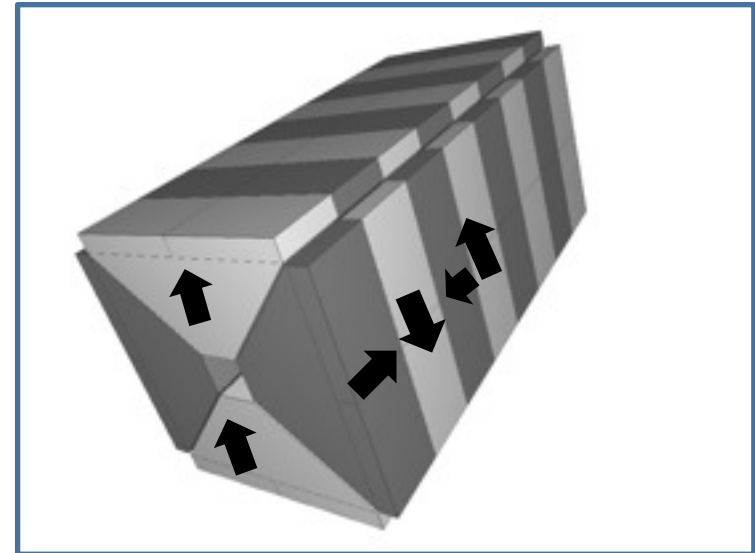
Modes	Bz [T]	Bx [T]
Linear H.	1,04	
Linear V.		1,04
Circular	1,04	

Undulator :

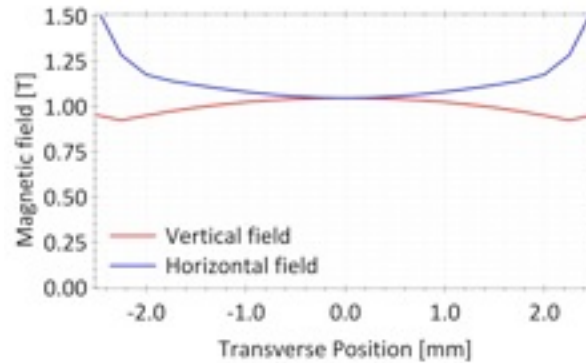
- Period : 30 mm
- Minimal gap : 5 mm

Magnets :

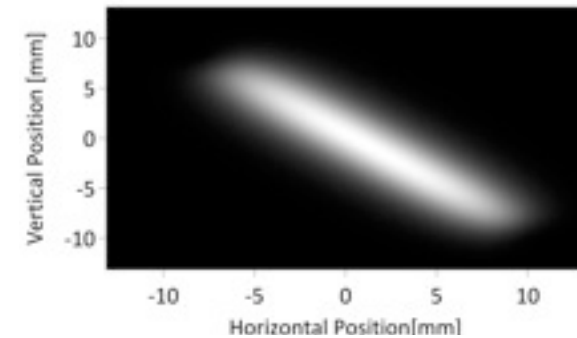
- NdFeB
- Size : 25 x 9 x 9 mm
- $B_r : 1,26$ T
- $\Theta_{mag} = 0^\circ$
- $X_{dist} = 0,5$ mm



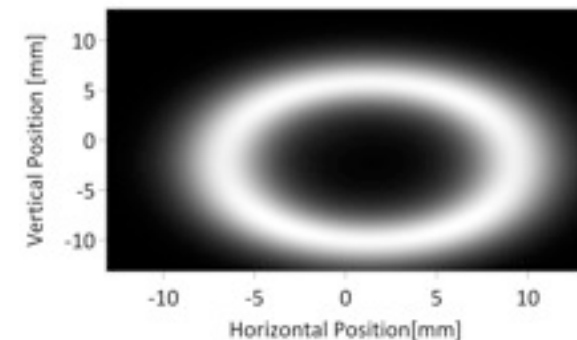
H. & V. fields at 0 mm shift.



H. & V field roll-off at minimal gap,



Without phase shift

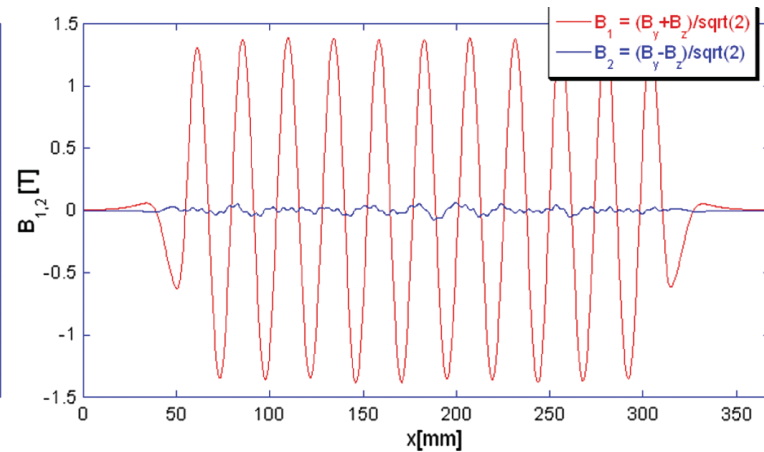
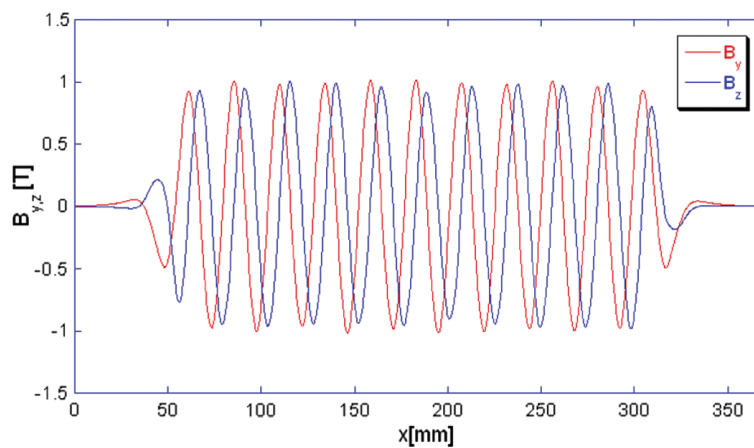
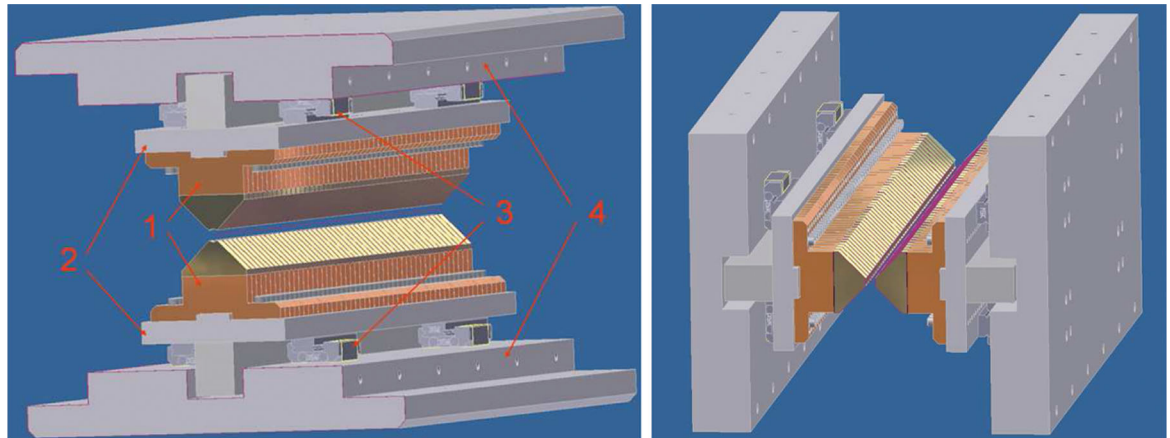
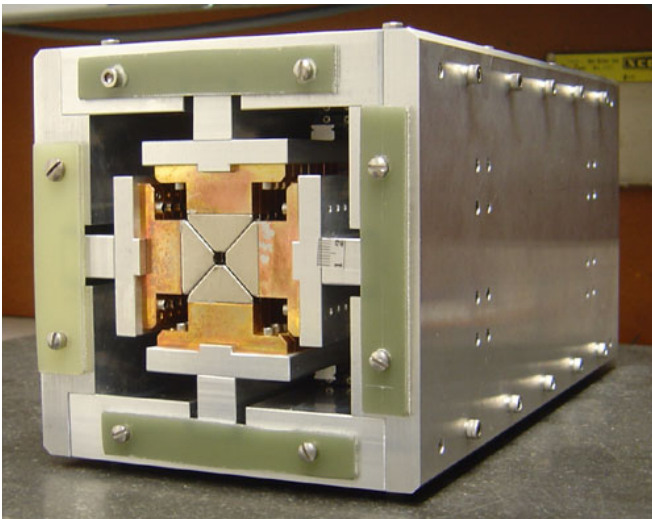


Quarter of period shift

A. B. Temnykh, Phys. Res. Spec. Topics AB, 11,120702 (2008)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU : DELTA



A. B. Temnykh, DELTA undulator for Cornell Energy Recovery Linac, *Phys. Res. Spec. Topics AB*, 11,120702 (2008)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU: 6 arrays

Kitamura undulators

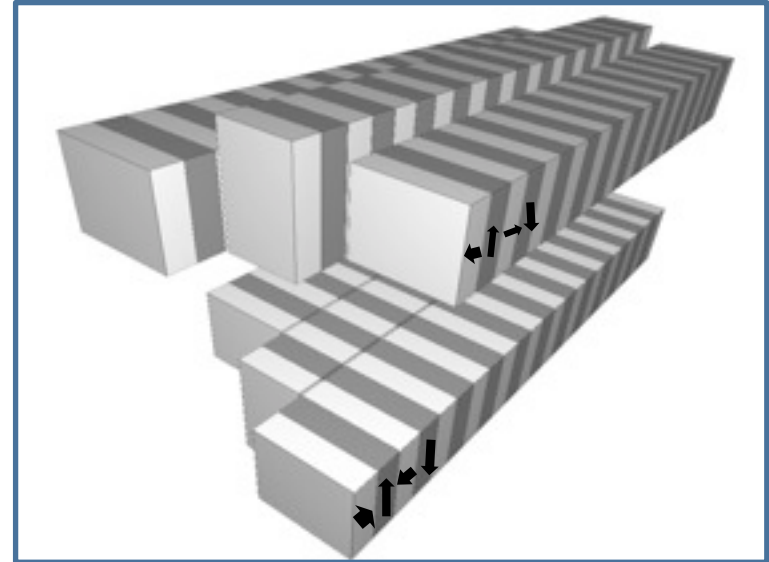
Modes	B_z [T]	B_x [T]
Linear H.	0,424	
Linear V.		0,06
Circular	-	

Undulator :

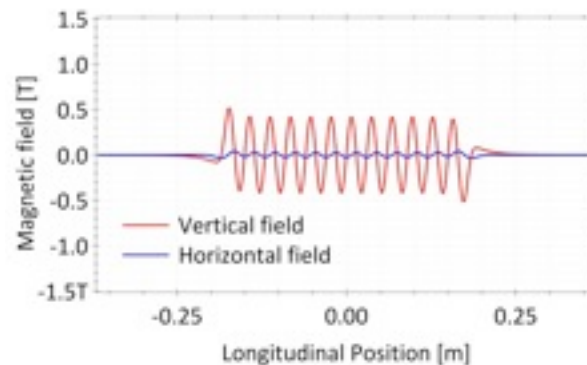
- Period : 30 & 60 mm
- Minimal gap : 15,5 mm

Magnets :

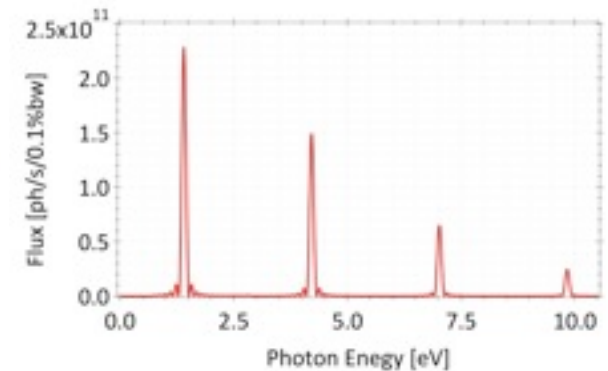
- NdFeB
- Size : 30 x 30 mm
 - 10 x 50 mm
- B_r : 1,26 T
- $\Theta_{\text{mag}} = 0^\circ$
- $X_{\text{dist}} = 1$ mm



- Degree of circular polar. maintained while changing the photon energy



H. & V. field at minimal gap



Flux density for a 400mA, 275 GeV beam without emittance an energy spread

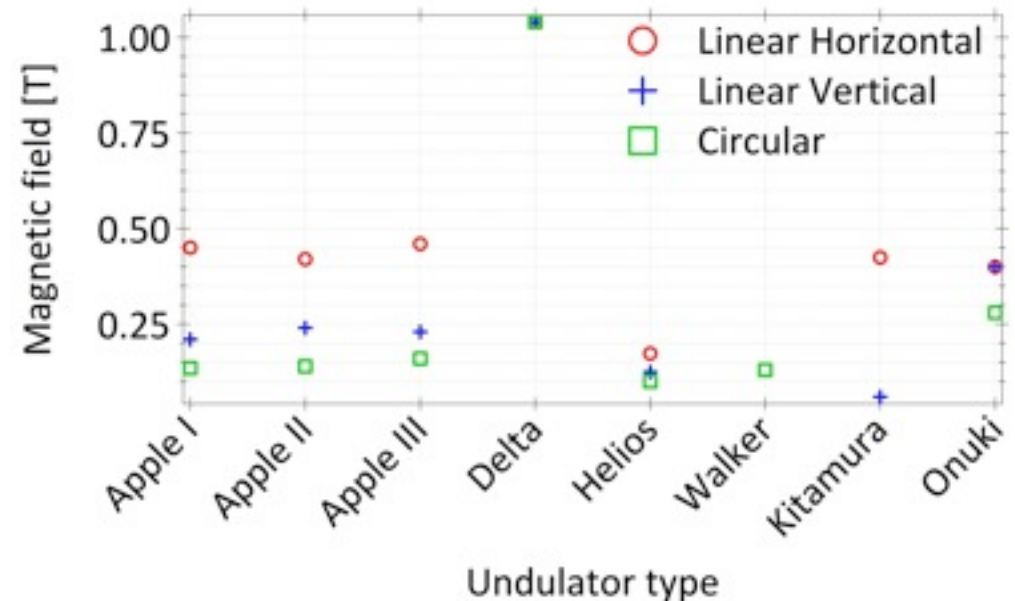
H. Kitamura et al, J. Electron Spectr. Relate Phenom., 80,437, (1996)

A. Hiraya et al, J. Synchr. Rad., 5, 445, (1998)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU

Polarisation modes	LH	LV	C	Remarks
Apple I	0,45	0,21	0,135	
Apple II	0,42	0,24	0,14	
Apple III	0,46	0,23	0,16	
Delta (Apple IV?)	1,04	1,04	1,04	5mm round gap
Helios	0,173	0,125	0,1	
Diviacco-Walker	-	-	0,13	Circular only
Kitamura	0,424	0,06	-	Low field strength in circular
Onuki	0,4	0,4	0,28	



Quasi periodic PM EPU: QP APPLE II

Apple II undulators

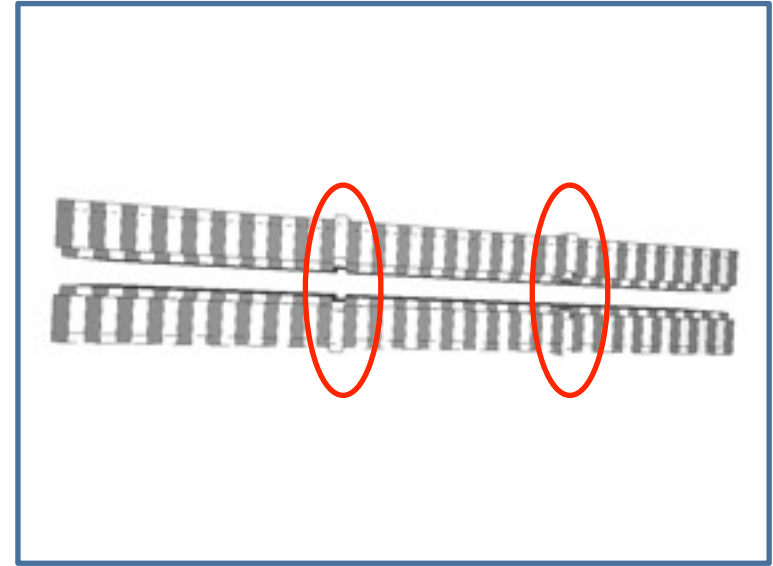
Modes	Bz [T]	Bx [T]
Linear H.	0,421	
Linear V.		0,247
Circular	0,145	

Undulator :

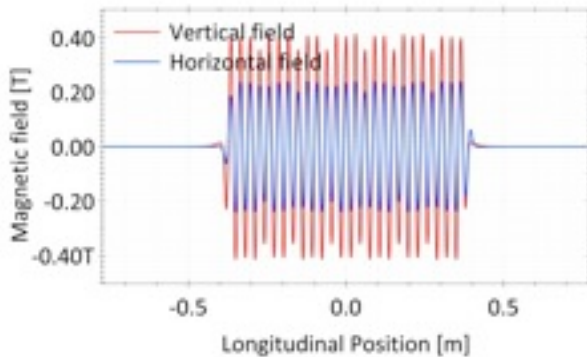
- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

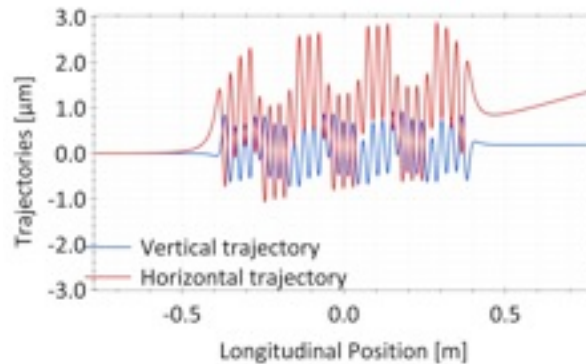
- NdFeB
- Size : 30 x 30 mm
- $B_r : 1,26 \text{ T}$
- $\Theta_{\text{mag}} = 0^\circ$
- $X_{\text{dist}} = 1 \text{ mm}$



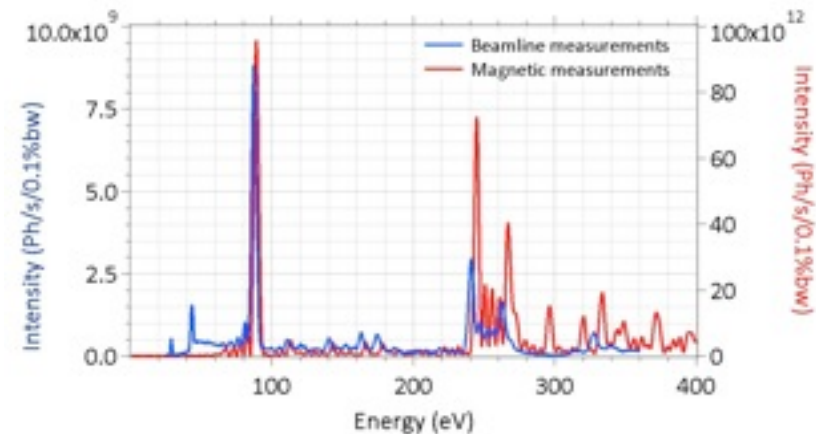
- Magnets creating aperiodicity are moved vertically



H. & V. field values in linear Horizontal (red line) and linear vertical (blue one)



H. & V. trajectories in linear Horizontal (red line) and linear vertical (blue one)



J. Chavanne et al, Proceedings of the European Particle Accelerator Conference, Sweden (1998)

B. Diviacco et al, Proceedings of the European Particle Accelerator Conference, Sweden (1998)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Quasi periodic PM EPU: Figure 8

T. Tanaka, H. Kitamura, *Nuclear Instruments And Methods*, A364, 368 (1995)

Figure8 undulators

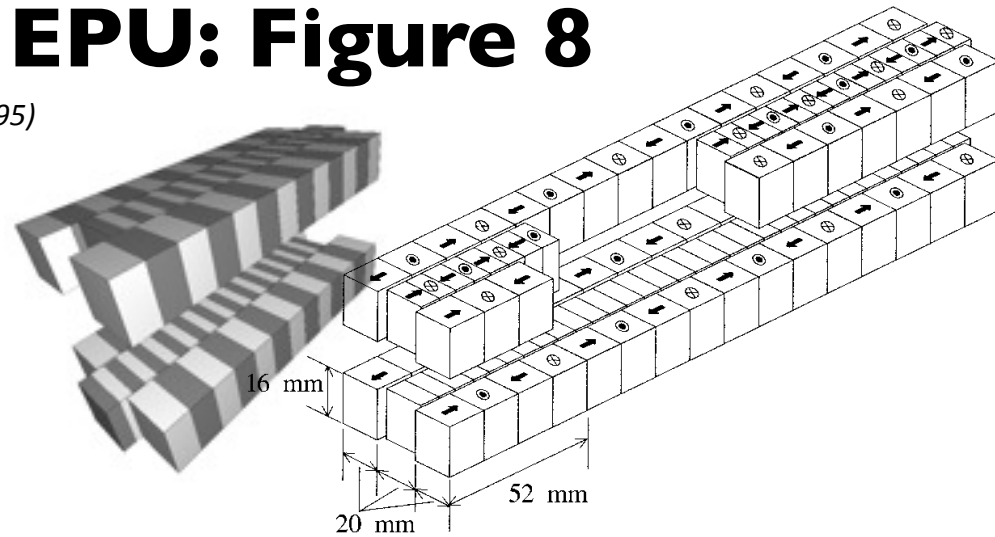
Modes	B_z [T]	B_x [T]
Linear H.	0,42	
Linear V.		0,22
Circular		

Undulator :

- Period : 30 mm
- Minimal gap : 15,5 mm

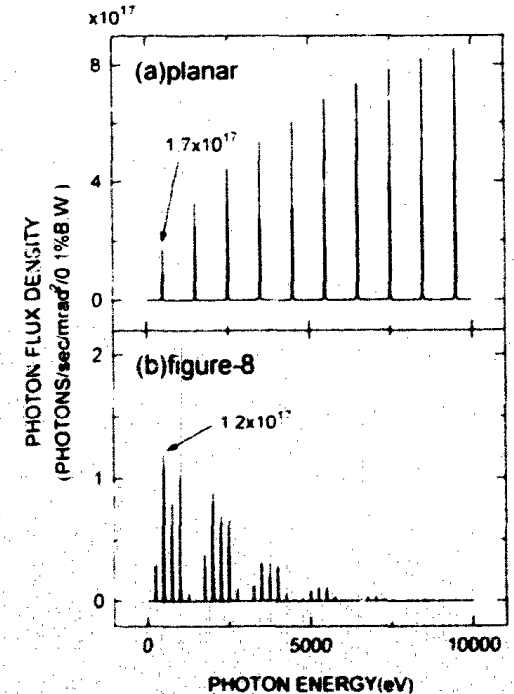
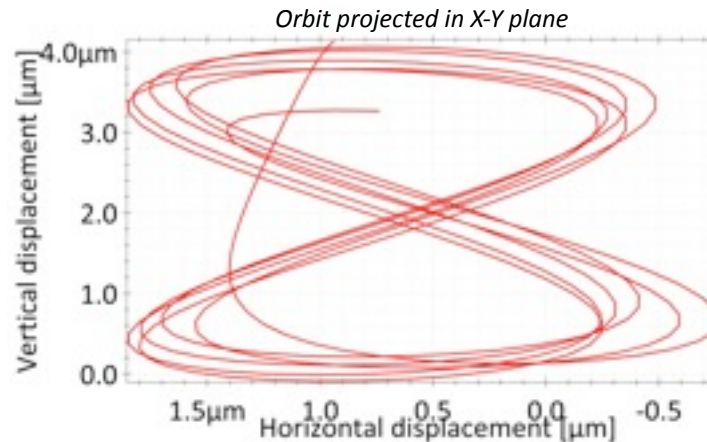
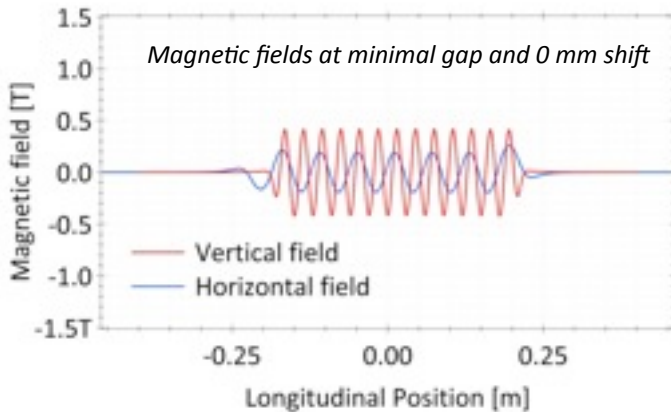
Magnets :

- NdFeB
- Size : 30 x 30 mm
- B_r : 1,26 T
- $\Theta_{mag} = 0^\circ$
- $X_{dist} = 1$ mm



- odd (LH), integer (LH), and half integer harmonics (LV)

- Low on-axis power density in linear mode
- Combination of different period length



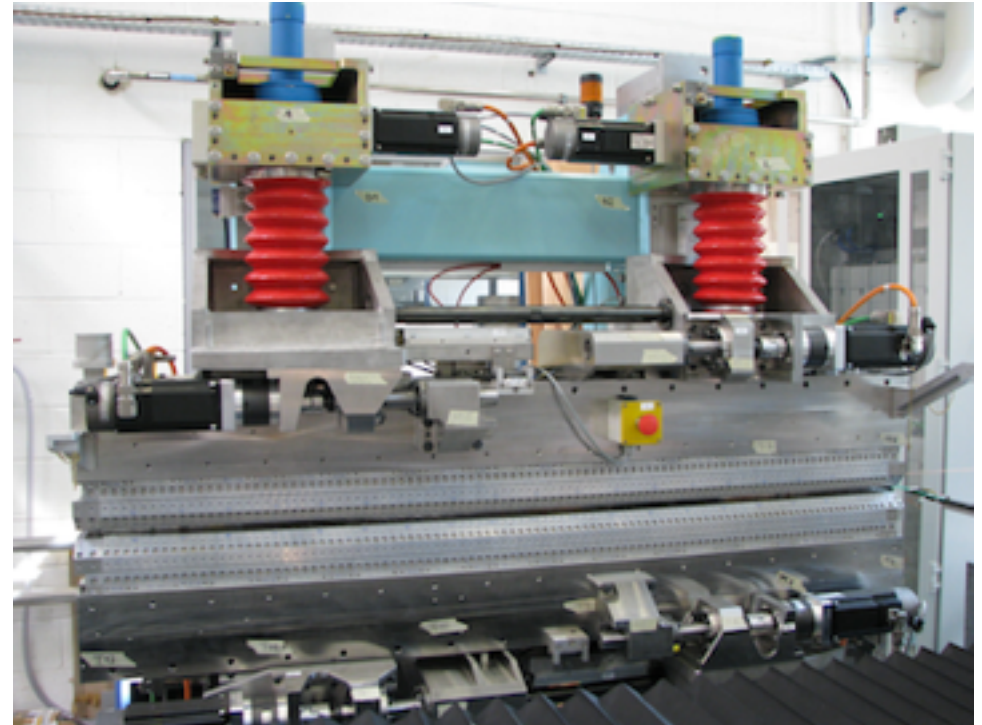
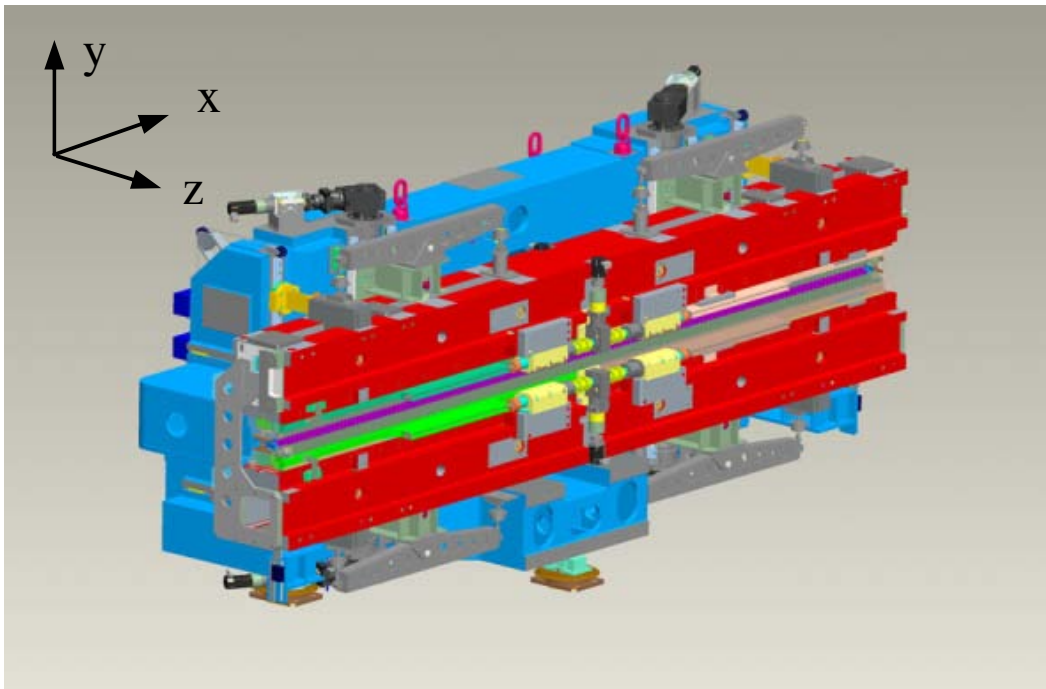
In vac helical

T. Tanaka, H. Kitamura, *J. Synchrotron Radiation* (1998), 5, 412-413

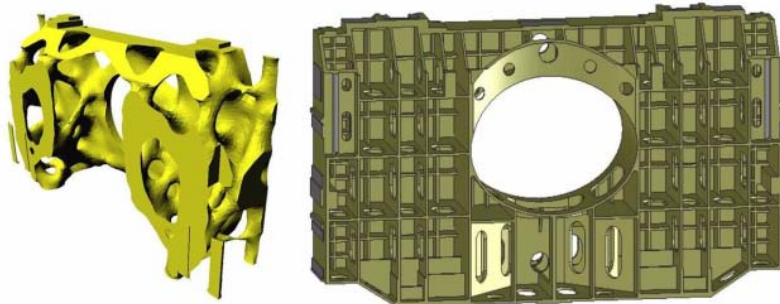
T. Hara et al. *Nucl. Instrum. Methods A* 467-468 (2001) 165-168

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Permanent magnets EPU carriages



HU64 at SOLEIL : 4 arrays and gap movement



phase and gap variation
aperiodicity
taper
correction coils

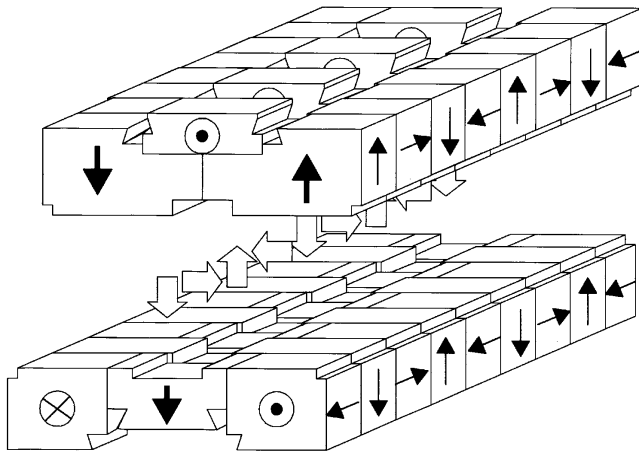
J. Bahrtdt et al., "APPLE Undulator for PETRA III", Proc. EPAC08, 2219 (2008)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

In vacuum Fig8 type helical undulator

T. Tanaka, H. Kitamura, *J. Synchrotron Radiation* (1998), 5, 412-413

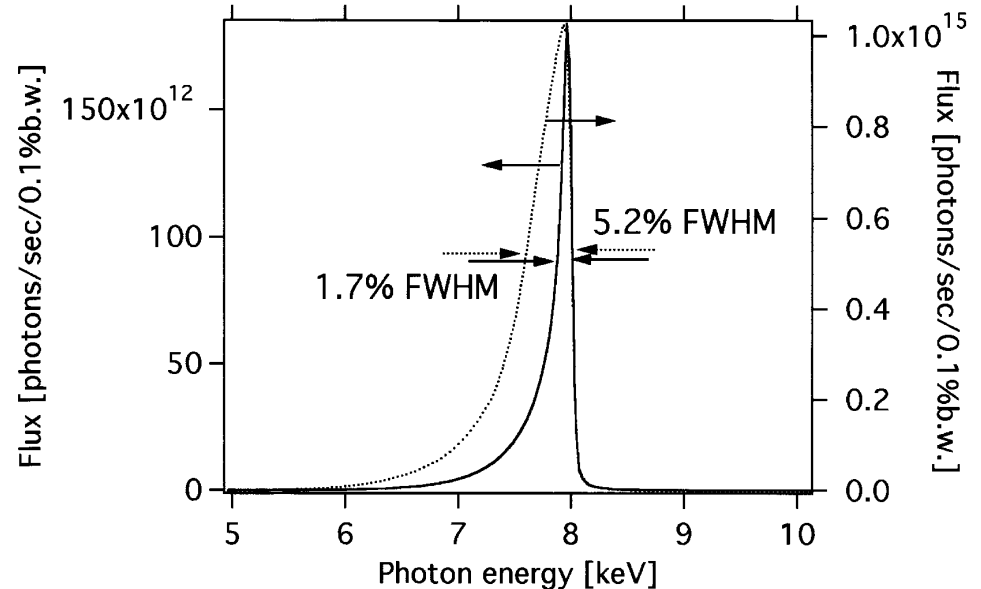
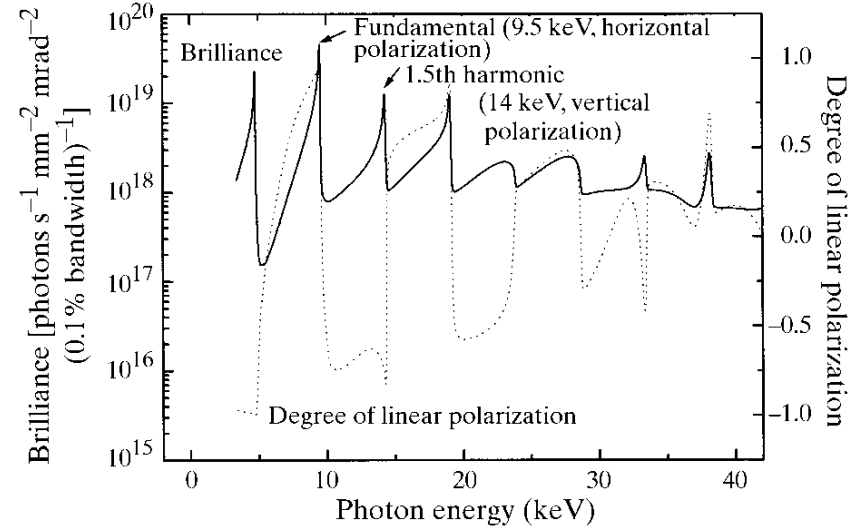
T. Hara et al. *Nucl. Instrum. Methods A* 467-468 (2001) 165-168



Central arrays : vertical field
side arrays : horizontal field

TiN coating on the magnets
Cu Ni foil, baking 145 °C
no phasing mechanics

Gap : 11.6 mm (min .8 mm)
Period : 26 mm
Length : 4.5 m
 $B_z = 0.728 \text{ T @ } 8 \text{ mm}$
 $B_x = 0.31 \text{ T @ } 8 \text{ mm}$
22kW



ElectroMagnetic Permanent magnet Helical Undulator

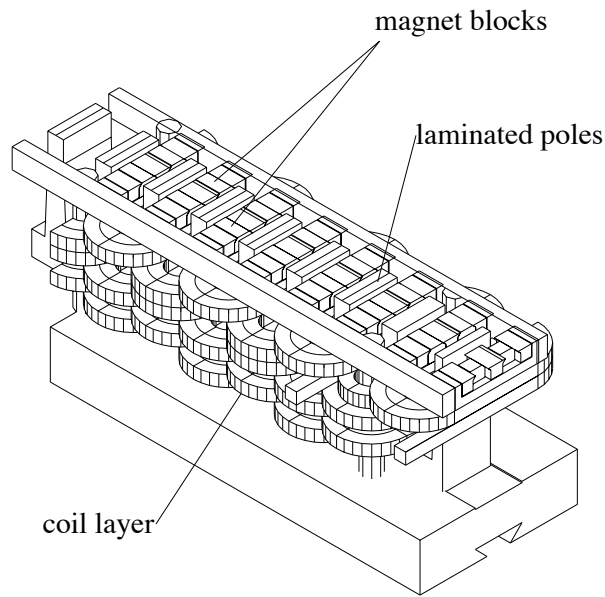
Vertical field : coil and laminated yoke, horizontal field : array of permanent magnets

ESRF

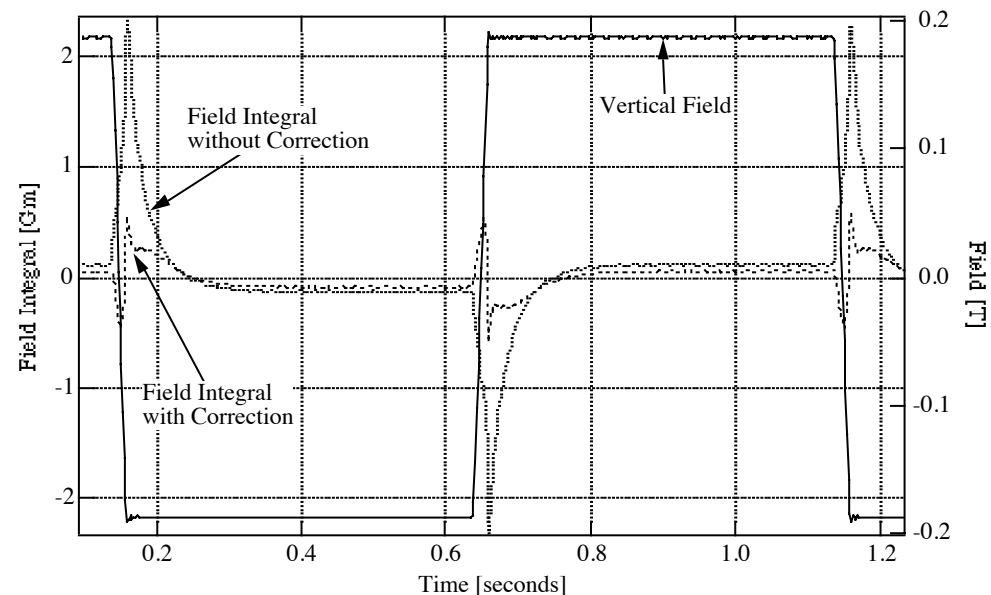
19 x 80 mm, B=0.2T

flipping the current in the coil in 20 ms, polarisation switching in 1 Hz
SmCo magnets

DSP card for real time synchronisation (eddy currents)



current flipping in 20 ms, gap 16 mm



J. Chavanne, P. Elleaume, P. VanVaerenbergh, "A novel fast switching linear/helical undulator", Proceedings of EPAC 98, p. 317 (1998).

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

EMPHU @ SOLEIL

Jefferson Lab

28 x 80 mm, B=0.134T



G. Biallas et al. an 8 cm period electromagnetic wiggler magnet with coils made from sheet copper", Proceedings of PAC 2005, Knoxville, 4093 ; FEL04, 554-557

SOLEIL

26 x 64 mm, B=0.24T

flipping the current in 100 ms

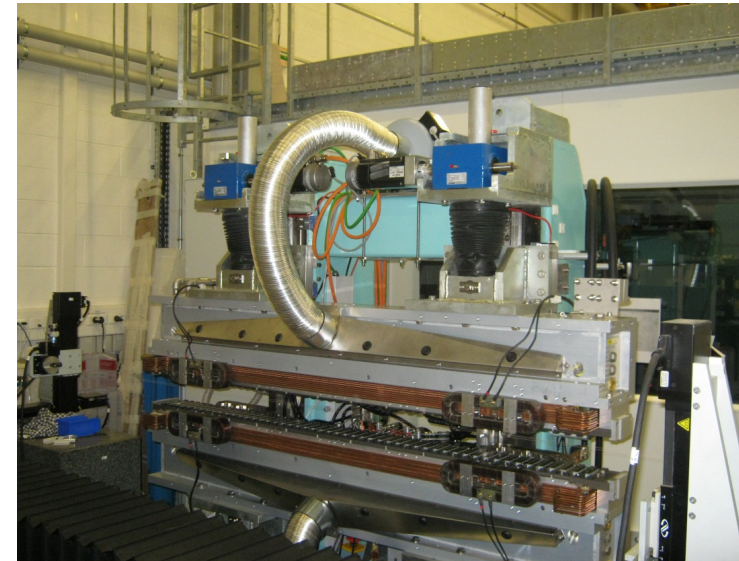
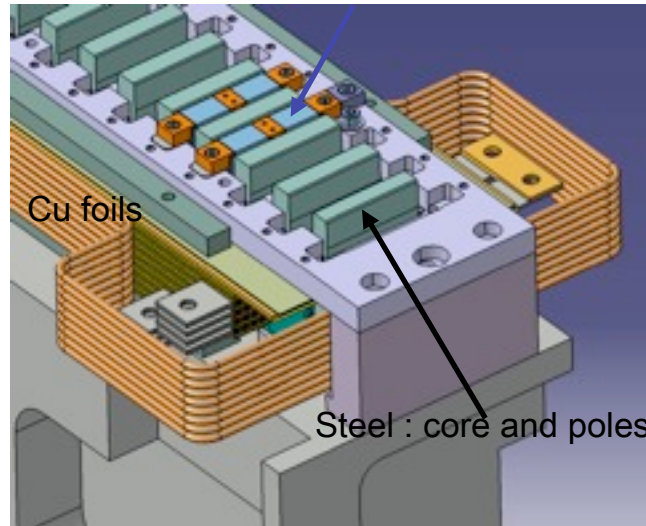
NdFeB magnets

Coils: 25 layers of copper sheets stacked together 516 with current and 9 with cooling)

SPI controller for real time synchronisation (eddy currents)



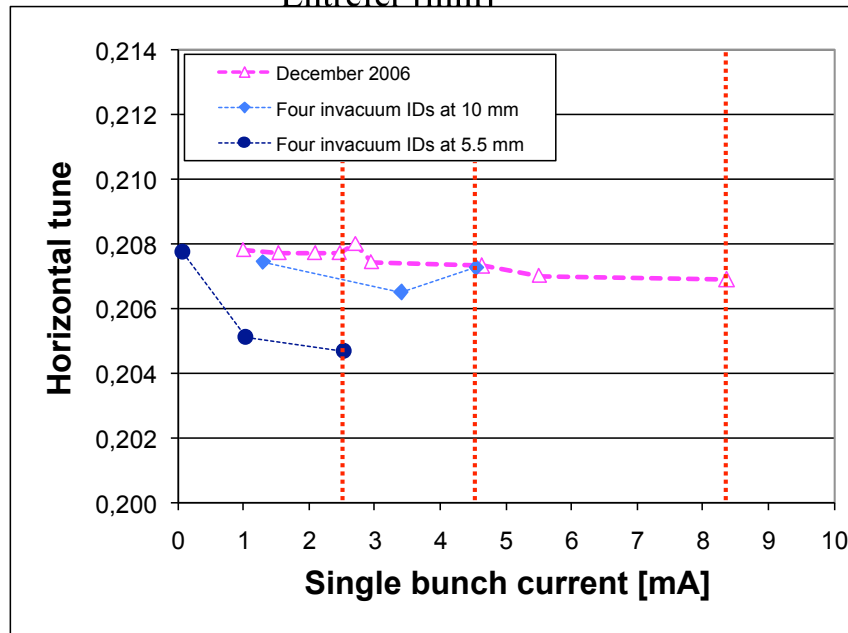
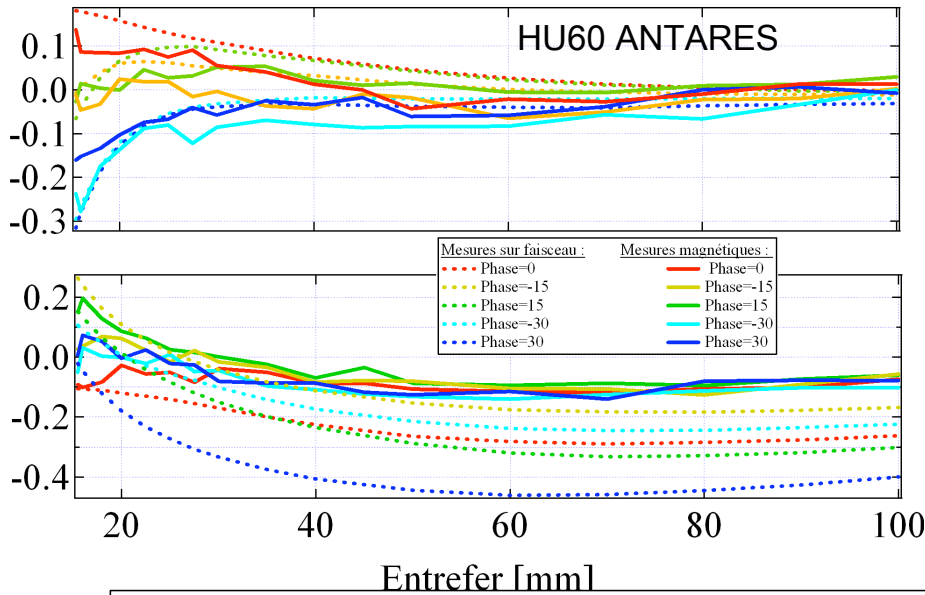
Permanent magnets



F. Marteau et al., Description of a EMPHU for fast polarisation switching , Proceedings MT, Marseille, Sept. 2011

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Multipolar terms



Dipolar terms: field integral

Comparison magnetic measurement/ electron beam
 => FFWD tables

+ Fast/slow orbit feedback to keep to source position and divergence in 10% of the electron beam size

Dynamic field integral compensation

J. Safranek et al, Phys. Rev. Special Topics (2002), Vol. 5, 010701, pp. 1-7
O. Marcoullé et al, IPAC 2011, 3236

Quadrupolar terms:

normal quadrupoles => tune shift => feedback on the tunes, or FFWD tables

Skew quadrupoles => coupling

Compensation : current sheet for APPLE-II devices

J. Bahrtdt, et. al., "Active shimming of the dynamic multipoles of the BESSY UE112 Apple Undulator", Proceedings of EPAC'08, p. 2222 (2008).

Sextupolar terms => chromaticity

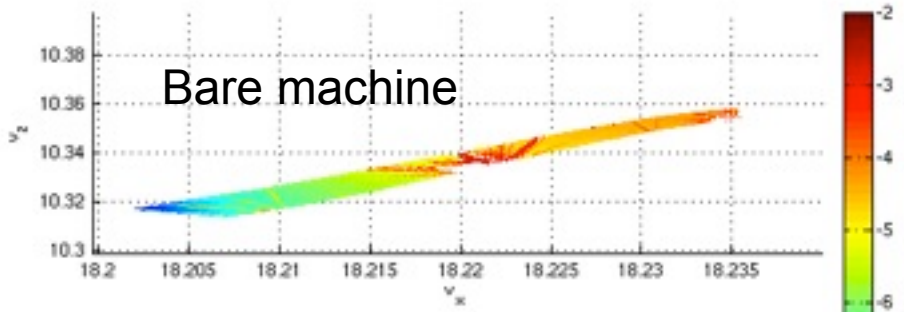
General approach

Magnetic field maps (RADIA; measurements)

introduced on TRACY electron beam simulation (on and off momentum) for injection efficiency and lifetime study

Modelisation with field maps

Simulation of the effect of the HU36 undulator located in a short straight section ($\beta_{\text{ax}}=17.8 \text{ m}$)



On-momentum dynamic aperture

11.5 mm minimum gap

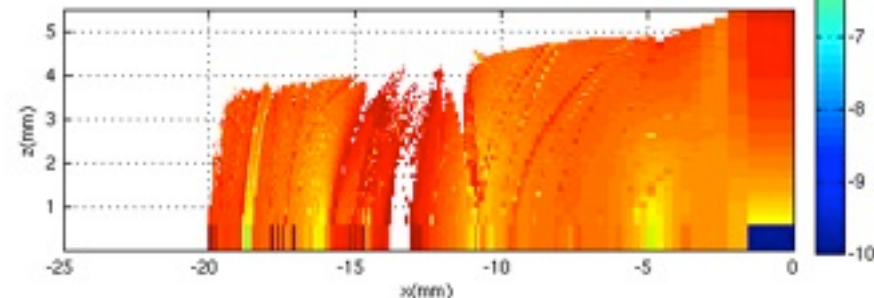
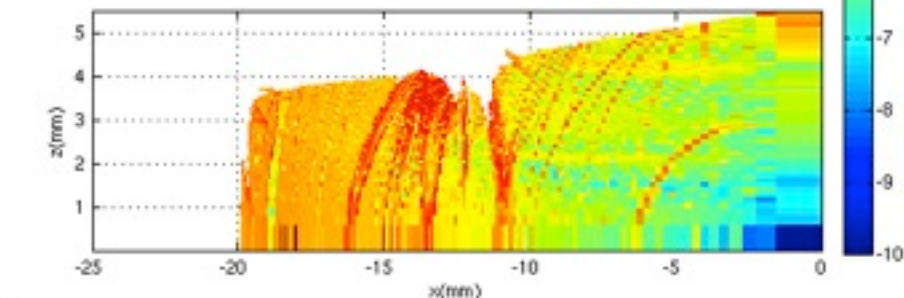
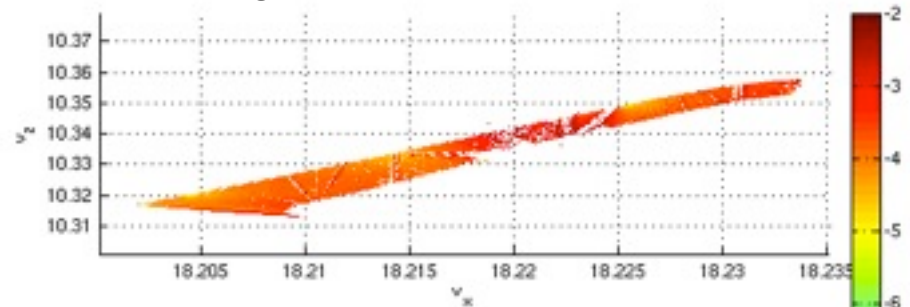
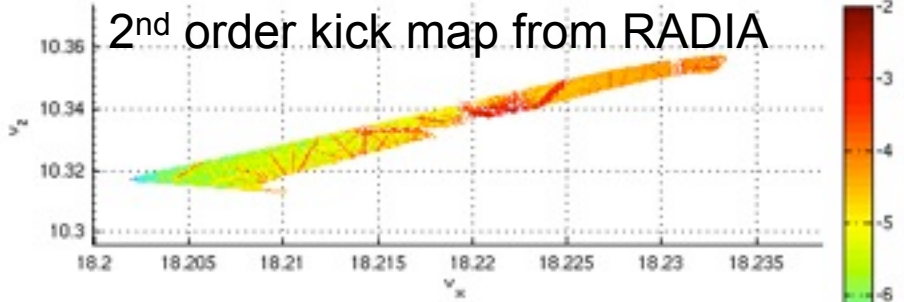
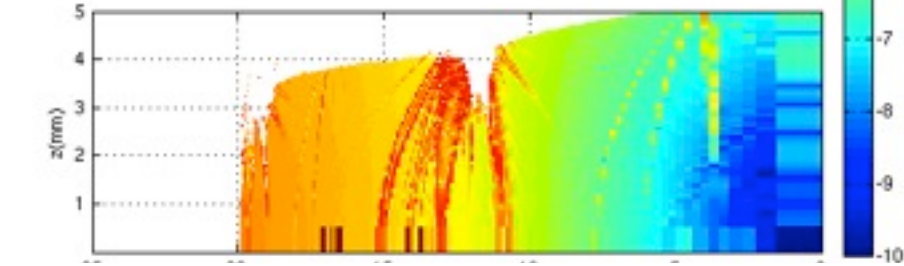
Phase = 0

Injection rate :

bare machine, 88% => 80%

RP configuration 52% => 55%

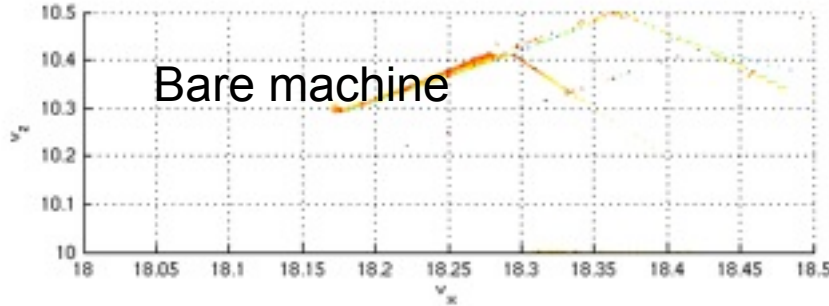
2nd order kick map from RADIA
+ magnetic measurement map



, Invited

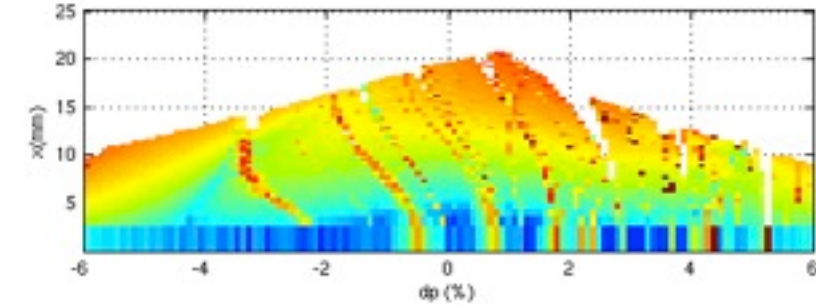
Modelisation with field maps

Simulation of the effect of the HU36 undulator located in a short straight section

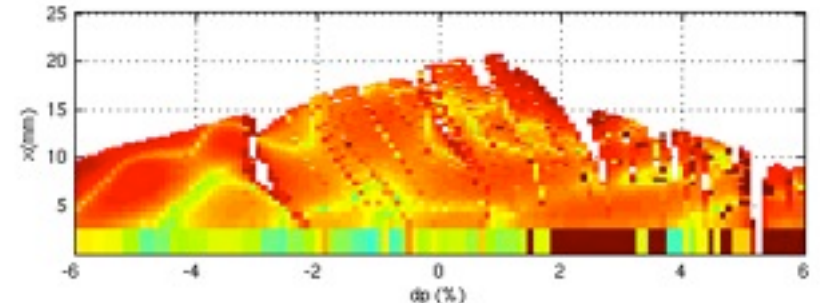
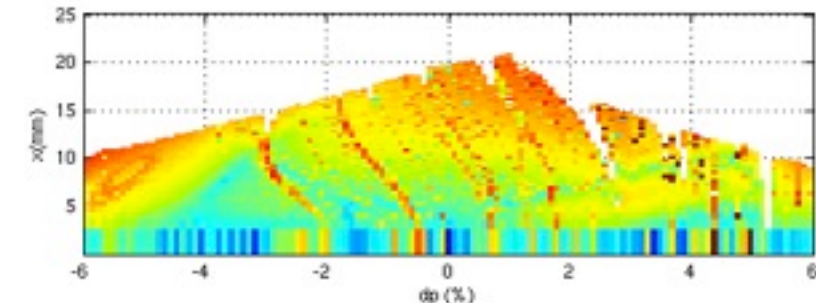
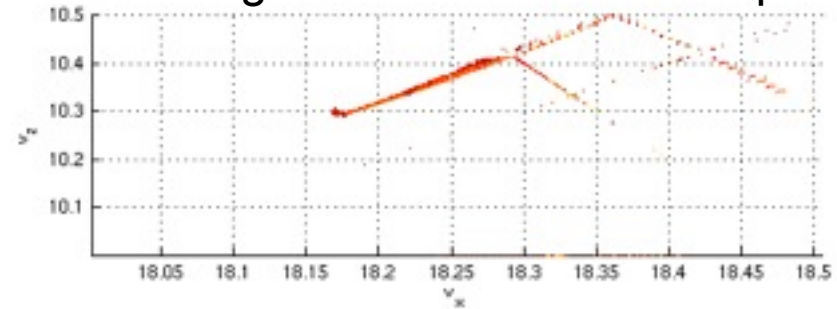
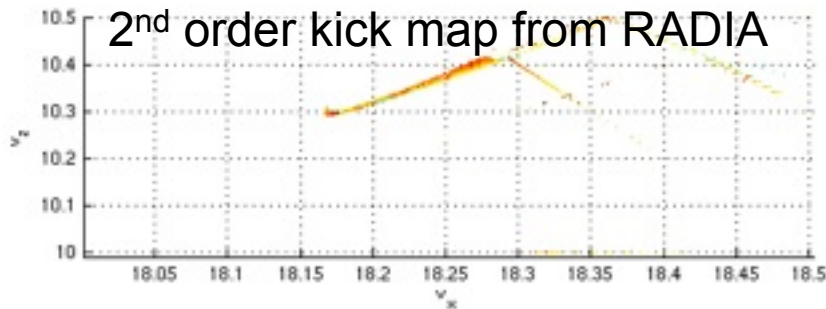


Off-momentum horizontal aperture
11.5 mm minimum gap
Phase = 0

Measured lifetime :
bare machine, 19.4 h@400 mA => 14.3 h
RP configuration 7.8 h => 6.6 h



2nd order kick map from RADIA
+ magnetic measurement map

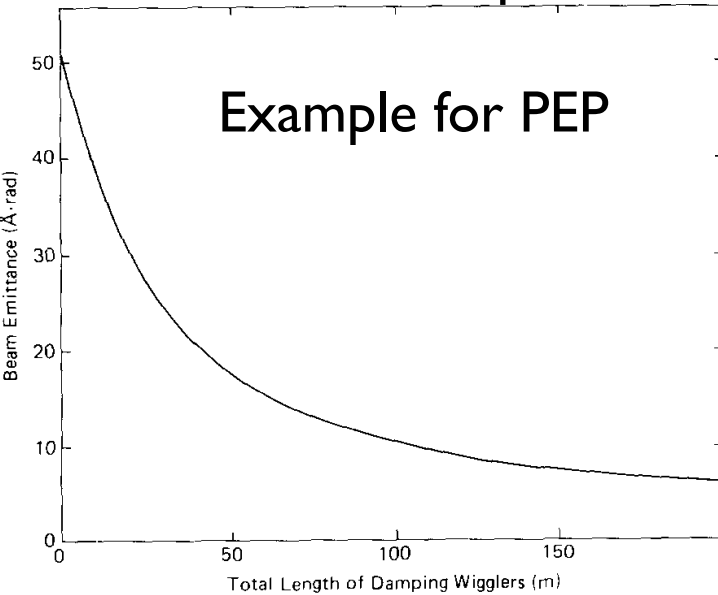


,T

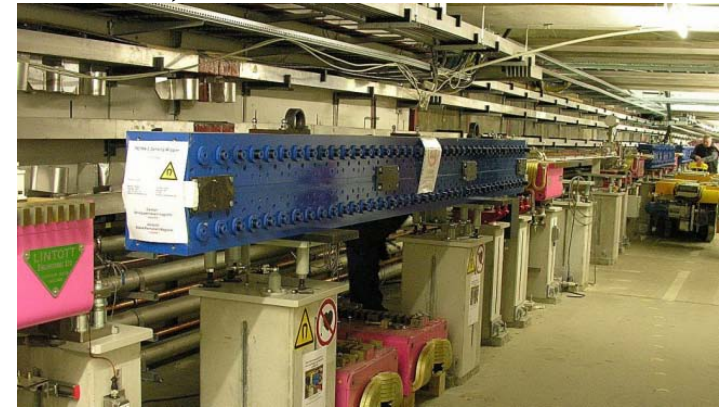
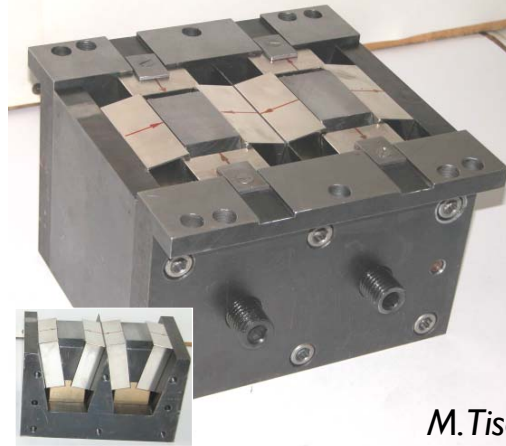
ited

Desired ID effects: damping wiggler

More damping with additional synchrotron radiation through installation of strong wiggler magnets placed in a dispersion free location (for the equilibrium orbit to be independent of the particle energy) => emittance reduction



PETRAIII: Horizontal emittance : 1 nm.rad, Vertical emittance : 0.01 nmrad



M. Tischer et al. Damping wigglers for the PETRA III light source, PAC 2005, Knoxville, 2446; EPAC08, 2317

H. Wiedemann, An ultra-low emittance mode for PEP using damping wigglers, Nucl. Instr. Meth. A266 (1988) 24-31.

T. Raubenheimer et al. SLAC PUB 4808, 1988

NLSII (3 GeV):

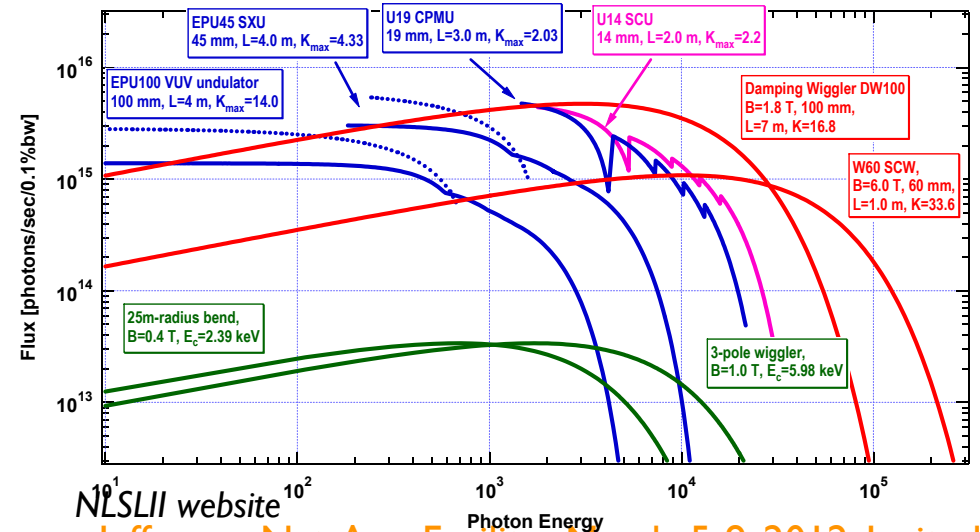
Horizontal emittance : 0.55 nm.rad

Vertical emittance : 0.008 nmrad

2x3.4 mperiod 9 cm, gap 12.5 mm, K=15.2

MAX-IV (3 GeV):

Horizontal emittance : 0.24 nm.rad



NLSII website

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility, March. 5-9, 2012, Invited

Desired ID effects: Robinson wiggler

$$\epsilon_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

D: partition number due to radiation damping

Generally, $D \sim 0$ and $J_x \sim I$

Robinson theorem : $J_x + J_z + J_s = 4$

$D = -1 \Rightarrow \epsilon_x/2$ and energy spread $\propto \sqrt{2}$

$B \cdot dB/dx \neq 0$ and $\eta_x \neq 0$

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

Short straight section : $\eta_x = 0.28$ m

$D = -1 \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

- $J_s = I$ damping in longitudinal plane
- high gradients?
- field homogeneity (injection, lifetime)
- radiation properties

Desired ID effects: Robinson wiggler

$$\epsilon_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

D: partition number due to radiation damping $J_x = 1 - D$

Generally, $D \sim 0$ and $J_x \sim 1$

Robinson theorem : $J_x + J_z + J_s = 4$

$$\epsilon_x = \epsilon_{x,0} \frac{1}{1-D} \quad \left(\frac{\sigma_E}{E_0} \right)^2 = \frac{2}{2+D} \left(\frac{\sigma_{E,0}}{E_0} \right)^2 \quad D=-1 \Rightarrow \epsilon_x/2 \text{ and energy spread } \times \sqrt{2}$$

$B^* dB/dx \neq 0$ and $\eta_x \neq 0$

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

Short straight section : $\eta_x = 0.28$ m

$D=-1 \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

- $J_s=1$ damping in longitudinal plane
- high gradients?
- field homogeneity (injection, lifetime)
- radiation properties

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$$\epsilon_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

D: partition number due to radiation damping $J_x = 1 - D$

Generally, $D \sim 0$ and $J_x \sim 1$

Robinson theorem : $J_x + J_z + J_s = 4$

$$\epsilon_x = \epsilon_{x,0} \frac{1}{1-D} \quad \left(\frac{\sigma_E}{E_0} \right)^2 = \frac{2}{2+D} \left(\frac{\sigma_{E,0}}{E_0} \right)^2$$

$D=-1 \Rightarrow \epsilon_x/2$ and energy spread $\times \sqrt{2}$

$$D = \frac{\oint \frac{\eta_x}{\rho_x^3} ds + \frac{2}{B^2 \rho_x^2} \oint \eta_x B \frac{dB}{dx} ds}{\oint \frac{ds}{\rho_x^2}}$$

$B \cdot dB/dx \neq 0$ and $\eta_x \neq 0$

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

Short straight section : $\eta_x = 0.28$ m

$D=-1 \Rightarrow$

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- radiation properties

Desired ID effects: Robinson wiggler

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D: partition number due to radiation damping $J_x = 1 - D$

Generally, $D \sim 0$ and $J_x \sim 1$

Robinson theorem : $J_x + J_z + J_s = 4$

$$\varepsilon_x = \varepsilon_{x,0} \frac{1}{1-D} \quad \left(\frac{\sigma_E}{E_0} \right)^2 = \frac{2}{2+D} \left(\frac{\sigma_{E,0}}{E_0} \right)^2$$

$D = -1 \Rightarrow \varepsilon_x / 2$ and energy spread $\times \sqrt{2}$

$$D = \frac{\oint \frac{\eta_x}{\rho_x^3} ds + \frac{2}{B^2 \rho_x^2} \oint \eta_x B \frac{dB}{dx} ds}{\oint \frac{ds}{\rho_x^2}}$$

$B \cdot dB/dx \neq 0$ and $\eta_x \neq 0$

Short straight section : $\eta_x = 0.28$ m

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

$D = -1 \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/)
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

- $J_s = 1$ damping in longitudinal plane
- high gradients?
- field homogeneity (injection, lifetime)
- radiation properties

Desired ID effects: Robinson wiggler

$$\epsilon_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

D: partition number due to radiation damping $J_x = 1 - D$

Generally, $D \sim 0$ and $J_x \sim 1$

Robinson theorem : $J_x + J_z + J_s = 4$

$$\epsilon_x = \epsilon_{x,0} \frac{1}{1-D} \quad \left(\frac{\sigma_E}{E_0} \right)^2 = \frac{2}{2+D} \left(\frac{\sigma_{E,0}}{E_0} \right)^2 \quad D=-1 \Rightarrow \epsilon_x/2 \text{ and energy spread } \times \sqrt{2}$$

$$D = \frac{\oint \frac{\eta_x}{\rho_x^3} ds + \frac{2}{B^2 \rho_x^2} \oint \eta_x B \frac{dB}{dx} ds}{\oint \frac{ds}{\rho_x^2}}$$

η_x = dispersion function

ρ_x = radius of curvature due to B

$B \cdot dB/dx \neq 0$ and $\eta_x \neq 0$

Short straight section : $\eta_x = 0.28 \text{ m}$

Application to SOLEIL

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Robinson theorem : $J_x + J_z + J_s = 4$

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$$D = \frac{\oint \frac{\eta_x}{\rho_x^3} ds + \frac{2}{B^2 \rho_x^2} \oint \eta_x B \frac{dB}{dx} ds}{\oint \frac{ds}{\rho_x^2}}$$

η_x = dispersion function

ρ_x = radius of curvature due to B

$B \cdot dB/dx \neq 0$ and $\eta_x \neq 0$

Short straight section : $\eta_x = 0.28 \text{ m}$

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

$$D=-1 \Rightarrow \frac{B_{w,z}^2}{2g} \approx 89 \text{ T}^2/\text{m}$$

Type	B(T)	g (mm)	dB/dx (T/
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

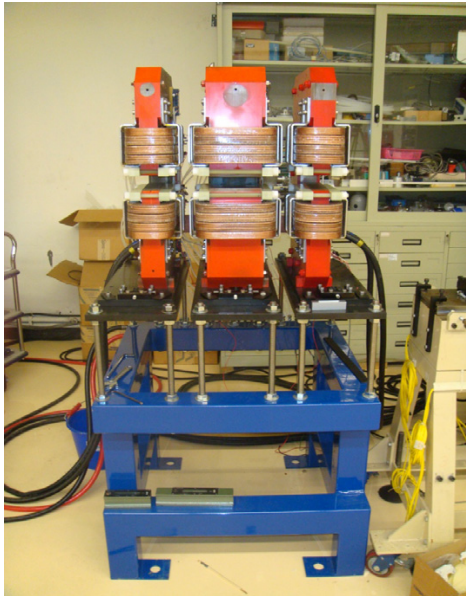
- $J_s=1$ damping in longitudinal plane
- high gradients?
- field homogeneity (injection, lifetime)
- radiation properties

Desired ID effects: Robinson wiggler

CERN PS (1983)

damping of horizontal betatron oscillations

$J_x=3$ et $D = -2$

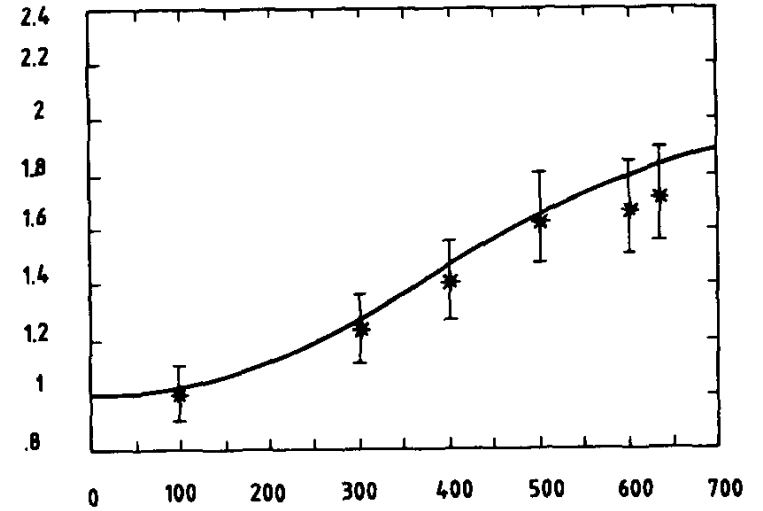


Y. Baconnier et al, Emittance control of the PSe± beamas using A Robinson wiggler, Nucl. Instr. Meth.A 234 (1985) 244-252 Nucl. Instr. Meth.A266 (1988) 24-31.

*Lee SY Kolski J Review of Scientific Instruments 78, 075107 (2007)
Z.W Huang et al. IPAC 2010, 3186, PAC 2011, 1265*

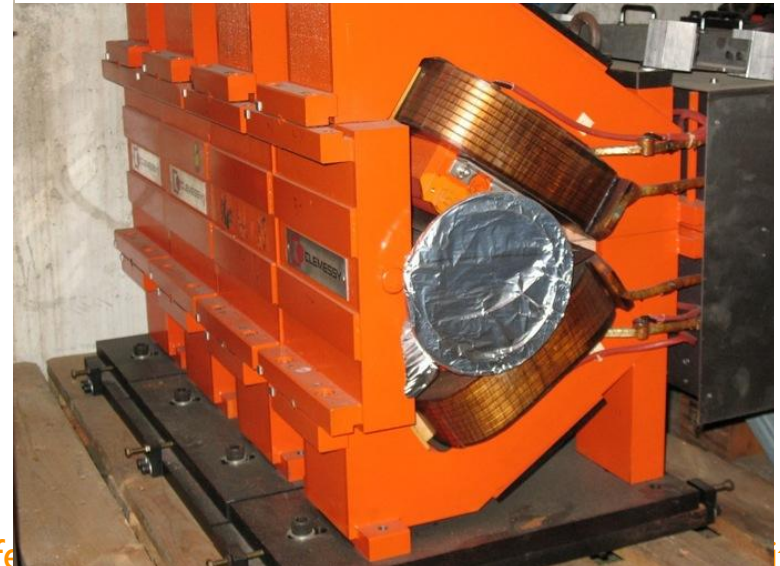
$\frac{J_x(lw)}{J_x(lw=0)}$

Test in DCI

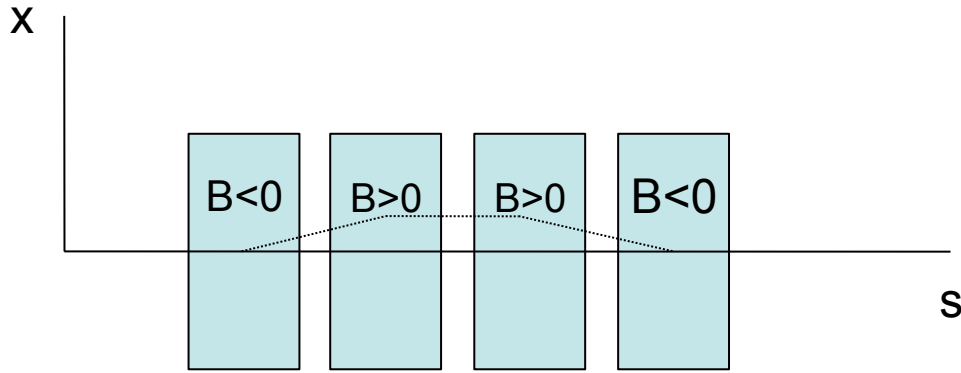


(b)

lw (A)



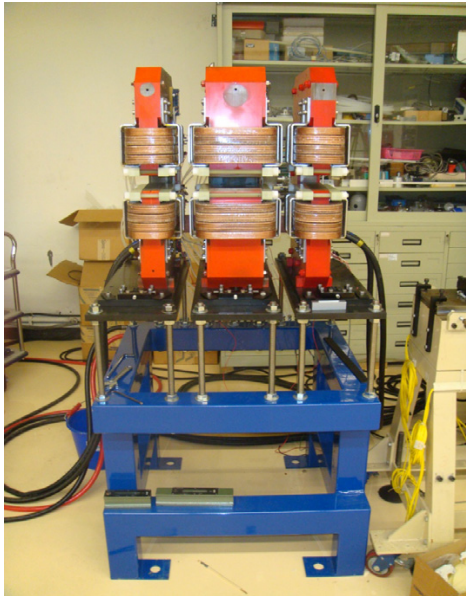
Desired ID effects: Robinson wiggler



CERN PS (1983)

damping of horizontal betatron oscillations

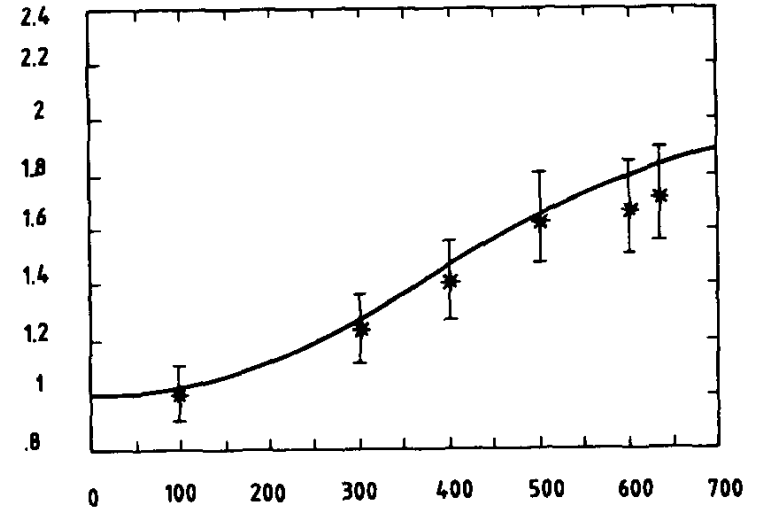
$J_x = 3$ et $D = -2$



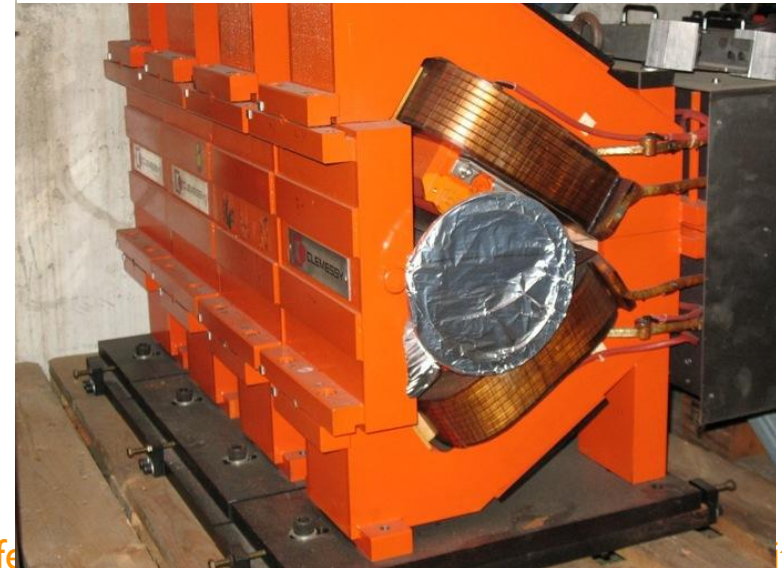
Y. Baconnier et al, *Emission control of the PSe± beamas using A Robinson wiggler*, Nucl. Instr. Meth.A 234 (1985) 244-252 Nucl. Instr. Meth.A266 (1988) 24-31.

Lee SY Kolski J *Review of Scientific Instruments* 78, 075107 (2007)
Z.W Huang et al. *IPAC 2010*, 3186, PAC 2011, 1265

Test in DCI
 $\frac{J_x(I_w)}{J_x(I_w=0)}$



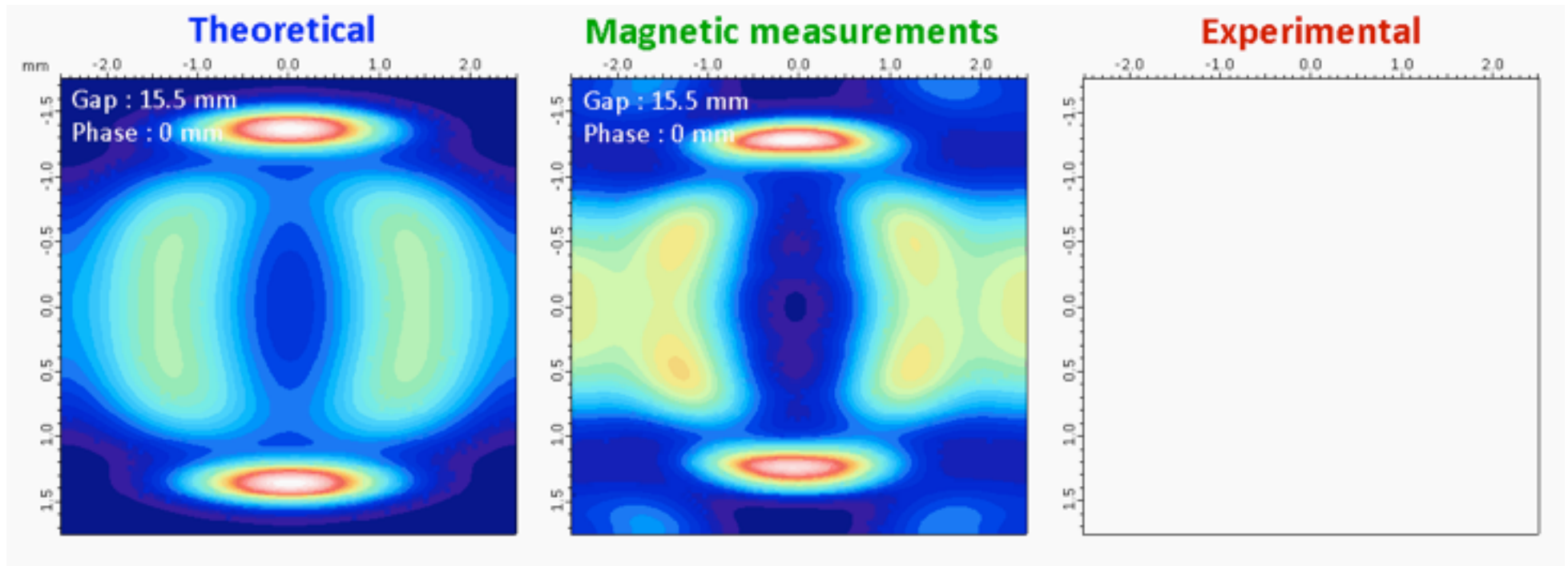
(b) Iw (A)



Conclusion

Interesting prospects with the advanced permanent magnet based insertion devices
New technological developments towards short period high fields

Superconducting undulators and wiggler are also quickly developing :
Thermal budget (resistance wall and synchrotron radiation) =>with (larger gap) /without
thermal shield
procedure of magnetic field correction



$$\phi(z) = \frac{2\pi}{\lambda} \left[\frac{z}{2\gamma^2} + \int_{-L/2}^z \frac{\beta_x^2(z') + \beta_y^2(z')}{2} dz' \right]$$

In vac NSLS P. Stefan et al. J. Synchrotron Rad. (1998)

H. Hsieh et al. NIM A246, 1983, 79

Quasi periodic PM EPU: PERA undulators

PERA undulators

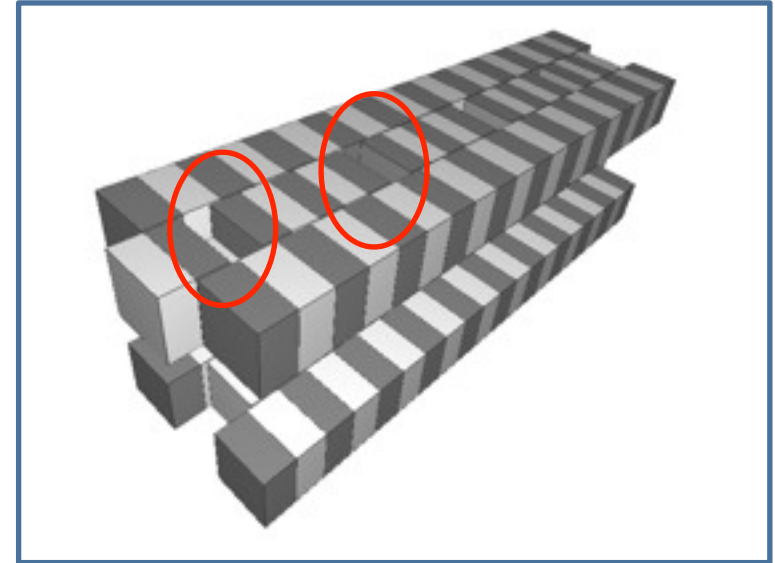
Modes	Bz [T]	Bx [T]
Linear H.	0,2	
Linear V.		0,26
Circular	-	

Undulator :

- Period : 30 mm
- Minimal gap : 15,5 mm

Magnets :

- NdFeB
- Size : 30 x 30 mm
- $B_r : 1,26 \text{ T}$
- $\Theta_{\text{mag}} = 0^\circ$
- $X_{\text{dist}} = 1 \text{ mm}$

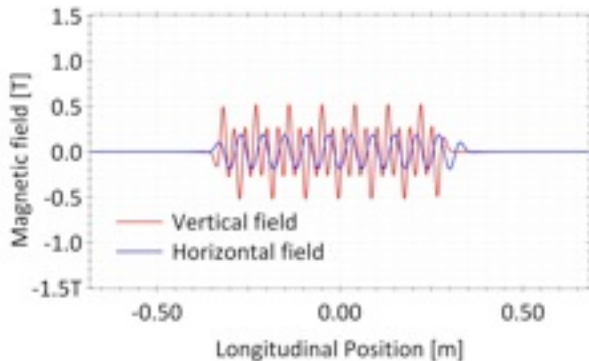


- No phase motion
- Linear polarization only
- Combination of different period length

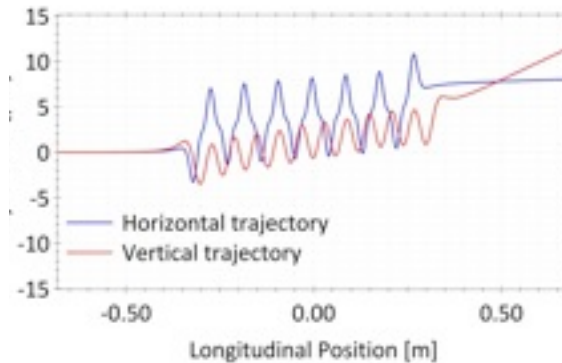
- Magnets creating aperiodicity have reduced height and opposite direction of magnetisation.

S. Sasaki, B. Diaviacco and R. P. Walker, Synchrotrone Trieste Internal Report, ST/MTN-98/8

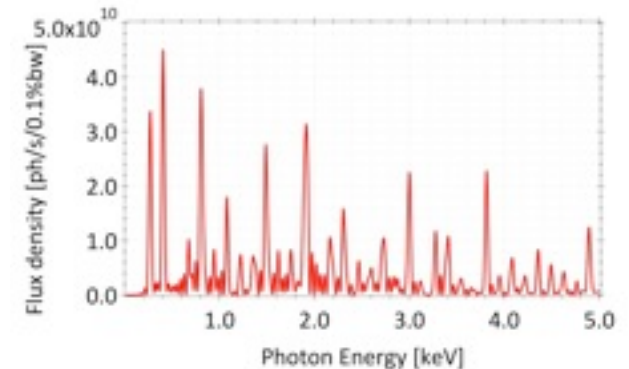
S. Sasaki, B. Diaviacco and R. P. Walker, Proceedings of EPAC 2008



H. & V. field values in linear mode



H. & V. trajectories in linear Horizontal (red line) and linear vertical (blue one)



Spectrum calculated for 400 mA, 2,75 GeV and zero emittance and energy spread,

Quasi periodic PM EPU: APPLE VIII

Apple VIII undulators

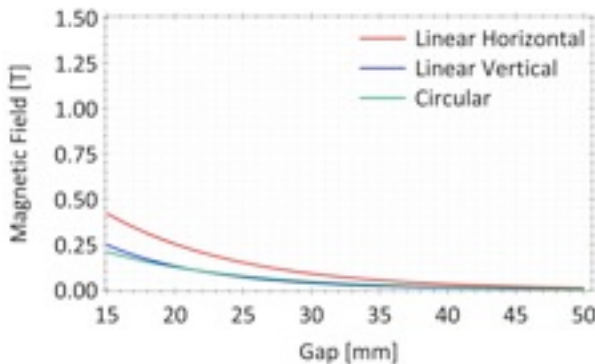
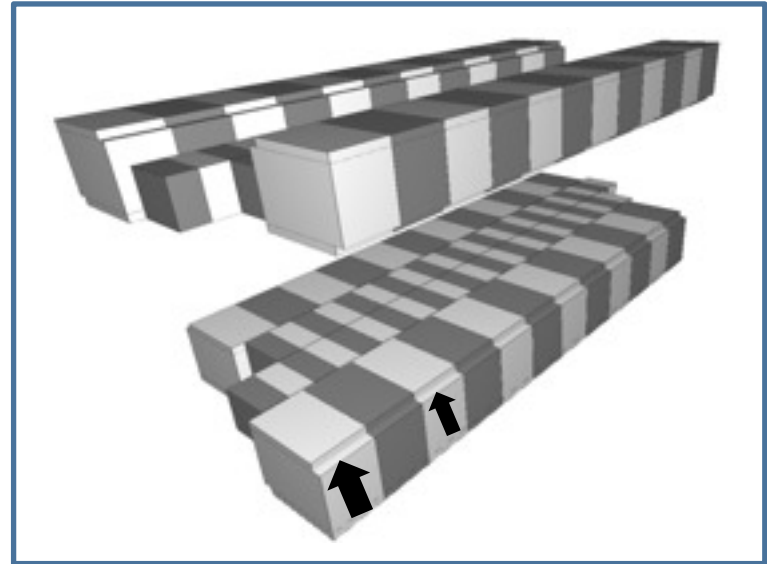
Modes	B_z [T]	B_x [T]
Linear H.	0,42	
Linear V.		0,24
Circular	0,21	

Undulator :

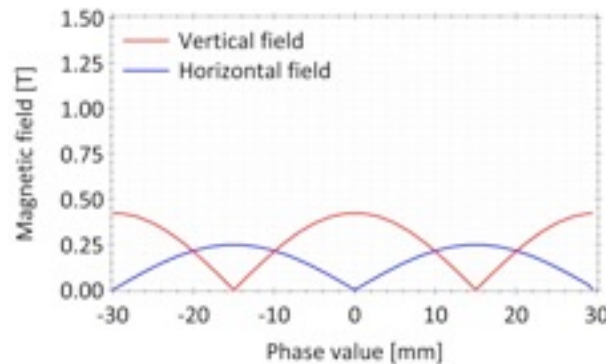
- Period : 30 & 60 mm
- Minimal gap : 15,5 mm

Magnets :

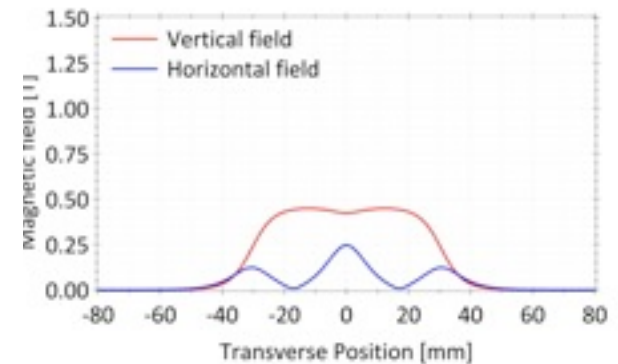
- NdFeB
- Size : 30 x 30 mm
 - 50 x 50 mm
- B_r : 1,26 T
- $\Theta_{mag} = 0^\circ$
- $X_{dist} = 1$ mm



H. & V. field values versus gap at 0 mm shift.



H. & V. field values versus shift at minimal gap



H. & V field roll-off at minimal gap,

S. Sasaki, B. Diviacco and R. P. Walker, Proceedings of European Particle Accelerator Conference, Sweden (1998)

S. Sasaki, Nuclear Instruments and Methods A347, 83 (1994)

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Quasi periodic PM EPU: APPLE VIII

Apple VIII undulators

- Complex structure
- Aperiodicity
- Low on-axis power density

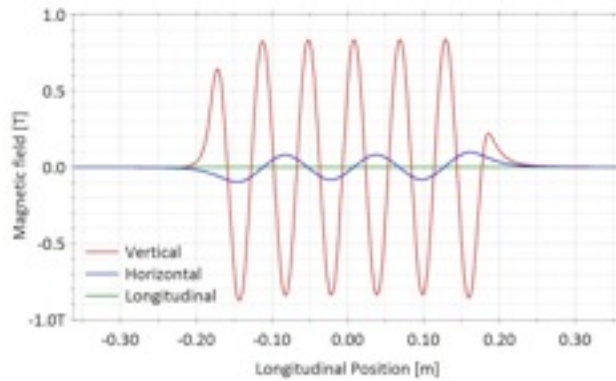


Fig. 1 : Magnetic fields at minimal gap and 0 mm shift

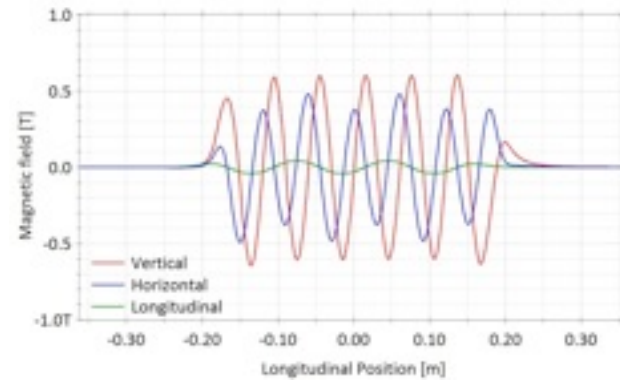


Fig. 1 : Magnetic fields at minimal gap and $\lambda/4$ mm shift

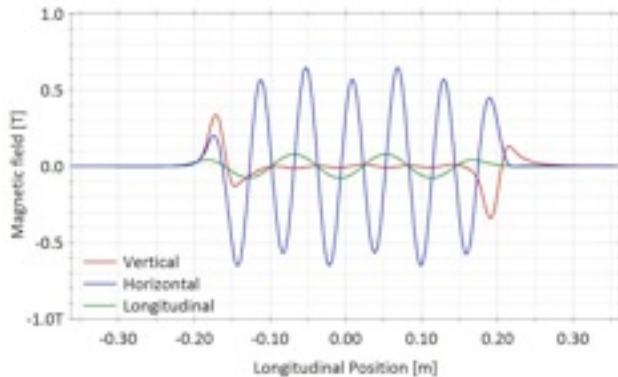


Fig. 1 : Magnetic fields at minimal gap and $\lambda/2$ mm shift

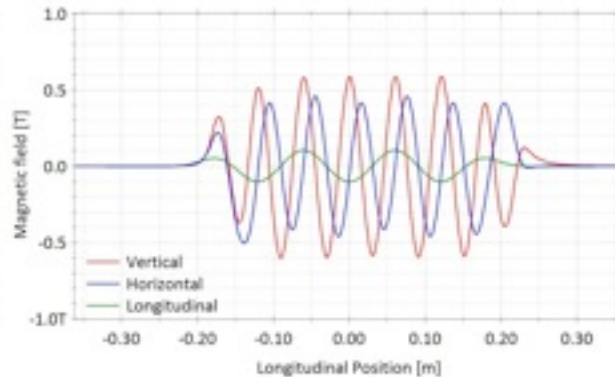


Fig. 1 : Magnetic fields at minimal gap and $3\lambda/4$ mm shift

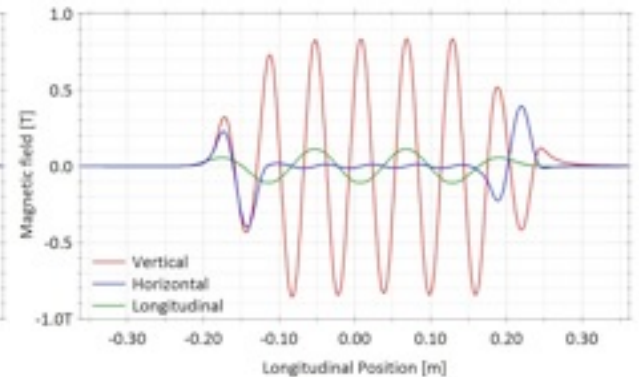
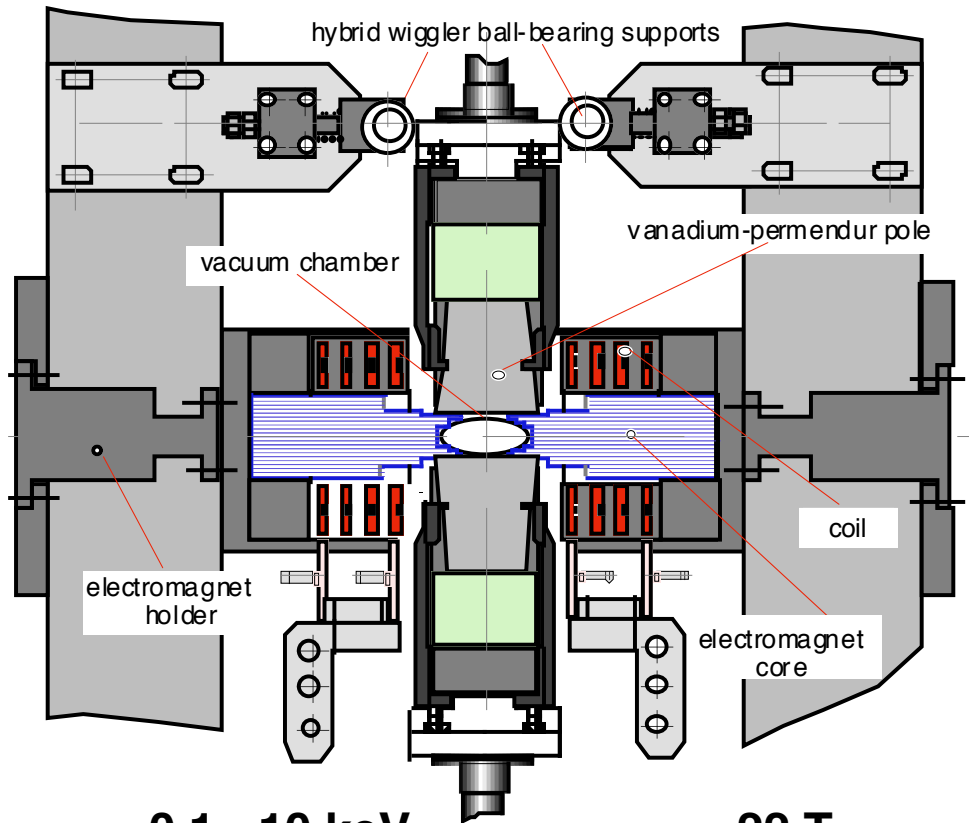


Fig. 1 : Magnetic fields at minimal gap and λ mm shift

ElectroMagnetic Permanent magnet Helical Wiggler

Modification of the polarisation at 100 Hz

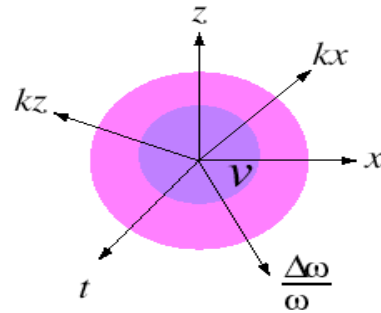
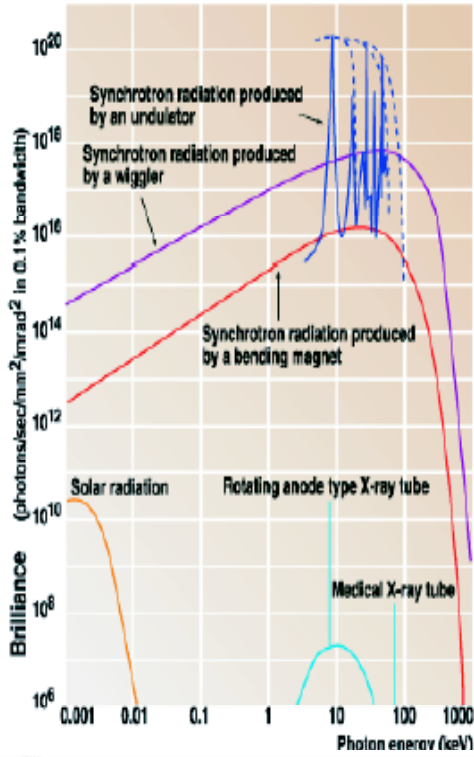
Gluskin et al.



0.1 - 10 keV
(2.6 keV)

.22 T
 $B_v = 0.8 \text{ T}$
 $\lambda_0 = 16 \text{ cm}$

Light Source Context



B: Nber of photons / phase space cell

$$V = \Delta x \Delta x' \Delta z \Delta z' \Delta t \Delta \omega / \omega$$

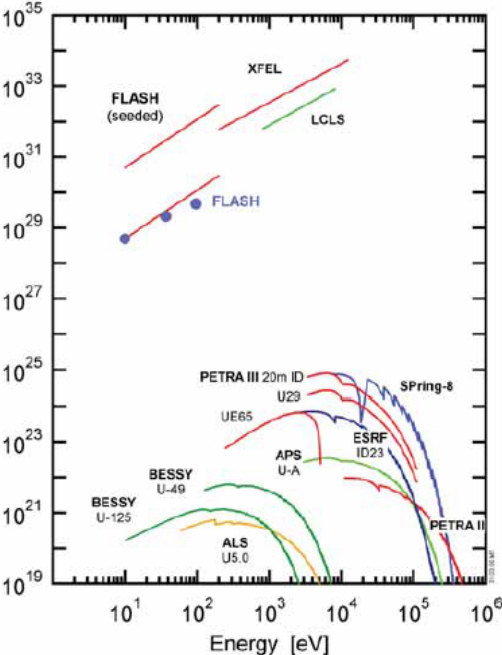
diffraction limit:
 $\Delta x \cdot \Delta x' \sim \lambda / 2\pi$

Fourier limit : $\Delta \omega \cdot \Delta T \sim 1$

Gaussian beams case :
 $c \Delta t \cdot \Delta \lambda / \lambda^2 = 0.44$

Synchrotron radiation used as spontaneous emission for the production of coherent intense radiation (emitters in phase)

Higher harmonics



generation	accelerator	
1	storage ring	parasitic use of synchrotron radiation
2	storage ring	few undulators, $\epsilon \sim \text{few } 10 \text{ nm} \cdot \text{rad}$
3	storage ring	Long straight sections for ID, $\epsilon \sim \text{few nm} \cdot \text{rad}$ Ultimate storage ring
4	Linac ERL	fs pulses, $\epsilon \sim \epsilon_n / E$ longitudinal coherence for FEL
5	LWFA	LWFA based FEL

op on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

❖ Horizontal (natural) Emittance:

$$\epsilon_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

J_x = Horizontal damping partition number

❖ Horizontal emittance is determined by the equilibrium between the quantum excitation due to the emission of photons and the damping due to the RF acceleration field used to compensate the energy loss of the synchrotron radiation.

❖ J_x is related to the **damping partition D** by : $J_x = 1 - D$

where

$$D = \frac{\frac{1}{2\pi} \oint \frac{\eta_x(s)}{\rho_x} \left[\frac{1}{\rho_x^2} + 2K(s) \right] ds}{\oint \frac{ds}{\rho_x^2}}$$

(the integral is to be evaluated only in dipoles).

- ❖ For an isomagnetic storage ring with separate function magnets, where $K(s) = 0$ in dipoles,

$$D = \frac{1}{2\pi\rho} \oint \frac{\eta(s)}{\rho_x} ds = \frac{\alpha R}{\rho_x}$$

- ❖ Since the momentum compaction $\alpha \ll 1$ then $D \ll 1$ for separate function machines.

- ❖ And since $J_x = 1 - D$

- ❖ Then, for an isomagnetic storage ring with separate function magnets, $J_x = 1$

Such as : $J_x + J_z + J_s = 4$ where $J_z = 1$ and $J_s = 2$

- ❖ Looking at the general expression of the damping partition D , J_x and \mathcal{E}_x :

$$D = \frac{1}{2\pi} \oint \frac{\eta_x(s)}{\rho_x} \left[\frac{1}{\rho_x^2} + 2K(s) \right] ds$$

$$J_x = 1 - D$$

$$\mathcal{E}_x = \frac{C_q \gamma^2 \langle H \rangle_{dipole}}{J_x \rho_x}$$

- ❖ If we can make $D = -1$ \longrightarrow $J_x = 2$

And the horizontal emittance can be divided by a factor 2!

Such as: $J_x + J_z + J_s = 4$ where $J_z = 1$ and $J_s = 1$

- ❖ Note that D depends on the dispersion function $\eta(s)$ and the quadrupole strength $K(s)$

$$D = \frac{\frac{1}{2\pi} \oint \frac{\eta_x(s)}{\rho_x} \left[\frac{1}{\rho_x^2} + 2K(s) \right] ds}{\oint \frac{ds}{\rho_x^2}}$$

- ❖ And can be re-written:

$$D = \frac{\frac{1}{2\pi} \left(\oint \frac{\eta_x}{\rho_x^3} ds + \frac{2}{B^2 \rho_x^2} \oint \eta_x B \frac{dB}{dx} ds \right)}{\oint \frac{ds}{\rho_x^2}}$$

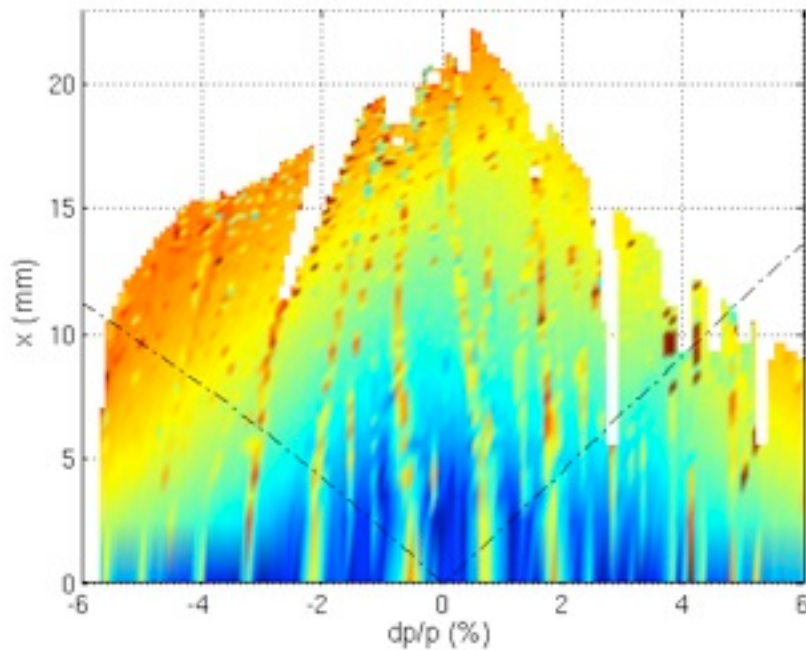
A magnetic element introducing the product $B * dB/dx$ in a straight section where the dispersion η_x is non zero contributes to the modification of D .

SOLEIL energy acceptance

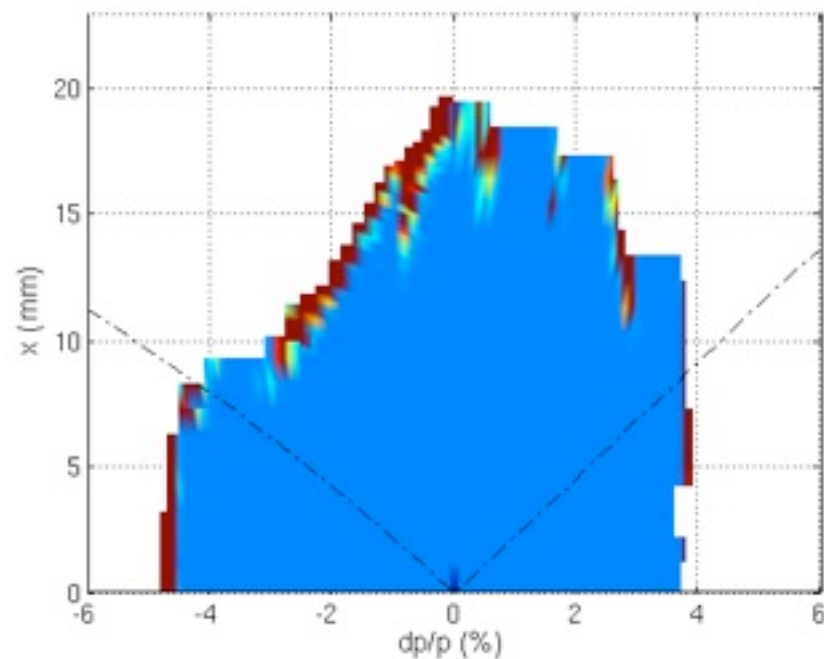
The energy acceptance of the bare machine is large : +/- 4%

Off-momentum (dp/p , x) map

Calculated



Measured

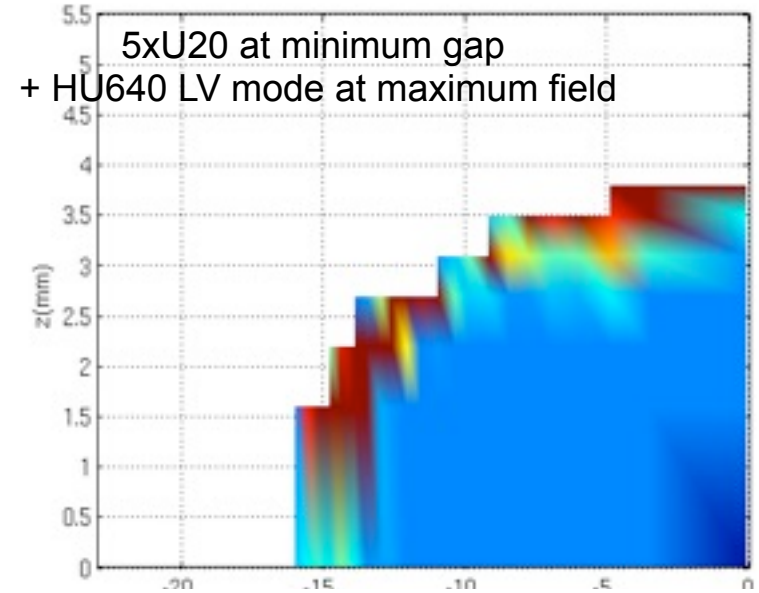
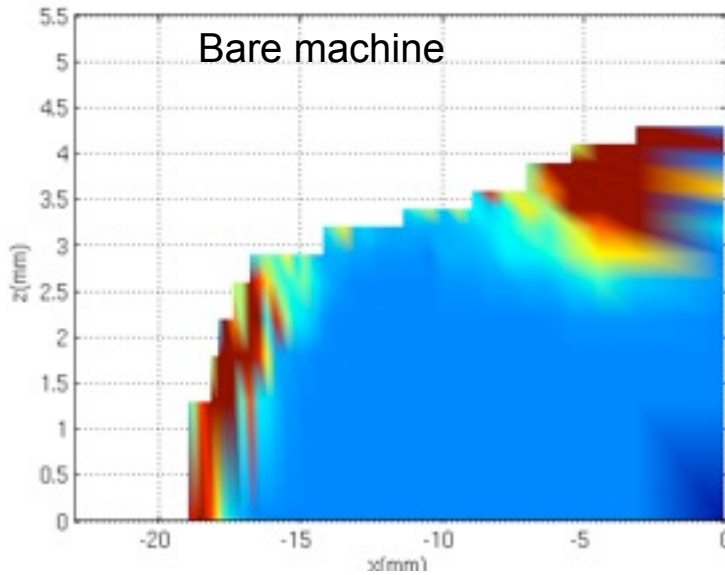


Vacuum chamber at 12 mm

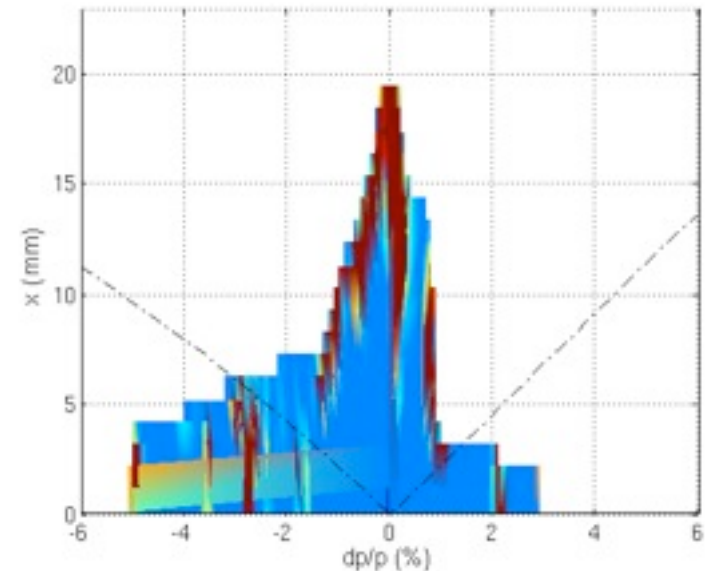
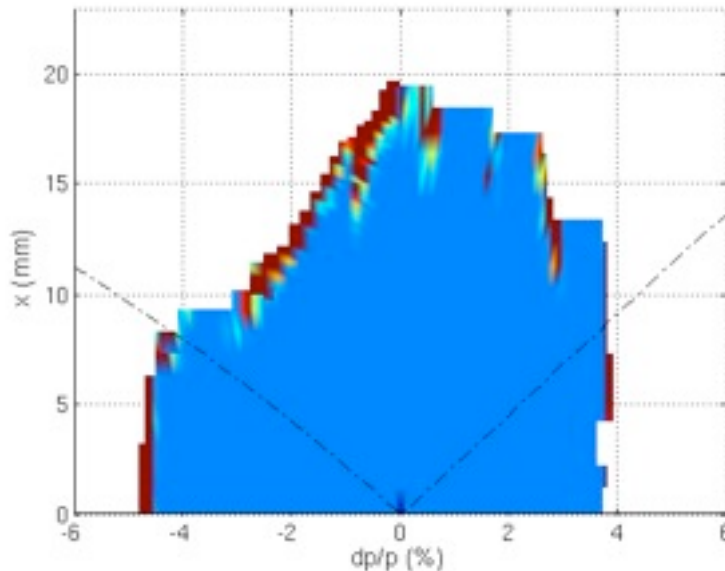
Effect on injection efficiency

Reduction of the on-momentum dynamic aperture and the energy acceptance in the presence of IDs => reduction of the injection rate

Measured
on-
momentum
(x, z) map



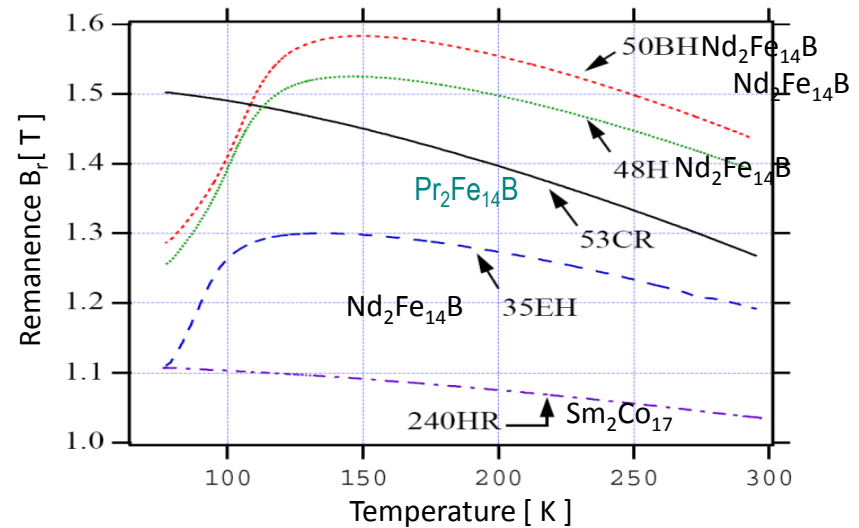
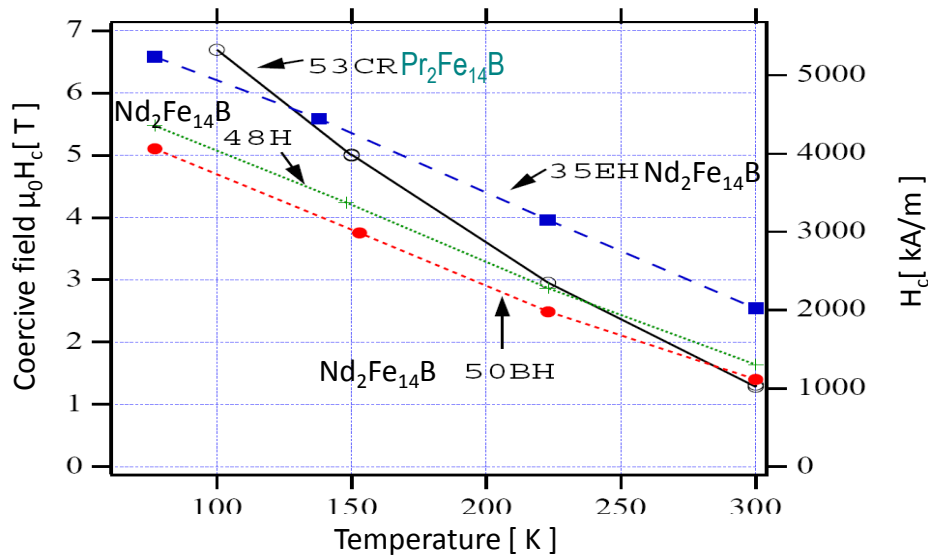
Measured
off-
momentum
(dp/p, x)
map



Rare Earth Magnet behaviour versus temperature

M. Sagawa et al. *J. Magn. Magn. Mater.* 70, 316 (1987)

T. Hara et al. *APAC2004*, Gyeongju, Korea, 216



Spin Transition Reorientation

NdFeB strong Magneto-Crystalline Anisotropy (MCA) => orientation along [001]

Magneto-crystalline orientation given by the energy : $E(T) = K_1 \sin^2(\theta) + K_2 \sin^4(\theta)$, θ angle between the magnetisation and [001]

at room temperature : magnetisation // c

Fe MCA independant of T, Nd : K_1 // [001] dominant at room T and K_2 // [110] at low T

D. Givord et al. *Solid State Comm.* 51 (1984) 857

L. M. Garcia et al. *Phys. Rev. Lett.* 85 (2) 429

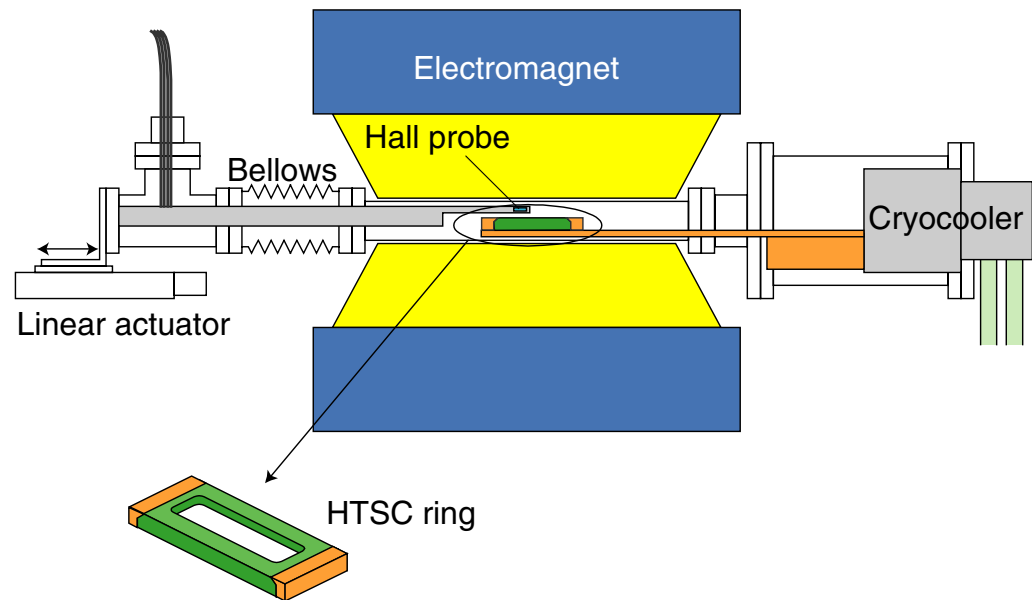
M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Examples of CPMU

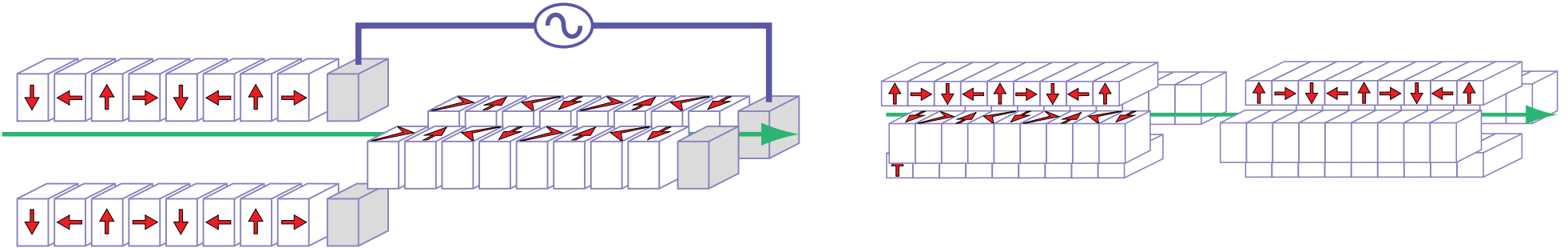
Lab.	Tech.	Period (mm)	Magnet	Br (T)	H_{c1} (kA/m)	Installation	Length (m)	Reference
SPring-8	PPM	15	Nd ₂ Fe ₁₄ B,	1.41	1114	Lab	0.6	T. Hara, et al., Phys. Rev. Spec. Topics 7, 050702 (2004)
NLSII	Hybrid	14.5	Nd ₂ Fe ₁₄ B	1.37		Lab	0.11	T. Tanabe, et al., AIP Conference Proceedings, Vol. 1234, p.29 (2010). 4.85 mm gap
SLS/SPring-8	Hybrid	14	Nd ₂ Fe ₁₄ B	1.33	1670	3G	1.7	T. Tanaka, et al., Phys. Rev. Spec. Topics 12, 120702 (2009)
ESRF n°1	Hybrid	18	Nd ₂ Fe ₁₄ B	1.16	2400	3G	2	J. Chavanne et al., PAC09,
ESRF n°2	Hybrid	18	Nd ₂ Fe ₁₄ B	1.16	2400	3G	2	J. Chavanne et al., IPAC 2008 2011, 3245
DIAMOND/ Danfysik	Hybrid	17.7	Nd ₂ Fe ₁₄ B	1.31	1670	3G	2	C. Benabderrahmane et al. NIMA A 669 (2012) 1-6
SOLEIL	Hybrid	20	Nd ₂ Fe ₁₄ B	1.41	1114		0.08	C. Benabderrahmane et al. NIMA A 669 (2012) 1-6
SOLEIL	Hybrid	18	Pr ₂ Fe ₁₄ B	1.35	1355		0.072	
SOLEIL	Hybrid	18	Pr ₂ Fe ₁₄ B	1.35	1355	3G	2	C. Benabderrahmane et al IPAC 2011
BESSY/UCLA	Hybrid	9	Pr ₂ Fe ₁₄ B			5G	2	J. Bahrndt et al. IPAC10, 3111 fixed gap=2.5 mm
NLSII/ADC	Hybrid	18	Nd ₂ Fe ₁₄ B			3G	2	T. Tanabe, et al.
NLSII	Hybrid	17				3G	2.7	T. Tanabe, et al., PAC 2011, 2090
SOLEIL/ LUNEX5	Hybrid	12-15	Nd _{2-x} Pr _{2x} Fe ₁₄ B			4-5G	3-5	

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

High Tc Tanaka PRST et New Journal of Physics

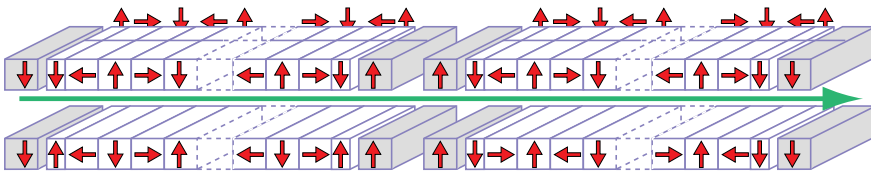


Permanent magnets EPU



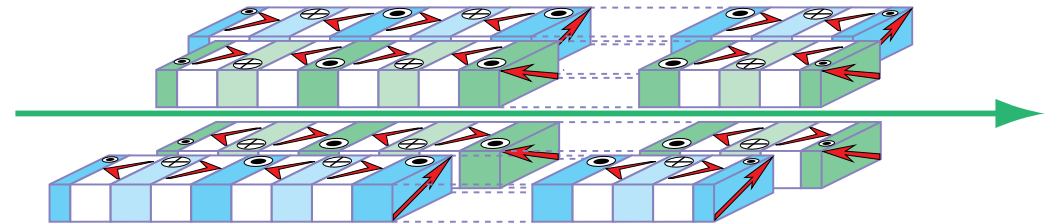
Cross undulators :

M. Moissev et al. Sov. Phys. J. 21, 332, 1978
K. J. Kim NIMA219, 426 (1986)



Helios et al.

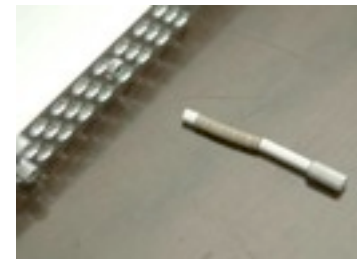
Onuki et al.



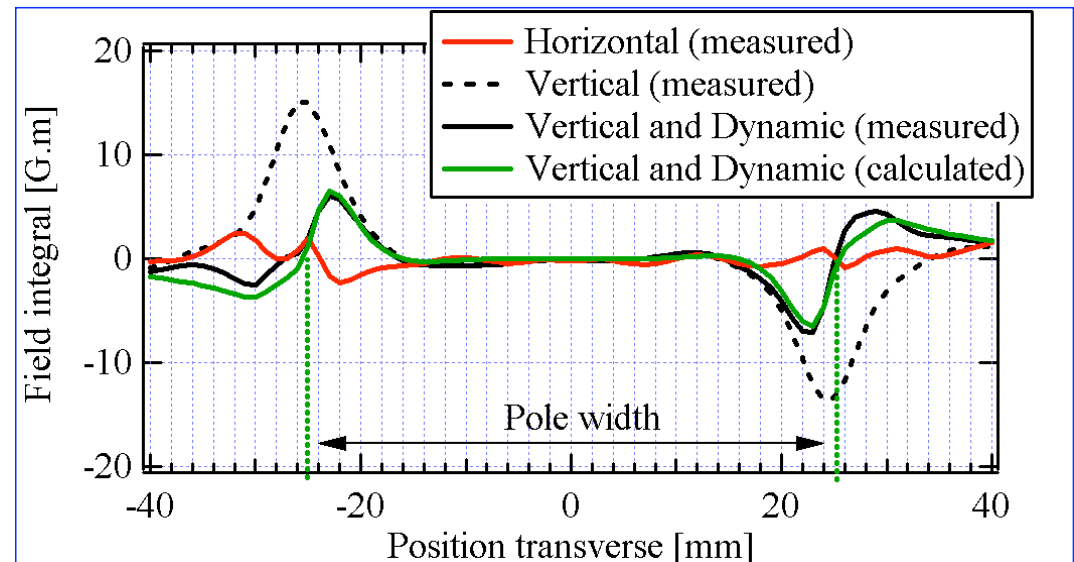
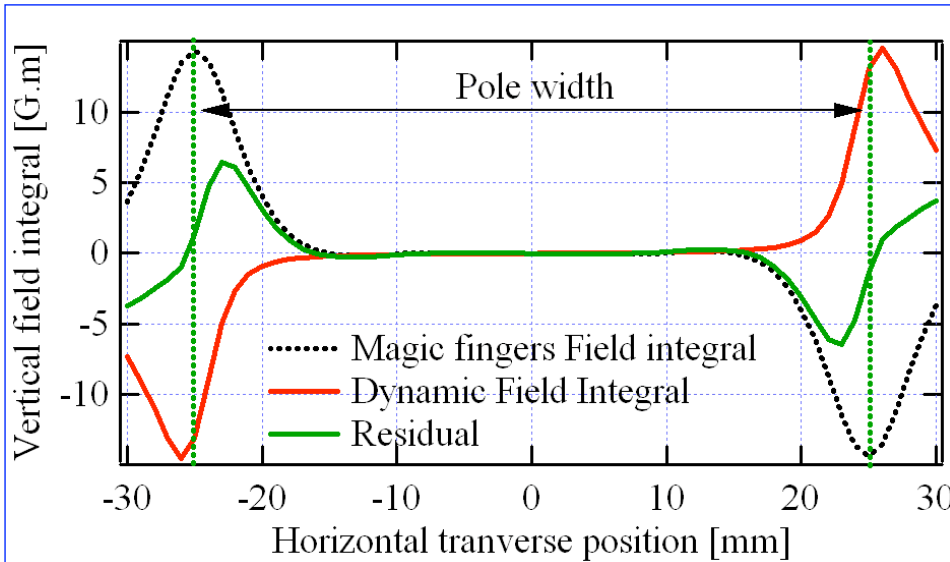
Sasaki et al.

Dynamic field integral compensation

Compensation of the dynamic integral by magic fingers



J. Safranek et al, *Phys. Rev. Special Topics* (2002), Vol. 5, 010701, pp. 1-7
 O. Marcoullé et al, *IPAC 2011*, 3236



M. L. Couprie, ICA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility, March 5-7, 2012, invited

Desired ID effects: damping wiggler

$$\epsilon_{xw} = C_a \frac{E^2}{J_x} \frac{\langle \mathcal{H}/\rho^3 \rangle_0 + \langle \mathcal{H}/\rho^3 \rangle_w}{\langle 1/\rho^2 \rangle_0 + \langle 1/\rho^2 \rangle_w}$$

emittance : equilibrium between
quantum excitation and radiation
damping (loss of transverse momentum)
 J_x : horizontal partition number

$$\left\langle \frac{\mathcal{H}}{\rho^3} \right\rangle_w = \frac{1}{C} \oint_w \frac{\mathcal{H}}{\rho^3} ds = \frac{1}{\rho_w^3} \langle \mathcal{H} \rangle_w$$

$$\left\langle \frac{\mathcal{H}}{\rho^3} \right\rangle_0 = \frac{1}{C} \oint_0 \frac{\mathcal{H}}{\rho^3} ds = \frac{1}{\rho_0^3} \langle \mathcal{H} \rangle_0$$

$$\left\langle \frac{1}{\rho^2} \right\rangle_w = \frac{1}{C} \oint_w \frac{1}{\rho^2} ds = \frac{L_w}{C} \frac{1}{\rho_w^2}$$

$$\left\langle \frac{1}{\rho^2} \right\rangle_0 = \frac{1}{C} \oint_0 \frac{1}{\rho^2} ds = \frac{1}{\rho_0 R}$$

$$\mathcal{H} = \frac{1}{\beta} \left\{ \eta^2 + (\beta \eta' - \frac{1}{2} \beta' \eta)^2 \right\}$$

$$C_a = c C_q / (2 C_D)$$

$$C_q = \frac{55}{48\sqrt{3}} \frac{r_e \hbar c}{(mc^2)^6}$$

$$C_D = \frac{c}{3} \frac{r_e}{(mc^2)^3}$$

More damping with additional synchrotron radiation through installation of strong wiggler magnets places in a dispersion free location (for the equilibrium orbit to be independant of the particle energy)

$$\frac{\epsilon_{xw}}{\epsilon_{x0}} = \frac{1 + \left(\frac{\rho_0}{\rho_w} \right)^3 \frac{\langle \mathcal{H} \rangle_w}{\langle \mathcal{H} \rangle_0}}{1 + \frac{L_w}{2\pi\rho_0} \left(\frac{\rho_0}{\rho_w} \right)^2}$$

$$\frac{\sigma_{Ew}^2}{\sigma_{E0}^2} = \frac{1 + \frac{L_w}{2\pi\rho_0} \left(\frac{\rho_0}{\rho_w} \right)^3}{1 + \frac{L_w}{2\pi\rho_0} \left(\frac{\rho_0}{\rho_w} \right)^2}$$

+ corrections due to the own
dispersion created by the wiggler

H. Wiedemann, An ultra-low emittance mode for PEP using damping wigglers, Nucl. Instr. Meth. A266 (1988) 24-31.

K. Robinson, Radiation effects in Circular electron accelerators, Phys. Rev. 111 (2), 1958, 373

M. E. Couprie, ICFA Workshop on Future Light Source, Thomas Jefferson Nat. Acc. Facility. March. 5-9, 2012, Invited

Modelisation with field maps

HU36 undulator : Measured horizontal field integrals at 11.5 mm minimum gap

HU36 undulator : Measured vertical field integrals at 11.5 mm minimum gap

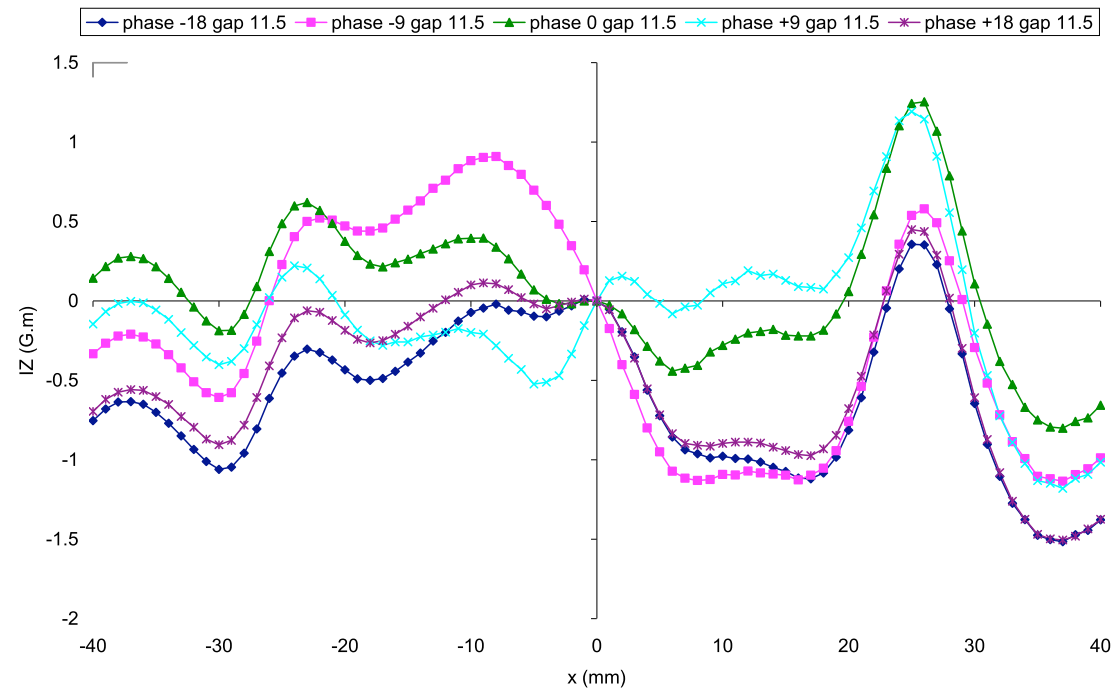
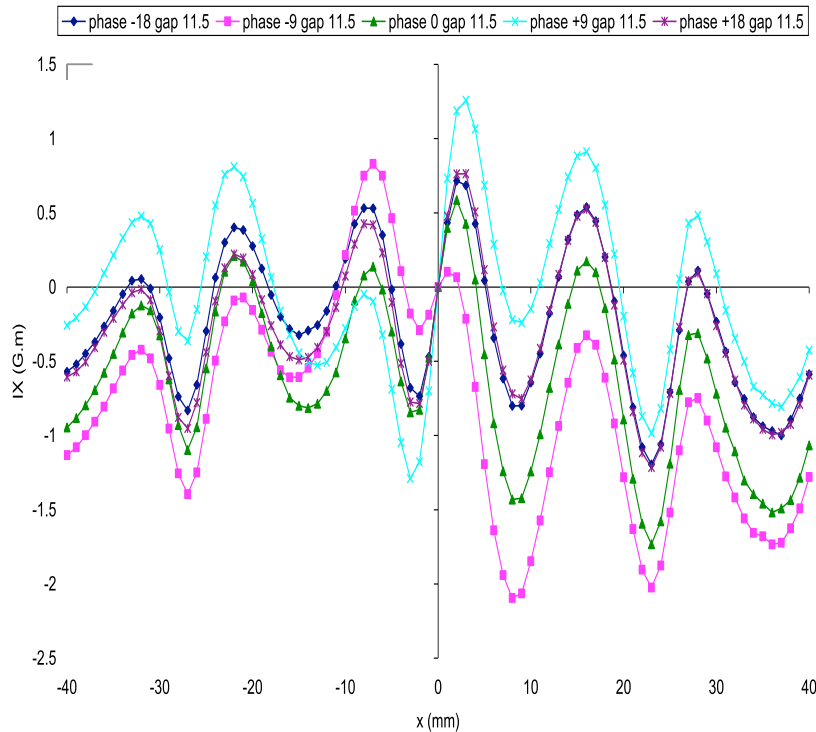


Figure8 or bi-periodic undulator

T. Tanaka, H. Kitamura, Nucl. Instrum. Methods A 346, 368-373

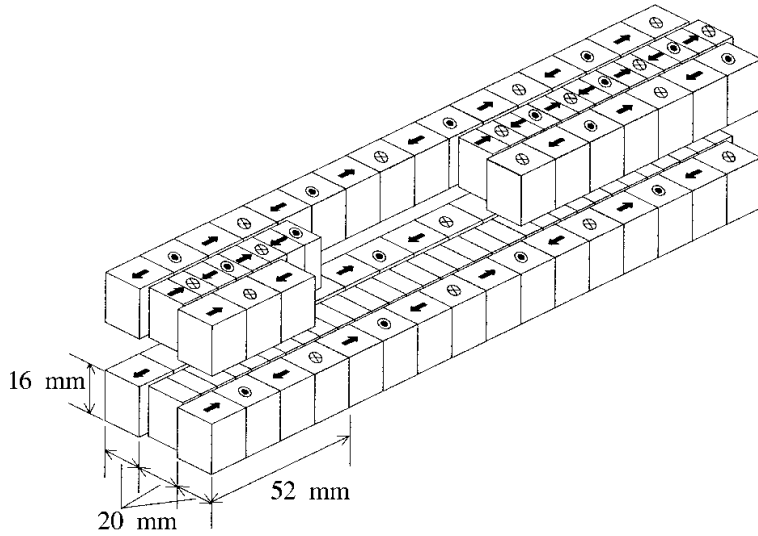
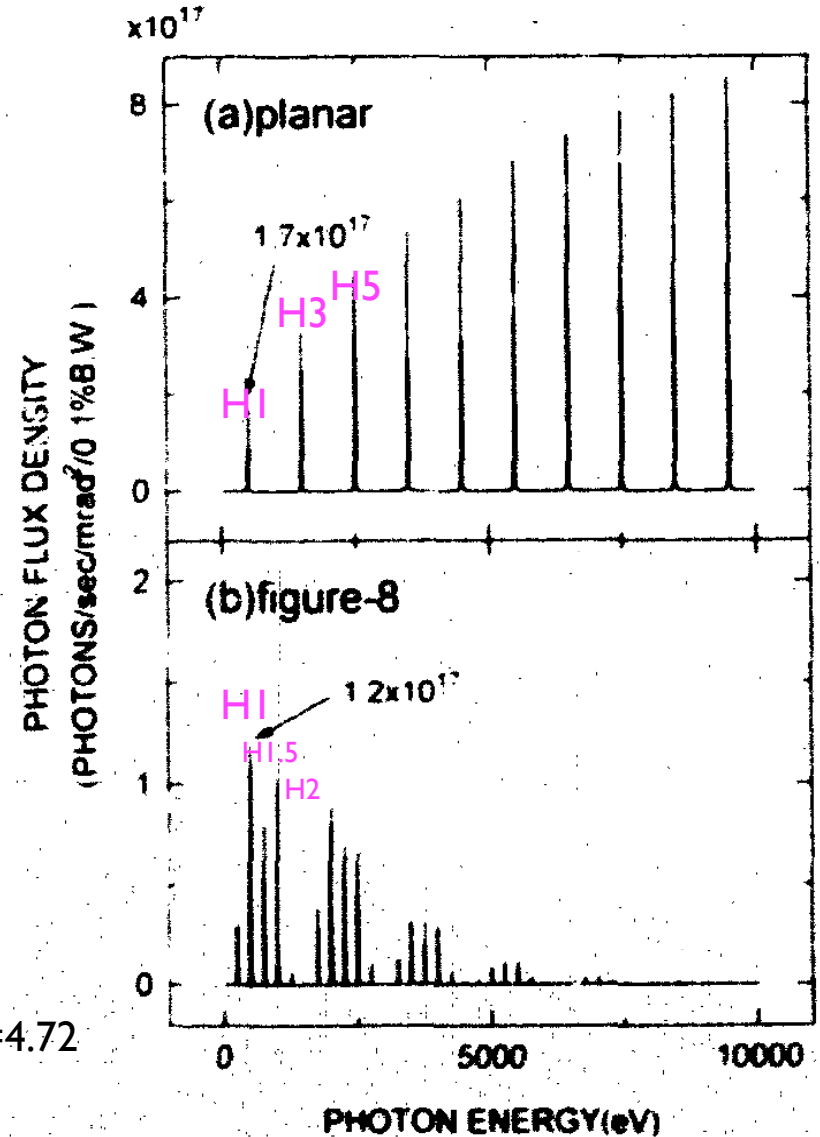


Figure 8

V. und. period = 2X H und. period

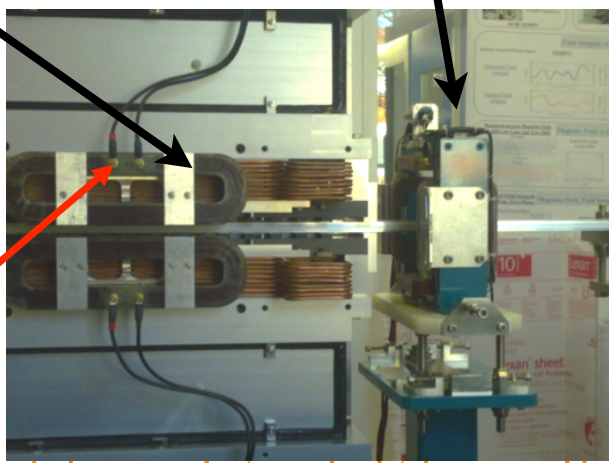
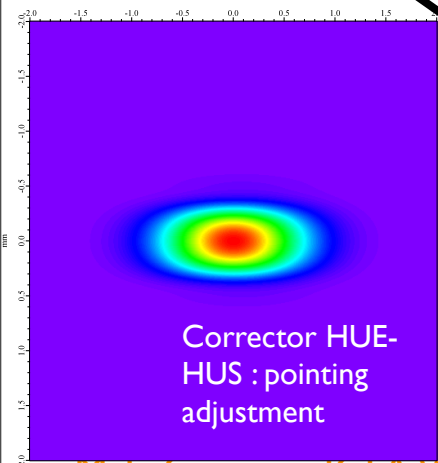
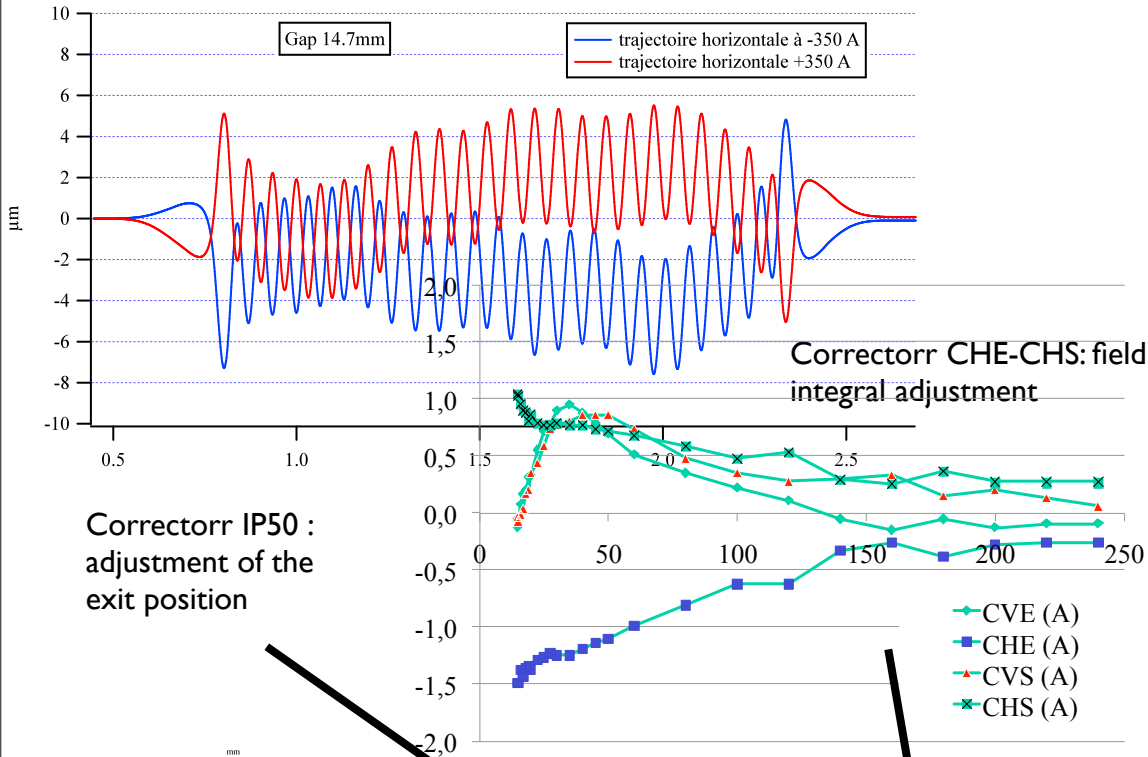
- Linear polarised soft X ray: on axis power density lower than for an ordinary undulator
- odd (LH), integer (LH), and half integer harmonics (LV)

On axis radiation, 8 GeV $K=4.72$
planar, Fig.8 $K_x=K_z=3.34$

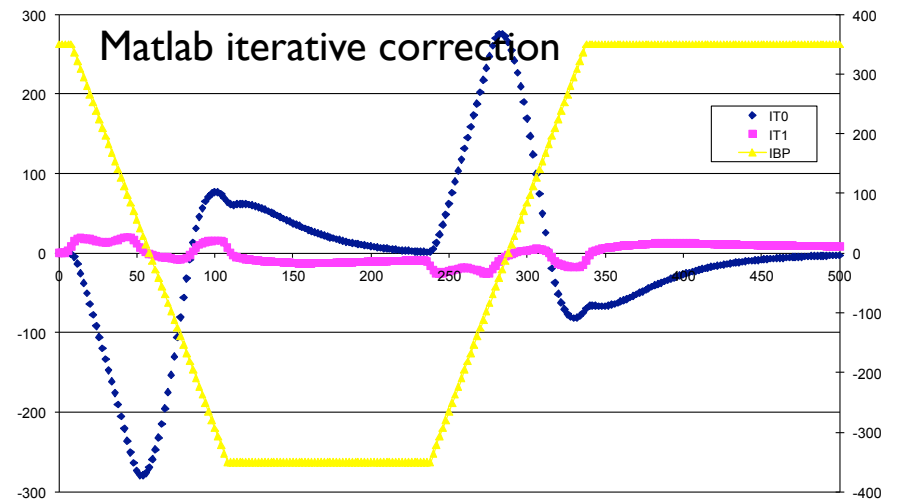
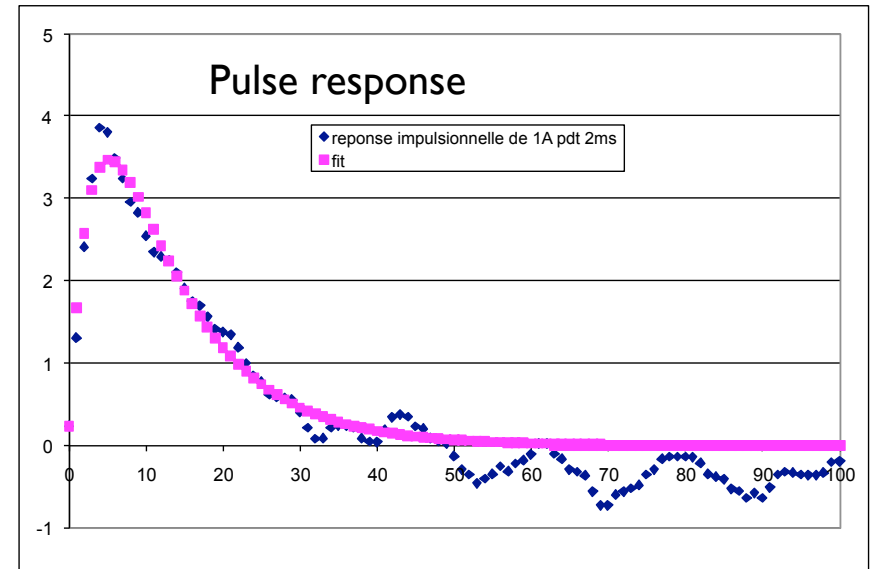


EMPHU @ SOLEIL

Static measurements



Dynamic measurements



Desired ID effects: Robinson wiggler

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

Short straight section : $\eta_x = 0.28$ m

\Rightarrow

$D = -I \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/)
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

- Questions :
- Js=I damping in longitudinal plane
 - high gradients?
 - field homogeneity (injection, lifetime)
 - radiation properties

Desired ID effects: Robinson wiggler

Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

$$D = \frac{\rho_0 \eta_x}{\pi (\rho_0 B_0)^2} \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle L_w$$

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($\rho_0 B_0 = 9.138 \text{ Tm}$ for SOLEIL)

Short straight section : $\eta_x = 0.28 \text{ m}$

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out of vacuum	1.4	11	140
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$$D = \frac{\rho_0 \eta_x}{\pi (\rho_0 B_0)^2} \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle L_w$$

B_w = wiggler peak field, L_w = wiggler length (2m) , g = wiggler gap

($\rho_0 B_0 = 9.138$ Tm for SOLEIL)

Short straight section : $\eta_x = 0.28$ m

\Rightarrow

$D = -1 \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/)
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Questions : - Js=I damping in longitudinal plane

- high gradients?
- field homogeneity (injection, lifetime)
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Application to SOLEIL

horizontal emittance : 3.7 nmrad \Rightarrow 1.85 nmrad

$$D = \frac{\rho_0 \eta_x}{\pi (\rho_0 B_0)^2} \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle L_w$$

B_w = wiggler peak field, L_w = wiggler length (2m) , g = wiggler gap

($\rho_0 B_0 = 9.138$ Tm for SOLEIL)

Short straight section : $\eta_x = 0.28$ m

$$D \approx 5.6 \times 10^{-3} \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle L_w$$

$$\frac{dB_{w,z}}{dx} \approx \frac{\hat{B}_{w,z}}{g} \Rightarrow \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle \approx \frac{\hat{B}_{w,z}^2}{2g}$$

$D = -1 \Rightarrow$

Type	B(T)	g (mm)	dB/dx (T/)
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

Questions : - Js=I damping in longitudinal plane

- high gradients?
- field homogeneity (injection, lifetime)
- radiation properties

Desired ID effects: Robinson wiggler

Application to SOLEIL

horizontal emittance : 3.7 nmrads \Rightarrow 1.85 nmrads

$$D = \frac{\rho_0 \eta_x}{\pi (\rho_0 B_0)^2} \left\langle B_w \frac{dB_{w,z}}{dx} \right\rangle L_w$$

B_w = wiggler peak field, L_w = wiggler length (2m), g = wiggler gap

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$$\frac{dB_{w,z}}{dx} \approx \frac{\hat{B}_{w,z}}{g} \Rightarrow \left\langle B_{w,z} \frac{dB_{w,z}}{dx} \right\rangle \approx \frac{\hat{B}_{w,z}^2}{2g}$$

$$D = -I \Rightarrow$$

$$\frac{\hat{B}_{w,z}^2}{2g} \approx 89 \text{ T}^2/\text{m}$$

Type	B(T)	g (mm)	dB/dx (T/)
out of vacuum	1.4	11	140
In vacuum	1.0	5.5	182

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- high gradients?
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- radiation properties