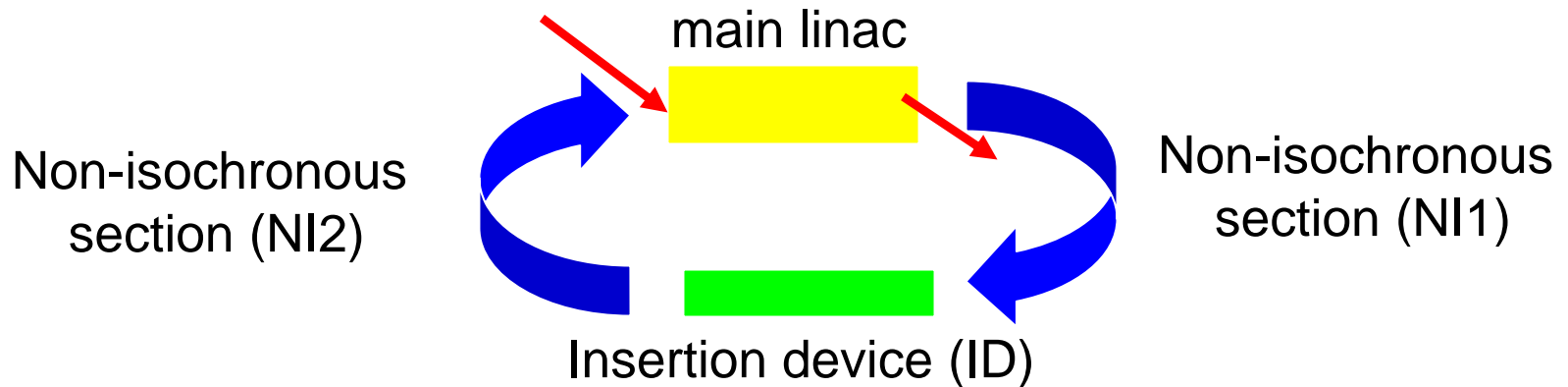


Longitudinal phase space manipulation at high and medium energy

■ Generic energy recovery linac:



- Injector \Rightarrow main linac (accelerate beam) \Rightarrow NI1: prepare beam for ID requirement \Rightarrow NI2: re-inject beam into linac on decelerating phase

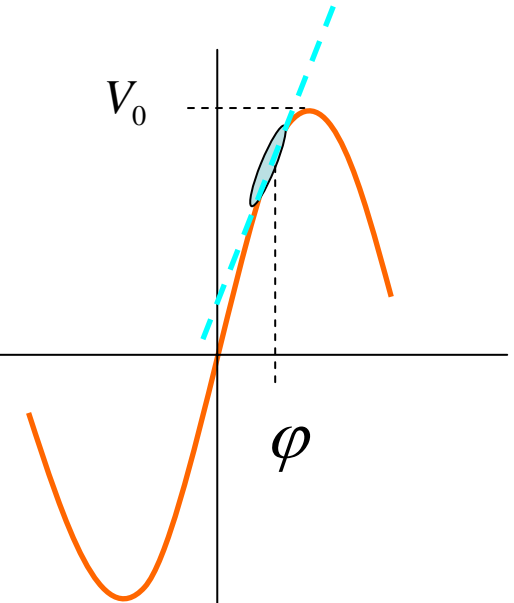
Linac to ID (linear theory)

Energy time correlation:

$$E(z) = E_0 + eV_0 \cos(kz + \varphi)$$

$$\delta = \frac{eV_0}{E_0 + eV_0 \cos \varphi} [\cos(kz + \varphi) - \cos \varphi] = \kappa z + O(z^2)$$

chirp: $\kappa \equiv \frac{d\delta}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \varphi} \sin \varphi$



Bunch compressor

$$z_f = z_i + R_{56} \delta_i$$

1st order momentum compaction

Final bunch length and energy spread (1st order):

$$\sigma_{z,f} = \sqrt{(1 + \kappa R_{56})^2 \sigma_{z,i}^2 + \underbrace{R_{56}^2 \sigma_{\delta,i}^2 E_0^2 / E^2}_{\text{Min bunch length}}}, \sigma_{\delta,f} = \sqrt{\kappa^2 \sigma_{z,i}^2 + \sigma_{\delta,i}^2 E_0^2 / E^2}$$

Min bunch length

getting very small at high energy!

Linac to ID (nonlinear effects)

■ Energy time correlation:

$$\delta = \kappa z + \mu z^2 + O(z^3)$$

■ Bunch compressor

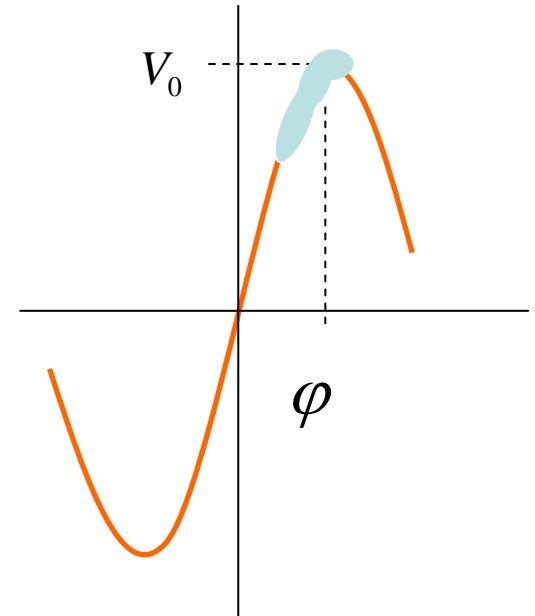
$$z_f = z_i + R_{56} \delta_i + T_{566} \delta_i^2$$

■ Final bunch length is minimized if

$$0 = z_i (1 + \kappa R_{56}) + \underbrace{z_i^2 (\mu R_{56} + \kappa^2 T_{566})}_{\text{Limit achievable minimum Bunch length}}$$

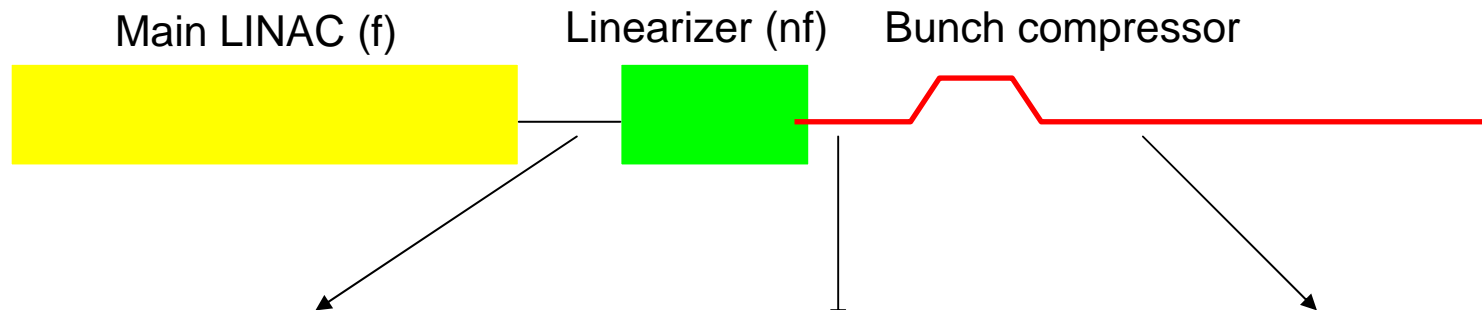
Limit achievable minimum
Bunch length

2nd order momentum
compaction

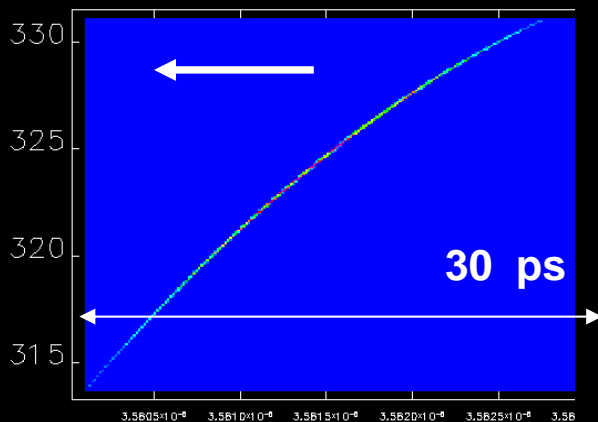


Higher order effects: pulse control

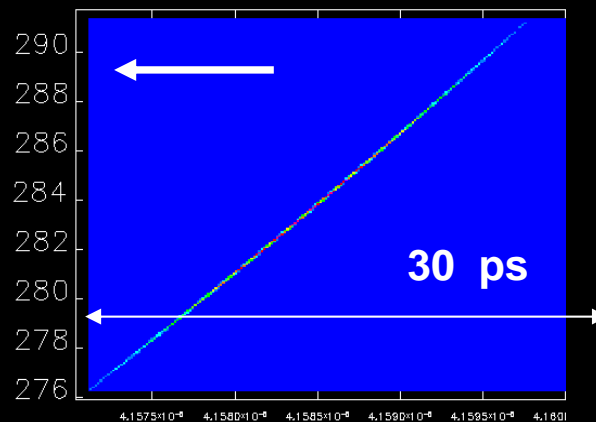
- Correction with higher harmonic rf-field provide two independent knobs (κ and μ parameters to minimize σ_z given R_{56} and T_{566}),
- sextupoles to some extent also provide these knobs



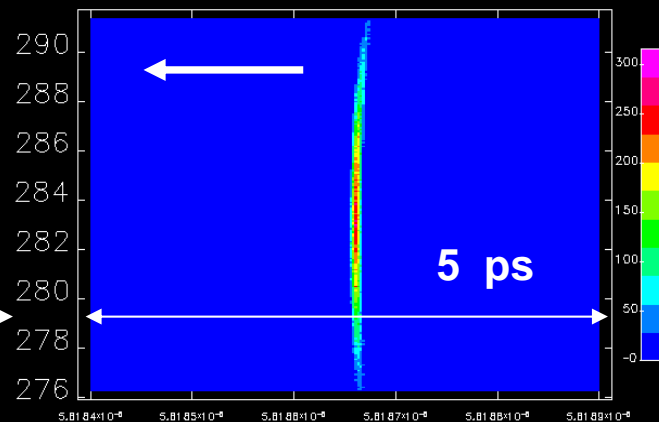
accelerating section



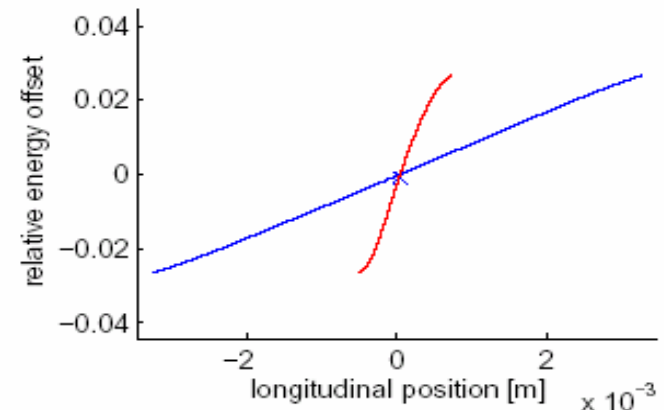
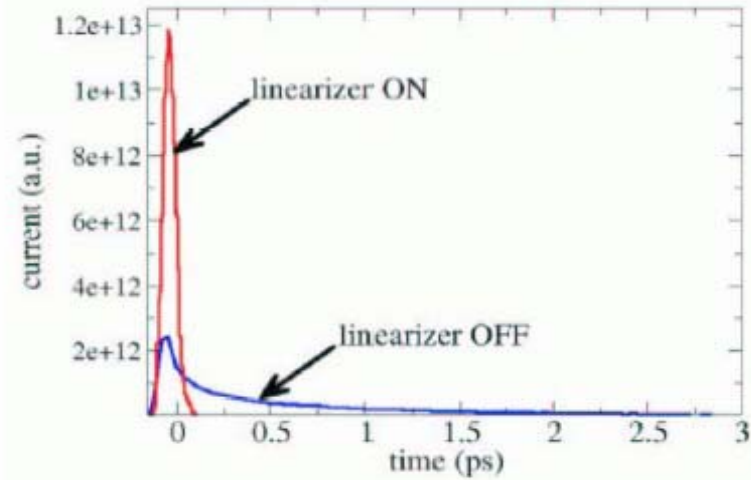
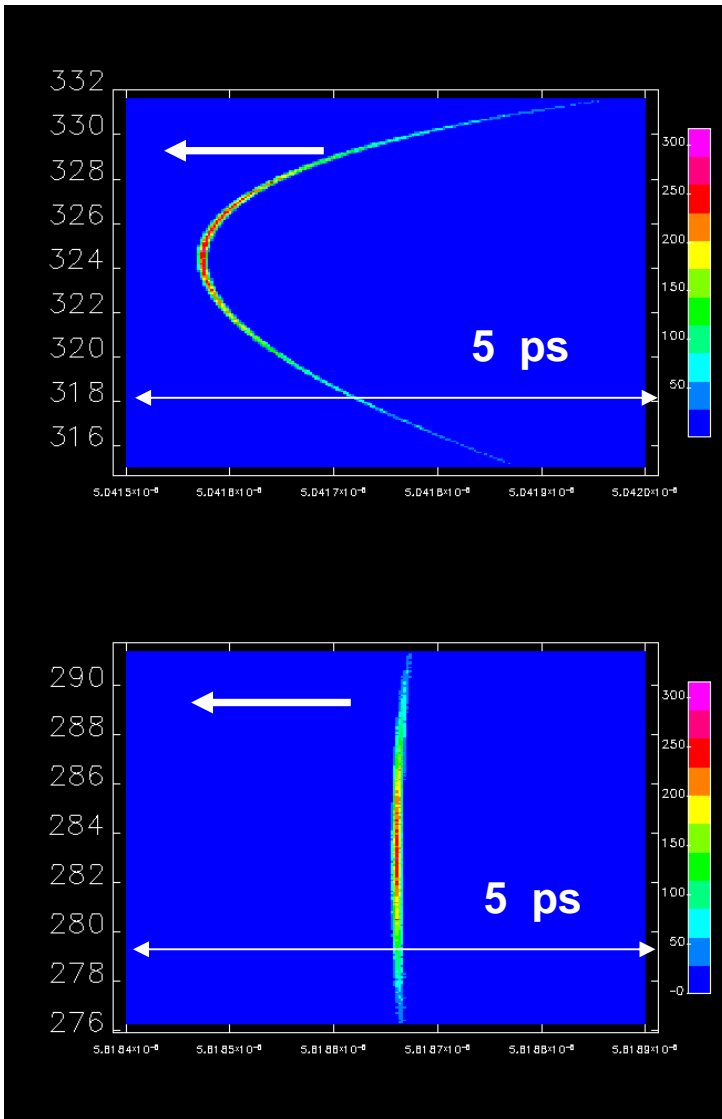
linearizing section



Bunch compressor

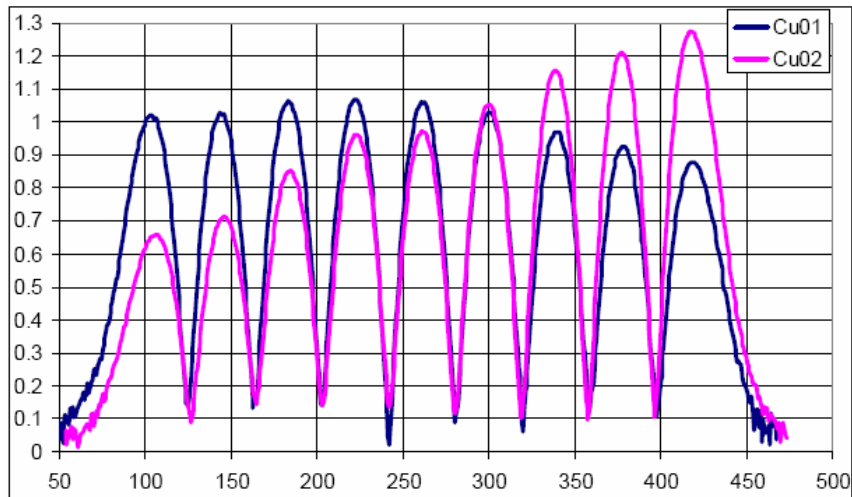
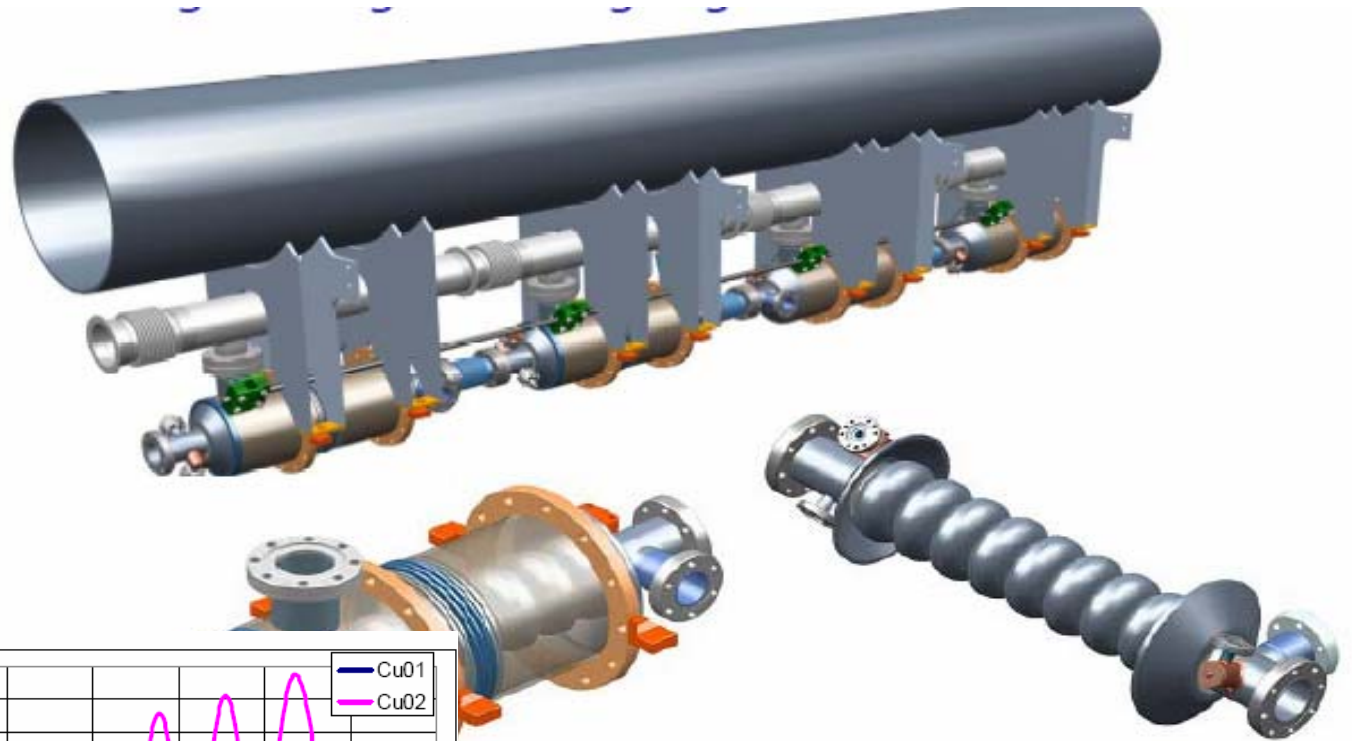


Higher order effects: pulse control



A third harmonic (3.9 GHz) SCRF cavity is being built at FNAL (Solyak, LINAC 2004)

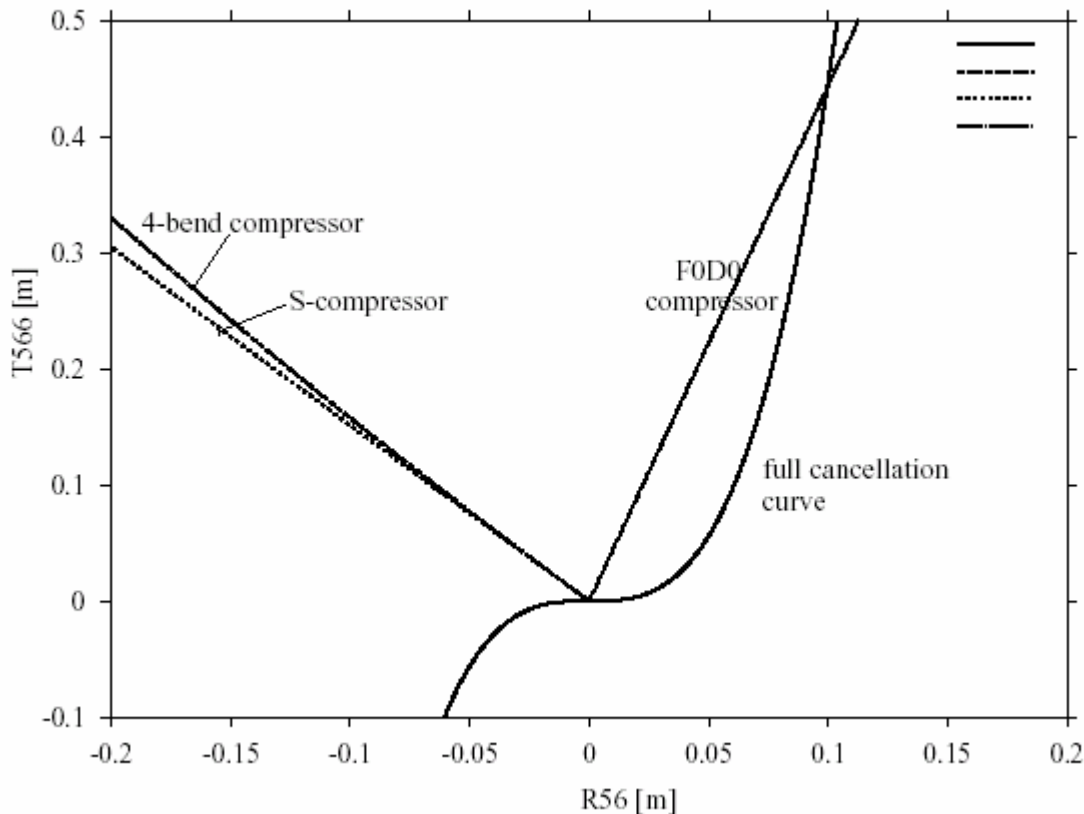
Higher order effects: 3.9 HZ harmonic cavity



(Solyak, LINAC 2004)

Higher order effects: pulse control

- Sextupoles, to some extent, also provide these knobs
- But coupling between longitudinal and transverse phase space is introduced



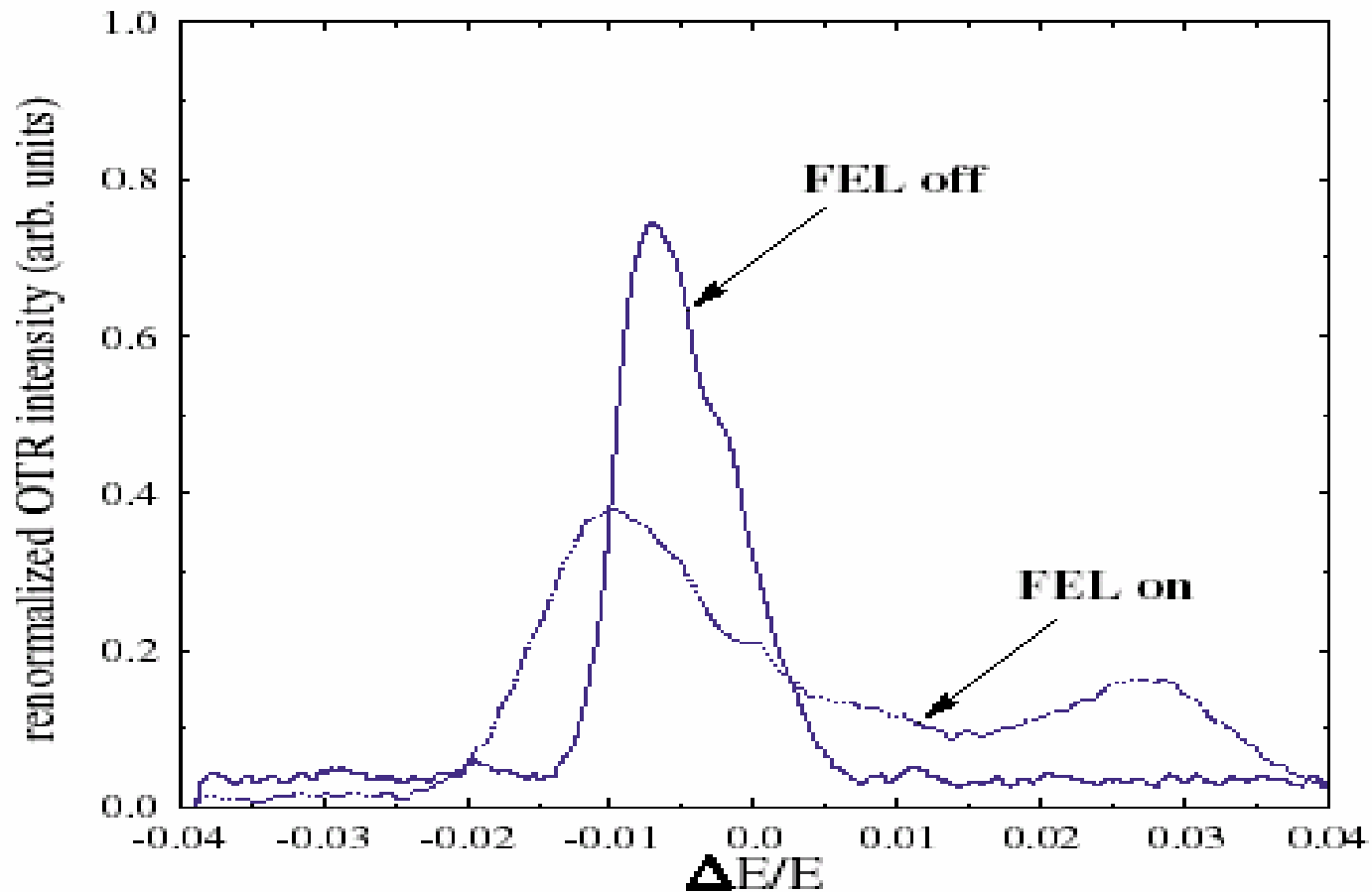
■ Chicane
 $R_{56} < 0, T_{566} > 0$

■ S-chicane
 $R_{56} < 0, T_{566} > 0$

■ FODO arc
 $R_{56} > 0, T_{566} > 0$

Effect of FEL interaction

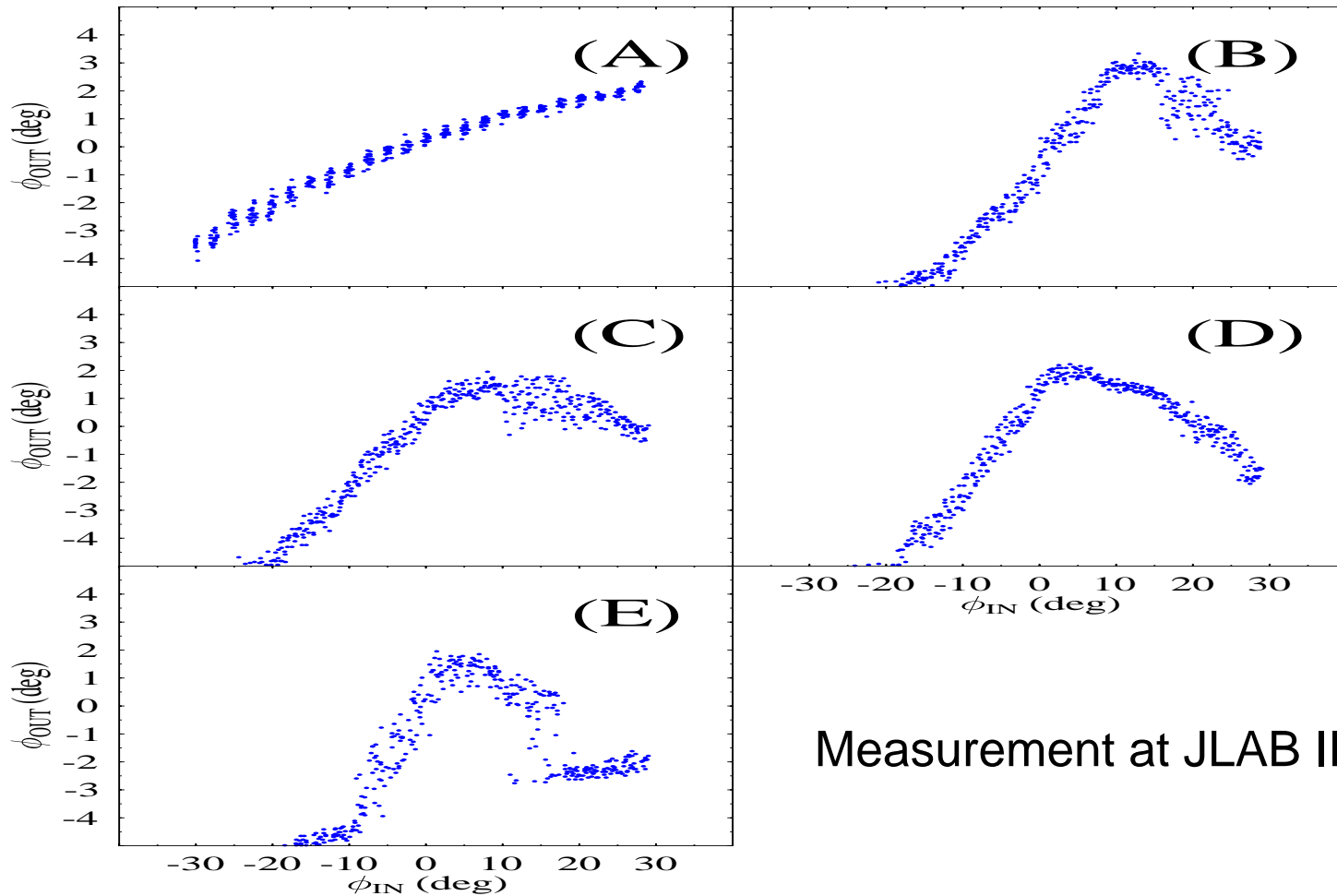
- Increase in uncorrelated momentum spread



Measurement at JLAB IR-DEMO

Effect of FEL interaction

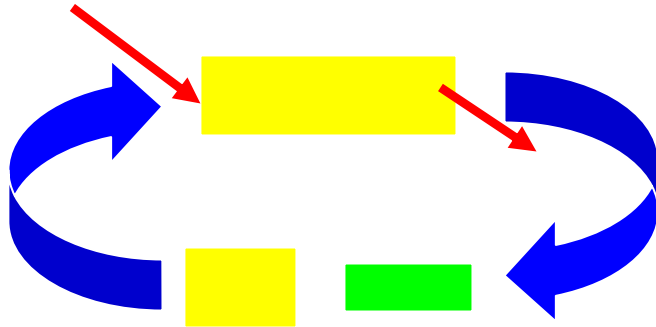
■ Change in time-of-flight?



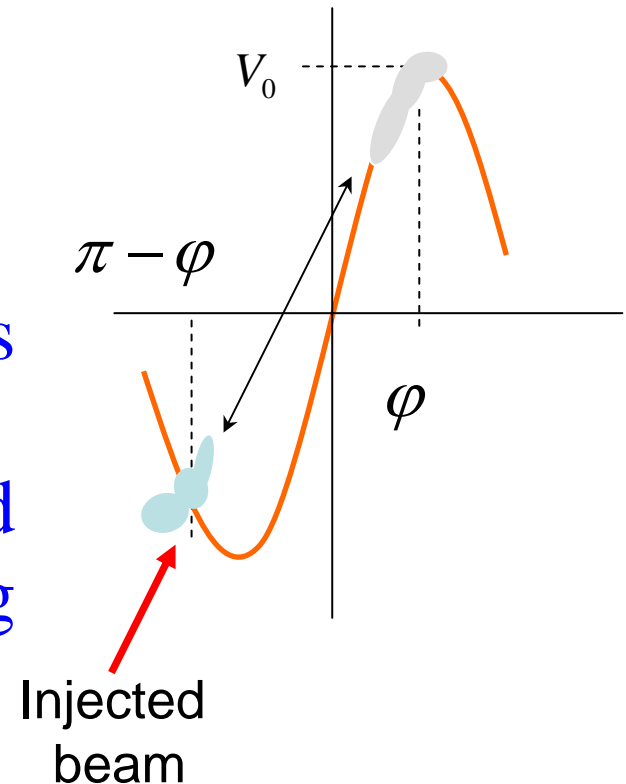
Measurement at JLAB IR-DEMO

Energy recovery

- Recirculation optics \Rightarrow match longitudinal phase space to slope of decelerating linac
- Need again to match slope and curvature

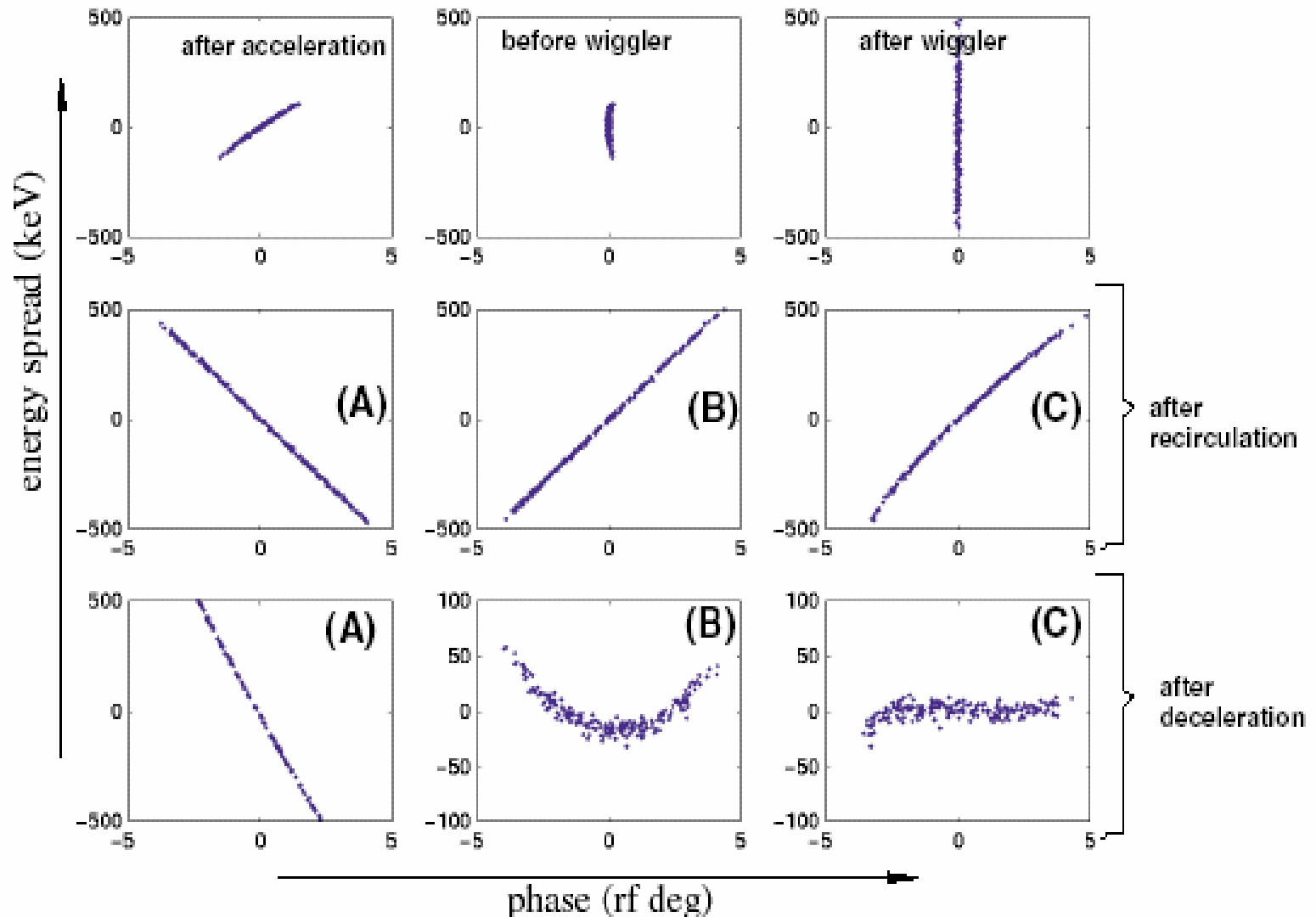


- Full recirculation loop is generally isochronous,
- Possible to use a dedicated cavity operated at zero crossing in the loop

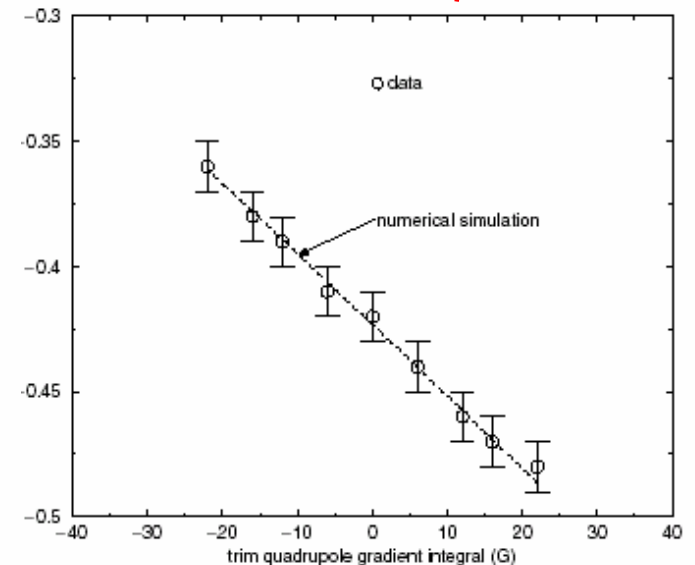
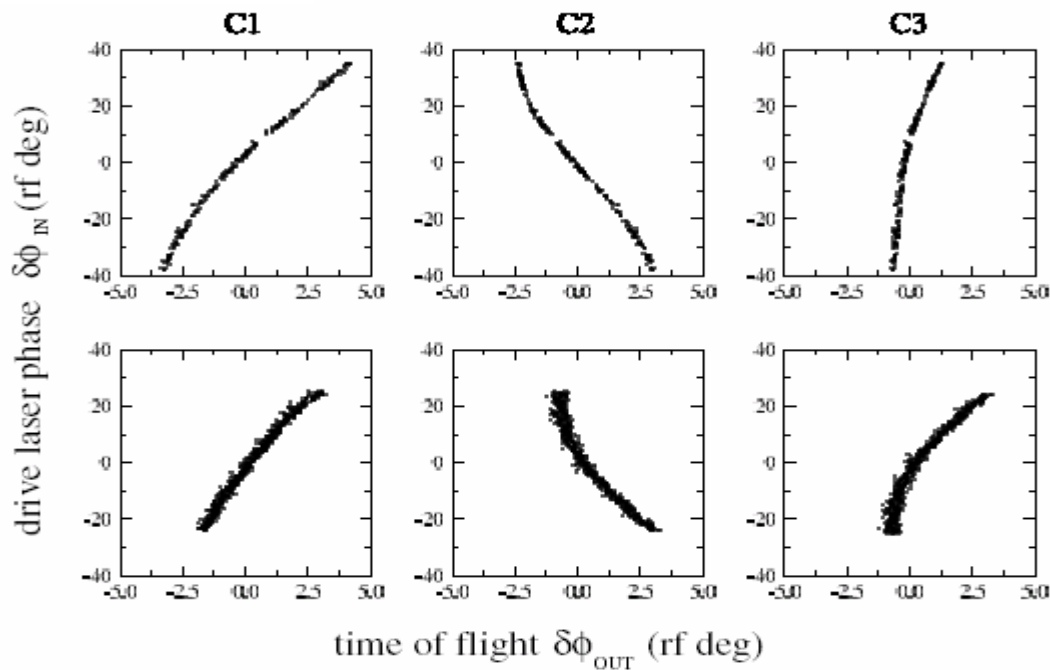
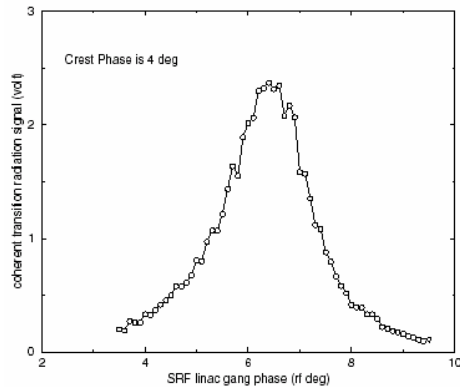
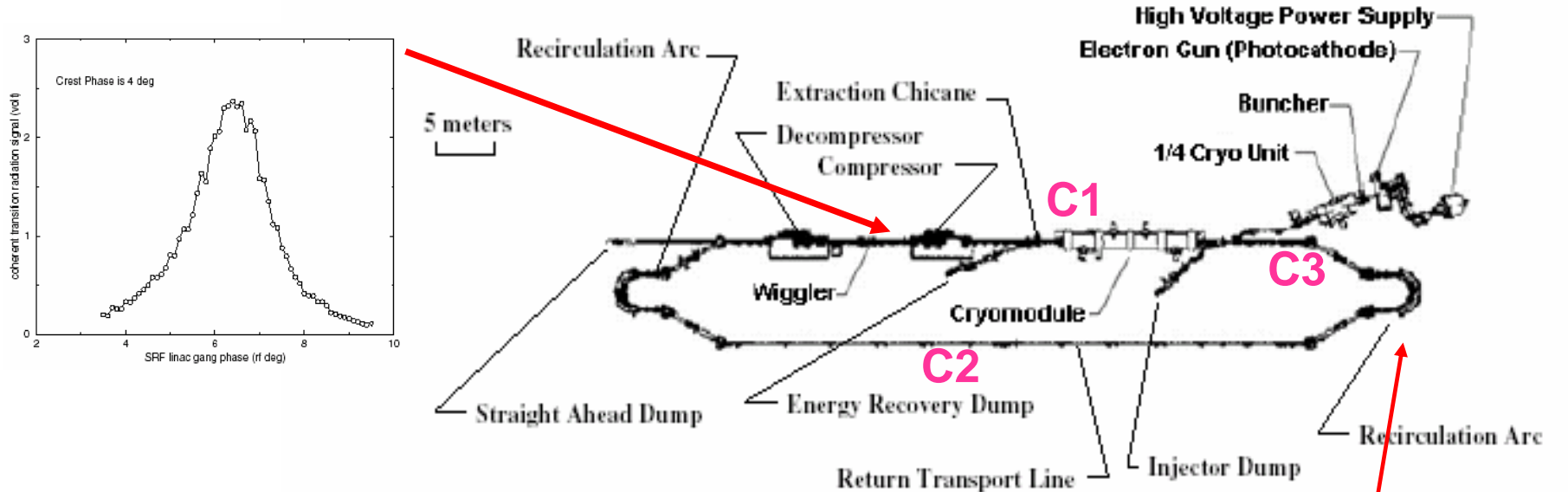


Energy recovery

■ Recirculation optics \Rightarrow match longitudinal phase



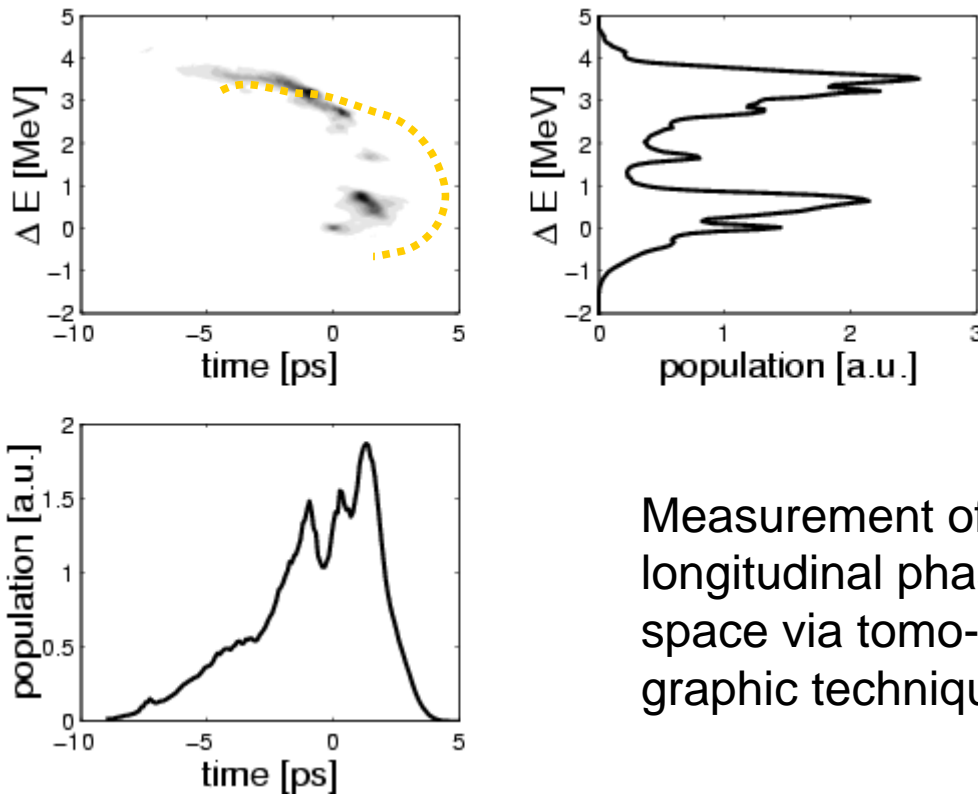
Example JLab IR-demo



comments

■ Don't want to compress too hard

$$\sigma_{z,f} = \sqrt{(1 + \kappa R_{56})^2 \sigma_{z,i}^2 + R_{56}^2 \sigma_{\delta,i}^2 E_0^2 / E^2}$$



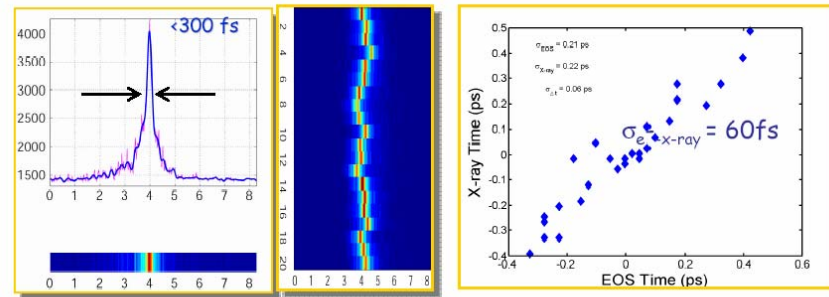
Measurement of longitudinal phase space via tomographic technique

(M. Huening, et al FEL'2000)

■ Parasitic time of flight measurement using EO imaging?

Femtosecond x-ray stopwatch

A. Cavalieri, D. Fritz, S. Lee, P. Bucksbaum, D. Reis and SPPS Collaboration



Single-Shot Electron Beam Timing measurement

Timing Jitter (20 shots)

Strong Correlation between measured Electron Beam and X-ray beam timing