

Merger Design session

Emittance control & multiple modes of operation

Merger design exercise

- merging energy
 - high energy = smaller emittance
 - low energy = better economics
- configuration
 - 3-dipole, zigzag, multi-loop
 - pros & cons
- multiple merger
 - how many ? configuration ?
- simulation tools
 - space charge, CSR in a curved path
 - comparison : simulation / real machine

- Energy balance

$$E_{inj} + (E_{acc} - E_{dec}) = E_{loss} + E_{dump}$$

RF for the injector

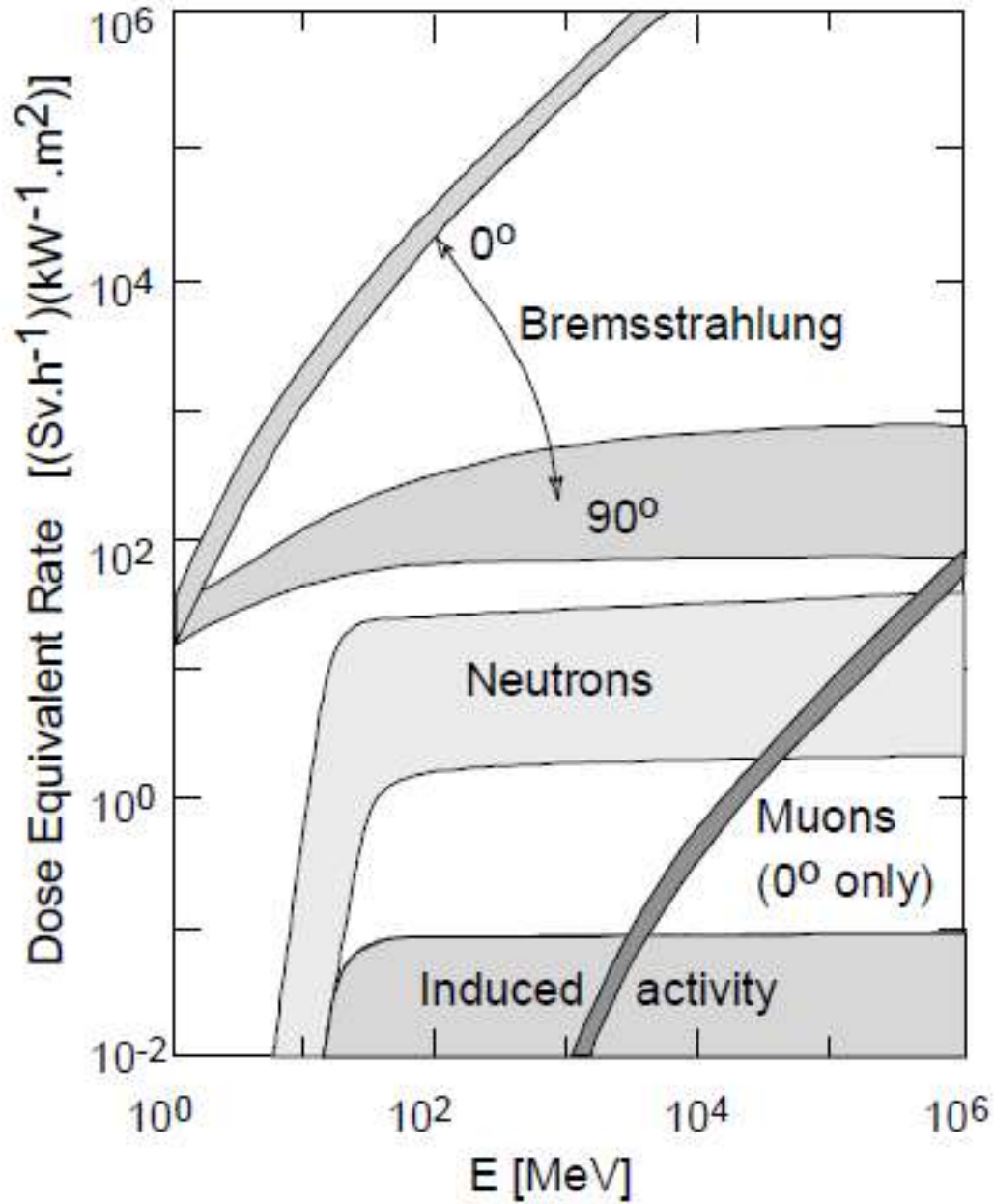
RF for the main linac

- dump energy < 10 MeV to avoid neutron generation, but must have some amount of kinetic energy for easy handling.

dump current is important information in the operation.

- large RF sources for the main linac = large investment (source, circulator, coupler ...)

dose per unit beam power



SLAC-PUB 9557

Merging Energy (cont.)

- injected by small energy causes "phase slip" but rapid acceleration eliminates it.

for 5-GeV light source (0.1% energy loss at most)

$$E_{inj} + (E_{acc} - E_{dec}) = E_{loss} + E_{dump}$$

$$5 \text{ MeV} + 5 \text{ MeV} = 5 \text{ MeV} + 5 \text{ MeV}$$



for 100mA, additional 5 kW per 20 MV acceleration

$$10 \text{ MeV} + 0 \text{ MeV} = 5 \text{ MeV} + 5 \text{ MeV}$$



need off-crest acc. for energy compression

Merging Energy (cont.)

for 50-MeV FEL (1% energy loss, 10% energy spread)

$$E_{inj} + (E_{acc} - E_{dec}) = E_{loss} + E_{dump}$$

$$5 \text{ MeV} + 0.5 \text{ MeV} = 0.5 \text{ MeV} + 5 \text{ MeV}$$



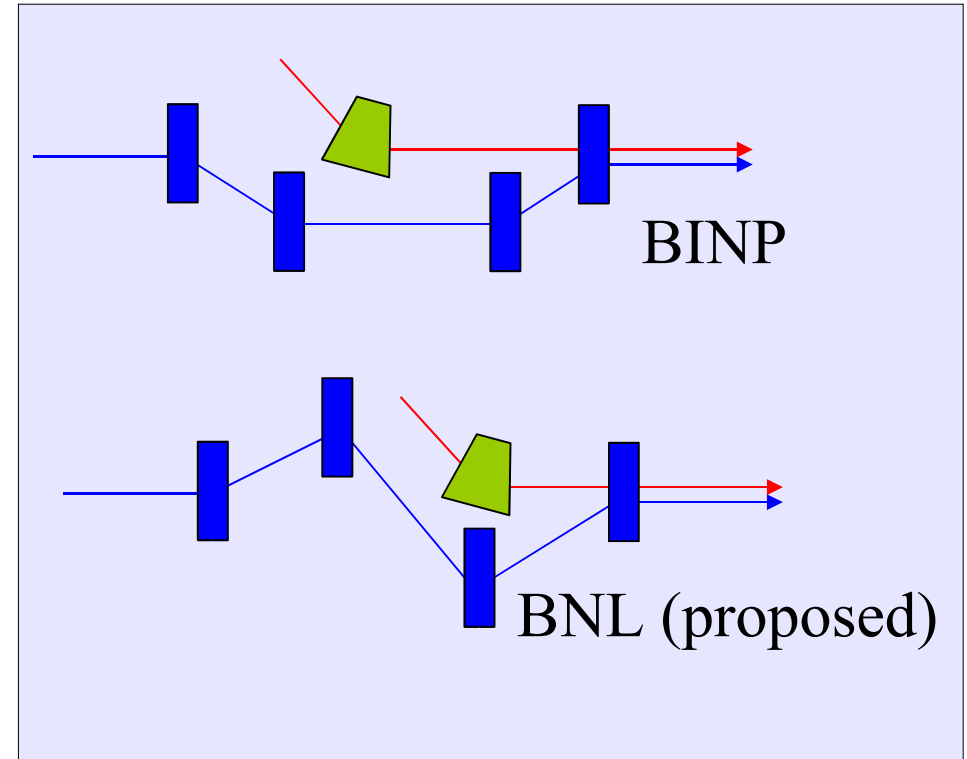
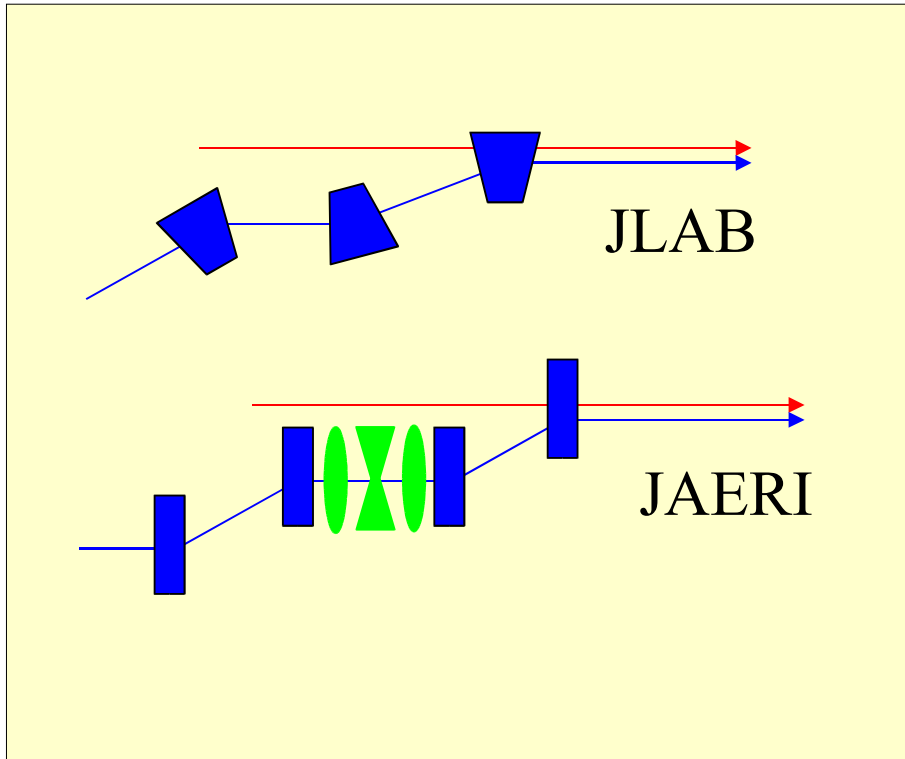
for 100 mA, additional 10 kW per 10 MV acceleration,
energy compression is possible, but maybe insufficient.
10 kW / 1 MW = 1% RF power budget.

$$5 \text{ MeV} + 0 \text{ MeV} = 0.5 \text{ MeV} + 4.5 \text{ MeV}$$



need off-crest acc. for energy compression

Merger Configuration



"slide injection"

injection / recirculation are tilted or shifted.

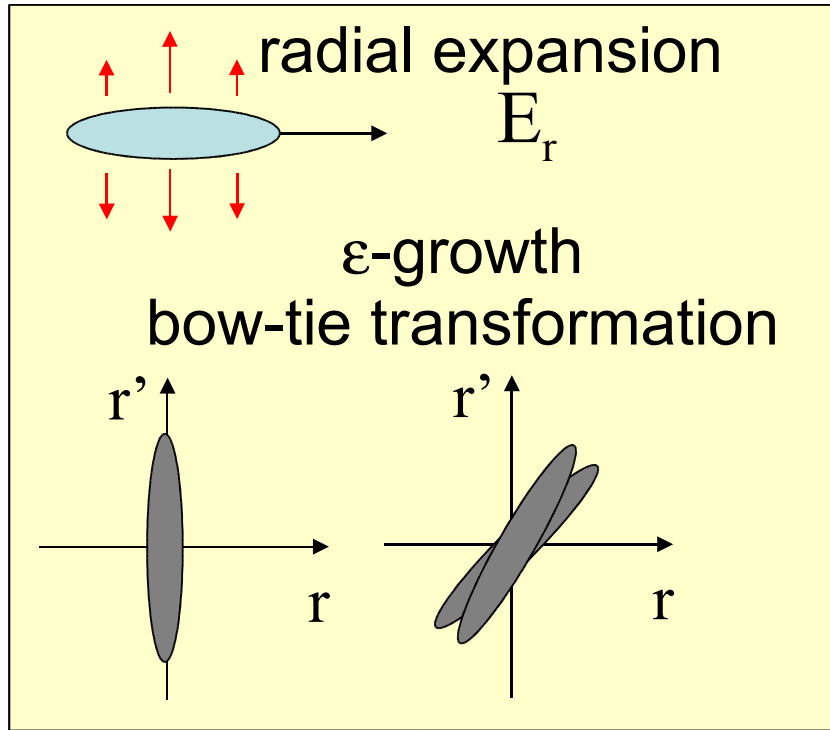
flexible BT for the high-E beam.

"in-line injection"

injection / recirculation are in line.

suitable for small E_{high} .

Transverse emittance growth by Ex, Ey

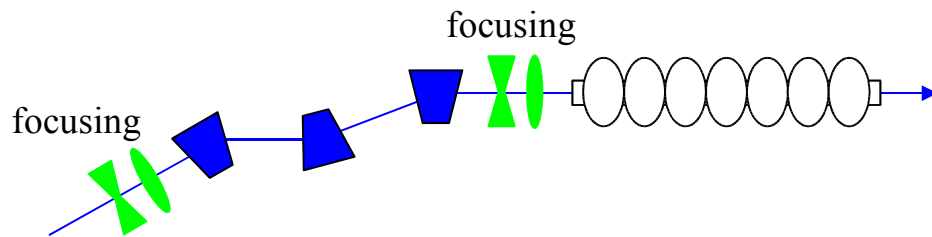


$$\sigma'' - \frac{(I/2I_0)}{\sigma \beta^3 \gamma^3} - \frac{\epsilon_n^2}{\sigma^3 \beta^2 \gamma^2} = 0$$

in the limit of zero slice emittance

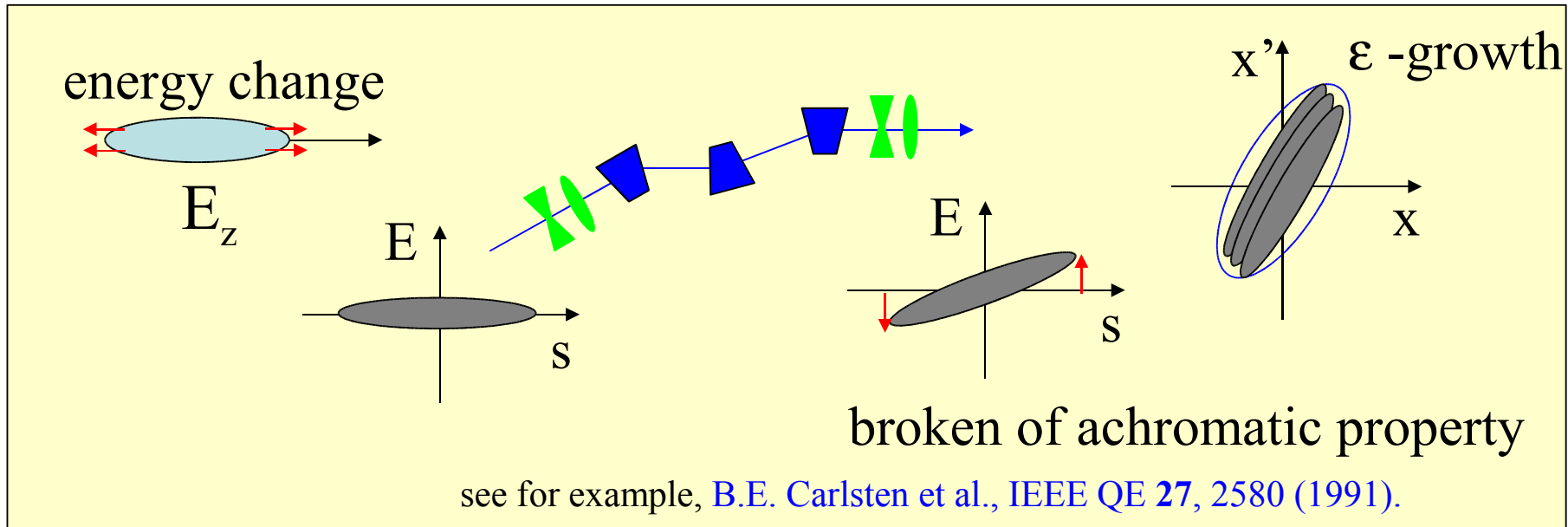
$$\epsilon_n \sim 0$$

$$\Delta \epsilon_n \sim \delta \sigma' \sigma \gamma \propto \gamma^{-2}$$



emittance compensation
by appropriate focusing

Transverse emittance growth by Ez



assuming steady-state Ez $\Delta E / E = \delta = \delta_0 + \kappa (s - s_0)$

We can track bunch slice motion by linear matrix.

$$\epsilon^2 = (\epsilon_0 \beta_x + D^2)(\epsilon_0 \gamma_x + D'^2) - (-\epsilon_0 \alpha_x + D D')^2$$

$$(D, D') = \Delta \kappa_{rms} (\zeta_x, \zeta_x')$$

similar to the CSR case

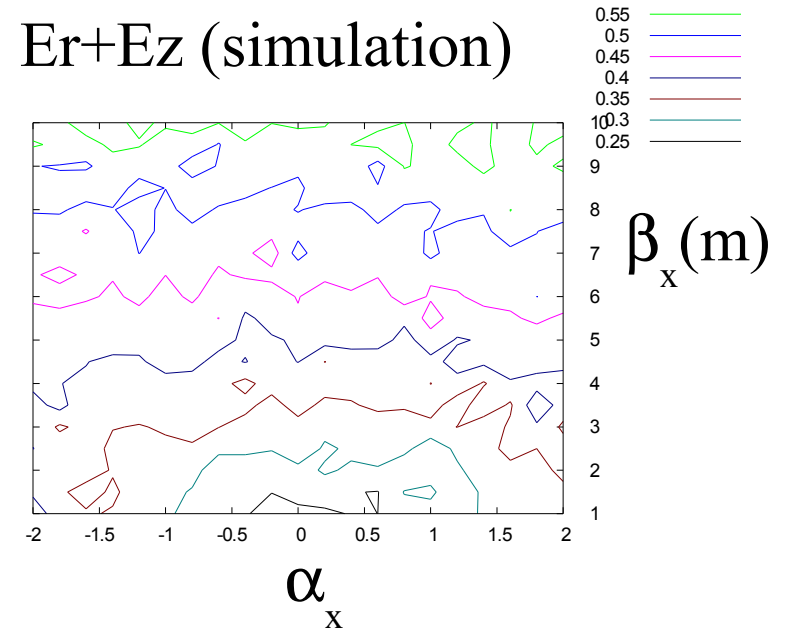
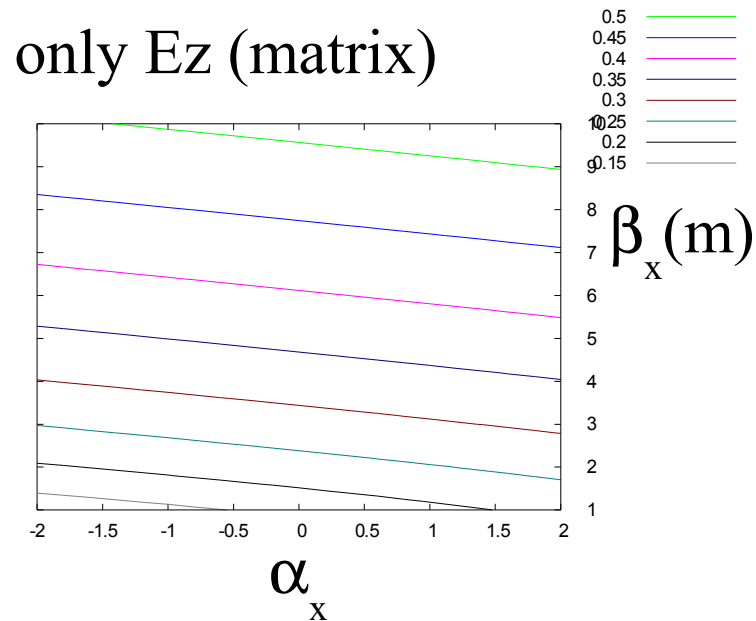
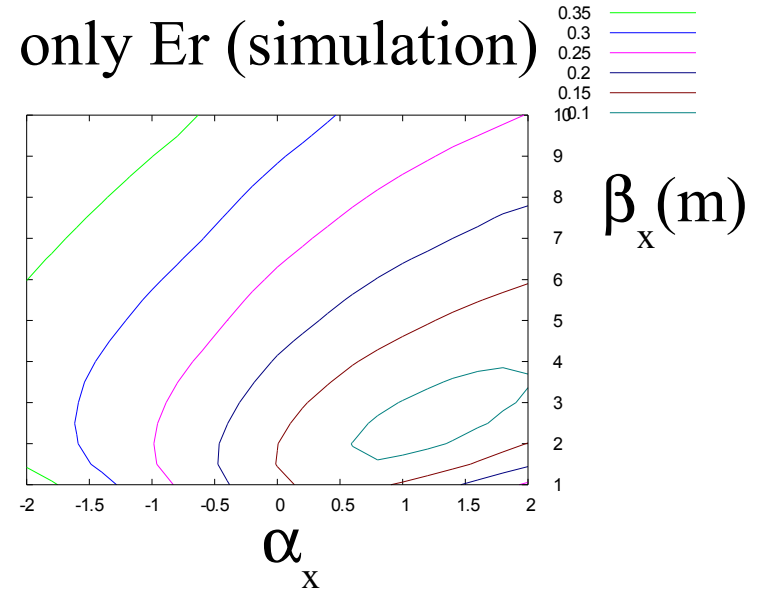
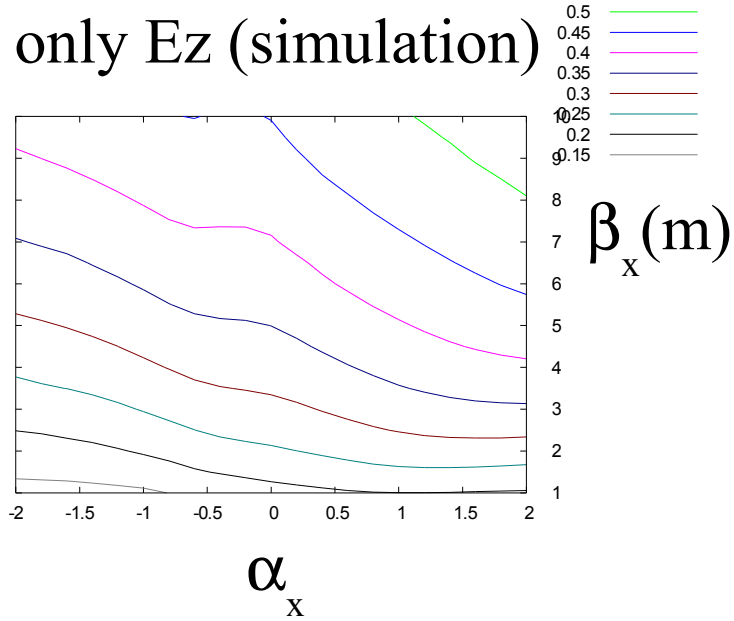
$$E_z \propto \gamma^{-1}$$

$$\Delta E / E \propto \gamma^{-2}$$

$$\Delta \epsilon_n \propto \gamma^{-3/2}$$

Optimum injection to a 3-dipole merger

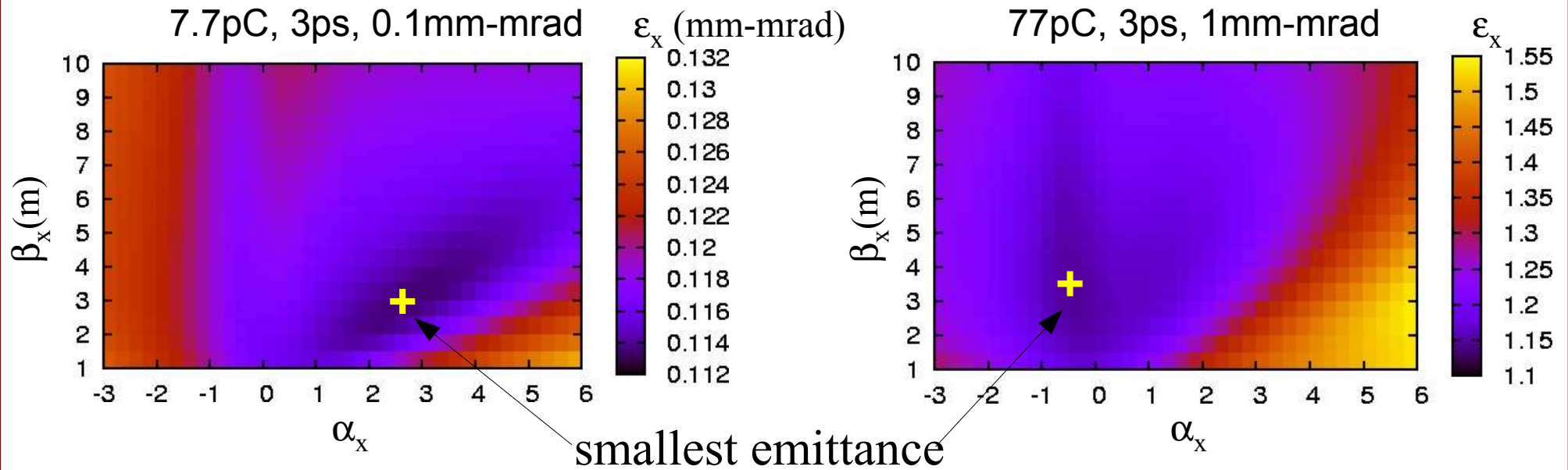
calculate emittance growth with varying injection parameters (α_x, β_x)



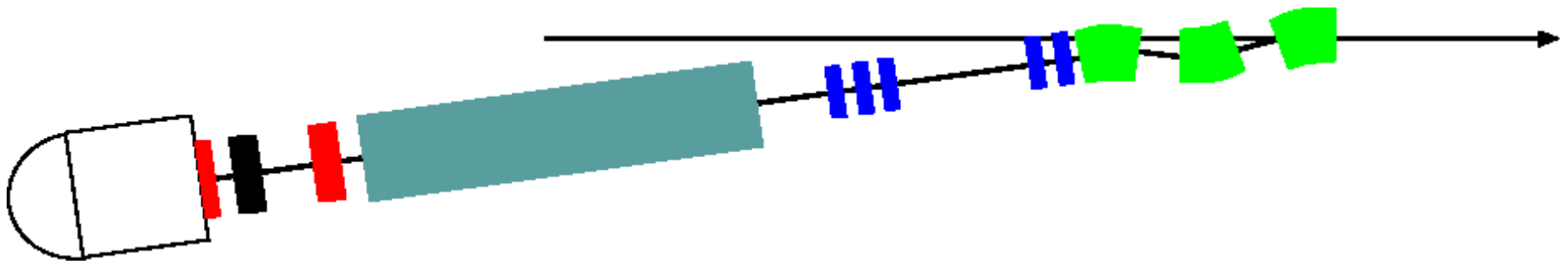
Optimum injection to a 3-dipole merger

optimum envelope is a function of bunch parameters.

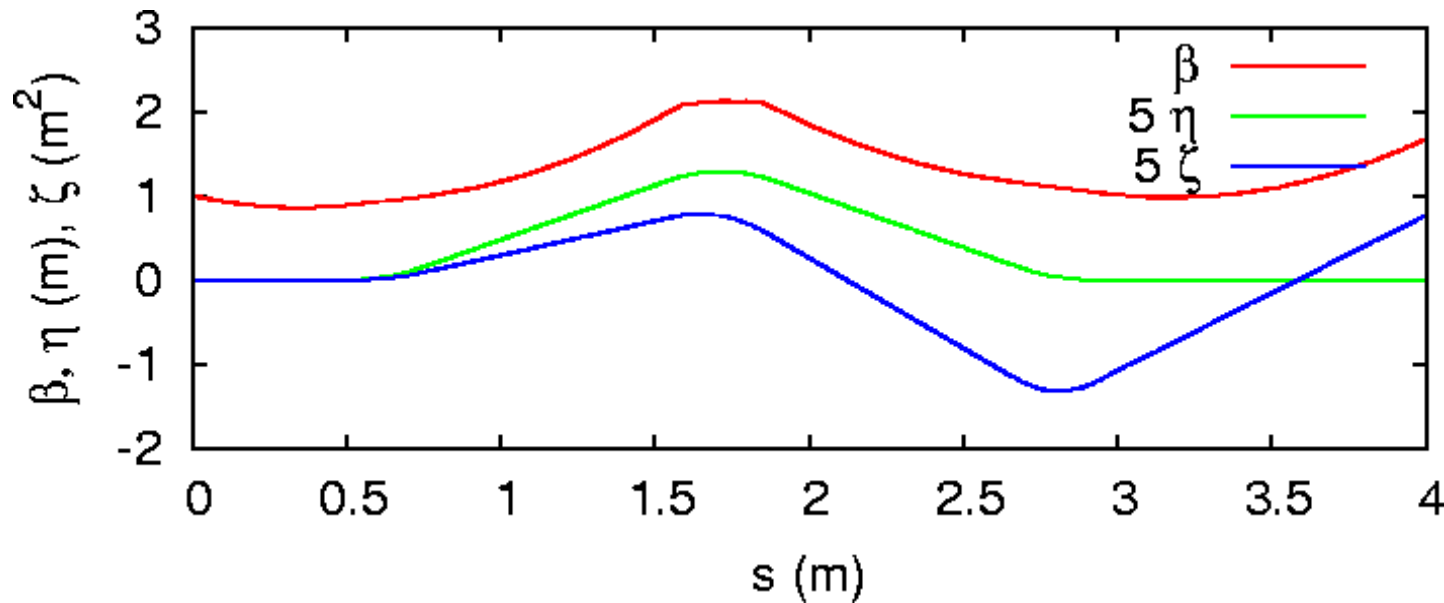
PARMELA runs for the merger (3 dipoles only) with varying α_x , β_x at the merger entrance.



3-dipole merger



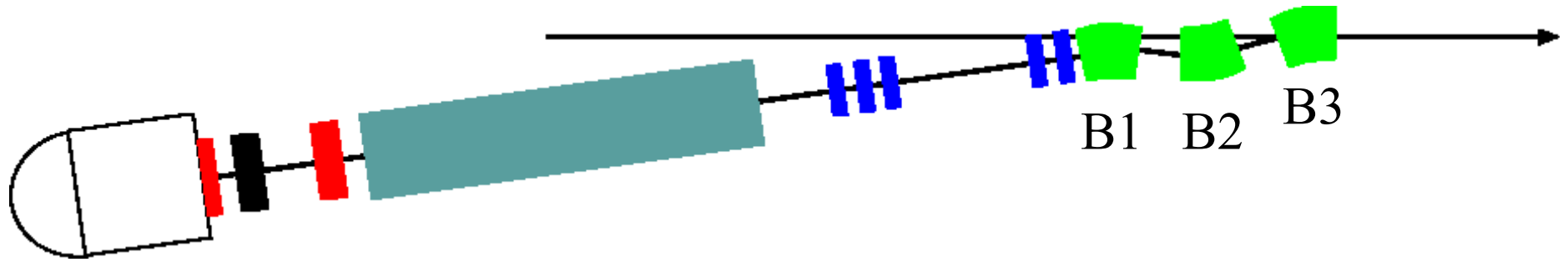
longitudinal space charge dispersion



bunch slice displacement by E_z

the bending angle should be small,
and the total length should be short

3-dipole merger



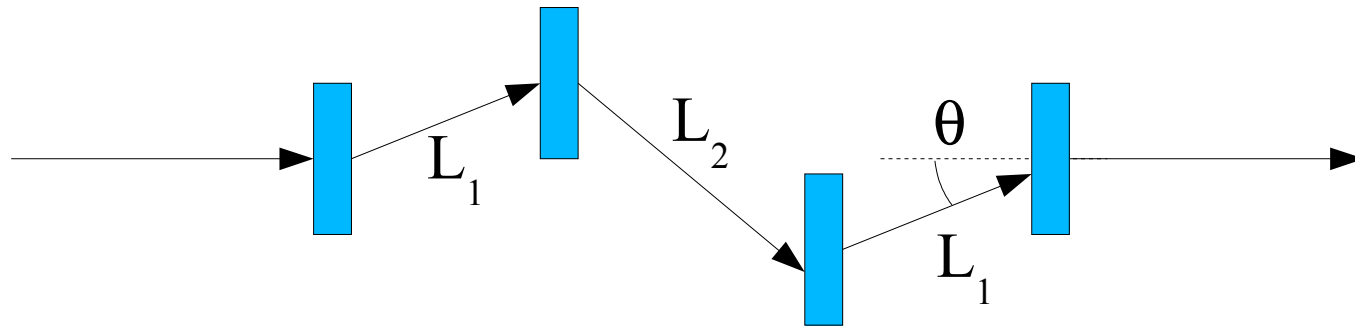
for example,

	B1 / B3	B2
bending radius	1m	1m
bending angle	15 deg.	22 deg.
edge angle	0	-20 deg.

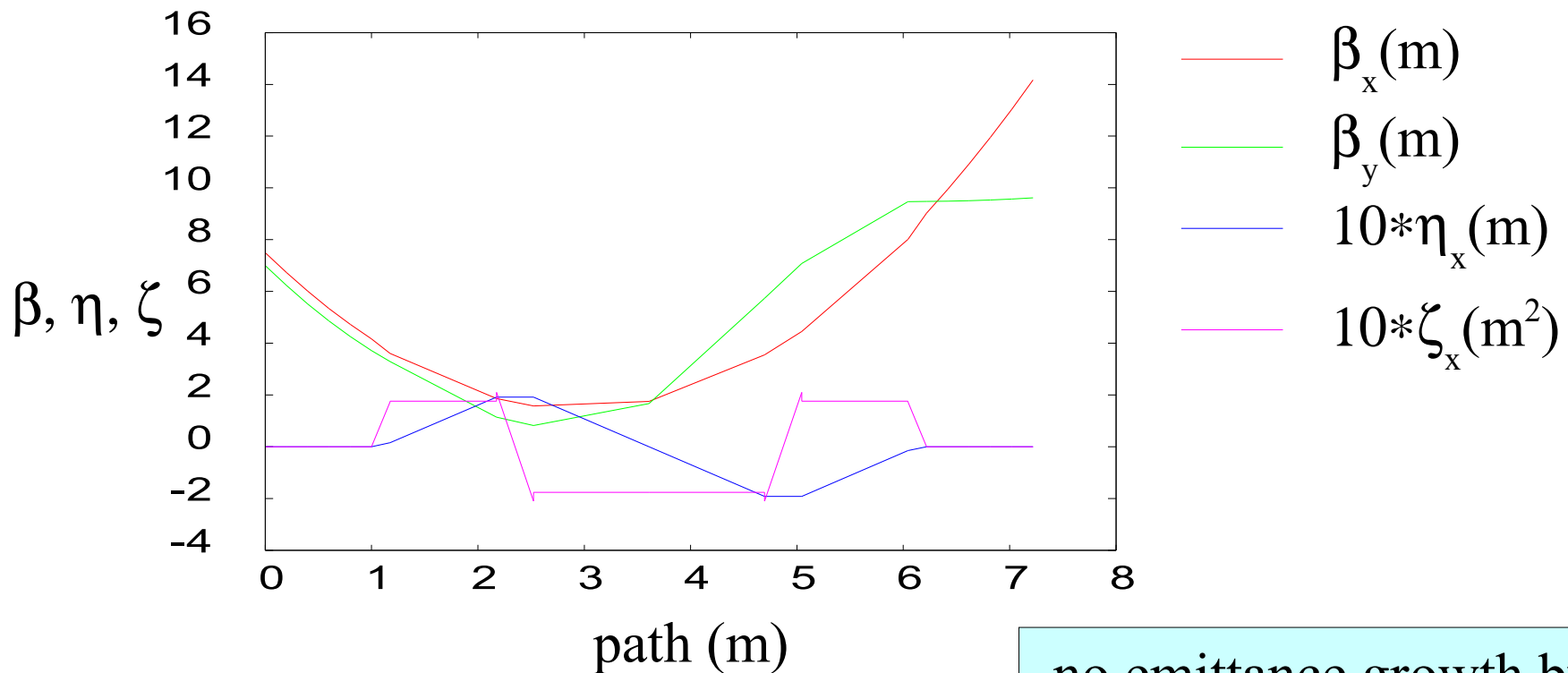
drift between bends = 0.316m
 total path length = 1.54m
 total deflection angle = 8 deg.

total deflection angle is determined so that we can keep space for the cryomodule (D=670mm).

zigzag merger

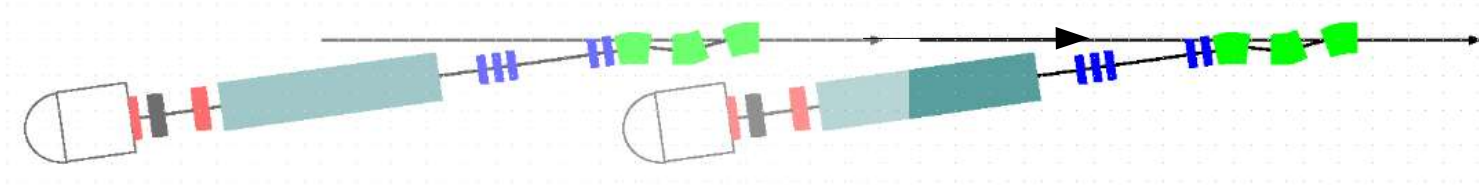


$\rho=1\text{m}, \theta=10\text{deg.}, L_1=1\text{m}, L_2=2.17\text{m}$

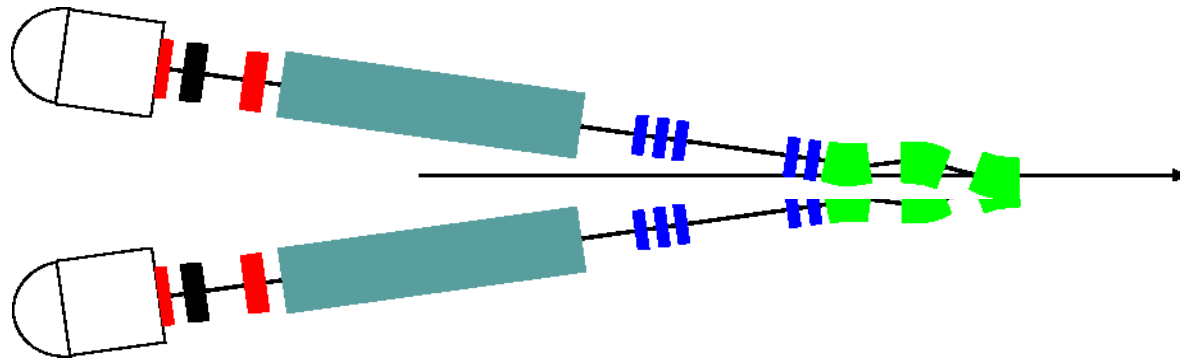


no emittance growth by Ez !

multi-merger for multi-injector



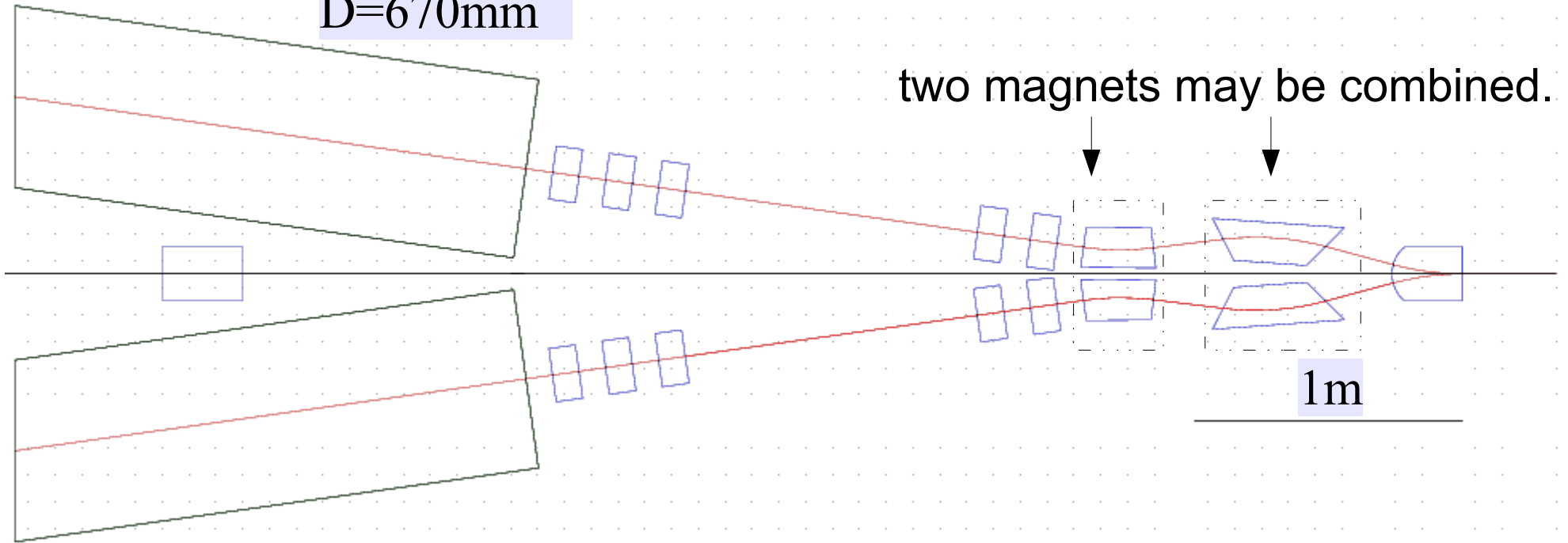
tandem configuration



symmetric configuration

Multi-merger example

Cryomodule
D=670mm



5x5 R-Matrix for the CSR Analysis

electron's motion in the bending plane is expressed by a vector

$$\vec{x}(s) = (x, x', \delta_0, \kappa L_b, \kappa)^T$$

$$\delta_{CSR}(s) = \kappa \underline{L_b}(s)$$



sum of bending path length in the upstream

before the bend

$$\vec{x}(s_0) = (x, x', \delta_0, \kappa L_b, \kappa)^T$$

after the bend

$$\vec{x}(s_1) = (x, x', \delta_0, \kappa L_b, \kappa)^T$$

transfer matrix of the bend

$$\vec{x}(s_1) = R_{bend} \vec{x}(s_0)$$

5x5 R-matrix for a sector bending magnet

$$R_{bend} = \begin{pmatrix} \cos \theta & \rho \sin \theta & \rho(1 - \cos \theta) & \rho(1 - \cos \theta) & \rho^2(\theta - \sin \theta) \\ -\rho^{-1} \sin \theta & \cos \theta & \sin \theta & \sin \theta & \rho(1 - \cos \theta) \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & \rho \theta \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

extension of the conventional 3x3 R-matrix

R. Hajima, JJAP 42, L974 (2003).

CSR-wake dispersion function

Following the momentum dispersion function “ η ”, we define the CSR wake dispersion function “ ζ ”

momentum dispersion function

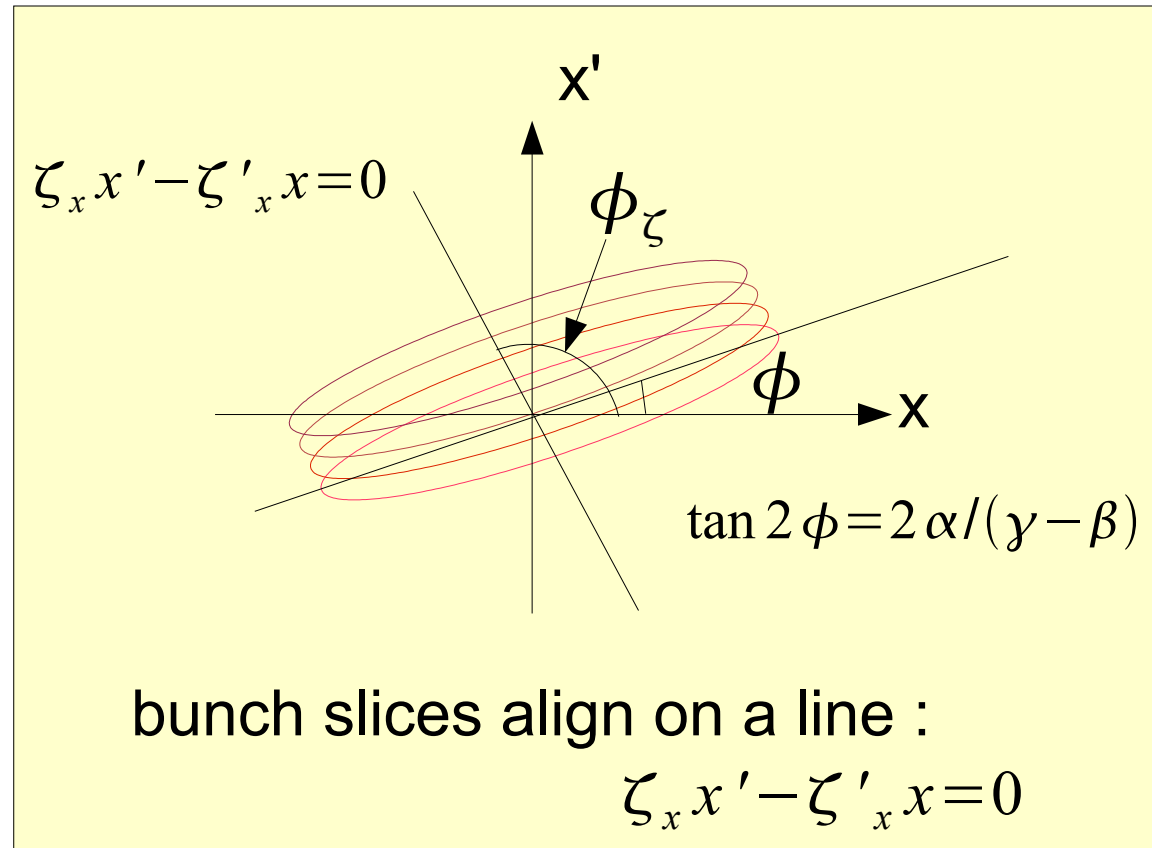
(η, η')

$$\begin{pmatrix} \eta_x(s_1) \\ \eta'_x(s_1) \\ 1 \\ 0 \\ 0 \end{pmatrix} = R_{0 \rightarrow 1} \begin{pmatrix} \eta_x(s_0) \\ \eta'_x(s_0) \\ 1 \\ 0 \\ 0 \end{pmatrix}$$

CSR wake dispersion function

(ζ, ζ')

$$\begin{pmatrix} \zeta_x(s_1) \\ \zeta'_x(s_1) \\ 0 \\ L_b(s_1) \\ 1 \end{pmatrix} = R_{0 \rightarrow 1} \begin{pmatrix} \zeta_x(s_0) \\ \zeta'_x(s_0) \\ 0 \\ L_b(s_0) \\ 1 \end{pmatrix}$$



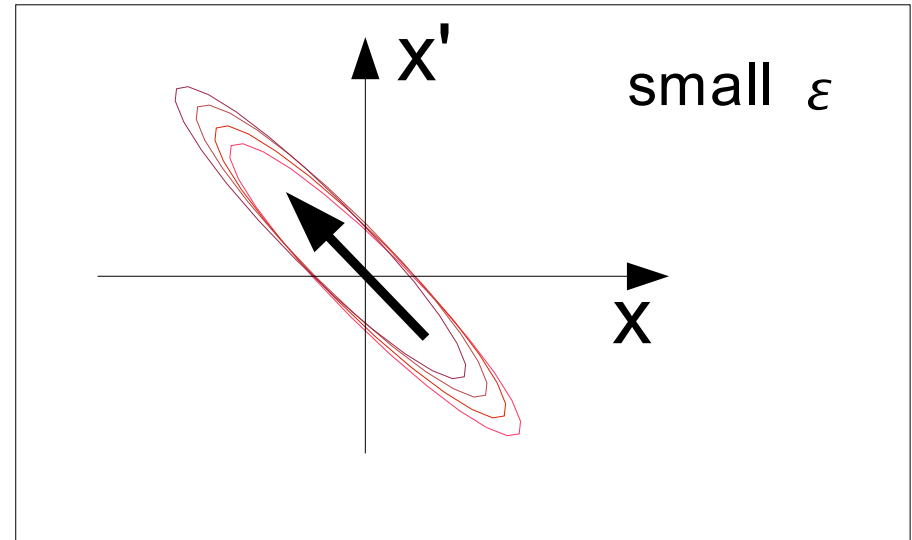
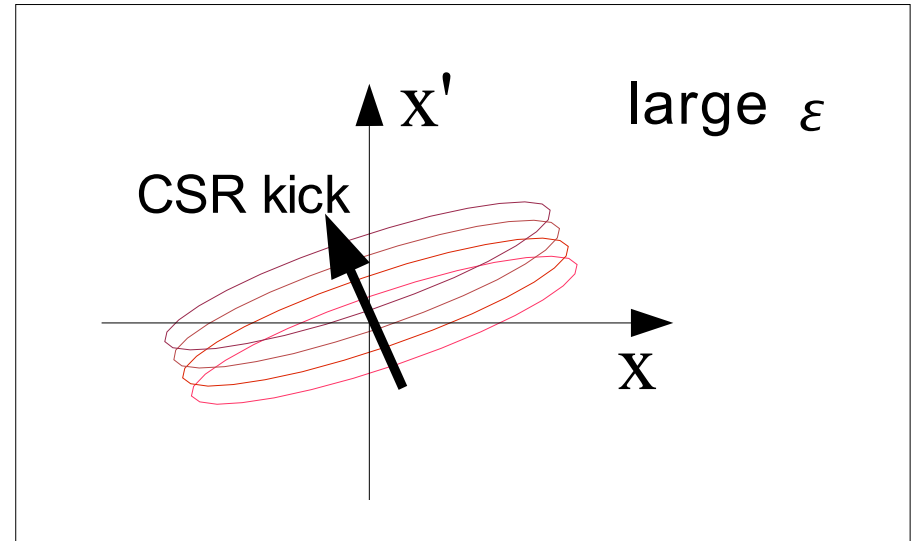
We can track the motion of bunch slices.

Emittance Growth by CSR, and its Compensation

coincidence between the CSR kick and the phase ellipse orientation.



minimum emittance growth



projection emittance is evaluated by

$$\varepsilon^2 = (\varepsilon_0 \beta_x + D^2)(\varepsilon_0 \gamma_x + D'^2) - (-\varepsilon_0 \alpha_x + D D')^2$$

$$(D, D') = \Delta \kappa_{rms} (\zeta_x, \zeta_x')$$

$$\Delta \kappa_{rms} = \frac{\Delta E_{rms}}{E_0 L_b}$$

$$\varepsilon^2 - \varepsilon_0^2 = \varepsilon_0 \frac{(\Delta \kappa_{rms})^2 (\beta_x \zeta'^2 + \gamma_x \zeta^2 - 2\alpha_x \zeta \zeta')}{}$$

bunch parameter

beam transport