

# Parton $k_{\perp}$ -broadening in DIS and DY in a scalar QED model

S. Peigné

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collaboration: J. Aichelin, F. Arleo, P.B. Gossiaux  
T. Gousset, M. Thomas.

hep-ph / 0505066

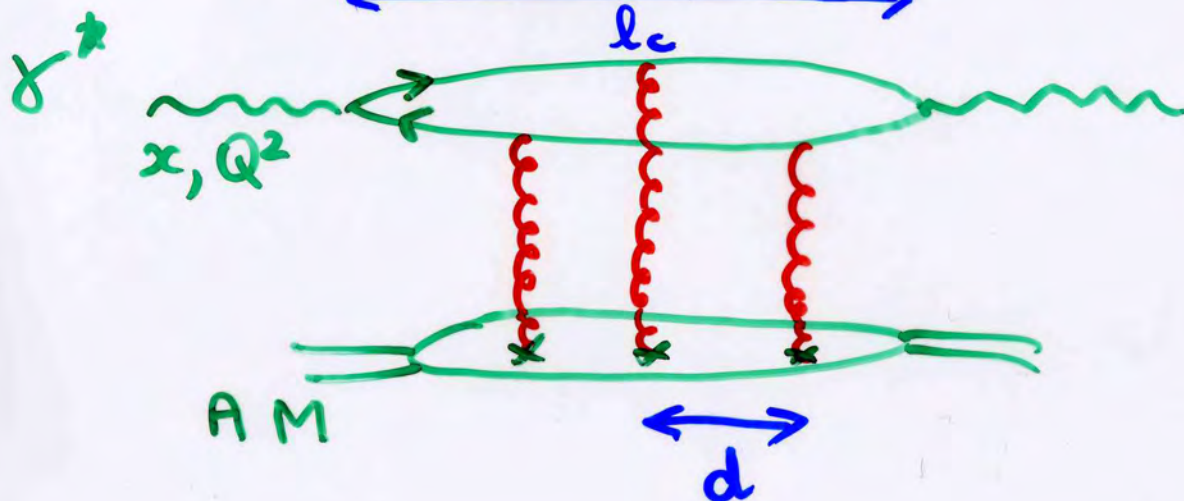
PRD72: 054010, 2005

- (NP) PDF's depend on target.

DIS:  $F_2^A \neq A F_2^P$   $\square$

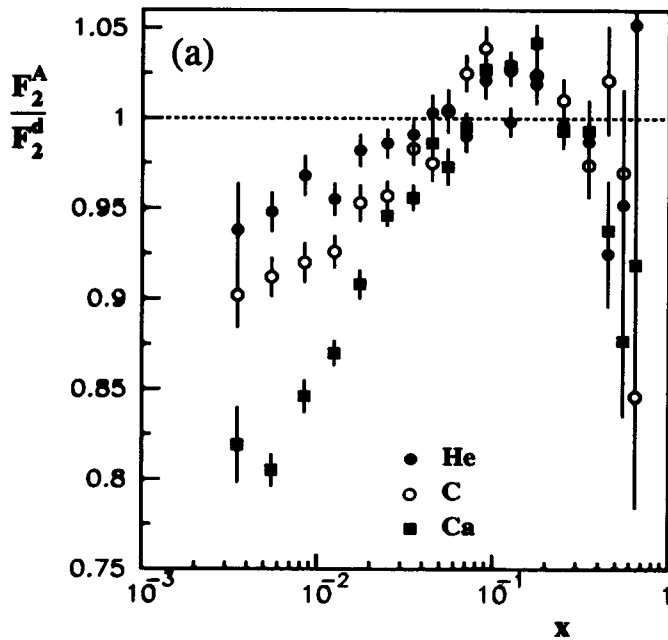
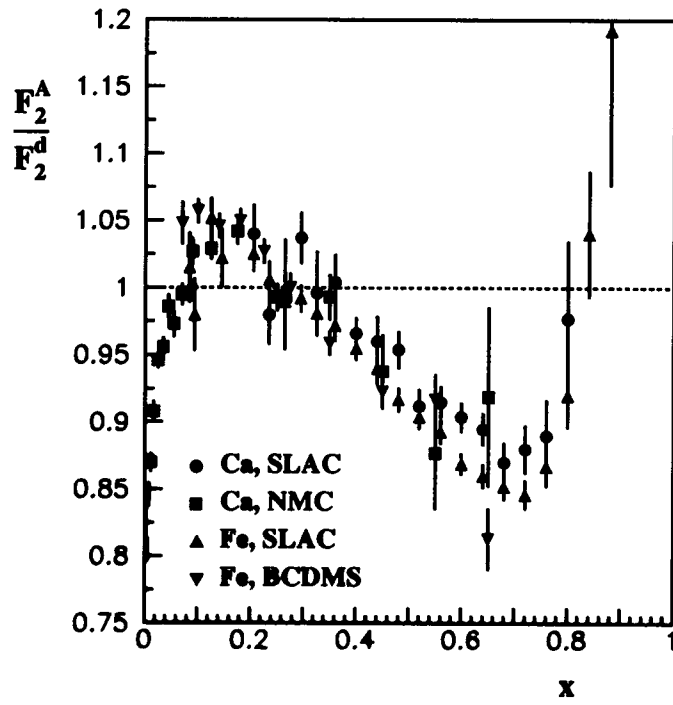
$x < 0.1 \Rightarrow F_2^A < A F_2^P$  (shadowing)

$$x < 0.1 \Rightarrow l_c = \frac{1}{Mx} > 2 \text{ fm} \simeq d$$



# DIS Nuclear Shadowing

G. Piller, W. Weise, Phys. Rept. 330 (2000) 1-94,  
hep-ph/9908230



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- QCD factorization theorems  
(Collins, Soper, Sterman)

$\Rightarrow f_{q/T}(x, Q^2)$  is "universal"  $\equiv$  process-independent

shadowing also seen in DY □  
compatible with shadowing in DIS

Universality of inclusive PDFs  
widely checked and successful

What about other NP quantities?

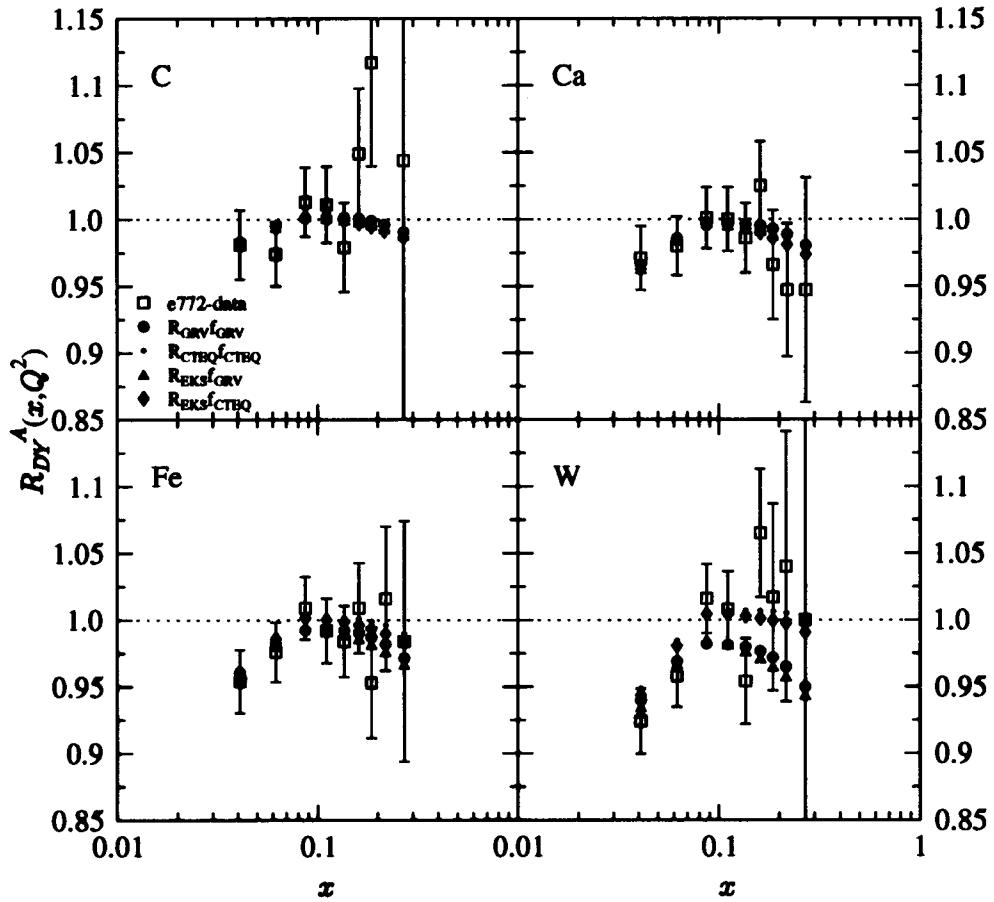
- nuclear  $k_T$ -broadening

-  $f_{q/T}(x, \underline{k_T})$

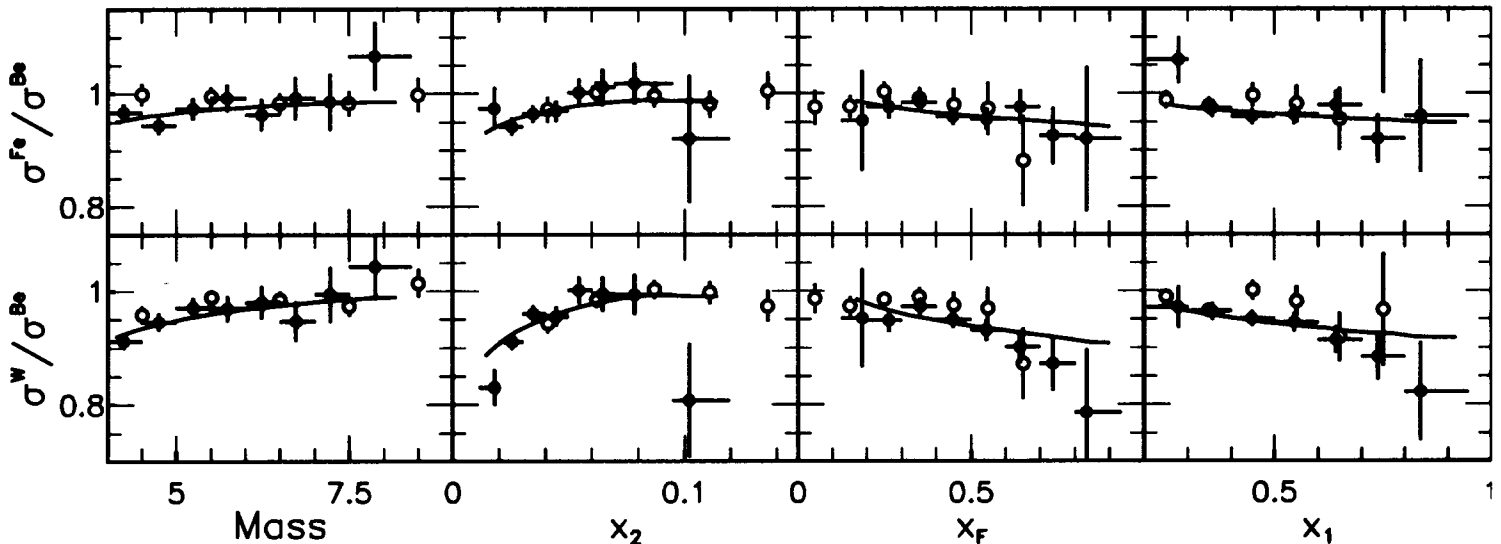
# Nuclear Shadowing in Drell-Yan Production

(Figure from Eskola, Kolhinen, Salgado,  
Eur.Phys.J.C9:61-68,1999)

E772 Collab., Phys. Rev. Lett. 64 (1990) 2479



E866/NuSea Collab., Phys. Rev. Lett. 83 (1999) 2304



large  $x > 0.1 \Rightarrow$  rescatterings  
and hard production process are  
incoherent

$$\rightarrow \langle P_T^2 \rangle_A \propto \Lambda_i^2 A^{1/3} \quad (i=q,g)$$

(random walk in  $\vec{P}_T$ -space

Chiappetta, Pomer (1987))

$\Lambda_i^2$  NP universal scale

Data on nuclear  $P_T$ -broadening?

- dijet  $\gamma A$  production [E683]
- dijet  $hA$  " [E609]
- quarkonium  $hA$   $P^0$  [NA3, E772]
- $DY$  ( $hA$ ) [NA3, E772]
- nuclear DIS [HERMES, CLAS]

gross feature :

$$(GeV^2) \quad \Lambda_{DY}^2 < \Lambda_{J/4, \gamma}^2 < \Lambda_{dijet}^2$$

0.02                      0.05 - 0.1                      0.2 - 0.6

difficult to understand :

- Luo, Qiu, Sterman (1994)
- Guo (1998)
- Johnson, Kopeliovich, Tarasov (2001)
- Raufeisen (2003)

breaking of universality ?

maybe not

most of the data involves  $x \sim 0.1$   
at the frontier between coherent and  
incoherent regimes

no universality of  $\langle p_T^2 \rangle_A$  expected  
at  $x \ll 1 \Rightarrow$  differences in  $\Lambda^2$   
could be due to coherent effects

$x \ll 1$  regime studied in

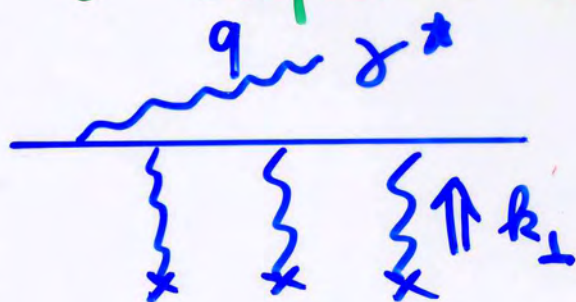
- Kopeliovich, Schäfer, Tarasov (1999)
- Kopeliovich, Raufeisen, Tarasov, Johnson (2003)

for  $\langle q_{\perp}^2 \rangle_{DY}$  and nuclear modification  
in "color dipole formulation"

- Connection with standard QCD fact? ?
- $\langle q_{\perp}^2 \rangle_{DY}$  compared to  $\langle q_{\perp}^2 \rangle_{dijet}$  ?
- Consistent with universality of  $f(x, t_{\perp})$  ?

To study those questions :

- "full" coherence  $x = \frac{Q^2}{2M_J} \ll 1$
- Explicit model (SQED) to compare



DY

AND



DIS

( $\sim$  dijet  $\delta P^0$ )

Pedagogical model illustrating several features :

- universality of  $f_{q,T}(x \ll 1, l_{\perp})$  checked for  $T = "p"$  and  $T = "A"$  ↓ probed quark

(agrees with factorization :

Collins, Soper (1981)  
Ji, Ma, Yuan (2005) )

- universality in other " $\perp$ " variables can be broken

$k_{\perp} \equiv$  Coulomb rescattering  $\neq l_{\perp}$

$$\langle k_{\perp}^2 \rangle_{DY}^{(x \ll 1)} \neq \langle k_{\perp}^2 \rangle_{DIS}$$

- trivially :  $P_{\perp}$  nuclear broadening differs (at  $x \ll 1$ ) if  $\neq$  transverse mom. variables are compared :

$$\langle l_{\perp}^2 \rangle = \langle q_{\perp}^2 \rangle_{DY} \neq \langle k_{\perp}^2 \rangle_{DIS}$$

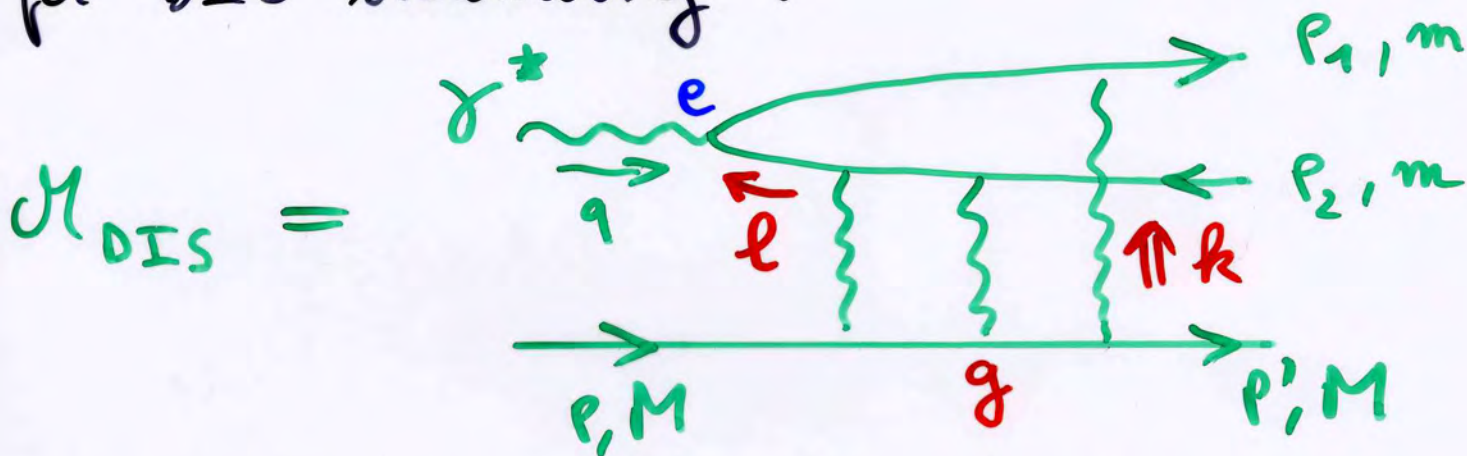
- equivalence between "PDF" and "color dipole" formulations is explicit



# ① Model in aligned-jet kinematics and interpretation

## DIS off a proton

use model of Brodsky et al (2002)  
for DIS shadowing:



- SQED ;  $k^\pm \equiv k^0 \pm k^z$
- Bjorken limit :  $q^- = 2\nu$ ,  $Q^2 \rightarrow \infty$   
at fixed  $x_B = \frac{Q^2}{2M\nu}$

$$q = (q^+, q^-, \vec{\sigma}_\perp) = (-Mx_B, q^-, \vec{\sigma}_\perp)$$

- full coherence :  $x_B \ll 1$
- Study Coulomb soft rescatterings  
at leading-twist  $\Rightarrow$  "ALIGNED-JET"

$$\begin{cases} p_1^- \approx q^- \rightarrow \infty \\ p_2^- \text{ fixed} \end{cases} \Rightarrow y = \frac{p_2^-}{2\nu} \rightarrow 0$$

$$(Q^2, J \rightarrow \infty \gg p_2^- \gg k_{i\perp}, p_{i\perp} \gg k_i^+, p_2^+ \sim Mx_B \gg p_1^+)$$

interpretation:

hard scale  $J$  does not flow in lower part

$\Rightarrow$  • hard vertex:  $\delta^* q \rightarrow q \sim \mathcal{O}(q^0)$

( $\infty$  mom. frame)

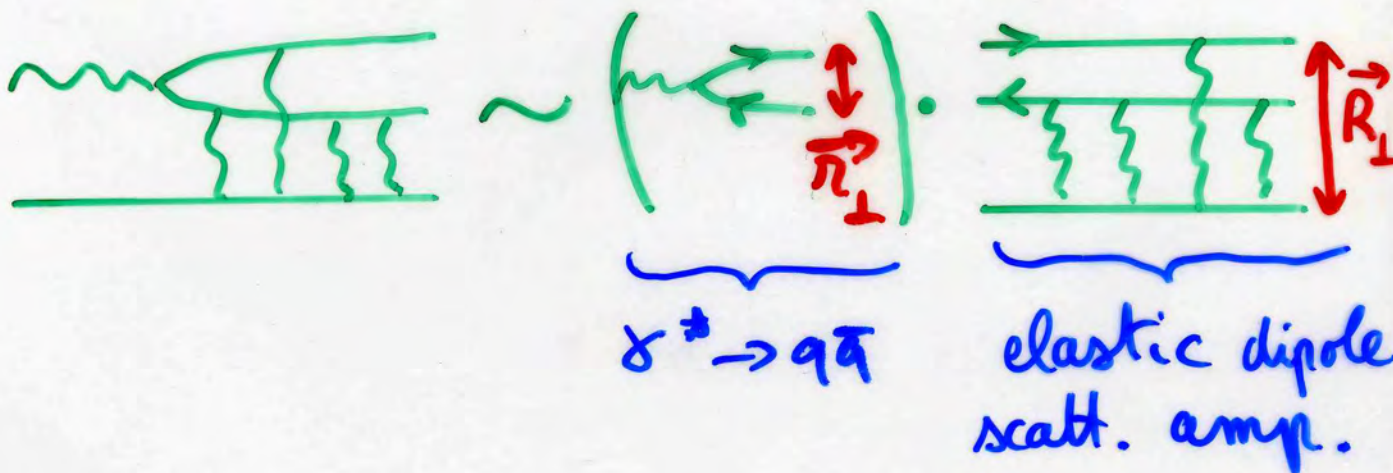
•  $|M_{\text{DIS}}|^2 \leftrightarrow$  soft dynamics  
contribution to  $f_{q/T}^{\text{DIS}}(x, l_\perp)$

probed quark momentum:

$$\begin{cases} x = \frac{l^+}{p^+} = \frac{p_1^+ - q^+}{p^+} = x_B \\ l_\perp = k_\perp - p_{2\perp} \neq k_\perp \end{cases}$$

exact calculation resumming Coulomb rescatterings

$$M_{\text{DIS}}(\vec{\pi}_\perp, \vec{R}_\perp) \sim \Psi(\pi_\perp) \cdot T_{q\bar{q}}(\vec{\pi}_\perp, \vec{R}_\perp)$$



$$\Psi(r_\perp) \sim K_0(m_\perp r_\perp) \quad m_{\parallel}^2 = p_2^- M x_B + m^2$$

dipole size  $r_\perp \lesssim m_{\parallel}^{-1} = y Q^2 + m^2$  (soft)

$$i T_{q\bar{q}}(\vec{\pi}_\perp, \vec{R}_\perp) = 1 - \exp[-ig^2 W(\vec{\pi}_\perp, \vec{R}_\perp)]$$

$W =$  dipole single scatt. amp.

$$= \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} \frac{1 - e^{i\vec{\pi}_\perp \cdot \vec{k}_\perp}}{k_\perp^2 + \lambda^2} e^{i\vec{R}_\perp \cdot \vec{k}_\perp}$$

← photon mass

$$= \frac{1}{2\bar{u}} \left[ \underbrace{K_0(\lambda R_\perp)}_{\text{quark rescatt.}} - \underbrace{K_0(\lambda |\vec{R}_\perp + \vec{\pi}_\perp|)}_{\text{antiquark rescatt.}} \right]$$

unitarity relation:

$$|T_{q\bar{q}}|^2 = -2 \text{Im}(T_{q\bar{q}})$$

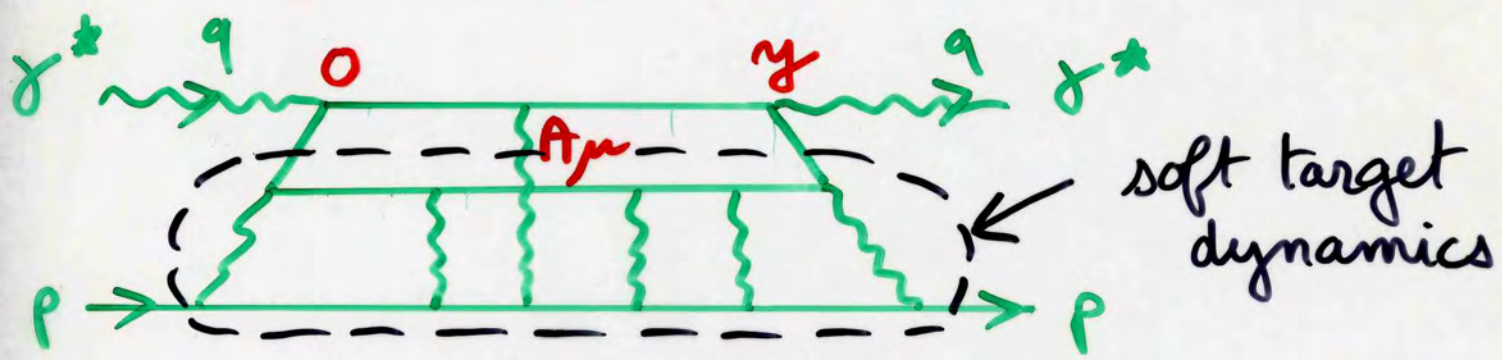
dipole scattering cross section:

$$\sigma_{q\bar{q}}(r_\perp) = \int d^2 \vec{R}_\perp |T_{q\bar{q}}(\vec{\pi}_\perp, \vec{R}_\perp)|^2$$

Recall QFT expression of  $f_{q/T}$  :

$$f_{q/T}(x_B, Q^2) = \int \frac{dy^-}{8\bar{a}} e^{-ix_B p^+ y^-} \langle T(p) | \bar{q}(y^-) \delta^+ P_{\text{exp}} \left[ ig \int_0^{y^-} A^+ \right] q(0) | T \rangle$$

(Collins, Soper 1982)



- in general gauge, struck quark rescatt. do modify  $\nabla_{\text{OIS}}^{\text{L.T.}}$  Brodsky et al 2002

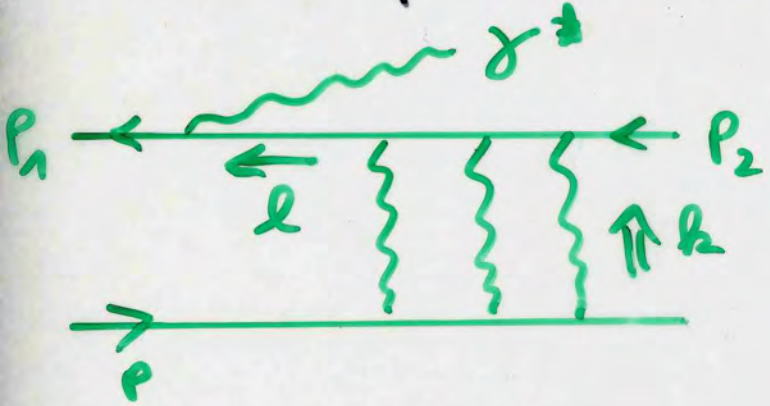
- they build  $P_{\text{exp}} \left[ \int_0^{y^-} ig A^+ \right]$  to ensure gauge invariance.

(• rescatterings in intermediate state  $\langle y^- \rangle \sim \frac{1}{Mx}$  are NOT a gauge artefact:  $A^+ = 0 \Rightarrow$  rescatt. within target spectators)

- in our perturbative model :
  - soft target dynamics
  - gauge links
 are treated on same footing (expansion in  $g^2$ )

# DY off a proton

DY model obtained from DIS by crossing and  $q^2 < 0 \rightarrow q^2 > 0$  (S.P. 2002)



- hard process:  $\bar{q}q \rightarrow \gamma^*$
- soft dynamics  $\leftrightarrow f_{q/T}^{DY}(x, l_\perp)$

$$\otimes \quad \mathcal{M}_{DY}(\vec{\pi}_\perp, \vec{R}_\perp) = -e^{ig^2 G(R_\perp)} \mathcal{M}_{DIS}(\vec{\pi}_\perp, \vec{R}_\perp)$$

$G(R_\perp) =$  Coulomb phase (IR sensitive)

$$= \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} \frac{e^{i\vec{R}_\perp \cdot \vec{k}_\perp}}{k_\perp^2 + \lambda^2} = \frac{1}{2\pi} \kappa_0(\lambda R_\perp)$$

(DY: scattering of a monopole  $\Rightarrow$  IR sensitive amplitude)

Simple consequences of  $\otimes$  :

•  $|\mathcal{M}_{DIS}|^2 = |\mathcal{M}_{DY}|^2 \Rightarrow \int_{q/T}^{DIS}(x) = \int_{q/T}^{DY}(x)$   
(inclusive)

- $\text{Im}(\mathcal{M}_{OY}) \neq \text{Im}(\mathcal{M}_{OIS})$   
 $\Rightarrow$  Pomeron / diffraction is not universal  
 Collins, Frankfurt, Strikman 1993  
 Berera, Soper 1994

- $\mathcal{M}_{OIS}$  and  $\mathcal{M}_{OY}$  not related by simple phase shift in conjugate  $k_{\perp}$  - space :

$$\frac{d\sigma_{OY}}{dk_{\perp}^2} \neq \frac{d\sigma_{OIS}}{dk_{\perp}^2}$$

non-univ. of Coulomb rescatt. at  $x \ll 1$

- not in contradiction with factorization :  
 $k_{\perp}$  internal to target structure,  
 integrated out in  $f_{q|T}(x, \underline{l}_{\perp})$

easy check:  $\frac{d\sigma}{dl_{\perp}^2}$  is universal

$$\Rightarrow f_{q|T}^{OY}(x, \underline{l}_{\perp}) = f_{q|T}^{OIS}(x, \underline{l}_{\perp})$$

↑ probed quark

$$\frac{d\sigma^{\text{DIS}, DY}}{d\ell_{\perp}^2} \sim \int d^2n_{\perp} d^2n'_{\perp} e^{-i(\vec{n}_{\perp} - \vec{n}'_{\perp}) \cdot \vec{\ell}_{\perp}}$$

$$\cdot \psi(n_{\perp}) \psi(n'_{\perp}) \left[ \frac{1}{2} \sigma_{q\bar{q}}(n_{\perp}) + \frac{1}{2} \sigma_{q\bar{q}}(n'_{\perp}) - \frac{1}{2} \sigma_{q\bar{q}}(|n_{\perp} - n'_{\perp}|) \right]$$

(Kopeliovich, Tarasov, Schäfer 1999)

universality  $\Rightarrow$  in DY (as in DIS),

$$\frac{d\sigma}{d\ell_{\perp}^2} \text{ in terms of } \sigma_{q\bar{q}}(n_{\perp})$$

(Kopeliovich 1996 (Born level))

Brodsky, Hebecker, Quack 1996

Raufeisen, Peng, Nayak 2002 )

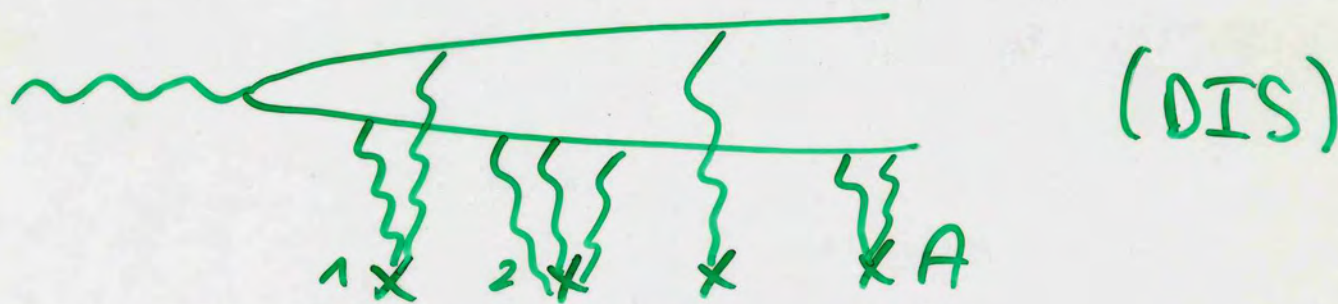
Remark:

$$\left\{ \begin{array}{l} \frac{d\sigma}{d\ell_{\perp}^2} = \frac{d\sigma}{dq_{\perp}^2} \quad (DY) \quad DY \text{ pair} \end{array} \right.$$

$$\left\{ \begin{array}{l} \frac{d\sigma}{d\ell_{\perp}^2} = \frac{d\sigma}{dp_{\perp}^2} \quad (DIS) \quad \text{leading jet} \end{array} \right.$$

# Model for nuclear target

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1 centre  $\rightarrow$  A centres

$$R_A \ll l_c = \frac{1}{M\alpha}$$

$$G(R_{\perp}) \rightarrow G_A(\vec{R}_{\perp}) = \sum_{i=1}^A G(\vec{R}_{\perp} - \vec{x}_{i\perp})$$

$$\mathcal{M}_{DIS}^A \sim \psi(r_{\perp}) T_{q\bar{q}}^A(\vec{\pi}_{\perp}, \vec{R}_{\perp})$$

$$\mathcal{M}_{DY}^A = -e^{ig^2 G_A(R_{\perp})} \mathcal{M}_{DIS}^A$$

$$iT_{q\bar{q}}^A = 1 - e^{-ig^2 W_A}$$

$$W_A = G_A(\vec{R}_{\perp}) - G_A(\vec{R}_{\perp} + \vec{\pi}_{\perp})$$



$\Rightarrow \frac{d\sigma^A}{d\vec{l}_\perp}$  is universal  $\Rightarrow$

$$f_{q/A}^{DY}(x, \vec{l}_\perp) = f_{q/A}^{DIS}(x, \vec{l}_\perp)$$

Average over  $\vec{x}_{i_\perp}$ :

$$\langle \rangle_A \equiv \int \prod_{i=1}^A \left( \frac{d^2 \vec{x}_{i_\perp}}{S} \right)$$

$$\langle e^{-ig^2 W_A} \rangle_A = \dots = \exp \left[ -T \frac{\sigma_{q\bar{q}}(n_\perp)}{2} \right]$$

$$T = \frac{A}{S} \text{ thickness}$$

total coherence  
+ simple averaging }  $\Rightarrow$

$$\frac{d\sigma^A}{d\vec{l}_\perp} \sim S \int d^2 \vec{n}_\perp d^2 \vec{n}'_\perp e^{-i(\vec{n}_\perp - \vec{n}'_\perp) \cdot \vec{l}_\perp} \psi(n_\perp) \psi(n'_\perp) \cdot \left[ 1 - e^{-T\sigma_{q\bar{q}}(n_\perp)/2} - e^{-T\sigma_{q\bar{q}}(n'_\perp)/2} + e^{-T\sigma_{q\bar{q}}(|\vec{n}_\perp - \vec{n}'_\perp|)/2} \right]$$

Kopeliovich, Tarasov, Schäfer (1999)

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- $\frac{d\sigma^A}{d\vec{l}_\perp}$  expressed in terms of  $f_{q/A}(\vec{l}_\perp)$

- same target size dependence in DIS and DY

⇒ same  $l_\perp$  - broadening

Compare DY (NA10, E772)

to nuclear DIS data :

HERMES (talk: V. Muccifora)

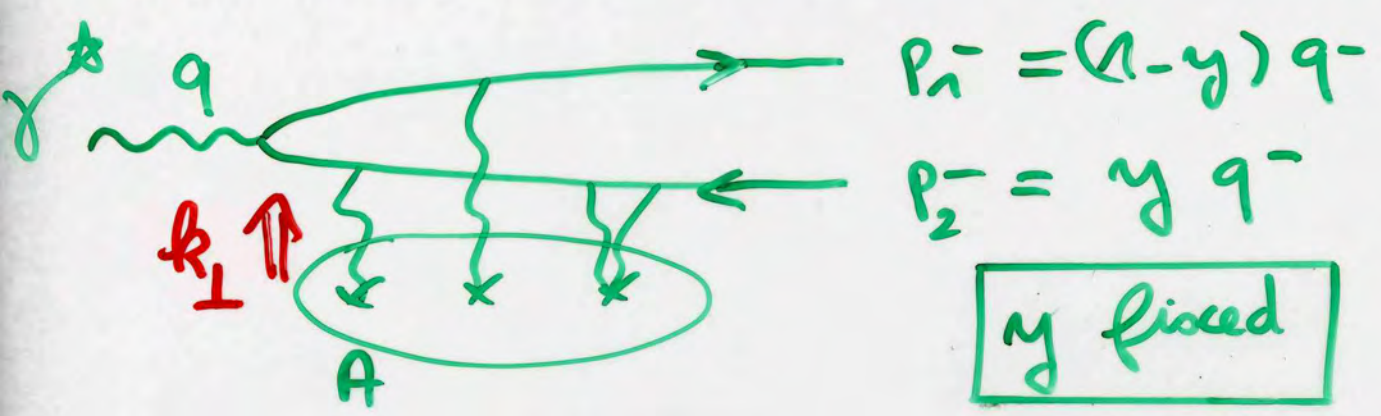
CLAS (talk: W. Brooks)

→ direct test of universality of

$f_{q/A}(x, \underline{\vec{l}_\perp})$

# ② Symmetric kinematics and $\langle k_{\perp}^2 \rangle$

Model for dijet production ?  
→ new kinematics :



$p_2^-$  scales as  $D \Rightarrow p_2$  part of hard sub-process :

- $\gamma^* g \rightarrow q \bar{q}$  (DIS  $\sim$  dijet leptop $^0$ )
- $\bar{q} g \rightarrow \bar{q} \gamma^*$  (DY + jet)

transverse mom. transfer to hard system :

$k_{\perp} = \text{Coulomb exchange} =$

- dijet mom. imbalance (DIS)
- $\gamma^*/\text{jet}$  mom. imbalance (DY)

$$\frac{d\Gamma_{OIS}}{d\vec{k}_\perp} \neq \frac{d\Gamma_{OY}}{d\vec{k}_\perp}$$

$k_\perp \neq l_\perp$  (probed in aligned-jet kinematics)

$\Rightarrow$  no contradiction with factorization

single center: a curious property

$$\frac{d\Gamma_{OIS}}{d\vec{k}_\perp} \sim \int d^2\vec{n}_\perp |\psi(n_\perp)|^2 \cdot \frac{d\Gamma_{q\bar{q}}(\vec{n}_\perp, \vec{k}_\perp)}{d\vec{k}_\perp}$$

$$\frac{d\Gamma_{OY}}{d\vec{k}_\perp} \underset{k_\perp \gg \lambda}{\sim} \left( \dots \right) \cdot \left[ \frac{d\Gamma_{q\bar{q}}(\vec{n}_\perp, \vec{k}_\perp)}{d\vec{k}_\perp} \right]_{\text{Born}}$$

(similar to  $e^-$  vs bremsstrahlung  
Bethe, Maximon (1954) )

$$\langle k_\perp^2 \rangle_{OIS} = \langle k_\perp^2 \rangle_{\text{Born}} + O(g^8 m''^2)$$

$$\langle k_\perp^2 \rangle_{OY} = \langle k_\perp^2 \rangle_{\text{Born}} + O(g^8 \lambda^2)$$

# "Nucleus"

$$\frac{d\sigma_{DIS}^A}{d^2\vec{k}_1} \sim \int d^2\vec{r}_1 |\psi(r_1)|^2 \cdot \frac{d\sigma_{q\bar{q}}^A(\vec{r}_1, \vec{k}_1)}{d^2\vec{k}_1}$$

$$\frac{d\sigma_{DY}^A}{d^2\vec{k}_1} \sim \frac{d\sigma_q^A}{d^2\vec{k}_1} \cdot \int d^2\vec{r}_1 |\psi(r_1)|^2 (2 - 2\cos\vec{k}_1 \cdot \vec{r}_1)$$

A-dependence is driven by:

DIPOLE rescattering (DIS)

MONOPOLE " (DY)

$\Rightarrow k_1$  (Coulomb) - broadening is non-universal ( $x \ll 1$ )

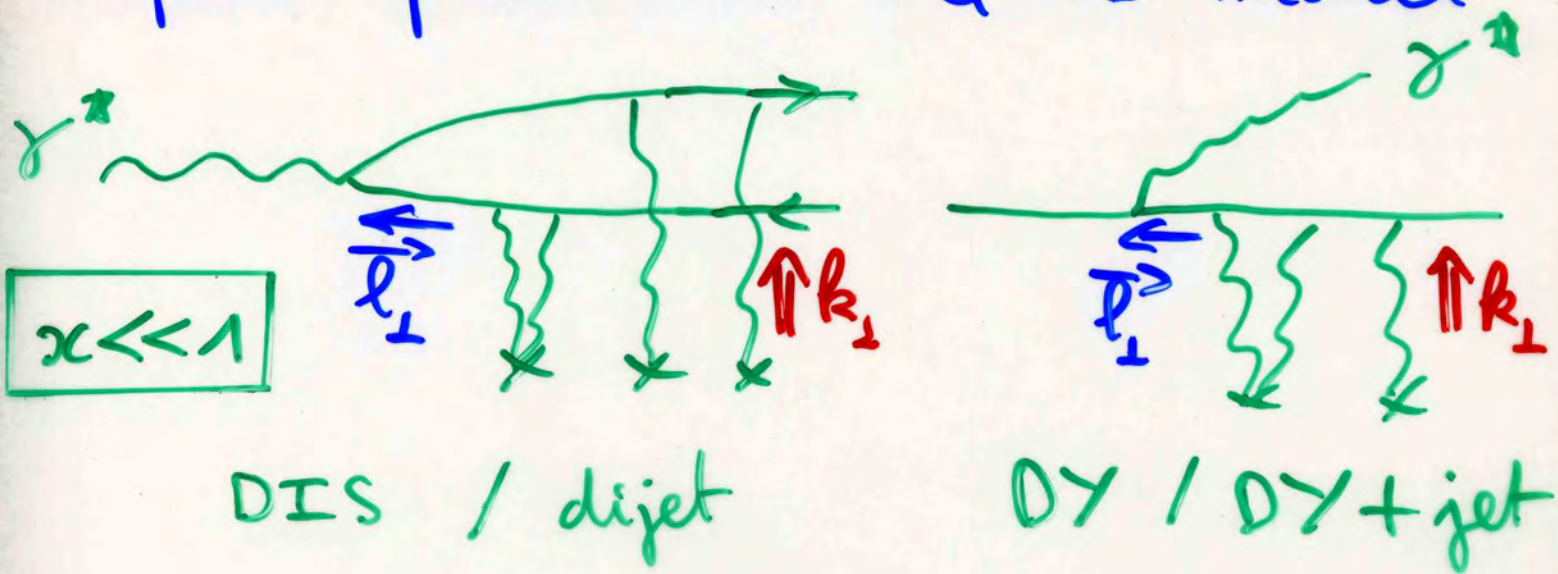
explicitly:  $\Delta\langle k_1^2 \rangle = \langle k_1^2 \rangle_A - \langle k_1^2 \rangle_p$

$$= \begin{cases} \left( \frac{g^4 T}{m_{\parallel}^2} \right) \times m_{\parallel}^2 = O(g^4 T) & \text{(DIS)} \\ \left( \frac{g^4 T}{k_1^2} \right) \times k_1^2 = O(g^4 T) & \text{(DY)} \end{cases}$$

(Dolejší, Hüfner, Kopeliovich, 1993)

# Summary

Explicit perturbative SQED model



- universality of  $\frac{d\sigma}{d\vec{l}_\perp} \Rightarrow$   
 $f_{q/T}^{DIS}(x, l_\perp) = f_{q/T}^{DY}(x, l_\perp)$  (aligned-jet)

dipole formulation  $\Leftrightarrow$  factorization approach

- non-universality of  $\frac{d\sigma}{d\vec{k}_\perp}$   
 does not violate factorization  
 ( $k_\perp$  integrated out in  $f_{q/T}(x, l_\perp)$ )

- single centre :  $\frac{d\sigma^{DY}}{d\vec{k}_\perp} = \left[ \frac{d\sigma^{DY}}{d\vec{k}_\perp} \right]_{\text{BORN}}$  21

- nucleus : DIS  $\rightarrow$  DIPOLE  
DY  $\rightarrow$  MONOPOLE

$$\mathcal{M}_{DY}(\vec{n}_\perp, \vec{R}_\perp) \sim e^{i\psi(R_\perp)} \mathcal{M}_{\text{DIS}}(\vec{n}_\perp, \vec{R}_\perp)$$

• trivially :  $\left. \frac{d\sigma}{d\vec{l}_\perp} \right)_{DY} \neq \left. \frac{d\sigma}{d\vec{k}_\perp} \right)_{\text{dijet}}$   
↖ ↗  
not the same variable

$$R_{DY}(l_\perp) = 1 + \frac{2g^4 T}{\pi m_{||}^2} \ln^2\left(\frac{m_{||}}{\lambda}\right)$$

$(\lambda \ll l_\perp \ll m_{||})$

$$R_{\text{dijet}}(k_\perp) = 1 - \frac{4g^4 T}{5\pi m_{||}^2} \ln\left(\frac{m_{||}}{\lambda}\right)$$

• smallness of  $\Delta\langle k_\perp^2 \rangle_{DY}$  could be simply due to onset of coherent effects.